State

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Objectives

- Describe the property of referential transparency.
- Explain how stateful computations complicate the meaning of programs.
- ► Use OCAML's references to model state.

Definition

The rule of referential transparency:

$$\frac{e_1 \to^* v \quad e_2 \to^* v \quad f e_1 \to^* w}{f e_2 \to^* w}$$

- If you have two expressions that evaluate to be the same thing then you can use one for the other without changing the meaning of the whole program.
- ► E.g. f(x) + f(x) == 2 * f(x)
- ➤ You can prove this by induction, using the natural semantic rules from the previous lectures.

You can use equational reasoning to make the following equivalence:

► You have the basis now of many compiler optimization opportunities!

A Complication

```
1 # let counter = -- something
2 val counter : unit -> int = <fun>
3 # counter ();;
4 - : int = 1
5 # counter ();;
6 - : int = 2
7 # counter ();;
8 - : int = 3
9 #
```

► Can we still use equational reasoning to talk about programs now?

A Counterexample

```
f(x) + f(x) == 2 * f(x)

# 2 * counter ();;

-: int = 8

# counter () + counter ();;

-: int = 11
```

► Congratulations. You just broke mathematics.

Reference Operator

Transition Semantics

ref $v \rightarrow \$i$, where \$i is a free location in the state, initialized to v.

 $! \$i \rightarrow v$, if state location \$i contains v.

 $\$i := v \rightarrow ()$, and state location \$i is assigned v.

$$(); e \rightarrow e$$

Note that references are different than pointers: once created, they cannot be moved, only assigned to and read from.

Natural Semantics

 $\frac{e \Downarrow v}{\text{ref } e \Downarrow \$i}$, where \$i is a free location in the state, initialized to v.

 $\frac{e \Downarrow \$i}{!e \Downarrow v}$, if state location \$i contains v.

 $rac{e_1 \Downarrow \$i \quad e_2 \Downarrow v}{e_1 := e_2 \Downarrow ()}$, and location \$i is set to v.

$$\frac{e_1 \Downarrow () \quad e_2 \Downarrow v}{e_1; e_2 \Downarrow v}$$

Counter, Method 1

```
1# let ct = ref 0;;
2 val ct : int ref = {contents=0}
3# let counter () =
    ct := !ct + 1;
     !ct::
6 val counter : unit -> int = <fun>
7# counter ();;
8 - : int = 1
9# counter ();;
_{10} - : int = 2
```

Bad Things for Counter

ct is globally defined. Two bad things could occur because of this.

- 1. What if you already had a global variable ct defined?
 - Correct solution: use modules.
- 2. The Stupid UserTM might decide to change ct just for fun.
 - Now your counter won't work like it's supposed to!
 - Now you can't change the representation without getting tech support calls.
 - Remember the idea of abstraction.

Conclusions about State

State is bad because:

- ► It breaks our ability to use equational reasoning.
- ▶ Users can get to our global variables and change them without permission.

State is good because:

- Certain constructs are almost impossible without state (e.g., graphs).
- Our world is a stateful one.