The State Monad

Dr. Mattox Beckman

University of Illinois at Urbana-Champaign Department of Computer Science

Objectives

- ▶ Describe the newtype keyword and the record type we use for representing state.
- ▶ Implement the pure operation for the state monad.
- Implement the bind operation for the state monad and trace an execution.
- ▶ Define get and put to allow direct manipulation of the stateful part of the monad.

Defining the Types

- ► The incoming Integer is the state.
- ► The output tuple is a result and a state.

```
1 ex1 :: Integer -> (Integer, Integer)
2 ex1 s = (s * 2, s+1)
3
4 *Main> ex1 10
5 (20,11)
```

Encapsulation

ŏ.

```
newtype State s a = State { runState :: s -> (a,s) }
3 ex2a :: State Integer Integer
4 ex2a = State { runState = ex1 }
5
6 ex2b :: State Integer Integer
7 ex2b = State ex1
8
9 *Main> runState ex2a 10
10 (20,11)
11 *Main> runState ex2b 10
12 (20,11)
```

Functor

```
newtype State s a = State { runState :: s -> (a,s) }
3 ex2b :: State Integer Integer
4 ex2b = State ex1
6 inc x = x + 1
*Main> runState ex2a 10
9 (20,11)
10 *Main> runState (fmap inc ex2a) 10
11 (21,11)
```

- ▶ Remember, Functor takes a container type.
- Think of (State s a) as a container that has values of type a in it.
- We need to define fmap.

```
newtype State s a = State { runState :: s -> (a,s) }
instance Functor (State s) where
fmap :: (a -> b) -> (State s a) -> (State s b)
fmap f g = ...
```

► We need to return a State ...

```
1 newtype State s a = State { runState :: s -> (a,s) }
2
3 instance Functor (State s) where
4  fmap :: (a -> b) -> (State s a) -> (State s b)
5  fmap f g = State ...
```

► That contains a function ...

```
1 newtype State s a = State { runState :: s -> (a,s) }
2
3 instance Functor (State s) where
4  fmap :: (a -> b) -> (State s a) -> (State s b)
5  fmap f g = State (\s1 -> ...
```

► That contains a function ...

```
inewtype State s a = State { runState :: s -> (a,s) }
instance Functor (State s) where
fmap :: (a -> b) -> (State s a) -> (State s b)
fmap f g = State (\s1 -> let (x,s2) = runState g s1
in (f x, s2))
```

Applicative

Similar reasoning gives us the Applicative functor.

The Monad