20210313-tarde-exercicio.R

rstudio-user

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```
# ANÁLISE MULTIVARIADA
# EXERCÍCIOS
# ANÁLISE FATORIAL
# 1) Usando o arquivo "Exerc A fatorial.xlsx", realize a análise fatorial, seguindo todos
# os passos, desde a verificação da adequação da característica dos dados para
# essa análise até chegar na visualização gráfica do modelo e suas cargas
# fatoriais.
# Pacotes e libs necessários
require(psych)
## Loading required package: psych
library(readxl)
library(zoo)
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
library(data.table)
# PASSO 1 - Importar os dados
data <- read_excel(</pre>
 "Exerc_A_fatorial.xlsx",
  col_types = c(
   "numeric",
    "numeric",
    "numeric",
    "numeric",
    "numeric",
    "numeric",
    "numeric",
    "numeric",
```

```
"numeric",
          "numeric",
          "numeric",
          "numeric",
          "numeric".
          "numeric",
          "numeric"
    )
\#data
# PASSO 2 - Verificar se os dados são numéricos
str(table)
## function (..., exclude = if (useNA == "no") c(NA, NaN), useNA = c("no",
                  "ifany", "always"), dnn = list.names(...), deparse.level = 1)
#
# PASSO 3 - Verificar se há dados faltantes
#is.na(data)
sum(is.na(data))
## [1] 731
#
# PASSO 4 - Tratar os dados faltantes definindo a média da coluna
                           usando as libs zoo e data.table
data <- na.aggregate(data)</pre>
data
## # A tibble: 2,800 x 28
##
                                                                                                                     C2
                                                                                                                                     C3
                                                                                                                                                    C4
                                                                                                                                                                                                   E2
                       A1 A2 A3
                                                                      Α4
                                                                                     A5
                                                                                                     C1
                                                                                                                                                                    C5
                                                                                                                                                                                    E1
                                                                                                                                                                                                                    E3
##
               <dbl> 
## 1
                2
                                                         3
                                                                                                       2
                                                                                                                                                                                      3
                                 4
                                                                       4
                                                                                4
                                                                                                                        3
                                                                                                                                       3
                                                                                                                                                       4
                                                                                                                                                                      4
                                                                                                                                                                                                      3 3
## 2
                         2
                                         4
                                                         5
                                                                         2
                                                                                        5
                                                                                                       5
                                                                                                                        4
                                                                                                                                       4
                                                                                                                                                       3
                                                                                                                                                                      4
                                                                                                                                                                                                      1 6
                                                                                                                                                                                      1
## 3
                         5
                                      4
                                                     5
                                                                    4
                                                                                    4
                                                                                                    4
                                                                                                                   5
                                                                                                                                    4
                                                                                                                                                   2
                                                                                                                                                                 5
                                                                                                                                                                                  2
                                                                                                                                                                                                   4 4
## 4
                        4
                                                        6
                                                                    5
                                                                                    5
                                                                                                    4
                                                                                                                        4
                                                                                                                                                   5
                                                                                                                                                                 5
                                                                                                                                                                                                     3 4
                                         4
                                                                                                                                       3
                                                                                                                                                                                  5
                                                                                                                                                   3
                                                                                                                                                              2
                     2
                                                                    4
                                                                                    5 4
## 5
                                         3
                                                        3
                                                                                                                   4
                                                                                                                                   5
                                                                                                                                                                                  2
                                                                                                                                                                                                      2 5
## 6
                     6
                                     6
                                                        5
                                                                    6 5 6
                                                                                                                   6
                                                                                                                                   6 1 3 2 1 6
```

```
##
               5
                     5
                           3
                                 5
                                       5
                                             4
                                                        2
                                                              3
##
               3
                     1
                           5
                                       3
                                                        2
                                                              4
                                                                             4
   8
         4
                                 1
                                             2
                                                  4
                                                                    3
                                                                          6
                                                                             4.00
##
   9
         4
               3
                     6
                           3
                                 3
                                       6
                                             6
                                                  3
                                                              5
                                                                    5
                                                                          3
                                       6
                                                        2
                                                                    2
                                                                          2
## 10
         2
               5
                     6
                           6
                                 5
                                             5
                                                  6
                                                              1
                                                                             4
## # ... with 2,790 more rows, and 15 more variables: E4 <dbl>, E5 <dbl>,
      N1 <dbl>, N2 <dbl>, N3 <dbl>, N4 <dbl>, N5 <dbl>, O1 <dbl>, O2 <dbl>,
      03 <dbl>, 04 <dbl>, 05 <dbl>, gender <dbl>, education <dbl>, age <dbl>
# PASSO 5 - Criar tabela de correlação
tablecor <- cor(data)
round(tablecor, 2)
                                                              C4
##
               Α1
                     A2
                           A3
                                       A5
                                            C1
                                                  C2
                                                        СЗ
                                                                    C5
                                                                          E1
                                 A4
## A1
             1.00 -0.34 -0.26 -0.15 -0.18
                                          0.03
                                                0.02 -0.02 0.13
                                                                  0.05
                                                                        0.11
## A2
            -0.34 1.00 0.48
                               0.33 0.39
                                          0.09 0.13 0.19 -0.14 -0.12 -0.21
## A3
            -0.26 0.48 1.00 0.36
                                    0.50 0.10 0.14 0.13 -0.12 -0.16 -0.21
                                    0.31 0.09 0.23 0.13 -0.15 -0.24 -0.11
## A4
            -0.15 0.33 0.36 1.00
## A5
            -0.18 0.39 0.50
                               0.31
                                    1.00
                                          0.12  0.11  0.13  -0.12  -0.17  -0.24
## C1
             0.03 0.09 0.10 0.09 0.12 1.00 0.42 0.31 -0.34 -0.25 -0.02
## C2
             0.02 0.13 0.14 0.23
                                    0.11
                                          0.42 1.00 0.35 -0.38 -0.30
## C3
            -0.02 0.19 0.13 0.13 0.13 0.31 0.35 1.00 -0.33 -0.34
                                                                        0.00
             0.13 -0.14 -0.12 -0.15 -0.12 -0.34 -0.38 -0.33
## C4
                                                            1.00
                                                                  0.47
                                                                        0.09
## C5
             0.05 -0.12 -0.16 -0.24 -0.17 -0.25 -0.30 -0.34 0.47
                                                                  1.00
                                                                        0.06
## E1
             0.11 -0.21 -0.21 -0.11 -0.24 -0.02 0.02 0.00 0.09
                                                                  0.06
                                                                        1.00
             0.09 -0.23 -0.28 -0.19 -0.33 -0.09 -0.06 -0.08 0.20 0.26
## E2
                                                                       0.46
## E3
            -0.05 0.25 0.39 0.19 0.41 0.12 0.15 0.09 -0.08 -0.16 -0.32
## E4
            -0.06 0.28 0.38 0.30 0.47 0.14 0.12 0.09 -0.11 -0.20 -0.42
## E5
            -0.02 0.29 0.25 0.16 0.27 0.25 0.24 0.21 -0.23 -0.23 -0.30
## N1
             0.16 -0.09 -0.08 -0.10 -0.19 -0.07 -0.02 -0.07
                                                           0.22
                                                                  0.21
                                                                       0.02
## N2
             0.14 -0.05 -0.09 -0.14 -0.19 -0.04 -0.01 -0.06 0.16
                                                                  0.25
                                                                        0.01
             0.10 -0.04 -0.04 -0.07 -0.13 -0.03 0.00 -0.07 0.21
## N3
                                                                  0.24
                                                                        0.05
## N4
             0.05 - 0.09 - 0.13 - 0.17 - 0.20 - 0.10 - 0.04 - 0.11 0.26
                                                                  0.34
                                                                        0.23
             0.02 0.02 -0.04 -0.01 -0.08 -0.05 0.05 -0.01
## N5
                                                           0.19
                                                                  0.17
## 01
             0.01 0.13 0.15 0.06 0.16 0.17 0.16 0.09 -0.09 -0.08 -0.10
## 02
             0.08 0.02 0.00 0.04 0.00 -0.11 -0.04 -0.03 0.21 0.14 0.04
            -0.06 0.16 0.22 0.07 0.24 0.19 0.19 0.06 -0.08 -0.08 -0.22
## 03
## 04
                        0.04 -0.04 0.02 0.11 0.06 0.02 0.05
                                                                  0.14
            -0.08 0.09
             0.11 -0.09 -0.05 0.02 -0.05 -0.12 -0.05 -0.01 0.20 0.06 0.10
## 05
## gender
            -0.16 0.18 0.14 0.13 0.10 0.01 0.07 0.05 -0.08 -0.09 -0.13
                                          0.02 0.00 0.05 -0.03
## education -0.13 0.01
                         0.00 - 0.01
                                    0.01
                                                                  0.03
                                                                       0.00
                                                0.02
## age
            -0.16
                  0.11
                         0.07
                               0.14
                                     0.13
                                          0.08
                                                      0.07 -0.15 -0.09
                                                                       -0.03
##
                     E3
                           E4
                                 E5
                                       N1
                                            N2
                                                  NЗ
                                                        N4
                                                              N5
                                                                    01
                                                                          02
               E2
## A1
             0.09 -0.05 -0.06 -0.02 0.16 0.14 0.10 0.05
                                                            0.02
                                                                  0.01
                                                                        0.08
## A2
            -0.23
                  0.25
                         0.28 0.29 -0.09 -0.05 -0.04 -0.09 0.02
                                                                  0.13
                                                                        0.02
## A3
            -0.28 0.39 0.38 0.25 -0.08 -0.09 -0.04 -0.13 -0.04
                                                                  0.15
                                                                        0.00
            -0.19 0.19 0.30 0.16 -0.10 -0.14 -0.07 -0.17 -0.01
## A4
                                                                  0.06
                                                                        0.04
## A5
            -0.33 0.41 0.47 0.27 -0.19 -0.19 -0.13 -0.20 -0.08
                                                                  0.16
                                                                       0.00
            -0.09 0.12 0.14 0.25 -0.07 -0.04 -0.03 -0.10 -0.05
## C1
                                                                  0.17 - 0.11
## C2
            -0.06 0.15 0.12 0.24 -0.02 -0.01 0.00 -0.04 0.05 0.16 -0.04
            -0.08 0.09 0.09 0.21 -0.07 -0.06 -0.07 -0.11 -0.01 0.09 -0.03
## C3
## C4
             0.20 -0.08 -0.11 -0.23 0.22 0.16 0.21 0.26 0.19 -0.09
## C5
             0.26 -0.16 -0.20 -0.23 0.21
                                          0.25
                                                0.24 0.34 0.17 -0.08
```

0.46 - 0.32 - 0.42 - 0.30 0.02 0.01 0.05 0.23 0.05 - 0.10 0.04

E1

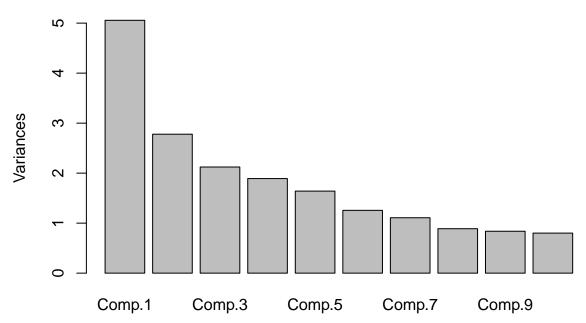
```
1.00 -0.38 -0.51 -0.37 0.17 0.19 0.20 0.34 0.25 -0.16 0.08
## E2
## E3
           -0.38 1.00 0.42 0.38 -0.05 -0.07 -0.02 -0.14 -0.07
                                                              0.32 - 0.07
## E4
           -0.51 0.42 1.00 0.31 -0.13 -0.14 -0.10 -0.29 -0.09
           ## E5
## N1
            0.17 -0.05 -0.13
                             0.04
                                  1.00 0.70 0.55
                                                  0.40
                                                        0.38 -0.05
## N2
            0.19 -0.07 -0.14 0.04 0.70 1.00 0.55 0.39 0.35 -0.05
                                                                    0.13
            0.20 -0.02 -0.10 -0.06
                                  0.55
                                        0.55
                                             1.00 0.52 0.43 -0.03
## N3
            0.34 -0.14 -0.29 -0.21
                                        0.39 0.52 1.00
## N4
                                  0.40
                                                        0.39 - 0.05
                                                                    0.08
## N5
            ## 01
## 02
            ## 03
           -0.23 0.39 0.21 0.29 -0.05 -0.03 -0.03 -0.06 -0.07 0.39 -0.26
## 04
            0.17 \quad 0.05 \quad -0.10 \quad 0.00 \quad 0.08 \quad 0.13 \quad 0.18 \quad 0.21 \quad 0.11 \quad 0.18 \quad -0.07
            0.08 - 0.11 \quad 0.05 - 0.11 \quad 0.11 \quad 0.04 \quad 0.06 \quad 0.04 \quad 0.13 - 0.24 \quad 0.32
## 05
           -0.05 0.04 0.08 0.07 0.04 0.10 0.12 0.00 0.21 -0.10 0.03
## gender
## education -0.01
                 0.00 - 0.04
                             0.05 -0.04 -0.04 -0.05 0.01 -0.05
                                                              0.03 -0.08
           -0.10 0.00 -0.01 0.11 -0.09 -0.10 -0.11 -0.03 -0.10 0.05 -0.04
## age
##
              03
                    04
                         05 gender education
                                              age
           -0.06 -0.08 0.11
## A1
                             -0.16
                                       -0.13 - 0.16
## A2
            0.16 0.09 -0.09
                              0.18
                                       0.01 0.11
## A3
            0.22 0.04 -0.05
                              0.14
                                       0.00 0.07
## A4
            0.07 -0.04 0.02
                              0.13
                                       -0.01
                                            0.14
## A5
            0.24 0.02 -0.05
                                       0.01
                                            0.13
                              0.10
## C1
            0.19
                 0.11 -0.12
                              0.01
                                            0.08
                                       0.02
## C2
            0.19 0.06 -0.05
                              0.07
                                       0.00 0.02
## C3
            0.06 0.02 -0.01
                              0.05
                                       0.05 0.07
## C4
           -0.08 0.05 0.20
                             -0.08
                                      -0.03 -0.15
## C5
           -0.08 0.14 0.06
                             -0.09
                                       0.03 -0.09
## E1
           -0.22 0.08 0.10
                             -0.13
                                       0.00 -0.03
## E2
           -0.23 0.17 0.08
                             -0.05
                                      -0.01 -0.10
## E3
            0.39 0.05 -0.11
                              0.04
                                       0.00 0.00
## E4
            0.21 -0.10 0.05
                              0.08
                                      -0.04 -0.01
## E5
            0.29 0.00 -0.11
                              0.07
                                       0.05 0.11
## N1
           -0.05 0.08 0.11
                              0.04
                                      -0.04 -0.09
## N2
           -0.03 0.13 0.04
                              0.10
                                      -0.04 - 0.10
## N3
           -0.03 0.18 0.06
                                      -0.05 -0.11
                              0.12
## N4
           -0.06 0.21 0.04
                              0.00
                                       0.01 - 0.03
## N5
           -0.07 0.11 0.13
                              0.21
                                      -0.05 -0.10
## 01
            0.39 0.18 -0.24
                             -0.10
                                       0.03 0.05
## 02
           -0.26 -0.07 0.32
                              0.03
                                      -0.08 -0.04
## 03
            1.00 0.19 -0.31
                             -0.04
                                       0.09 0.04
## 04
            0.19 1.00 -0.18
                              0.00
                                       0.05 0.01
## 05
           -0.31 -0.18 1.00
                              0.02
                                       -0.05 - 0.10
           -0.04 0.00 0.02
                              1.00
                                       0.01 0.05
## gender
## education 0.09 0.05 -0.05
                              0.01
                                       1.00
                                            0.23
            0.04 0.01 -0.10
                              0.05
                                       0.23
                                            1.00
## age
#
# PASSO 6 - Apresentar a matriz de correlação
corrplot::corrplot(tablecor, method = "circle")
```

```
8.0
A4512CC344CC512EE344ST12N33N45100034CS5gender education
                                                                          0.6
                                                                          0.4
                                                                          0.2
                                                                           0
                                                                          -0.2
                                                                          -0.4
                                                                          -0.6
                                                                         -0.8
# PASSO 7 - Realizar o teste de esfericidade (Bartlett)
cortest.bartlett(data)
## R was not square, finding R from data
## $chisq
## [1] 20886.2
##
## $p.value
## [1] 0
##
## $df
## [1] 378
# O teste indica que não é uma Matriz de Identidade, pois não atende: (p>0,05)
# PASSO 8 - Realizar o teste KMO
KMO(data)
## Kaiser-Meyer-Olkin factor adequacy
## Call: KMO(r = data)
## Overall MSA = 0.84
```

```
## MSA for each item =
##
                             A3
                                                   A5
                                                              C1
                                                                        C2
                                                                                  C3
          A 1
                  A2
                                         A4
                                                            0.83
##
        0.76
                  0.85
                            0.87
                                       0.86
                                                 0.90
                                                                      0.78
                                                                                0.84
          C4
                             E1
                                                   ЕЗ
##
                    C5
                                         E2
                                                             E4
                                                                        E5
                                                                                  N1
##
        0.83
                  0.86
                            0.84
                                       0.88
                                                 0.89
                                                            0.87
                                                                      0.89
                                                                                0.78
##
          N2
                    NЗ
                              N4
                                         N5
                                                   01
                                                              02
                                                                        03
                                                                                  04
##
        0.78
                  0.86
                            0.88
                                       0.85
                                                 0.85
                                                            0.77
                                                                      0.84
                                                                                0.77
##
          05
                gender education
                                        age
##
        0.76
                  0.71
                             0.59
                                       0.67
#
# Quando MSA maior que 0,5 na análise KMO, então indica que a análise
# fatorial é adequada para o conjunto de dados
#
# PASSO 9 - Realizar a análise de componentes principais
fit <- princomp(data, cor = TRUE)</pre>
fit
## Call:
## princomp(x = data, cor = TRUE)
##
## Standard deviations:
##
      Comp.1
                Comp.2
                          Comp.3
                                     Comp.4
                                               Comp.5
                                                          Comp.6
                                                                    Comp.7
                                                                              Comp.8
## 2.2486256 1.6669375 1.4568856 1.3752625 1.2808576 1.1206502 1.0525531 0.9426700
      Comp.9
               Comp.10
                         Comp.11
                                    Comp.12
                                              Comp.13
                                                        Comp.14
                                                                   Comp.15
##
                                                                             Comp.16
## 0.9152718 0.8948278 0.8698727 0.8391293 0.8283451 0.8196937 0.8074144 0.7933696
                                                                   Comp.23
     Comp.17
               Comp.18
                         Comp.19
                                    Comp.20
                                              Comp.21
                                                        Comp.22
## 0.7605745 0.7415045 0.7314891 0.7234228 0.7079037 0.6955327 0.6688457 0.6568648
     Comp.25
               Comp.26
                         Comp.27
                                    Comp.28
## 0.6418048 0.6295751 0.6202402 0.5254656
##
  28 variables and 2800 observations.
##
#
# Com o summary de fit, temos um entendimento maior da análise
summary(fit)
## Importance of components:
                                        Comp.2
                                                   Comp.3
                                                               Comp.4
                             Comp.1
                                                                          Comp.5
## Standard deviation
                          2.2486256 1.6669375 1.45688565 1.37526252 1.28085761
## Proportion of Variance 0.1805828 0.0992386 0.07580414 0.06754811 0.05859272
## Cumulative Proportion 0.1805828 0.2798214 0.35562549 0.42317359 0.48176632
##
                                                     Comp.8
                               Comp.6
                                          Comp.7
                                                                 Comp.9
## Standard deviation
                           1.12065024 1.05255314 0.94267003 0.91527179 0.89482782
## Proportion of Variance 0.04485203 0.03956672 0.03173667 0.02991866 0.02859703
## Cumulative Proportion 0.52661835 0.56618507 0.59792174 0.62784040 0.65643743
##
                              Comp.11
                                         Comp.12
                                                    Comp.13
                                                                Comp.14
                                                                           Comp.15
## Standard deviation
                           0.86987267 0.83912935 0.82834510 0.81969370 0.80741440
## Proportion of Variance 0.02702423 0.02514779 0.02450556 0.02399635 0.02328279
## Cumulative Proportion 0.68346166 0.70860945 0.73311500 0.75711135 0.78039414
##
                              Comp.16
                                         Comp.17
                                                    Comp.18
                                                                Comp.19
                                                                           Comp.20
## Standard deviation
                          0.79336961 \ 0.76057447 \ 0.74150445 \ 0.73148913 \ 0.72342282
```

```
## Proportion of Variance 0.02247983 0.02065977 0.01963674 0.01910987 0.01869073
## Cumulative Proportion 0.80287397 0.82353374 0.84317049 0.86228036 0.88097109
                                                   Comp.23
##
                             Comp.21
                                        Comp.22
                                                               Comp.24
## Standard deviation
                          0.70790372 0.69553266 0.66884569 0.65686475 0.64180482
## Proportion of Variance 0.01789742 0.01727735 0.01597695 0.01540969 0.01471119
## Cumulative Proportion 0.89886851 0.91614585 0.93212280 0.94753249 0.96224368
                             Comp.26
                                        Comp.27
                                                    Comp.28
                          0.62957506 0.62024022 0.525465642
## Standard deviation
## Proportion of Variance 0.01415588 0.01373921 0.009861219
## Cumulative Proportion 0.97639957 0.99013878 1.000000000
# Apresentando o resultado através de gráfico de barras
# \acute{E} possível verificar que 7 fatores possuem variância maior que 1
# e devem ser considerados
screeplot(fit)
```

fit

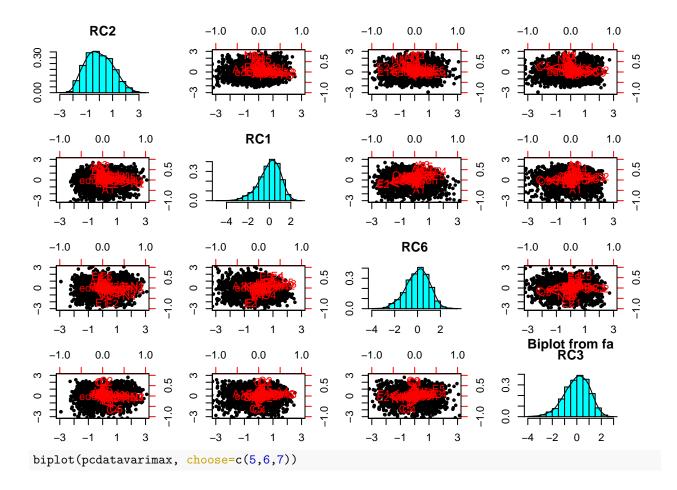


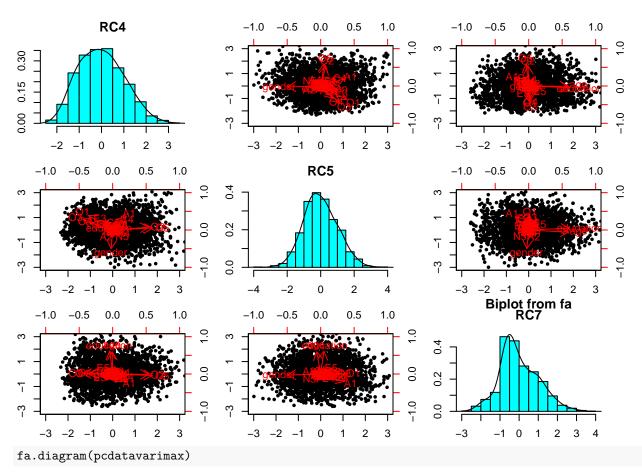
```
#
# Apresentando o resultado através de gráfico de linhas
#
plot(fit, type = "lines")
```

```
0
     2
Variances
     \mathcal{C}
     ^{\circ}
                         Comp.3
         Comp.1
                                        Comp.5
                                                       Comp.7
                                                                       Comp.9
# Rodando a Análise de Componentes Principais (sem rotacionar)
pcdata <- principal(data, nfactors = 7, n.obs = 2800, rotate = "none", scores = TRUE)
pcdata
## Principal Components Analysis
## Call: principal(r = data, nfactors = 7, rotate = "none", n.obs = 2800,
##
       scores = TRUE)
## Standardized loadings (pattern matrix) based upon correlation matrix
                     PC2
                           PC3
##
               PC1
                                  PC4
                                        PC5
                                              PC6
                                                    PC7
                                                          h2
## A1
             -0.26 -0.03
                          0.12
                                0.00 - 0.66
                                             0.15 0.18 0.57 0.43 1.7
## A2
              0.49
                    0.33 - 0.17
                                0.11
                                       0.38
                                             0.08 -0.07 0.56 0.44 3.3
## A3
              0.55
                    0.33 -0.26
                                0.05
                                       0.25
                                             0.21 -0.03 0.59 0.41 3.0
## A4
              0.44
                    0.15 - 0.17
                                0.31
                                       0.19
                                             0.17
                                                   0.05 0.41 0.59 3.4
## A5
              0.61
                    0.21 -0.28 -0.01
                                       0.14
                                             0.22
                                                  0.09 0.57 0.43 2.2
## C1
                    0.12
                          0.51
                                0.23 - 0.14
                                             0.09
                                                   0.09 0.49 0.51 2.8
                                             0.17
## C2
                                0.40 - 0.12
              0.35
                    0.21
                          0.47
                                                   0.04 0.60 0.40 3.8
## C3
              0.34
                    0.07
                          0.36
                                0.45 - 0.04
                                             0.05
                                                   0.11 0.47 0.53 3.1
## C4
             -0.49
                    0.14 -0.42 -0.33
                                      0.01
                                             0.23
                                                   0.17 0.63 0.37 3.8
## C5
                   0.18 -0.22 -0.39
                                       0.15
                                             0.09
                                                   0.14 0.55 0.45 3.0
             -0.52
## E1
             -0.44 - 0.21
                          0.32
                                0.21
                                       0.21
                                             0.38 0.14 0.59 0.41 4.7
                                      0.26
                                             0.28 -0.02 0.64 0.36 2.3
## E2
             -0.63 - 0.03
                          0.28
                                0.13
## E3
              0.56
                   0.34 -0.12 -0.26 -0.18
                                             0.14 0.05 0.56 0.44 2.7
## E4
              0.60
                    0.20 -0.39 0.01 -0.25
                                            0.06 0.05 0.62 0.38 2.4
## E5
                    0.30
                          0.10 -0.05 -0.25 -0.21
                                                   0.18 0.54 0.46 2.7
              0.55
## N1
             -0.43
                    0.64
                          0.04
                                0.05 -0.22 -0.24
                                                   0.07 0.71 0.29 2.4
             -0.42
                    0.65
                          0.09
                                0.03 -0.17 -0.26
## N2
                                                  0.00 0.70 0.30 2.3
## N3
             -0.41
                    0.68
                          0.06  0.04  -0.04  -0.07  -0.04  0.64  0.36  1.7
## N4
             -0.54
                    0.46
                          0.15 - 0.04
                                      0.20 0.08
                                                  0.07 0.57 0.43 2.5
## N5
             -0.36
                                0.25
                                            0.05 -0.12 0.51 0.49 2.5
                    0.53 - 0.05
                                       0.11
## 01
              0.36
                    0.20
                         0.32 -0.42 -0.10 0.22 0.11 0.52 0.48 4.3
```

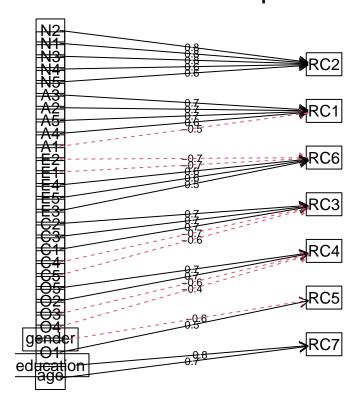
```
## 02
            -0.22 0.14 -0.42 0.37 -0.08 0.20 0.32 0.53 0.47 4.3
## O3
             -0.06 0.31 0.33 -0.26 0.32 0.30 -0.02 0.48 0.52 4.9
## 04
## 05
            -0.24 -0.02 -0.41 0.43 -0.19 0.16 0.31 0.56 0.44 4.2
## gender
             0.10 0.26 -0.14 0.31 0.24 -0.34 -0.37 0.51 0.49 5.1
## education 0.07 -0.04 0.14 -0.13 0.34 -0.35 0.56 0.59 0.41 2.8
             0.21 -0.06 0.10 0.03 0.40 -0.36 0.49 0.59 0.41 3.4
## age
##
##
                        PC1 PC2 PC3 PC4 PC5 PC6 PC7
## SS loadings
                       5.06 2.78 2.12 1.89 1.64 1.26 1.11
## Proportion Var
                       0.18 0.10 0.08 0.07 0.06 0.04 0.04
                       0.18 0.28 0.36 0.42 0.48 0.53 0.57
## Cumulative Var
## Proportion Explained 0.32 0.18 0.13 0.12 0.10 0.08 0.07
## Cumulative Proportion 0.32 0.49 0.63 0.75 0.85 0.93 1.00
##
## Mean item complexity = 3.2
## Test of the hypothesis that 7 components are sufficient.
##
## The root mean square of the residuals (RMSR) is 0.05
## with the empirical chi square 6091.66 with prob < 0
##
## Fit based upon off diagonal values = 0.92
# Rodando a Análise de Componentes Principais (com rotação varimax)
# Agora é possível verificar a relação de variáveis em relação aos fatores
pcdatavarimax <- principal(data, nfactors = 7, n.obs = 2800, rotate = "varimax", scores = TRUE)
pcdatavarimax
## Principal Components Analysis
## Call: principal(r = data, nfactors = 7, rotate = "varimax", n.obs = 2800,
      scores = TRUE)
## Standardized loadings (pattern matrix) based upon correlation matrix
##
             RC2
                   RC1
                         RC6
                              RC3
                                          RC5
                                    RC4
                                               RC7
                                                     h2
## A1
             0.13 -0.46 0.11 0.12 0.25 0.45 -0.25 0.57 0.43 3.6
## A2
             0.02 0.70 0.11 0.11 -0.10 -0.17 0.08 0.56 0.44 1.3
                             0.08 -0.04 -0.01 -0.02 0.59 0.41 1.2
## A3
            -0.03 0.74 0.20
## A4
            -0.10 0.55 0.08 0.24 0.17 -0.08 0.03 0.41 0.59 1.8
## A5
            -0.15 0.67 0.28 0.07 0.00 0.11 0.03 0.57 0.43 1.6
             0.01 0.05 0.03 0.66 -0.14 0.17 0.04 0.49 0.51 1.2
## C1
## C2
             0.08 0.16 -0.03 0.74 -0.04
                                        0.11 -0.05 0.60 0.40 1.2
## C3
            -0.02 0.13 -0.02 0.67 0.06 0.00 0.08 0.47 0.53 1.1
## C4
             0.24 0.01 -0.13 -0.65 0.21
                                        0.28 -0.07 0.63 0.37 2.1
## C5
             0.31 -0.05 -0.21 -0.60 0.01 0.20 0.06 0.55 0.45 2.1
## E1
            -0.02 -0.15 -0.72 0.10 0.14 0.15 0.01 0.59 0.41 1.3
## E2
             ## E3
             0.02 0.43 0.49 0.07 -0.19 0.31 -0.08 0.56 0.44 3.2
## E4
            -0.12 0.44 0.60 0.08 0.14
                                        0.12 -0.11 0.62 0.38 2.3
## E5
             0.08 0.17 0.56 0.35 -0.14 0.16 0.17 0.54 0.46 2.5
## N1
             0.81 -0.19 0.10 -0.03 0.10 0.01 0.01 0.71 0.29 1.2
## N2
             0.81 -0.18 0.08 -0.02 0.01 -0.04 0.00 0.70 0.30 1.1
## N3
             0.79 -0.01 -0.06 -0.05 0.00 -0.02 -0.07 0.64 0.36 1.0
## N4
             0.62 -0.02 -0.39 -0.16 -0.04 0.08 0.05 0.57 0.43 1.9
             0.62  0.14  -0.21  -0.02  0.14  -0.17  -0.13  0.51  0.49  1.7
## N5
```

```
0.00 0.17 0.16 0.15 -0.45 0.49 0.02 0.52 0.48 2.7
## 01
## N2
           ## 03
           0.04 0.24 0.25 0.09 -0.56 0.35 0.02 0.56 0.44 2.7
## 04
           ## 05
           0.22 0.22 0.11 0.09 -0.03 -0.62 -0.04 0.51 0.49 1.7
## gender
## education -0.01 -0.02 0.00 -0.01 -0.06 0.06 0.76 0.59 0.41 1.0
          -0.09 0.10 0.02 0.09 -0.01 -0.07 0.75 0.59 0.41 1.1
##
##
                     RC2 RC1 RC6 RC3 RC4 RC5 RC7
## SS loadings
                     3.16 2.81 2.62 2.54 1.99 1.42 1.31
## Proportion Var
                    0.11 0.10 0.09 0.09 0.07 0.05 0.05
## Cumulative Var
                    0.11 0.21 0.31 0.40 0.47 0.52 0.57
## Proportion Explained 0.20 0.18 0.17 0.16 0.13 0.09 0.08
## Cumulative Proportion 0.20 0.38 0.54 0.70 0.83 0.92 1.00
##
## Mean item complexity = 1.8
## Test of the hypothesis that 7 components are sufficient.
## The root mean square of the residuals (RMSR) is 0.05
## with the empirical chi square 6091.66 with prob < 0
## Fit based upon off diagonal values = 0.92
# PASSO 10 - Interpretação dos fatores e análise dos componentes
biplot(pcdatavarimax, choose=c(1,2,3,4))
```





Components Analysis



```
#
# Relações identificadas (Fator x Variáveis)
# RC2 - N2, N1, N3, N4, N5
# RC1 - A3, A2, A5, A4, A1
# RC6 - E2, E1, E4, E5, E3
# RC3 - C2, C3, C1, C4, C5
# RC4 - 05, 02, 03, 04
# RC5 - gender, 01
# RC7 - education, age
#
```