The Mini-Java Programming Language

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Participation

The table below expresses the percentage of participation of each member in the realization of the versions of this work.

Version 1

Name	Participation (%)
Jackson Rauup	25
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Table 1: Participation in Version 1.

Version 2

Name	Participation (%)
Jackson Rauup	25
Joel Felipe	25
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Vitor Greati	25

Table 2: Participation in Version 2.

1 Mini-Java Language Reference

1.1 Syntax

The following sections are dedicated to illustrate examples of valid Mini-Java constructs and other syntactic aspects.

1.1.1 Reserved words

The words listed below have special usages in Mini-Java, so that they cannot be used as identifiers. Mini-Java is case sensitive, so such words are reserved just for their lowercase versions.

```
program
   class
   method
   val
   int
   string
   void
    declarations
    enddeclarations
9
    i f
10
11
    else
12
    for
13
   to
   step
14
   while
15
   switch
16
   case
   print
19
   read
   not
20
```

1.1.2 Valid Identifiers

Identifiers are used for uniquely representing variables, classes, programs, methods and parameters. Every identifier accepts alphanumeric characters plus the underline ("_"). The ids' first character cannot be a number, only a letter or an underline. The following examples are valid identifiers, except for the last one:

```
abcd2
a1b2c3
AaBb
black_sabbath
-
___
abcd
_AbCd
_1234
```

1.1.3 Data Types

The Mini-Java language supports the following types: integer, string, arrays, and personalized ones, given by classes, in the object-oriented approach. The integer type is denoted by the keyword int, the string type is denoted by string, and the array type is represented by some type name followed by a sequence of left and right square brackets. Integer literals are just written as ordinary numbers and string constants are written between double quotes. Classes are explained in Section 1.1.11.

1.1.4 Expressions

There are three types of expressions: arithmetic, logical and relational. Arithmetic expressions are those which result in integers or strings, while logical and relational expressions have boolean-valued outcomes. In therms of syntax, the three expressions may be intertwined; though this may be semantically invalid.

The arithmetic expressions mix the basic operations, literal constants, variables, more expressions and even method calls. The following are examples of valid arithmetic expressions. Note that the expressions are not associated to a context, e.g. variable assignments, since they may appear in many different situations.

```
1
1
   +5
2
3
   -7
   (17)
4
   90 + 90
   -21 + 12
   90 * 2
   78 / 3
   25 \% 4
   add(2, 5)
10
   add(num, 5*7)
   assume ("control", 2112)
   doMagic(i * (2 + const) - shift, (flag * 5) + year / month)
13
14
   #These expressions are not standalone.
15
   #They may be part of variable assignments or relational expressions
```

The remaining expressions are even more heterogeneous than arithmetic expressions. Logic and Relational expressions may combine arithmetic expressions with boolean operations ($logical\ and$, and $logical\ or$) and relations (less than, equals, different, greater or equal, etc.).

```
1 73
2 73 == 1001001
3 2112 < 5
4 isEven(number) && isPrime(number) && number == 2
5 (1 || false) && true
6 length("Rush") <= length("Caress of Steel") - 13</pre>
```

```
8 #Relational statements are normally encapsulated in statements
9 #that may change the execution flow, e.g. if, while and for
```

It may seem confusing to treat integers as valid logic expressions. However, note that Mini-Java does not natively support boolean variables. Henceforth, similarly to C, integers will be used to simulate booleans. Also, note that false and true in line 5 are actually variables; hence, the expression may be evaluated to false if true == 0.

1.1.5 Variables Declaration and Initialization

Declarations can only be stated in the beginning of the class body. It must contain a type (Section 1.1.3), a valid variable identifier and an optional initialization value. Many variables of the same type may be declared in the same line, separated by commas. Every declaration must finish with a semicolon.

A valid variable identifier consists of an identifier (Section 1.1.2) followed by optional brackets. The brackets represent arrays. For instance, the following example illustrates valid identifiers (the first two) and invalid variable identifiers (last two):

```
1 color
2 names[]
3 []
4 telephoneNumbers[]]
```

The initial value may be either expressions (Section 1.1.4) or array initializers or creators. The array creator will be responsible for explicitly specifying the size of the array, even though it does not specify its contents. On the other hand, the array initializer implicitly declares the array size by stating its value.

Combining the variables identifiers with the expressions and arrays initializers and creators, it is possible to obtain the following valid examples:

```
1  string str;
2  int a, b = 2, c, d, e = 5;
3  string[] str_arr = @string[10];
4  int[] vec = @int [size + 2];
5  int[][] identity = { {1, 0, 0}, {0, 1, 0}, {0, 0, 1} };
6  int[][] unknown_line = { @int[2], {73, 2112} };
7  #this shall be generally inside a "declarations" block
```

1.1.6 Assignments

Similar to Pascal, the assignment operator is :=, which can't be used to initialize a variable, only for assignment. The examples below show how assignments are written in Mini-Java:

```
8  str := "text";
9  a := 2;
10  b := 3;
11  c := 5;
12  str_arr[a] := "a";
13  str_arr[5] := "c";
```

1.1.7 Conditional structures

The project language supports the following conditional structures: If/Else and Switch/Case. The following codes exemplify their use:

1.1.7.1 If/Else Statements

```
1  #this shall be inside a method definition (class body)
2  declarations
3     string str;
4     int a = 5;
5  enddeclarations
6
7  if a > 10 {
8     str := "bigger"
9  } else if a == a {
10     str := "equal"
11  } else {
12     str := "smaller"
13  }
```

1.1.7.2 Switch/Case Statements

```
#this shall be inside a method definition (class body)
  declarations
       string[] str_arr = @string[10];
3
       int control = 3;
4
   enddeclarations
   switch(control) {
       case 0 { str_arr[0] := "zero" }
8
       case 1 { str_arr[0] := "one" }
9
       case 2 { str_arr[0] := "two" }
10
       case 3 { str_arr[0] := "three" }
       case 4 { str arr[0] := "four" }
       default { str\_arr[0] := "minus one"}
13
14 }
```

1.1.8 Repetition structures

The repetition structures available in the language project are "while" and "for" statements. The structure of while is similar to that of Java, with the difference that parentheses are optional. The for statement is similar to that of Pascal, using only one

initialization, one expression for the limit of the variable loop and allowing to define a step via the step keyword. Examples of these constructs are below.

1.1.8.1 While Statement

```
#this shall be inside a method definition (class body)
   declarations
       int i = 0;
3
       int max = 100;
4
   enddeclarations
   while i < 100 {
7
       i := i + 1;
8
   1.1.8.2 For Statement
   #this shall be inside a method definition (class body)
   declarations
       int max = 100;
3
       int i;
4
   enddeclarations
   for i := 0 to \max \{
       i := i + 1;
8
9
10
11
   for i := \max to 10 step -1 
12
       i := i - 1;
13
```

1.1.9 Subprograms declaration and call

All subprograms need to be declared with the keyword method, followed by a return type (use void for no return), an identifier, a list of formal parameters between parentheses, and, finally, the statements block. Such block can begin with a section of variable declarations. To call a subprogram, one just have to type its name and provide, between parentheses, the list of actual parameters. Below is an example of a class with various subprograms:

```
program MethodExamples;
2
    class Math {
5
          declarations
               int i = 1;
6
         enddeclarations
7
8
         method void toIncrease() {
9
               \mathbf{i} \ := \ \mathbf{i} \ + \ \mathbf{1}
10
11
12
```

```
method void toDecrease() {
13
               \mathbf{i} \ := \ \mathbf{i} \ - \ \mathbf{1}
14
15
16
         method void toIncreaseN(int n) {
17
               int j = 0;
18
               while (j < n) {
19
                    toIncrease();
20
21
                    j := j + 1
               }
22
23
         }
24
^{25}
         method void toDecreaseN(int n) {
26
27
               int j = 0;
28
               while (j < n) {
29
                    toDecrease();
30
                    \mathbf{j} \ := \ \mathbf{j} \ + \ \mathbf{1}
31
               }
         }
32
33
34
         method int toIncrease() {
               i := i + 1;
35
36
               return i
37
38
         method int toDecreaseN(int n) {
39
40
               i := i - n;
41
               return i
42
         }
43
    }
```

1.1.10 Statement blocks

Blocks are statements lists containing optionally a variables declarations section. Below, an example of one that declares its local variables:

```
{\tt declarations}
1
2
        String str;
        int a, b, c = 8;
3
   end declarations\\
4
5
   {
6
        str := "text";
7
        a := 2;
8
        b := 3;
9
        c := 5;
10
11 }
      Next, an example of one without the declaration section:
1 {
```

Blocks are commonly used in the definition of methods, specifying the list of statements to be executed, as well as the local variables to be used.

1.1.11 Classes

A class is divided in two parts: declaration, which assigns the name of the class; and body, which describes its variables declarations and methods.

The class body necessarily describes all declarations before the methods. The body is allowed to have neither declaration or methods. The following examples illustrate valid classes declarations:

```
class ClassExample1
2
        declarations
3
             int i = 0;
4
        end declarations\\
5
6
        method void method1() {}
7
   }
8
9
   class ClassExample2
10
11
        method void method1() {}
12
13
   }
14
15
   class ClassExample3
16
        declarations
17
             int i = 0;
18
        enddeclarations
19
20
   }
21
   class ClassExample4
22
   {
23
   }
24
```

1.1.12 IO

Similar to many languages, the IO's commands are "print" and "read". They print an expression to and read an identifier from the standard IO. The following examples illustrate valid IO's commands usages:

```
1 #this code shall be inside a body of a class or method 2 print "Hello World" 3 print a +\ b
```

```
\begin{array}{lll} \textbf{4} & \textbf{print} & \textbf{"Hello} & \textbf{"} + \textbf{world} \\ \textbf{5} & \textbf{read} & \textbf{world} \end{array}
```

1.1.13 Comments

Comments can be made using "#" and all of characters after this symbol will be ignored. The following examples illustrate valid comments:

```
1 #This line is commented 2 a:= "This part is not commented" #This part is commented
```

2 Examples

This section presents three very important algorithms written in Mini-Java to exemplify its syntax.

2.1 Merge Sort

```
program MergeSortProgram;
1
   class MergeSort
2
   {
3
       method void merge(int[] v; int begin; int middle; int end)
4
           declarations
5
               int i = begin, j = middle+1, k = begin, length = end-begin+1;
6
7
                int[] aux;
           enddeclarations
8
       {
9
           10
11
                if v[i] < v[j] 
12
                   aux[k] := v[i];
13
                    i := i + 1
14
                }
15
                else
16
                {
17
                    aux[k] := v[j];
18
19
                    j := j + 1
                };
20
                k \;:=\; k \;+\; 1
21
            };
22
23
           ^{24}
25
                aux[k] := v[i];
26
                i := i + 1;
27
                k := k + 1
28
            };
29
30
           while j \le end
31
           {
                aux[k] := v[j];
33
34
                j := j + 1;
                k := k + 1
35
           };
36
37
           for k := begin to end step 1
38
39
           {
               aux[k] := v[k]
40
41
42
       method void mergeSort(int[] v; int begin; int end)
43
```

```
{\tt declarations}
                 int middle;
45
46
             enddeclarations
47
        {
             if \quad \text{begin} \, < \, \text{end}
48
49
             {
                 middle := (end + begin)/2;
50
                 mergeSort(v, begin, middle);
51
                 mergeSort(v, middle, end);
52
                 merge(v, begin, middle, end)
53
             }
54
        }
55
   }
56
   2.2
          Binary search
   program BinarySearchProgram;
1
2
    class BinarySearch
3
   {
4
5
        method int binarySearch(int[] arr; int 1; int r; int x)
             declarations
6
                 int mid;
7
             end declarations\\
8
        {
9
10
             i\,f\ r\ >=\ 1
             {
11
                 mid := 1 + (r - 1)/2;
12
                 if \ arr[mid] == x
13
                 {
14
                      return mid
                 };
17
                 if (arr[mid] > x)
18
19
                      return binarySearch(arr, l, mid-1, x)
20
^{21}
                 return binarySearch (arr, mid+1, r, x)
22
23
             };
             return -1
24
        }
25
26
   }
   2.3
          Quick Sort
   program QuickSortProgram;
   class QuickSort
3
   {
4
        method void quickSort(int[] v; int begin; int end)
5
```

declarations

```
7
                                                                                                          \  \, int \  \, i \, = \, begin \, , \  \, j \, = \, end \, -1, \  \, pivot \, = \, v \, [\, (\, begin \, + \, end \, ) \, / \, 2 \, ] \, , \  \, aux \, ; \  \,
                                                                             end declarations\\
    8
    9
                                                 {
10
                                                                              while \ i <= j
                                                                             {
11
                                                                                                         \label{eq:while} \begin{tabular}{ll} \begin{
12
13
                                                                                                                                    i \ := \ i \ + \ 1
 14
                                                                                                         };
15
                                                                                                         while (v[j] > pivo) && (j > begin)
16
17
                                                                                                                                   \mathbf{j} \ := \ \mathbf{j} \ - \ \mathbf{1}
18
                                                                                                        };
if i <= j
19
20
21
22
                                                                                                                                   aux := v[i];
23
                                                                                                                                  v\,[\;i\;]\;:=\;v\,[\;j\;]\,;
24
                                                                                                                                  v\left[\,j\,\right]\ :=\ aux\,;
                                                                                                                                   i := i + 1;
25
                                                                                                                                   j := j - 1
26
                                                                                                         }
27
                                                                           f : if j > begin
28
29
30
                                                                                                         quickSort(v, begin, j + 1)
31
                                                                            32
33
34
                                                                                                        \mathtt{quickSort}\,(\mathtt{v}\,,\ \mathtt{i}\,,\ \mathtt{end}\,)
35
36
37
                                                 }
38 }
```

3 Extended Backus-Naur Form (EBNF)

```
"program" \langle id \rangle ";" \langle class-decl \rangle \{\langle class-decl \rangle \}
                \langle program \rangle
                                          "class" (id) (class-body)
               (class-decl)
             \langle class-body \rangle
                                           "{" [\langle decls \rangle] {\langle method-decl \rangle} "}"
                                          "declarations" \{\langle \text{field-decl} \rangle ";"\} "enddeclarations"
                      \langle decls \rangle
                (field-decl)
                                          (type) (field-decl-aux)
         (field-decl-aux)
                                          \langle \text{var-decl-id} \rangle  ["," \langle \text{field-decl-aux} \rangle ] | \langle \text{var-decl-id} \rangle "=" \langle \text{var-init} \rangle  ["," \langle \text{field-decl-aux} \rangle ]
             ⟨var-decl-id⟩
                                          \langle id \rangle \{ "[" "]" \}
                                          ⟨expression⟩ | ⟨array-init⟩ | ⟨array-creation-expr⟩
                  (var-init)
                                          "{" \langle var-init \rangle {"," \langle var-init \rangle} "}"
              (array-init)
(array-creation-expr)
                                          "@"\langle type \rangle \langle array-dim-decl \rangle \{\langle array-dim-decl \rangle\}
       ⟨array-dim-decl⟩
                                          "[" (expression) "]"
                                          "method" (method-decl-aux) (id) "(" [(formal-param-list)] ")" (block)
          (method-decl)
                                          "void" | \langle type \rangle
    (method-decl-aux)
  (formal-param-list)
                                          ["val"] \langle type \rangle \langle id \rangle \{", "\langle id \rangle\} ["; "\langle formal-param-list \rangle]
                     (block)
                                          [\langle decls \rangle] \langle stmt-list \rangle
                                          \langle \text{type-aux} \rangle \{ "[]" \}
                      \langle \text{type} \rangle
                                          (id) | "int" | "string"
                (type-aux)
                \langle stmt-list \rangle
                                          "{" (stmt) {";" (stmt)} "}"
                      \langle stmt \rangle
                                          (assign-stmt) | (method-call-stmt) | (return-stmt) | (if-stmt)
                      (stmt)
                                          \langle while-stmt \rangle | \langle for-stmt \rangle | \langle switch-stmt \rangle | \langle print-stmt \rangle | \langle read-stmt \rangle |
            \langle assign-stmt \rangle
                                          ⟨variable⟩ ":=" ⟨expression⟩
   (method-call-stmt)
                                          ⟨variable⟩ "(" [⟨expression⟩ {"," ⟨expression⟩} ] ")"
                                          "return" [(expression)]
           (return-stmt)
                   ⟨if-stmt⟩
                                           "if" (expression) (stmt-list) ["else" (if-stmt-aux)]
            ⟨if-stmt-aux⟩
                                          \langle if\text{-stmt} \rangle \mid \langle stmt\text{-list} \rangle
                                          "for" (assign-stmt) "to" (expression) ["step" (expression)] (stmt-list)
                 (for-stmt)
             ⟨while-stmt⟩
                                           "while" (expression) (stmt-list)
                                           "switch" \langle expression \rangle "{" \langle case \rangle {\langle case \rangle} [\langle default-stmt \rangle] "}"
           (switch-stmt)
                                          "case" \langle expression \rangle \langle stmt-list \rangle
                       \langle case \rangle
                                          "default" (stmt-list)
          ⟨default-stmt⟩
             ⟨expression⟩
                                          \langle \text{simple-expr} \rangle [\langle \text{rel-op} \rangle \langle \text{simple-expr} \rangle]
                    \langle \text{rel-op} \rangle
                                           "<" \mid "<=" \mid "!==" \mid "!=" \mid ">=" \mid ">"
                                          [\langle simple-un-op \rangle] \langle term \rangle \{\langle simple-bin-op \rangle \langle term \rangle\}
           (simple-expr)
                                          "+" | "-"
         \langle \text{simple-un-op} \rangle
        (simple-bin-op)
                                          "+" | "-" | "||"
                      \langle \text{term} \rangle
                                          \langle factor \rangle \{\langle term-bin-op \rangle \langle factor \rangle \}
                                          "*" | "/" | "&&" | "%"
           ⟨term-bin-op⟩
                                          (unsig-lit) | (variable) | (method-call-stmt) | "(" (expression) ")" | "not" (factor)
                    (factor)
```

```
\begin{array}{lll} \langle unsig\text{-lit} \rangle & \models & \langle integer\text{-lit} \rangle \mid \langle string\text{-lit} \rangle \\ & \langle variable \rangle & \models & \langle id \rangle \; \{ \langle variable\text{-aux} \rangle \} \\ & \langle variable\text{-aux} \rangle & \models & "[" \; \langle expression \rangle \; \{"," \; \langle expression \rangle \} \; "]" \; | \; "." \; \langle id \rangle \\ & \langle print\text{-stmt} \rangle & \models & "print" \; \langle expression \rangle \\ & \langle read\text{-stmt} \rangle & \models & "read" \; \langle id \rangle \end{array}
```

4 mjc: a compiler for Mini-Java

4.1 Compiler steps

A compiler is generally organized in two big parts: the front-end and the back-end. Each of them have sub-parts, which will be detailed in the course of this section.

Also called the *analysis* part of the compiler, the first step worries about precisely recognizing and representing the form of the source program in a precise and meaningful way. The basic tasks are to identify each language symbol in the code – which can be a string of one or more characters – and submit the resulting sequence of symbols to the set of grammar rules that characterize the language syntax. The result of this process is an intermediate representation of the program that will be used in the next steps. Some optimization may occur as one or more interleaved step in this process, but *mjc* doesn't perform this for a matter of simplicity.

The front-end encompasses two main phases: the *lexical analysis* or *scanning* and the *syntax analysis* or *parsing*. Sections 4.2 and 4.3 detail each one's peculiarities and present how they are implemented in mjc.

The back-end phase is about producing semantics for the program. This will be discussed in future versions of this document, since the current focus is in the front-end phase.

4.2 Lexical Analysis or Scanning

The scanning phase is performed by the *lexical analyser*, which reads the stream of characters and groups them into meaningful sequences, named *lexemes*. Each lexeme l is categorized in a *token* t, and the output of the analyser for each lexeme is the token symbol together with an *attribute value* a, say $\langle t, a \rangle$, where a points to an entry in the *symbol table* for t.

Symbol tables are used by compilers to store additional information about the recognized constructs, being incremented during the compilation phases. In the case of variables, for example, it holds the name, the type, the position in storage and any other variable's relevant attribute.

Once a token is recognized, it is transmitted to the parsing phase. Generally, the lexical analyzer is not the compiler's entry point. Instead, the parser – which acts in the parsing phase – occupies such position and calls the lexical analyzer to recognize and retrieve the next token.

There are tools to specify and generate lexical analyzers. One of the most used is *Lex*, or, more recently, *Flex*, which allows to describe the lexemes of each token by regular expressions. *Lex* specify its own language and has a compiler that generates code for simulating the transition diagrams which represent the indicated string patterns. The list of Mini-Java tokens, together with the corresponding lexemes' regular expressions, can be found in Appendix A.1.

mjc's lexical analyzer was generated by Lex due to the ease of implementation and the optimizations provided by such tool. An example of output of the lexical analyzer for the Quick Sort algorithm (Section 2.3) is in Appendix A.2. In order to submit a Mini-Java program to it, the following steps must be executed:

1. If bin/mjclexer doesn't exist, execute, from the root directory, make lexer.

2. Having a program in a file called program.mj, one can execute the following command from the root:

```
./bin/mjclexer [write_path [output_to_std] ] < /path/to/program.mj
```

Notice that it is possible to execute the analyzer without arguments, making it printing a table of tokens in the standard output. Also, one can pass a path to a file in which the table will be printed and, having that, also inform if the table must still be printed in the standard output (the default is always to print). The columns of the printed table represent, respectively, for each recognized token: the line of occurrence in the code, the column of occurrence of the first lexeme character, the lexeme length, the token name and the lexeme itself. When a character or sequence is not recognized by the analyzer, a warning is printed in the standard error output.

Finally, the lexical analyzer accepts a compilation flag called __EXECUTABLE__ which causes the compilation of the main function and other auxiliary print functions. The compilation performed when make lexer is executed activates such tag, since it is of interest of such usage to execute the analyzer as an ordinary program and show its result. However, when compiling it for the parsing purpose, no execution is needed, as the parser will mainly need the yylex function.

4.3 Syntax Analysis or Parsing

Parsing worries about checking if a sequence of tokens can be generated by the language grammar. Generally, the parser produces an intermediate representation in the form of a tree – explicitly or implicitly – to be processed by the rest of the compiler. Also, parsers are expected to inform to the users the occurrence of any syntax errors by intelligible messages.

There are three main parser categories: universal, top-down and bottom-up. The first encompasses algorithms that can parse any grammar, although they can be very inefficient. The other two imposes some restrictions to the grammars, but are faster and suitable for the most common programming language's constructs.

Next sections present the implementation of common parser algorithms for mjc. The most important concepts for understanding them were summarized and the instructions for running each parser in this compiler is explained at the end of the corresponding section.

4.3.1 Top-down parsing

In order to execute a top-down parsing, it is necessary to execute a top-down analysis. The grammar productions will be executed starting from an initial non-terminal and a parse tree will be generated. The parse tree may have terminal and non-terminal symbols. However, only terminal symbols will be leaf nodes.

The nodes of the token tree will be compared and matched with the grammar's productions. If the grammar is ambiguous, there may exist multiple parse trees for a given program, considering left or right derivations.

For top-down parsing, the left-most symbols will be analyzed first. However, even if the grammar is unambiguous, the parsing may execute an infinite loop. For instance, any grammar with left- recursive productions can cause an infinite loop. This happens because the algorithm would not stop generating new derivations.

In addition, it may be the case that two different productions generate the same terminal symbol. When this happens, the parser will have to guess which production generated that terminal. Also, if the parse tree does not match the chosen productions, the parser will have to keep backtracking until it has chosen every possible production before it fails. To avoid the need of "looking forward" and backtracking, it is necessary to change the grammar to LL(1) form.

Basically, a LL(1) grammar parser only needs to check one terminal symbol to decide which production should be chosen. This terminal is the next symbol given by the lexer. Hence, LL(1) grammar parsers do not need to backtrack. LL(2) grammars parsers would need to look to two symbols to decide which one to choose, and so on. It is important to note that grammars that are not LL(1) may be inefficient. As a consequence, compiling a programming language would be unfeasible.

LL(1) grammars do not have left recursions as well. However, a formal definition demands the concepts of FIRST and FOLLOW sets.

4.3.1.1 FIRST Set

Essentially, the FIRST set is the set of all terminal symbols that begin strings derived from a given variable. For instance, consider the following simple grammar:

$$\langle S \rangle \hspace{0.2cm} \models \hspace{0.2cm} \langle A \rangle \hspace{0.1cm} \langle B \rangle$$

$$\langle \mathbf{A} \rangle \hspace{0.2cm} \models \hspace{0.2cm} \lambda \mid \mathbf{a} \langle \mathbf{A} \rangle$$

$$\langle B \rangle \models b \mid b \langle B \rangle$$

Then, $FIRST(B) = \{b\}$, $FIRST(A) = \{\lambda, a\}$, $FIRST(S) = \{a, b\}$ (due to the λ -production). The FIRST set for the Mini-Java language can be found in Appendix A.3.

4.3.1.2 FOLLOW Set

Intuitively, the FOLLOW set of a non-terminal A is the set of all terminal symbols that can be found immediately to the right of A in some sentential form. Consider the following grammar as an example:

$$\langle S \rangle \models \langle A \rangle \langle B \rangle$$

$$\langle A \rangle \models \lambda \mid a \langle A \rangle$$

$$\langle B \rangle \models \lambda \mid b \langle B \rangle$$

Then, $FOLLOW(S) = FOLLOW(B) = \{\$\}$. Also, $FOLLOW(A) = \{\$, b\}$, since $FIRST(B) = \{\lambda, b\}$. The FOLLOW set for the Mini-Java language can be found in Appendix A.4.

4.3.1.3 LL(1) Grammar

Recall that a LL(1) grammar cannot be ambiguous neither have left-recursive productions. Also, a LL(1) may be able to determine which production was taken by looking only to the next terminal symbol. The grammar presented in this section generates the same language as the grammar in Section 3. However, the left recursive productions were removed and there are no "ambiguous" productions. A production may be ambiguous if a given non-terminal has two different productions with common elements in their FIRST set.

For instance, consider the grammar (which is not LL(1)):

$$\begin{array}{ccc} \langle S \rangle & \models & \langle A \rangle \mid \langle B1 \rangle \\ \langle A \rangle & \models & a \langle A \rangle \mid \langle B2 \rangle \\ \langle B2 \rangle & \models & b \mid b \langle B2 \rangle \\ \langle B1 \rangle & \models & \lambda \mid b \langle B1 \rangle \\ \end{array}$$

The grammar is not LL(1) because it is ambiguous. For example, b is in its language, however, it is impossible to know if b was generated by production B1 or B2.

The restrictions of LL(1) will only guarantee that a production can be chosen given the next terminal. For instance, consider the following grammar snippet:

$$\begin{array}{ccc} \langle \mathbf{S} \rangle & \models & \langle \mathbf{A} \rangle \; \langle \mathbf{B} \rangle \; | \; \langle \mathbf{C} \rangle \\ \langle \mathbf{A} \rangle & \models & \langle \alpha \rangle \; | \; \langle \beta \rangle \\ \end{array}$$

If the previous grammar is LL(1), then $FIRST(\alpha)$ and $FIRST(\beta)$ must be disjoint sets. Otherwise, the parser may not know which production to choose. A similar thought can be traced regarding FIRST(A) and FIRST(C).

In addition, if β generates λ , it will be necessary to check if $FIRST(\alpha)$ and FOLLOW(A) are disjoint sets. In other words, to guarantee that $FIRST(\alpha)$ and FIRST(B) are disjoint sets. Otherwise, the parser will not know which production between αB and βB (i.e. λB) was taken without backtracking.

Analogously, if β generates λ , it will be necessary to verify that FIRST(B) and FIRST(C) are disjoint sets.

The generated LL(1) grammar for the Mini-Java Language can be found in Appendix A.5.

4.3.1.4 Recursive Predictive Parser

The recursive definition of the Predictive Parse is rather intuitive. It basically consists on matching each non-terminal to a procedure.

If the procedure for non-terminal P is called, verify if the current token is in FIRST(P). If it is, consume that token and calls the procedures corresponding to the right side of the chosen production. If it does not match, then error. The procedure for the start symbol is called first, and this makes the parsing start.

mjc comes with a recursive predictive parser, which relies on recursive call for functions representing each non-terminal in the language LL(1) grammar. In order to execute it, follow these steps:

- 1. If bin/mjcll1 doesn't exist, execute, from the root directory, make ll1parser.
- 2. Having a program called program.mj, execute the following command from the root:
 - ./bin/mjcll1 R < /path/to/program.mj

Error Handling Two types of errors are handled differently in this parser. When some expected token is not encountered in the input, mjc inserts one of the expected tokens and continues the parsing process. When a non-terminal A cannot be consumed because none of the terminals in its first set is in the input, the parser skips the input sequence until some of the elements in the set $FIRST(A) \cup FOLLOW(A)$ is found. For example, for the problematic example in Appendix A.7, the output is:

```
Parsing with LL(1) recursive parsing.
              (1,9) parse error: unexpected string, expecting identifier (1,9) inserting identifier
       error]
mjc
        note
     warning
               (3,7) unknown character or sequence $
               (5,17) parse error: unexpected /, expecting identifier, \{, (, @, +, -,
[mjc
       error
    not, integer literal, string literal
[mjc
               (5,18) parse error: unexpected integer literal, expecting;,,
       error
               (5,18) inserting;
        note
                      parse error: unexpected ;, expecting identifier,
[mjc
               (5, 19)
    enddeclarations, int, string
[mjc
               (5,19) inserting enddeclarations
        note
               (6,5) parse error: unexpected enddeclarations, expecting }, method
mjc
       error
_{\rm mjc}
        note
                     inserting }
               (7,1) parse error: unexpected }, expecting class, eof
mjc
       error
                     inserting eof
mic
        finished. No output means no parse errors.
```

4.3.1.5 Non-Recursive Predictive Parser

The iterative version of the Predictive Parser focuses on simulating the calls made in the recursive algorithm. This is done with the help of another stack for the productions and a table called parse table, which associates productions to its terminal symbols in FIRST (check Appendix A.6 for the Mini-Java parse table). Whenever the production stack matches the symbol in the terminal stack, both are popped. Whenever a production is matched, it is popped from the production stack and the right side of the production is inserted into it.

For instance, consider the following grammar:

$$\begin{array}{ccc} \langle S \rangle & \models & \langle A \rangle \mid b \langle B \rangle \\ \langle A \rangle & \models & \lambda \mid a \langle A \rangle \\ \langle B \rangle & \models & \lambda \mid b \langle B \rangle \\ \end{array}$$

This grammar will generate the parse table found in Table 3:

	a	b	\$
S	A	bB	A
A	aA		λ
В		bB	λ

Table 3: Example of Parse Table

So, the behaviour for generating the empty string can be found in Table 4

Production Stack	Token Stack	Production Matched
S\$	\$	$S \to A$
A\$	\$	$A \rightarrow \lambda$
\$	\$	SUCCESS

Table 4: Generating the empty String using the example grammar

If trying to generate the string "bbb", the step-by-step process can be found in Table 5

Production Stack	Token Stack	Production Matched
S\$	bbb\$	$S \to bB$
bB\$	bbb\$	match and pop
B\$	bb\$	$\mathrm{B} o \mathrm{bB}$
bB\$	bb\$	match and pop
В\$	b\$	$\mathrm{B} o \mathrm{bB}$
bB\$	b\$	match and pop
В\$	\$	$\mathrm{B} o \lambda$
\$	\$	SUCCESS

Table 5: Generating String "bbb" using the example grammar

Lastly, the procedure of evaluating a String that is not in the language, e.g. "ab", can be found in Table 6.

Production Stack	Token Stack	Production Matched
S\$	ab\$	$S \to A$
A\$	ab\$	$\mathrm{A} o \mathrm{aA}$
aA\$	ab\$	match and pop
A\$	b\$	ERROR

Table 6: Trying to generate invalid String

mjc also comes equipped with a non-recursive predictive parser, which can be executed by following the steps below:

- 1. If bin/mjcll1 doesn't exist, execute, from the root directory, make ll1parser.
- 2. Having a program called program.mj, execute the following command from the root:
 - ./bin/mjcll1 N < /path/to/program.mj

Error Handling The compiler tries to match the current token with an element of the stack, in order to continue the parser. For that, it verify if the current token and top of stack have a production in parse table. If this is the case, then it pushes the production in stack and continues the parsing, otherwise it pops the stack and verifies again, while the stack is non empty. When a terminal is on top of the stack, but the current symbol doesn't match, an error message is shown and a pop is performed in the stack. If a non-terminal doesn't have an entry in the parse table for the current token, an error is shown and the stack is popped until a non-terminal is found whose predict set contains the current input token. For example, for the problematic example in Appendix A.7, the output is:

```
Parsing with LL(1) non-recursive parsing. 
 [mjc error] (1,9) parse error: unexpected string, expecting identifier [mjc error] (1,9) parse error: unexpected string, expecting; [mjc error] (1,9) parse error: unexpected string, expecting class Parsing finished. No output means no parse errors.
```

A Appendices

A.1 Mini-Java tokens

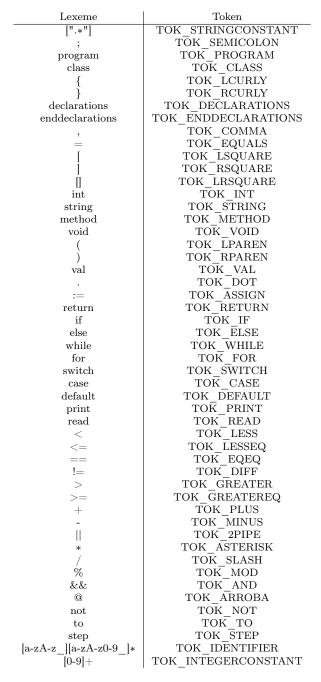


Table 7: Tokens of the Mini-Java language.

A.2 Quick-sort lexical analysis

Line	Column	Lexeme Size	Token	Lexeme
0	0	7	TOK PROGRAM	program
0	8	16	TOK IDENTIFIER	QuickSortProgram
0	24	1	TOK_SEMICOLON	;
2	0	5	TOK CLASS	class
$\overline{2}$	6	9	TOK IDENTIFIER	QuickSort
3	0	1	TOK LCURLY	{
4	1	6	TOK METHOD	method
4	8	4	TOK VOID	void
4	13	9	TOK IDENTIFIER	quickSort
4	22	1	TOK LPAREN	,
4	23	3	TOK_INT	(int
4	26	1	TOK_INT TOK LSQUARE	[
		1		l 1
4	27		TOK_RSQUARE	
4	29	1	TOK_IDENTIFIER	V
4	30	1	TOK_SEMICOLON	;
4	32	3	TOK_INT	int
4	36	5	TOK_IDENTIFIER	begin
4	41	1	TOK_SEMICOLON	;
4	43	3	TOK_INT	int
4	47	3	TOK_IDENTIFIER	end
4	50	1	TOK_RPAREN)
5	2	12	TOK_DECLARATIONS	declarations
6	12	3	TOK_INT	int
6	16	1	TOK_IDENTIFIER	i
6	18	1	TOK EQUALS	=
6	20	5	TOK IDENTIFIER	begin
6	25	1	TOK COMMA	,
6	27	1	TOK IDENTIFIER	j
6	29	1	TOK EQUALS	=
6	31	3	TOK IDENTIFIER	end
6	34	1	TOK MINUS	_
6	35	1	TOK INTEGERCONSTANT	1
6	36	1	TOK COMMA	-
6	38	5	TOK IDENTIFIER	pivot
6	44	1	TOK_IDENTIFIER	-
6		1	TOK_EGOALS TOK IDENTIFIER	=
	46		_	V
6	47	1	TOK_LSQUARE	[
6	48	1	TOK_LPAREN	(
6	49	5	TOK_IDENTIFIER	begin
6	55	1	TOK_PLUS	+ ,
6	57	3	TOK_IDENTIFIER	end
6	60	1	TOK_RPAREN)
6	61	1	TOK_SLASH	
6	62	1	TOK_INTEGERCONSTANT	2
6	63	1	$TOK_RSQUARE$]
6	64	1	TOK_COMMA	,
6	66	3	TOK_IDENTIFIER	aux
6	69	1	TOK_SEMICOLON	;
7	2	15	TOK_ENDDECLARATIONS	enddeclarations
8	1	1	TOK LCURLY	{
9	8	5	TOK WHILE	while
9	14	1	TOK IDENTIFIER	i
9	16	2	TOK LESSEQ	<=
9	19	1	TOK IDENTIFIER	j
10	8	1	TOK LCURLY	, {

Line	Column	Lexeme Size	Token	Lexeme
11	12	5	TOK_WHILE	while
11	18	1	TOK_LPAREN	(
11	19	1	TOK_IDENTIFIER	v
11	20	1	$TOK_LSQUARE$	[
11	21	1	TOK_IDENTIFIER	i
11	22	1	$TOK_RSQUARE$]
11	24	1	TOK_LESS	<
11	26	4	TOK_IDENTIFIER	pivo
11	31	2	TOK_AND	&&
11	34	1	TOK_IDENTIFIER	i
11	36	1	TOK_LESS	<
11	38	3	TOK_IDENTIFIER	$_{ m end}$
11	41	1	TOK_RPAREN)
12	12	1	TOK_LCURLY	{
13	16	1	TOK_IDENTIFIER	i
13	18	2	TOK_ASSIGN	:=
13	21	1	TOK_IDENTIFIER	i
13	23	1	TOK_PLUS	+
13	25	1	TOK_INTEGERCONSTANT	1
14	12	1	TOK_RCURLY	}
14	13	1	TOK_SEMICOLON	;
15	12	5	TOK_WHILE	while
15	18	1	TOK_LPAREN	(
15	19	1	TOK_IDENTIFIER	v
15	20	1	$TOK_LSQUARE$	[
15	21	1	TOK_IDENTIFIER	j
15	22	1	$TOK_RSQUARE$]
15	24	1	TOK_GREATER	>
15	26	4	TOK_IDENTIFIER	pivo
15	31	2	TOK_AND	&&
15	34	1	TOK_IDENTIFIER	j
15	36	1	TOK_GREATER	>
15	38	5	TOK_IDENTIFIER	begin
15	43	1	TOK_RPAREN)
16	12	1	TOK_LCURLY	{
17	16	1	TOK_IDENTIFIER	j
17	18	2	TOK_ASSIGN	:=
17	21	1	TOK_IDENTIFIER	j
17	23	1	TOK_MINUS	-
17	25	1	TOK_INTEGERCONSTANT	1
18	12	1	TOK_RCURLY	}
18	13	1	TOK_SEMICOLON	; :c
19	12	2	TOK_IF	if
19	15	1	TOK_IDENTIFIER	i
19	17	2	TOK_LESSEQ	<=
19	20	1	TOK_IDENTIFIER	J
20	12	1	TOK_LCURLY	{
21	16	3	TOK_IDENTIFIER	aux
21	20	2	TOK_ASSIGN	:=
21	23	1	TOK_IDENTIFIER	V [
21	24	1	TOK_LSQUARE	[
21	25 26	1	TOK_IDENTIFIER	i 1
21	26 27	1 1	TOK_RSQUARE TOK_SEMICOLON]
$\frac{21}{22}$	27 16	1	_	,
$\frac{22}{22}$	16 17	1	TOK_IDENTIFIER TOK_LSQUARE	V [
$\frac{22}{22}$	18	1	TOK_LSQUARE TOK_IDENTIFIER	[i
$\frac{22}{22}$	18 19	1	TOK_IDENTIFIER TOK_RSQUARE]
$\frac{22}{22}$	21	2	TOK ASSIGN] :=
	21	△	TOIZ WOOTGIA	<u>:-</u>

Line	Column	Lexeme Size	Token	Lexeme
22	24	1	TOK_IDENTIFIER	V
22	25	1	TOK_LSQUARE	[
22	26	1	TOK_IDENTIFIER	j
22	27	1	$TOK_RSQUARE$]
22	28	1	TOK_SEMICOLON	;
23	16	1	TOK_IDENTIFIER	V
23	17	1	$TOK_LSQUARE$	[
23	18	1	TOK_IDENTIFIER	j
23	19	1	TOK_RSQUARE]
23	21	2	TOK_ASSIGN	:=
23	24	3	TOK_IDENTIFIER	aux
23	27	1	TOK_SEMICOLON	;
24	16	1	TOK_IDENTIFIER	i
24	18	2	TOK_ASSIGN	:=
24	21	1	TOK_IDENTIFIER	i
24	23	1	TOK_PLUS	+
24	25	1	TOK_INTEGERCONSTANT	1
24	26	1	TOK_SEMICOLON	;
25	16	1	TOK_IDENTIFIER	j
25	18	1	TOK_EQUALS	=
25	20	1	TOK_IDENTIFIER	j
25	22	1	TOK_MINUS	-
25	24	1	TOK_INTEGERCONSTANT	1
26	12	1	TOK_RCURLY	} }
27	8	1 1	TOK_RCURLY	}
27	9		TOK_SEMICOLON	; if
$\frac{28}{28}$	8 11	2 1	TOK_IF TOK_IDENTIFIER	
28 28	13	1	TOK_IDENTIFIER TOK_GREATER	j >
28	15	5	TOK_GREATER TOK_IDENTIFIER	begin
29	8	1	TOK_LCURLY	{
30	12	9	TOK IDENTIFIER	quickSort
30	21	1	TOK LPAREN	(
30	22	1	TOK_IDENTIFIER	v
30	23	1	TOK COMMA	
30	25	5	TOK IDENTIFIER	begin
30	30	1	TOK COMMA	,
30	32	1	TOK IDENTIFIER	j
30	34	1	TOK PLUS	+
30	36	1	TOK INTEGERCONSTANT	1
30	37	1	TOK RPAREN)
31	8	1	TOK_RCURLY	}
31	9	1	TOK_SEMICOLON	;
32	8	2	TOK_IF	if
32	11	1	TOK_IDENTIFIER	i
32	13	1	TOK_LESS	<
32	15	3	TOK_IDENTIFIER	end
33	8	1	TOK_LCURLY	{
34	12	9	TOK_IDENTIFIER	quickSort
34	21	1	TOK_LPAREN	(
34	22	1	TOK_IDENTIFIER	v
34	23	1	TOK_COMMA	;
34	25	1	TOK_IDENTIFIER	i
34	26	1 3	TOK_COMMA TOK_IDENTIFIER	, and
$\frac{34}{34}$	28 31	3 1	TOK_IDENTIFIER TOK_RPAREN	end
$\frac{34}{35}$	8	1	TOK RCURLY) l
36	4	1	TOK RCURLY	}
37	0	1	TOK RCURLY	}
				J

A.3 First Set

Non Torminal	Final Cat
Non Terminal	First Set
PROGRAM	program
CLASS-DECL-LIST	λ ,class
CLASS-DECL	class
CLASS-BODY	{
DECLS-OPT	λ , declarations
DECLS	declarations
METHOD-DECL-LIST	λ ,method
FIELD-DECL-LIST-DECLS	λ ,id,int,string
FIELD-DECL	id,int,string
FIELD-DECL-AUX1	$=$, $,$ λ
FIELD-DECL-AUX2	$, \lambda$
TYPE	id,int,string
TYPE-AUX	id,int,string
BRACKETS-OPT	$[],\lambda$
METHOD-DECL	method
METHOD-RETURN-TYPE	void,id,int,string
FORMAL-PARAMS-LIST	val,id,int,string
FORMAL-PARAMS-LIST-AUX	$;,\lambda$
ID-LIST-COMMA	$, \lambda$
FORMAL-PARAMS-LIST-OPT	$\lambda, \text{val,id,int,string}$
	id
VAR-DECL-ID	
VAR-INIT	$\{,@,(,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id}\}$
ARRAY-INIT	{
VAR-INIT-LIST-COMMA	$,,\lambda$
ARRAY-CREATION-EXPR	@ r
ARRAY-DIM-DECL	\ [
ARRAY-DIM-DECL-LIST	λ ,
BLOCK	declarations,{
STMT-LIST	{
STMT-LIST-SEMICOLON	$;,\lambda$
STMT	id,return,if,while,for,switch,print,read
VARIABLE-START-STMT	:=,(
ASSIGN-STMT	:=
METHOD-CALL-STMT	(
ACTUAL-PARAMS-LIST	$\lambda, (,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
EXPRESSION-LIST-COMMA	$,,\lambda$
RETURN-STMT	return
EXPRESSION-OPT	$\lambda, (,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
IF-STMT	if
ELSE-PART	else, λ
IF-STMT-AUX	if,{
FOR-STMT	for
FOR-INIT-EXPR	id
STEP-OPT	$step, \lambda$
WHILE-STMT	while
SWITCH-STMT	switch
CASE	case
CASE-LIST	default, λ ,case
PRINT-STMT	print
READ-STMT	read
EXPRESSION	(,+,-,not,num,str,id
REL-EXPR	(,+,-,not,num,str,id
REL-EXPR-AUX	$\lambda, <, <=, ==, !=, >=, >$
ADD-EXPR	(,+,-,not,num,str,id
ADD-EXPR-AUX	$\lambda,+,-, $
Λυυ-ΕΛΓ Ν-ΑΟΛ	^,⊤, - ,

Non Terminal	First Set
MULT-EXPR	$(,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
MULT-EXPR-AUX	$\lambda, *, /, \&\&, \%$
UNARY-EXPR	(,+,-,not,num,str,id)
METHOD-CALL-OPT	λ ,(
REL-OP	<,<=,==,!=,>=,>
UNARY-OP	+,- $,$ not
ADD-OP	+,-,
MULT-OP	*,/,&&,%
UNSIG-LIT	$_{ m num,str}$
VARIABLE	id
VARIABLE-AUX	$.,\lambda,[$

A.4 Follow Set

Non Terminal	Follow Set
PROGRAM	\$
CLASS-DECL-LIST	\$ \$
CLASS-DECL	class,\$
CLASS-BODY	class,\$
DECLS-OPT	method,},{
DECLS	method,},{
METHOD-DECL-LIST	}
FIELD-DECL-LIST-DECLS	enddeclarations
FIELD-DECL	·
FIELD-DECL-AUX1	•
FIELD-DECL-AUX2	•
TYPE	, id,[
TYPE-AUX	[],id,[
BRACKETS-OPT	id,=,,,,,[
METHOD-DECL	method,}
METHOD-RETURN-TYPE	id
FORMAL-PARAMS-LIST)
FORMAL-PARAMS-LIST-AUX	
ID-LIST-COMMA	;,)
FORMAL-PARAMS-LIST-OPT)
VAR-DECL-ID	=, , ;;
VAR-INIT	,,,,,}
ARRAY-INIT	;;;}
VAR-INIT-LIST-COMMA	}
ARRAY-CREATION-EXPR	,;,}
ARRAY-DIM-DECL	[, , ,;,}
ARRAY-DIM-DECL-LIST	;;,}
BLOCK	method,}
STMT-LIST	method,},else,;,default,case
STMT-LIST-SEMICOLON	}
STMT	;,}
VARIABLE-START-STMT	;,}
ASSIGN-STMT	;,},to
METHOD-CALL-STMT	;,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
ACTUAL-PARAMS-LIST)
EXPRESSION-LIST-COMMA),]
RETURN-STMT	;,}
EXPRESSION-OPT	;,}
IF-STMT	;,}
ELSE-PART	;,}
IF-STMT-AUX	;,}

Non Terminal	Follow Set
FOR-STMT	;,}
FOR-INIT-EXPR	to
STEP-OPT	{
WHILE-STMT	;,}
SWITCH-STMT	;,}
CASE	default,case,}
CASE-LIST	}
PRINT-STMT	;,}
READ-STMT	;,}
EXPRESSION	,;,,],},,{,step,to
REL-EXPR	$, ; ,], \},), \{, \text{step,to} \}$
REL-EXPR-AUX	,
ADD-EXPR	<,<=,==,!=,>=,>,,,:,],,, $<,$ step,to
ADD-EXPR-AUX	<,<=,==,!=,>=,>, , ,;,],},),{,step,to
MULT-EXPR	$+,-, ,<,<=,==,!=,>=,>,,,:,],\},),\{,step,to$
MULT-EXPR-AUX	$+,-, ,<,<=,==,!=,>=,>,,,:,],\},),\{,step,to$
UNARY-EXPR	$*,/,\&\&,\%,+,-, ,<,<=,==,!=,>=,>,,,:,],\},),\{,step,to\}$
METHOD-CALL-OPT	$*,/,\&\&,\%,+,-, ,<,<=,==,!=,>=,>,,,:,],},),\{,step,to\}$
REL-OP	$(,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
UNARY-OP	$(,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
ADD-OP	$(,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
MULT-OP	$(,+,-,\mathrm{not},\mathrm{num},\mathrm{str},\mathrm{id})$
UNSIG-LIT	*,/,&&,%,+,-, ,<,<=,==,!=,>=,>, , ,;,],},),{,step,to
VARIABLE	$:=,(,*,/,\&\&,\%,+,-, ,<,<=,==,!=,>=,>,\;,\;,;,],\},),\{,step,to\}$
VARIABLE-AUX	$:=,(,*,/,\&\&,\%,+,-, ,<,<=,==,!=,>=,>,\;,\;,;,],\},),\{,step,to$

A.5 Numbered Grammar

Number	Grammar rule
0	PROGRAM ⊨ program id ; CLASS-DECL CLASS-DECL-LIST
1	$CLASS-DECL-LIST \models CLASS-DECL CLASS-DECL-LIST$
2	CLASS-DECL-LIST $\models \lambda$
3	$CLASS-DECL \models class id CLASS-BODY$
4	CLASS-BODY = DECLS-OPT METHOD-DECL-LIST
5	DECLS-OPT ⊨ DECLS
6	$DECLS-OPT \models \lambda$
7	DECLS = declarations FIELD-DECL-LIST-DECLS enddeclarations
8	$METHOD\text{-}DECL\text{-}LIST \models METHOD\text{-}DECL METHOD\text{-}DECL\text{-}LIST$
9	METHOD-DECL-LIST $\models \lambda$
10	FIELD-DECL-LIST-DECLS = FIELD-DECL ; FIELD-DECL-LIST-DECLS
11	FIELD-DECL-LIST-DECLS $\models \lambda$
12	FIELD-DECL = TYPE VAR-DECL-ID FIELD-DECL-AUX1
13	FIELD-DECL-AUX1 = FIELD-DECL-AUX2
14	FIELD-DECL-AUX1 \models = VAR-INIT FIELD-DECL-AUX2
15	FIELD-DECL-AUX2 \models , VAR-DECL-ID FIELD-DECL-AUX1
16	FIELD-DECL-AUX2 $\models \lambda$
17	TYPE ⊨ TYPE-AUX BRACKETS-OPT
18	TYPE-AUX = id
19	$TYPE-AUX \models int$
20	$TYPE-AUX \models string$
21	BRACKETS-OPT ⊨ [] BRACKETS-OPT
22	BRACKETS-OPT $\models \lambda$
23	METHOD-DECL = method METHOD-RETURN-TYPE id (FORMAL-PARAMS-LIST-OPT) BLOCK
$\frac{1}{24}$	METHOD-RETURN-TYPE = void
25	$METHOD-RETURN-TYPE \models TYPE$
26	FORMAL-PARAMS-LIST = val TYPE id ID-LIST-COMMA FORMAL-PARAMS-LIST-AUX
27	$FORMAL-PARAMS-LIST \models TYPE id ID-LIST-COMMA FORMAL-PARAMS-LIST-AUX$
28	$FORMAL-PARAMS-LIST-AUX \models ; FORMAL-PARAMS-LIST$
29	FORMAL-PARAMS-LIST-AUX $\models \lambda$
30	$ID-LIST-COMMA \models$, id $ID-LIST-COMMA$
31	ID-LIST-COMMA $\models \lambda$
32	$FORMAL-PARAMS-LIST-OPT \models FORMAL-PARAMS-LIST$
33	$FORMAL-PARAMS-LIST-OPT \models \lambda$
34	$VAR-DECL-ID \models id BRACKETS-OPT$
35	$VAR-INIT \models EXPRESSION$
36	$VAR-INIT \models ARRAY-INIT$
37	$VAR-INIT \models ARRAY-CREATION-EXPR$
38	$ARRAY-INIT \models VAR-INIT VAR-INIT-LIST-COMMA$
39	$VAR-INIT-LIST-COMMA \models$, $VAR-INIT VAR-INIT-LIST-COMMA$
40	VAR-INIT-LIST-COMMA $\models \lambda$
41	$ARRAY$ -CREATION-EXPR \models @ TYPE $ARRAY$ -DIM-DECL $ARRAY$ -DIM-DECL-LIST
42	$ARRAY-DIM-DECL \models [EXPRESSION]$
43	$ARRAY-DIM-DECL-LIST \models ARRAY-DIM-DECL ARRAY-DIM-DECL-LIST$
44	$ARRAY-DIM-DECL-LIST \models \lambda$
45	$BLOCK \models DECLS-OPT STMT-LIST$
46	$STMT-LIST \models STMT STMT-LIST-SEMICOLON$
47	$STMT-LIST-SEMICOLON \models ; STMT STMT-LIST-SEMICOLON$
48	$STMT-LIST-SEMICOLON \models \lambda$
49	$STMT \models VARIABLE VARIABLE-START-STMT$
50	$STMT \models RETURN-STMT$

Number	Grammar rule
51	$STMT \models IF-STMT$
52	$STMT \models WHILE-STMT$
53	$STMT \models FOR-STMT$
54	$STMT \models SWITCH-STMT$
55	$STMT \models PRINT-STMT$
56	$STMT \models READ-STMT$
57	$VARIABLE-START-STMT \models ASSIGN-STMT$
58	$VARIABLE-START-STMT \models METHOD-CALL-STMT$
59	$ASSIGN-STMT \models := EXPRESSION$
60	$METHOD\text{-}CALL\text{-}STMT \models (ACTUAL\text{-}PARAMS\text{-}LIST)$
61	ACTUAL-PARAMS-LIST ⊨ EXPRESSION EXPRESSION-LIST-COMMA
62	$ACTUAL-PARAMS-LIST \models \lambda$
63	EXPRESSION-LIST-COMMA ⊨, EXPRESSION EXPRESSION-LIST-COMMA
64	EXPRESSION-LIST-COMMA $\models \lambda$
65	$RETURN-STMT \models return EXPRESSION-OPT$
66	$EXPRESSION-OPT \models EXPRESSION$
67	EXPRESSION-OPT $\models \lambda$
68	$IF-STMT \models if EXPRESSION STMT-LIST ELSE-PART$
69	$ELSE-PART \models else IF-STMT-AUX$
70	ELSE-PART $\models \lambda$
71	$IF-STMT-AUX \models IF-STMT$
72	$IF-STMT-AUX \models STMT-LIST$
73	$FOR-STMT \models for FOR-INIT-EXPR to EXPRESSION STEP-OPT STMT-LIST$
74	$FOR-INIT-EXPR \models id ASSIGN-STMT$
75	$STEP-OPT \models step EXPRESSION$
76	$STEP-OPT \models \lambda$
77	WHILE-STMT \models while EXPRESSION STMT-LIST
78	$SWITCH-STMT \models switch EXPRESSION CASE CASE-LIST$
79	$CASE \models case EXPRESSION STMT-LIST$
80	$CASE-LIST \models CASE CASE-LIST$
81	$CASE-LIST \models default STMT-LIST$
82	$CASE-LIST \models \lambda$
83	$PRINT-STMT \models print EXPRESSION$
84	$READ-STMT \models read id$
85	$EXPRESSION \models REL-EXPR$
86	$REL-EXPR \models ADD-EXPR REL-EXPR-AUX$
87	$REL-EXPR-AUX \models REL-OP ADD-EXPR$
88	REL-EXPR-AUX $\models \lambda$
89	$ADD-EXPR \models MULT-EXPR ADD-EXPR-AUX$
90	$ADD-EXPR-AUX \models ADD-OP MULT-EXPR ADD-EXPR-AUX$
91	ADD-EXPR-AUX $\models \lambda$
92	MULT-EXPR = UNARY-EXPR MULT-EXPR-AUX
93	MULT-EXPR-AUX ⊨ MULT-OP UNARY-EXPR MULT-EXPR-AUX
94	$MULT-EXPR-AUX \models \lambda$

```
Number
           Grammar rule
95
           UNARY-EXPR \models UNARY-OP UNARY-EXPR
           UNARY-EXPR \models UNSIG-LIT
96
           UNARY-EXPR |= VARIABLE METHOD-CALL-OPT
97
98
           UNARY-EXPR \models (EXPRESSION)
99
           METHOD\text{-}CALL\text{-}OPT \models METHOD\text{-}CALL\text{-}STMT
100
           METHOD-CALL-OPT \models \lambda
101
           REL-OP \models <
           REL-OP ⊨ <=
102
103
           REL-OP \models ==
104
           REL-OP \models !=
           REL-OP \models >=
105
           REL-OP |= >
106
107
           UNARY-OP ⊨ +
108
           UNARY-OP \models -
           \text{UNARY-OP} \models \text{not}
109
110
           ADD-OP \models +
           ADD-OP ⊨ -
111
           ADD-OP \models ||
112
           MULT-OP \models *
113
114
           MULT-OP ⊨ /
115
           MULT-OP \models \&\&
           MULT-OP \models \%
116
117
           UNSIG-LIT \models num
118
           \mathrm{UNSIG\text{-}LIT} \models \mathrm{str}
119
           VARIABLE \models id VARIABLE-AUX
120
           VARIABLE-AUX \models . id VARIABLE-AUX
           VARIABLE-AUX \models \lambda
121
122
           VARIABLE-AUX ⊨ [ EXPRESSION EXPRESSION-LIST-COMMA ] VARIABLE-AUX
```

A.6 Parse Table

```
Non-terminal
                                       Grammar rules
PROGRAM
                                       (program, 0)
CLASS DECL LIST
                                       ( class, 1 ),( $, 2 )
CLASS_DECL
CLASS_BODY
DECLS_OPT
                                       (class, 3)
                                       ( \{, 4 )
                                       ( {, 6 ),( }, 6 ),( declarations, 5 ),( method, 6 )
DECLS
                                       (declarations, 7)
METHOD DECL LIST
                                       ( }, 9 ), ( method, 8 )
\begin{array}{c} {\rm FIELD\_D\bar{E}CL\_L\bar{I}\bar{S}T\_DECLS} \\ {\rm FIELD\_DECL} \end{array}
                                       ( id, 10 ),( enddeclarations, 11 ),( int, 10 ),( string, 10 )
                                       (id, 12),(int, 12),(string, 12)
FIELD_DECL_AUX1
                                       (;, 13), (=, 14), (;, 13)
{\tt FIELD\_DECL\_AUX2}
                                       (;, 16),(,, 15)
                                       ( id, 17 ),( int, 17 ),( string, 17 )
TYPE
TYPE AUX
                                       (id, 18),(int, 19),(string, 20)
BRACKETS OPT
                                        id, 22 ),( ;, 22 ),( =, 22 ),( ,, 22 ),( [], 21 ),( [, 22 )
METHOD DECL
                                       ( method, 23 )
METHOD_RETURN_TYPE
                                       (id, 25),(int, 25),(string, 25),(void, 24)
FORMAL_PARAMS_LIST
                                       ( id, 27 ),( int, 27 ),( string, 27 ),( val, 26 )
                                       (;, 28),(), 29)
FORMAL\_PARAMS\_LIST\_AUX
ID_LIST
                                       (;, 31),(,, 30),(), 31)
FORMAL PARAMS LIST OPT
                                       ( id, 32 ),( int, 32 ),( string, 32 ),( ), 33 ),( val, 32 )
VAR DECL ID
VAR INIT
                                       (id, 35), ({, 36}, (, 35), (@, 37), (+, 35), (-, 35), (not, 35), (num, 35),
                                       str, 35)
```

```
Non-Terminal
                                                                                                                                        Grammar rules
 ARRAY INIT
                                                                                                                                        (\{,38\})
  VAR INIT LIST
                                                                                                                                        (}, 40),(,, 39)
ARRAY_CREATION_EXPR
                                                                                                                                        (@, 41)
ARRAY DIM DECL
                                                                                                                                        ([, 42])
ARRAY\_DIM\_DECL\_LIST
                                                                                                                                        (;, 44),(}, 44),(,, 44),([, 43)
                                                                                                                                        ( {, 45 ),( declarations, 45 )
BLOCK
STMT LIST
STMT_LIST_SEMICOLON
                                                                                                                                        (;, 47), (\}, 48)
                                                                                                                                         (id, 49), (return, 50), (if, 51), (for, 53), (while, 52), (switch, 54), (print,
STMT
                                                                                                                                        55),( read, 56)
                                                                                                                                        ((,58),(:=,57)
VARIABLE START STMT
ASSIGN STMT
                                                                                                                                         (:=, 59)
METHOD CALL STMT
                                                                                                                                        ((,60))
ACTUAL PARAMS LIST
                                                                                                                                        (id, 61),((, 61),(), 62),(+, 61),(-, 61),(not, 61),(num, 61),(str, 61)
EXPRESSION LIST ,
                                                                                                                                        ( ,, 63 ),( ), 64 ),( ], 64 )
RETURN STMT
                                                                                                                                         (return, 65)
EXPRESSION OPT
                                                                                                                                        (id, 66), (;, 67), (;, 67), (;, 66), (;, 66), (;, 66), (;, 66), (;, 66), (;, 66), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), (;, 67), 
                                                                                                                                        str. 66)
IF STMT
                                                                                                                                        (if, 68)
\overline{\text{ELSE}}_{-}PART
                                                                                                                                        ( ;, 70 ),( }, 70 ),( else, 69 )
IF STMT AUX
                                                                                                                                         ( {, 72 ),( if, 71 )
FOR STMT
                                                                                                                                        ( for, 73 )
FOR INIT EXPR
                                                                                                                                        (id, 74)
STEP OPT
                                                                                                                                        ( {, 76 ),( step, 75 )
WHILE STMT
                                                                                                                                         ( while, 77 )
SWITCH\_STMT
                                                                                                                                          ( switch, 78 )
CASE
                                                                                                                                         (case, 79)
CASE LIST
                                                                                                                                        (), 82), (case, 80), (default, 81)
\begin{array}{c} \text{PRINT\_STMT} \\ \text{READ\_STMT} \end{array}
                                                                                                                                         ( print, 83 )
                                                                                                                                         ( read, 84 )
EXPRESSION
                                                                                                                                         ( id, 85 ),( (, 85 ),( +, 85 ),( -, 85 ),( not, 85 ),( num, 85 ),( str, 85 )
REL EXPR
                                                                                                                                        ( id, 86 ),( (, 86 ),( +, 86 ),( -, 86 ),( not, 86 ),( num, 86 ),( str, 86 )
REL EXPR AUX
                                                                                                                                        (;, 88),({, 88},(}, 88),(}, 88),(}, 88),(}, 88),(}, 88),(}, 1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1, 88),(1,
                                                                                                                                        87),( <=, 87),( ==, 87),( =, 87),( >=, 87),( >=, 87)
ADD EXPR
                                                                                                                                        ( id, 89 ),
( (, 89 ),
( +, 89 ),
( -, 89 ),
( not, 89 ),
( num, 89 ),
( str, 89 )
ADD EXPR AUX
                                                                                                                                         ( ;, 91 ), ( {, 91 }, {, 91 }, {, 91 }, {, 91 }, {, 91 }, {, 91 }, {, 91 }, {, 91 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 }, {, 100 },
                                                                                                                                        91),( <=, 91),( ==, 91),(!=, 91),( >=, 91),( >, 91),( +, 90),( -, 90),(
\mathrm{MULT}_{\mathrm{-}}\mathrm{EXPR}
                                                                                                                                         ( id, 92 ),( (, 92 ),( +, 92 ),( -, 92 ),( not, 92 ),( num, 92 ),( str, 92 )
MULT_EXPR_AUX
                                                                                                                                        ( ;, 94 ),( {, 94 ),( }, 94 ),( ,, 94 ),( ), 94 ),( ], 94 ),( to, 94 ),( step, 94 ),( <,
                                                                                                                                        94 ),( <=, 94 ),( ==, 94 ),( !=, 94 ),( >=, 94 ),( >, 94 ),( +, 94 ),( -, 94 ),(
                                                                                                                                        ||, 94 ),( *, 93 ),( /, 93 ),( &&, 93 ),( %, 93 )
UNARY EXPR
                                                                                                                                         (id, 97),((, 98),(+, 95),(-, 95),(not, 95),(num, 96),(str, 96)
METHOD CALL OPT
                                                                                                                                        (;, 100),({, 100),(}, 100),(,, 100),(,, 99),(), 100),(], 100),(to, 100
                                                                                                                                        ),
( step, 100 ),
( <, 100 ),
( <, 100 ),
( =, 100 ),
( =, 100 ),
( =, 100 ),
( >, 100 ),
( +, 100 ),
( -, 100 ),
( |+, 100 ),
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( |+, 100 ),
( |+, 100 ),
( |+, 100 ),
( |+, 100 ),
                                                                                                                                        (<, 101), (<=, 102), (==, 103), (!=, 104), (>=, 105), (>, 106)
REL OP
UNARY OP
                                                                                                                                        (+, 107),(-, 108),(not, 109)
ADD_OP
                                                                                                                                        ( \ +, \ 110 \ ), ( \ -, \ 111 \ ), ( \ ||, \ 112 \ )
\begin{array}{ccc} \mathrm{MULT\_OP} \\ \mathrm{UNSIG} & \mathrm{LIT} \end{array}
                                                                                                                                         ( *, 113 ),( /, 114 ),( &&, 115 ),( \%, 116 )
                                                                                                                                        ( num, 117 ),( str, 118 )
VARIABLE
                                                                                                                                        (id. 119)
VARIABLE AUX
                                                                                                                                        (;, 121),({, 121),(}, 121),(,, 121),((, 121),(), 121),([, 122),(], 121),(
                                                                                                                                        :=, 121 ),( to, 121 ),( step, 121 ),( <, 121 ),( <=, 121 ),( ==, 121 ),( !=, 121 ),( >=, 121 ),( >, 121 ),( +, 121 ),( -, 121 ),( ||, 121 ),( *, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( ||, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( *, 121 ),( 
                                                                                                                                        &&, 121 ),( %, 121 ),( ., 120 )
```

A.7 Example of a program with errors

```
program string;

class $oi {
    declarations
    int a = /2;
    enddeclarations
}
```