Prolog

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Outline

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Prolog

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Activity

Objectives

You should be able to...

In this lecture, we will introduce Prolog.

- Explain how Prolog uses a unification to drive computation.
- Write some simple programs in Prolog.

Logic

Question: How do you decide truth?

- Start with some objects. "socrates," "john," "mary"
- ▶ Write down some *facts* (true statements) about those objects.
 - Facts express either properies of the object, or "socrates is human"
 - relationship to other objects.
 "mary likes iohn"
- Write down some rules (facts that are true if other facts are true).
 "if X is human then X is mortal"
- ► Facts and rules can become *predicates*.

 "is socrates mortal?"



First-Order Predicate Logic

First-order predicate logic is one system for encoding these kinds of questions.

- Predicate means that we have functions that take objects and return "true" or "false." human(socrates).
- Logic means that we have *connectives* like and, or, not, and implication.
- First order means that we have variables (created by "for all" and "there exists"), but that they only work on objects.
 - \forall X . human(X) \rightarrow mortal(X).

History

- Starting point: First-order predicate logic.
- Realization: computers can reason with this kind of logic.
- Impetus was the study of mechanical theorem proving
- Developed in 1970 by Alain Colmerauer and Rober Kowalski and others
- Uses: databases, expert systems, Al

The Two Questions

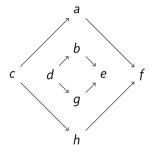
What is the nature of data?

Prolog data consists of facts about objects and logical rules.

What is the nature of a program?

A program in Prolog is a set of facts and rules, followed by a *query*.

The Database



```
1 connected(c,a).
2 connected(c,h).
3 connected(d,b).
4 connected(d,g).
5 connected(a,f).
6 connected(h,f).
7 connected(b,e).
8 connected(g,e).
```

Rules

```
1 mortal(X) :- human(X).
2 human(Y) :- fatherof(X,Y), human(X).
3
4 pathfrom(X,Y) :- connected(X,Y).
5 pathfrom(X,Y) :- connected(X,Z),
6 pathfrom(Z,Y).
```

- Capital letters are variables.
 - ► Appearing left of : means "for all"
 - Appearing right of : means "there exists"

$$\forall x.human(x) \rightarrow mortal(x).$$

$$\forall y.(\exists x.fatherof(x,y) \land human(x)) \rightarrow human(y)$$



How It Works

Programs are executed by searching the database and attempting to perform unification.

```
1?- human(socrates). -- listed, therefore true
2?- mortal(socrates). -- not listed
```

Relevant rules:

```
human(socrates).
human(Y) :- fatherof(X,Y), human(X).
mortal(X) :- human(X).
```

Socrates is not listed as being mortal, but mortal (socrates) unifies with mortal (X) if we replace X with socrates. This gives us a *subgoal*. Replace X with socrates and try it....

How It Works, Next Step

Replace X with socrates in this rule:

```
nmortal(X) :- human(X).
to get
nmortal(socrates) :- human(socrates).
```

Since human(socrates) is in the database, we know that mortal(socrates) is also true.

?- mortal(jane).

```
> ?- mortal(jane).
mortal(X) :- human(X).
```

```
> ?- mortal(jane).
mortal(jane) :- human(jane).
```

```
> ?- mortal(jane).
mortal(jane) :- human(jane).

    human(jane)
    human(Y) :- fatherof(X,Y), human(X).
```

```
> ?- mortal(jane).
mortal(jane) :- human(jane).

    human(jane)
human(jane) :- fatherof(X,jane), human(X).
```

```
P ?- mortal(jane).
mortal(jane) :- human(jane).

    human(jane)
    human(jane) :- fatherof(X,jane), human(X).

    fatherof(X,jane)
```

```
> ?- mortal(jane).
mortal(jane) :- human(jane).

    human(jane)
    human(jane) :- fatherof(X,jane), human(X).

    fatherof(X,jane)

    fatherof(socrates,jane)
```

```
> ?- mortal(jane).
mortal(jane) :- human(jane).

    human(jane)
    human(jane) :- fatherof(socrates,jane), human(socrates).

    fatherof(X,jane)

    fatherof(socrates,jane)
```

```
> ?- mortal(jane).
mortal(jane) :- human(jane).

    human(jane)
    human(jane) :- fatherof(socrates,jane), human(socrates).

    fatherof(X,jane)

        fatherof(socrates,jane)

    human(socrates)
```

You Try ...

- ► Given the connected rules, try to come up with a predicate exactlybetween(A,B,C) that is true when B is connected to both A and C.
- ▶ Now make a predicate between(A,B,C) that is true if there's a path from A to B to C.

```
1 exactlybetween(A,B,C) :- connected(A,B), connected(B,C).
2
3 between(A,B,C) :- pathfrom(A,B), pathfrom(B,C).
```

More Than Just Yes or No

► Prolog can also give you a list of elements that make a predicate true. Remember unification.

```
1?- fatherof(Who,apollo).
2 Who = zeus;

4?- pathfrom(c,X).
5 X = a;
6 X = h;
7 X = f;
8 X = f;
9 No
```

The semicolon is entered by the user — it means to keep searching.

Tracing pathfrom

```
1?- pathfrom(c,X).
2---> pathfrom(c,Y) :- connected(c,Y).
3 X = a;
```

When we hit semicolon, we tell it to keep searching. So we *backtrack* through our database to try again.

```
pathfrom(c,Y) :- connected(c,Y).
2---> X = h;
```

We tell it to try again with this one, too. At this point, we no longer have any rules that say that c is connected to something.

Tracing pathfrom, II

```
pathfrom(c,Y) :- connected(c,Z), pathfrom(Z,Y).
```

We will first find something in the database that says that c is connected to some Z, and then check if there is a path between Z and Y.

We find a and h as last time. When we check a, we check for pathfrom(a, Y), and find that connected(a,f) is in the database. The same thing happens for h, which is why f is reported as an answer twice.

Arithmetic via the is Keyword.

```
1 fact(0,1).
2 fact(N,X) :- M is N-1, fact(M,Y), X is Y * N.
3 ?- fact(5,X).
```

- Unify fact(5,X) with fact(N,X). fact(5,X) :- M is 5-1, fact(M,Y), X is Y * 5.
- Next compute M. fact(5,X) :- 4 is 5-1, fact(4,Y), X is Y * 5.
- ► Recursive call sets Y to 24. fact(5,X) :- 4 is 5-1, fact(4,24), X is 24 * 5.
- Compute X.
 fact(5,120) :- 4 is 5-1, fact(4,24), 120 is 24 * 5.

Lists

- ► Empty list: []
- ► Singleton list: [x]
- ► List with multiple elements: [x,y,[a,b],c]
- ► Head and tail representation: [H|T]

Differences:

Prolog lists are not monotonic!

List Example: mylength

The length predicate is built in.

This example looks like badfact, in that the is clause happens after the recursion. Why is this safe?

List Example: Sum List

Try writing list product now!

List Example: Append

```
_{1} myappend([],X,X).
2 \text{ myappend}([H|T], X, [H|Z]) :- \text{ myappend}(T, X, Z).
3?- myappend([2,3,4],[5,6,7],X).
_{4}X = [2, 3, 4, 5, 6, 7]:
5 No
6?-myappend(X,[2,3],[1,2,3,4]).
7 No
8?- myappend(X,[2,3],[1,2,3]).
_{9}X = [1]:
10 No
```

List Example: Reverse

Accumulator recursion works in Prolog, too!

```
imyreverse(X,Y) := aux(X,Y,[]).
2 aux([],Y,Y).
3 aux([HX|TX],Y,Z) := aux(TX,Y,[HX|Z]).
4?- myreverse([2,3,4],Y).
5Y = [4, 3, 2]

myreverse([2,3,4],Y) \rightarrow aux([2,3,4],Y,[]) \rightarrow aux([3,4],Y,[2]) \rightarrow aux([4],Y,[3,2]) \rightarrow aux([4],Y,[3,2]) \rightarrow aux([3,4],Y,[2]) \rightarrow myreverse([2,3,4],[4,3,2])
```

Activity

- ▶ Write the Fibonacci predicate. Let $F_0 = 0$ and $F_1 = 1$.
- ► Make sure you can write it the exponential way.
- ► Can you write it the linear way?

Solution

Fibonacci predicate: exponential complexity:

Fibonacci predicate: linear complexity: