Clustering Trees into Topological Classes
Project Plan

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1 Objective

Phylogenetic inference on modern datasets containing large numbers of genes from a group of taxa will in most cases produce discordant trees. This project aims to identify and characterise this discordance by applying a variety of clustering methods to a matrix of tree distances derived from single-gene tree inferences.

2 Principles

Phylogenetic inference from molecular sequences aims to provide a description of the evolutionary history of the marker sequences being analysed. The resulting tree summarises two aspects of the evolutionary process: the branching order of the tree corresponds to the order of duplications of the marker sequences, and the branch lengths reflect the process of evolution along the branch - they estimate the evolutionary rate according to the model, multiplied by the time spent evolving. The tree describes the history of the marker sequences used, but if we are investigating species history we may wish to conflate the marker's branching history with the history of speciation events. However, there are many reasons why a segment of DNA can have a different history to the organism it resides in, including horizontal gene transfer, recombination, hybridisation, incomplete lineage sorting and others.
To get a better estimate of the species history we can use several markers, in the hope that the speciation signal

3 Methods

3.1 Tree Inference

I align sequences using some alignment method (for example Prank (Löytynoja and Goldman, 2005)), and then infer trees using either a Maximum-Likelihood approach, for which I use PhyML (Guindon et al., 2010), or a distance based approach, TreeCollection, for which distances and variances between sequences in an alignment are estimated using Darwin, with the resulting distance-variance matrices being the input for TreeCollection, which uses a Least-Squares approach to reconstruct the tree.

3.2 Estimating Tree Distances

As a way of avoiding representing trees as vectors of features observed in a defined space I use pairwise distances to construct a distance matrix as a basis for clustering. A number of distance metrics are available for comparing phylogenetic trees. I chose to use the following (not an exhaustive list of all metrics available).

- Distance Metrics:
  - Robinson-Foulds Distance (Robinson and Foulds, 1981)
  - Euclidean Distance (the Branch Length Distance of Kuhner and Felsenstein (1994))
  - Geodesic Distance (Billera et al., 2001)

The first two of these measures are calculated using the Python module DendroPy (Sukumaran and Holder, 2010). The fourth is calculated using a modified version of the GeoMeTree program (Kupczok et al., 2008). The unweighted Robinson-Foulds measure is based only on topology, the Branch Length distance is based only on branch lengths and the Geodesic distance is explicitly based on topology and branch lengths.

3.3 Clustering Methods

Clustering is a process of separating data points into groups, the members of which share common characteristics more than they share the characteristics with members of other groups. There is a large number of methods available for doing clustering.

1. Hierarchical Clustering Methods
   - Single-linkage
   - Complete-linkage
   - Average-linkage
   - Ward-linkage
2. Exemplar Methods
   - K-medoids (k-centres)
   - Affinity Propagation
3. Matrix Decomposition Methods
   - Classical Multidimensional Scaling + K-means
   - Spectral Clustering + K-means

3.3.1 Hierarchical Clustering

Possibly the simplest methods which can act directly on distance matrices are (agglomerative) hierarchical clustering. These methods iteratively combine the two closest points, representing them by a single point. How this point is taken to relate to the remaining points is defined by the linkage method used. Let u be the newly defined cluster formed by combining points s and t, and v be any other point (or cluster) in the dataset, and let $d(u,v)$ be the distance between u and v:

- Single-linkage - closest member point

$$d(u,v) = \min_{i \in u, j \in v} (d(i,j))$$

- Complete-linkage - furthest member point

$$d(u,v) = \max_{i \in u, j \in v} (d(i,j))$$

- Average-linkage - mean of member distances

$$d(u,v) = \frac{1}{|u|\,|v|}\sum_{i\in u}\sum_{j\in v} d(i,j)$$

- Ward-linkage - minimum variance

$$d(u,v) = \sqrt{\frac{|v|+|s|}{T}d(v,s)^2 + \frac{|v|+|t|}{T}d(v,t)^2 + \frac{|v|}{T}d(s,t)^2}$$
$$T = |v| + |s| + |t|$$

3.3.2 Exemplar Methods

Other methods acting directly on distance matrices are k-medoids (also known as k-centres), and affinity propagation (Frey and Dueck, 2007). These search for points in the data set to act as exemplars, that is cluster centres to which surrounding points are grouped. K-medoids requires that the number of clusters be set in advance, whereas with affinity propagation the number of clusters depends on the value of a tuning parameter, called the preference, which can take a value between $\min(d)$ and $\max(d)$, and is usually set as the median.

3.3.3 Matrix Decomposition Methods

Classical multidimensional scaling maps distances to points in a multidimensional space. The distance matrix is double-centred (from each element subtract the row mean, subtract the column mean, add the overall mean and divide by -2). This eigenvectors of this matrix - the Gower matrix - corresponding to the k largest eigenvalues map the data into a k-dimensional space. The points can then be clustered using k-means.
Spectral decomposition is carried out using the Ng-Jordan-Weiss (NJW) algorithm (Ng et al., 2002) with local scaling approach of Perona and Zelnik-Manor (2004).

4 Investigating the clustering procedures

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