

# CS350A Course Project

## $\lambda$ -calculus interpreter

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## Description

An interpreter for  $\lambda$ -calculus implemented in `ruby`, as part of our course project CS350A: Principles of Programming Languages under Prof. Satyadev Nandakumar, in Fall Semester 2022-23, IIT Kanpur.

The grammar specification is:

```
 $\lambda$  - term ::= variable |  
              (\variable  $\cdot$   $\lambda$  - term) |  
              [ $\lambda$  - term] [ $\lambda$  - term]
```

The allowed variables are single lowercase English letters - a, b, c etc.

## Features

It supports the following features:

- ✓ Lexer and grammar checker for lambda term expression using LL(1) parser
- ✓ Determine free variables in given lambda term
- ✓ Free variables substitution
- ✓ Alpha Renaming and Beta Reduction

## Code Structure

```
.
├── assets/
├── lexer.rb
├── LICENSE
├── main.rb
├── parser.rb
├── README.md
├── reducer.rb
├── tests/
└── utils.rb
```

2 directories, 14 files

## Usage

Keep your  $\lambda$ -expression in a file and pass its filepath as an argument to `main.rb`.

```
Lambda Calculus Interpreter
```

```
=====
```

```
Usage: main.rb [options]
```

```
    -i, --input FILE
```

Input file containing  $\lambda$ -expression

```
    -o, --output FILE
```

(Optional) Output file to store

reduced  $\lambda$ -expression. Default: out.txt

## Demo Example

**Note** that we use the notation of  $v\{i\}$ , where  $i := [1, 2, 3, \dots]$  for our bound variables after the processing of alpha-renaming and beta-reduction. This helps in easily identifying the bound variables and keep their count in the final reduced form.

```
$ ruby main.rb -i tests/9.lc ## or
```

```
$ ruby main.rb --input=tests/9.lc
```

```
=====
```

```
Course Project
```

```
Lambda Calculus Interpreter
```

```
Created by: Ayush, Gurbaaz and Kritin
```

```
=====
```

```
Grammar checker :-
```

```
[ ( \ x . x ) ] [ y ] is a valid lambda term
```

```
=====
```

```
Free variables :- y
```

```
=====
```

```
 $\alpha$ -renaming :- [ ( \ v0 . v0 ) ] [ y ]
```

```
=====
```

```

> Please provide the free variable name along with its substitution.
e.g. x:=M denotes replacing free occurrences of x with lambda term M
> or press ENTER to finish
y:=(\x.x)
Free variable substitution :- [ ( \ v1 . v1 ) ] [ ( \ v2 . v2 ) ]
=====
> All free variables have been substituted successfully! (Closed Form)
Exiting...
=====
β-reduction :-
Step 1. ( \ v2 . v2 )
No further reduction possible!
=====
Final β-reduced form '( \ v2 . v2 )' saved to 'out.txt'
=====

```

You may find some of the lambda expression files in `tests/` directory.

## Team Members

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