

First of all this is based on the book Using Mathematica for quantum mechanics by Roman Schmied, this is simply exercise 2.2

**Q2.2** The eigenstate basis for the description of the infinite square well of unit width is made up of the ortho-normalized functions

$$\langle x|n\rangle = \phi_n(x) = \sqrt{2} \sin(n\pi x) \quad (2.9)$$

defined on the interval  $[0, 1]$ , with  $n \in \{1, 2, 3, \dots\}$ .

1. Calculate the function  $P_\infty(x, y) = \langle x| [\sum_{n=1}^{\infty} |n\rangle \langle n|] |y\rangle$ .
2. In computer-based calculations we limit the basis set to  $n \in \{1, 2, 3, \dots, n_{\max}\}$  for some large value of  $n_{\max}$ . Using Mathematica, calculate the function  $P_{n_{\max}}(x, y) = \langle x| [\sum_{n=1}^{n_{\max}} |n\rangle \langle n|] |y\rangle$  (use the [Sum](#) function). Make a plot for  $n_{\max} = 10$  (use the [DensityPlot](#) function).
3. What does the function  $P$  represent?

1. For the First part we know that the  $\phi_n$  form a complete orthonormal basis therefore  $\sum_{n=1}^{\infty} |n\rangle \langle n| = 1$ , so we end up with  $P_\infty(x,y) = \langle x | y \rangle = \delta(x-y)$

2. So with finite n, we could simply use  $P_{n_{\max}}(x,y) = \sum_{n=1}^{n_{\max}} \langle x | n \rangle \langle n | y \rangle = 2 \sum_{n=1}^{n_{\max}} \sin(n \pi x) \sin(n \pi y)$  our variable for  $n_{\max}$  will be  $m$

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In[ ]:= m = 10
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Out[ ]:= 10
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In[ ]:= 10
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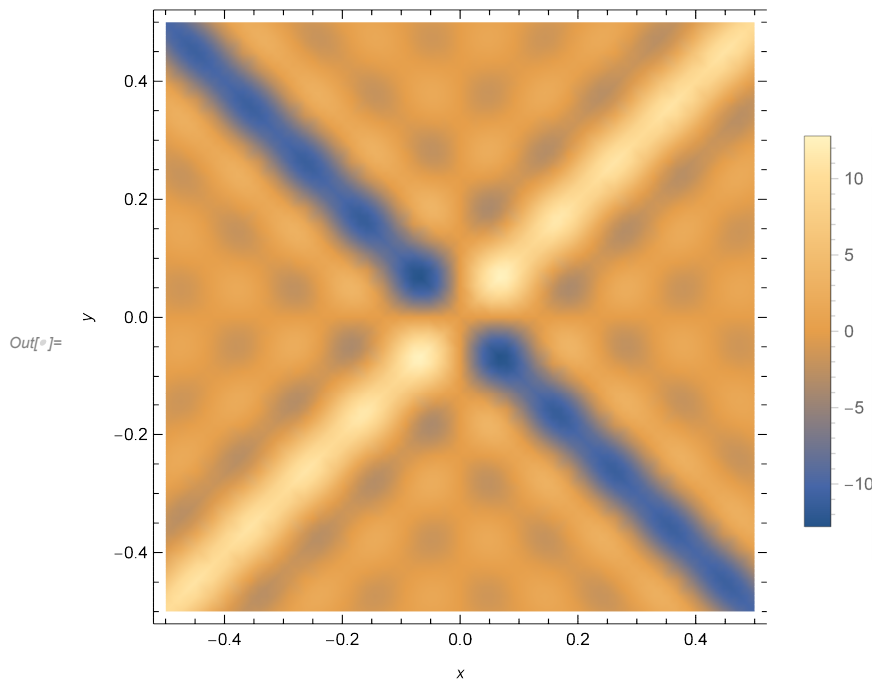
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Out[ ]:= 10
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In[ ]:= P[x_, y_] = 2 * Sum[Sin[n * π * x] * Sin[n * π * y], {n, m}];
```

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In[ ]:= DensityPlot[P[x, y], {x, -0.5, 0.5}, {y, -0.5, 0.5}, PlotRange -> All,
PlotPoints -> 2 * m, FrameLabel -> {x, y}, PlotLegends -> Automatic]

```



3. The function  $\Pi = \sum_{n=1}^{\infty} |n\rangle \langle n|$  is the projector onto the computational subspace, and  $P$  is its representation in coordinate space, when we truncate it, we leave it with finite spatial resolution