Continuations

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Objectives

You should be able to ...

It is possible to use functions to represent the *control flow* of a program. This technique is called *continuation passing style*. After today's lecture, you should be able to

- Explain what CPS is.
- Give an example of a programming technique using CPS.
- Write a recursive function using CPS.

Direct Style

Example Code

```
inc x = x + 1
2double x = x * 2
3half x = x `div` 2
4
5result = inc (double (half 10))
```

► Consider the function call above. What is happening?

The Continuation

```
result = inc (double (half 10))
```

- ▶ We can 'punch out' a subexpression to create an expression with a 'hole' in it. result = inc (double [])
- ► This is called a *context*. After half 10 runs, its result will be put into this context.
- ▶ We can call this context a continuation.

Making Continuations Explicit

▶ We can make continuations explicit in our code.

```
| cont = | v -> inc (double v)
```

▶ Instead of returning, a function can take a *continuation argument*.

Using a Continuation

```
half x k = k (x 'div' 2)
result = half 10 cont
```

► Convince yourself that this does the same thing as the original code.

Properties of CPS

- ▶ A function is in *Direct Style* when it returns its result back to the caller.
- ► A *Tail Call* occurs when a function returns the result of another function call without processing it first.
 - ▶ This is what is used in accumulator recursion.
- ▶ A function is in *Continuation Passing Style* when it passes its result to another function.
 - Instead of returning the result to the caller, we pass it forward to another function.
 - ► Functions in CPS "never return."
- Let's see some more examples.

Comparisons

Introduction

Direct Style

```
inc x = x + 1
2double x = x * 2
3half x = x `div` 2
4
5result = inc (double (half 10))
```

CPS

CPS and Imperative Style

► CPS look like imperative style if you do it right.

CPS

Imperative Style

```
v1 := half 10
v2 := double v1
result := inc v2
```

The GCD Program

GCD of a List

```
1 gcdstar [] = 0
2 gcdstar (x:xs) = gcd x (gcdstar xx)
3
4 > gcdstar [44, 12, 80, 6]
5 2
6 > gcdstar [44, 12]
7 4
```

- ▶ Question: What will happen if there is a 1 near the beginning of the sequence?
- ▶ We can use a continuation to handle this case.

Continuation Solution

Other Topics

- ► Continuations can simulate exceptions.
- ▶ They can also simulate cooperative multitasking.
 - ► These are called co-routintes.
- ► Some advanced routines are also available: call/cc, shift, reset.