

## Assignment #2

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CSCE 433: Formal Languages and Automata

February 16, 2016

**Question 1. Construct the NFA that accepts the language  $\{w \mid w \text{ contains an odd number of 1's and exactly two 0's}\}$  with exactly six states.**

First let's build a machine that accepts strings with odd number of 1's:

Now we build a machine that accepts strings with exactly 2 zeros:

Notice that we used 6 states already. Then, since we don't need to keep track of strings that go to state  $r_3$ , we could simply remove this state, then all the strings with more than 2 zeros would halt on this machine.

Now we can create a new state that goes to both machines without consuming characters of the string:

**Question 2. Construct an NFA that accepts the set of binary strings that contain both substrings 010 and 101.**

A machine that accepts strings with both substrings 010 and 101 has either the substring 010 or 101 first, then we could build different machines for both cases:

- 010 and then 101

Notice that the machine consider the case in which 010 and 101 overlaps.

- 101 and then 010

**Question 3. Convert the NFA below to a DFA**

To solve this question we are going to use the same algorithm used to prove that  $\epsilon$ -NFAs are equivalent to DFAs. We are going to call this NFA  $N = (Q, \Sigma, \delta, q, F)$  and build an equivalent DFA  $M = (Q', \Sigma, \delta', q', F')$  such that  $q' = C_\epsilon(0) = \{0, 1\}$ ;  $\delta' : \mathcal{P}(Q) \times \Sigma$  where  $\delta'(R, a) = \bigcup_{r \in R} C_\epsilon(\delta(r, a))$  as it follows:

- Start with the initial state

- Calculate the transitions of  $\{0, 1\}$

$$\delta'(\{0, 1\}, a) = C_\epsilon(1) \cup \emptyset = \{1\}$$

$$\delta'(\{0, 1\}, b) = \emptyset \cup C_\epsilon(2) = \{0, 1, 2\}$$

- Calculate the transitions of  $\{1\}$  and  $\{0, 1, 2\}$

$$\delta'(\{1\}, a) = \emptyset$$

$$\delta'(\{1\}, b) = C_\epsilon(2) = \{0, 1, 2\}$$

$$\delta'(\{0, 1, 2\}, a) = C_\epsilon(1) \cup \emptyset \cup C_\epsilon(3) = \{1, 3\}$$

$$\delta'(\{0, 1, 2\}, b) = \emptyset \cup C_\epsilon(2) \cup \emptyset = \{0, 1, 2\}$$