

# HAN House model RC Analysis

**Author:** Luca Gennari

**Version:** Draft\_V01

**Date:** 17/11/2021

## Contents

1. Introduction .....	2
2. Research steps .....	2
3. Dutch housing typologies and energy consumption .....	3
1. Dutch energy consumption per private dwellings typologies and per year: .....	3
2. Most common Dutch housing typologies .....	4
Terraced houses additional information .....	5
3. Relevant construction characteristics .....	5
4. Literature study .....	7
5. Literature study - Takeaways Summary .....	20
6. HAN Model - Analysis of the main (current) parameters .....	21
4. Current RC model .....	21
7. Possible implementations for the HAN model .....	27
8. Rc-waarde, Rsi, Rse and U-waarde: a brief explanation .....	30
9. Follow-up future research steps .....	31
10. Discussion .....	33
11. References .....	34

## 1. Introduction

To support the residential energy transition, tools that allow designers and decision-makers to easily compare renovation options and address their magnitude are necessary. The HAN in collaboration [TO BE COMPLETED] has developed a dynamic simulation 'grey-box'<sup>1</sup> tool, with a simple Excel based interface for users (planners, architects, and engineers) to enter their design parameters.

Hereinafter referred to as the '**HAN model**'. The model used is based on an equivalent resistance-capacitance (R-C) model. The building envelope is simulated with an R-C\* electrical analogy to model the building thermal mass and heat transfer as respectively (lumped) capacities and resistances. Lumped-capacitance models assume that the distributed thermal mass of the dwelling is lumped into a discrete number of thermal capacitances, depending on the model type (G. Reynders et al., 2014). Whereas state-of-the-art 'white-box' building energy simulation models show good performance in validation studies, the number of model parameters and thus the required input data, increases drastically with the model complexity (Glenn Reynders et al., 2015). Grey-box RC models greatly reduce the computational effort.

RC models are mathematically a set of ordinary differential equations (ODEs). For ODEs, the number of orders is equivalent to the number of C terms (Li et al., 2021).

Previous studies have shown a strong dependency between heating energy demand, outdoor environment, building characteristics and efficiency of the control strategy [ref 8 (G. Reynders et al., 2014)]. The HAN model particularly aims to specialise on the simulation of the control strategies.

In this research several RC models have been analysed and compared to the HAN model. The objective is to address the accuracy of the HAN model, identify which modifications to suggest to the HAN RC model and which simplifications can be used to better represent and simulate specific building typologies. Building typologies have been analysed based on the TABULA project (Delf University of Technology, n.d.) and (Agentschap NL, 2011a) data for the Dutch housing situation.

*\*Thermal resistance R and capacitance C are defined as:*

$$R = \frac{x}{k} = \frac{\Delta T}{\dot{Q}_A} = \left[ \frac{m^2 \cdot K}{W} \right] \quad \text{and} \quad C = x \cdot \rho \cdot C_p = \left[ \frac{J}{m^2 \cdot K} \right]$$

*with thermal conductivity (k), thickness (x), density (ρ), and specific heat (Cp).*

## 2. Research steps

The following workpackages are presented in this report:

- Analysis of the main house typologies in the Netherlands and their construction characteristics
- Literature study of RC network analogy models
  - o including simplifications and rules of thumb
- Comparison of the literature study RC models with the HAN RC model
  - o Including a check of the equations used in the current HAN model
- Suggestions of implementations for the HAN model RC-layout based on building characteristics and literature study findings.

---

<sup>1</sup> Based on the provided definition, the grey-box model is a representation of physical model but ignores minor fidelity and preserves major fidelity (Li et al., 2021).

Follow-up workpackage (further explained at the end of the report):

- Estimation (i.e., quantify magnitude) and validation of the selected RC layouts and possible simplifications to represent specific building typologies through inter-model comparison with a detailed 'white-box' dynamic simulation.

### 3. Dutch housing typologies and energy consumption

The following elements of consideration have been analysed:

1. Dutch houses' average energy consumption per year
2. Dutch houses' energy consumption per dwelling typology
3. Identify most common Dutch housing typologies
4. Define relevant construction characteristics (such as light floor/roof/walls, high % of glass, cavity ground floor etc.). **NOTE: this point needs further research. See paragraph 'Follow-up future research steps'.**

#### 1. Dutch energy consumption per private dwellings typologies and per year:

Housing characteristics ▼			Average consumption of natural gas	Average consumption of electricity	District heating
Regions ▼					
Periods ▼					
			m3	kWh	%
Total dwellings	The Netherlands	2010	1,850	3,300	4.6
		2017	1,240	2,860	5.6
		2019*	1,180	2,730	5.9
Apartment	The Netherlands	2010	1,200	2,250	.
		2017	840	2,050	.
		2019*	770	1,970	.
Terraced house	The Netherlands	2010	1,650	3,350	.
		2017	1,190	2,990	.
		2019*	1,100	2,830	.
Corner house	The Netherlands	2010	2,000	3,500	.
		2017	1,430	3,100	.
		2019*	1,320	2,950	.
Semi-detached house	The Netherlands	2010	2,400	3,950	.
		2017	1,680	3,430	.
		2019*	1,540	3,270	.
Detached house	The Netherlands	2010	3,100	4,600	.
		2017	2,200	4,040	.
		2019*	2,040	3,950	.
Owner-occupied house	The Netherlands	2010	.	.	.
		2017	1,470	3,330	.
		2019*	1,370	3,180	.
Rented house	The Netherlands	2010	.	.	.
		2017	1,010	2,210	.
		2019*	930	2,120	.

Source: CBS

This table shows regional figures on the average consumption of energy (natural gas and electricity) of private dwellings broken down by type of dwelling and ownership for Nederland, group of provinces, provinces and municipalities. Besides, for total dwellings only, the share of heat distribution

(district heating) has been added, because this is relevant for the interpretation of the height of the average consumption of natural gas.

Data available from: 2010

Source:(cbs, 2019) <https://www.cbs.nl/en-gb/figures/detail/81528ENG?q=parts%20of%20the%20country>

## 2. Most common Dutch housing typologies

There are five main types of dwellings in the Netherlands:

- *Vrijstaand* (detached)
- *Twee onder een kap* (semi-detached)
- *Rijtjeshuis* (terraced /town house/ row house)
- *Appartement* (apartment)
- *Woonboot* (houseboat)

The most common type of dwelling are the Terraced housing (*rijtjeshuis*) and Apartments.

Typology	Total number of dwellings in the Dutch residential sector	Number of dwellings with an energy label	Percentage of dwellings with in the Dutch residential sector with a energy label
Apartments	1,946,055 <b>26% of total</b>	787,572	40%
Terraced housing	2,444,436 <b>34%</b>	769,850	31%
Terraced housing (end)	1,031,139 <b>14%</b>	336,282	33%
Unknown	183,286	153,683	84%
Semi-detached housing	737,968	89,005	12%
Detached housing	907,916	32,295	4%
<b>TOTAL</b>	<b>7,250,800</b>	<b>2,168,687</b>	<b>30%</b>

**Table:** Overview energy consumption labelling in the Dutch residential sector (adjusted from Kadaster, 2013). **Source:** More connect report from page 81 onwards (van Oorschot, 2016) and (Delf University of Technology, n.d.). The last one can be found online at <https://episcopus.eu/building-typology/country/nl.html>.

Percentage of the Dutch housing typologies:

Woningtype	Bouwperiode					totaal
	voor 1946	1946-1964	1965-1974	1975-1991	1992-2005	
vrijstaande woning	6,5%		1,8%	3,3%	2,6%	14,1%
2 onder 1 kap woning	4,2%		2,1%	3,3%	2,6%	12,1%
<b>rijwoning</b>	<b>7,7%</b>	<b>7,0%</b>	<b>8,9%</b>	<b>12,9%</b>	5,2%	41,7%
maisonnetwoning	3,3%		0,3%	1,4%	0,6%	5,6%
galerijwoning	1,0%		2,6%	1,6%	1,7%	6,8%
portiekwoning	3,8%	3,9%	1,7%	2,1%	1,0%	12,5%
(overig) flatwoning	1,5%		1,8%	1,8%	2,0%	7,1%
<b>totaal</b>	<b>38,8%</b>		<b>19,1%</b>	<b>26,4%</b>	<b>15,6%</b>	<b>100,0%</b>

Tabel 3: deel van de Nederlandse woningvoorraad per 1-1-2006

Average energy index (representative of the energy performance, the higher the better):

Woningtype	Bouwperiode					
	voor 1946	1946-1964	1965-1974	1975-1991	1992-2005	totaal
vrijstaande woning	2,70		2,29	1,52	1,15	2,09
2 onder 1 kap woning	2,51		2,21	1,54	1,21	1,92
rijwoning	2,69	2,46	2,11	1,57	1,19	1,99
maisonnetwoning	2,91		2,50	1,56	1,27	2,38
galerijwoning	2,91		2,60	1,66	1,21	2,09
portiekwoning	3,01	2,95	2,40	1,54	1,21	2,52
(overig) flatwoning	2,77		2,65	1,75	1,24	2,05
totaal	2,71		2,28	1,57	1,20	2,09

Tabel 4: gemiddelde energie-index per voorbeeldwoning

Source: (Agentschap NL, 2011b)

Based on the above data, the main attention should go to **apartments and terraced houses** (including terraced-corner - or end - houses) as they are in the largest number. The HAN house model is currently set-up for terraced houses. Particularly relevant are the ones **built before 1974** due to their poor energy performance, which count for around the 24% of the total Dutch house market (data from 2011).

#### Terraced houses additional information

Since the 1920's the housing stock in the Netherlands is dominated by low-rise mass housing development. At first by municipalities and housing corporations, later also by project developers. This has resulted in only a few, very common, typologies which have been used for a large number of houses throughout the Netherlands. The appearance of these houses may vary, but the structure and floor plans are mostly identical.

A very common typology that is developed from the 1950's onwards is the 'doorzonwoning'; a type of terraced housing with an open floor plan and large windows in both façades. This typology dominated the mass housing design of the 1970's and 1980's. **These dwellings are originally barely insulated and contain –due to the method and speed of construction- many air leaks.** In spite of later renovations and retrofit insulation of these houses, their energy performance is inferior. Despite differences in appearance, detail and energy performance, these houses are quite similar to contemporary mass housing design concerning dimensions and floor plan. The quantity, popularity, structure and potential for improving the energy performance of this housing typology makes it highly attractive for the development of a passive house renovation concept for mass production. Such a concept, with the potential to be repeated on a much larger scale [...]

Source: (Herwin Sap, Ronald Rovers, 2014)

### 3. Relevant construction characteristics

Additional information about the construction characteristics of Dutch terraced houses should be researched (i.e. frequency of light vs heavy floor/roof/walls, percentage of glass on the façades, presence of a cavity ground floor etc.). This additional research about the envelope (especially which components can be expected as light or heavy) is necessary in order to possibly decide to implement a 3<sup>rd</sup> order (3 capacities) model for the HAN model (especially in case of mixed use of heavy and light construction elements) or select possible simplifications such as reducing the model to the 1<sup>st</sup> order

(1 capacity) in case of light structures (see coming paragraph ‘Possible implementations for the HAN model’). Possible sources for those pieces of information are the:

- brochure ‘Voorbeeldwoningen 2011 Bestaande bouw’ (Agentschap NL, 2011a),
- ‘Voorbeeldwoningen 2011 Onderzoeksverantwoording’ (Agentschap NL, 2011b) and
- (van Oorschot, 2016) pag. 88 onwards – link to online pdf in the Bibliography.

<b>6 Rijwoning</b>	<b>34</b>
Gebouwd tot en met 1945	36
Gebouwd in de periode 1946-1964	38
Gebouwd in de periode 1965-1974	40
Gebouwd in de periode 1975-1991	42
Gebouwd in de periode 1992-2005	44

Fig. Screenshot from ‘Voorbeeldwoningen 2011 Bestaande bouw’ (Agentschap NL, 2011a) table of contents. Possible information about terraced houses construction materials used could be found at page 34 to 40 (up to yr ’74).

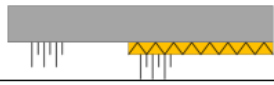

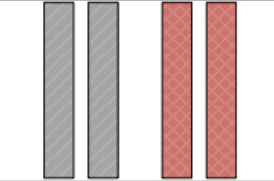
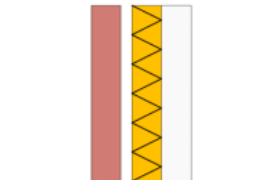

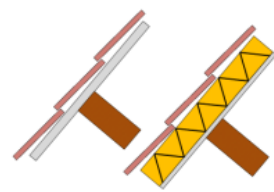
(B1) Ground floor entry and kitchen		Concrete ground floor – direct bearing at the entry and kitchen (no/minimum insulation)
(B2) Ground floor living		Wooden ground floor including crawl space at the living (no/minimum insulation)
(C) Separation and load bearing wall structures		(Coreless cavity wall; concrete or masonry)
(D) Façade (combination)		Cavity wall; piled – masonry – outer layer; no/minimum insulation; NOT structural. Integration facade with load bearing structure (thermal bridges): there is an opportunity to remove outer skin. HVAC system integration with building façade: The pipes of the installation run through the facade.  (Infill facade elements; NOT
(E) (Second/third/...) floors		(Prefabricated – hollow core – concrete floor elements)
(F) Balcony / loggia / gallery	X	X
(G) Roof / top floor		Pitched roof; purlins; tiles on roof boarding; no/minimum insulation

Fig. Example of envelope and structural materials for a terraced house from 1965 from (van Oorschot, 2016) page 105. The row houses that were built in the period 1965-1974 represent 606,000 dwellings (9%). Almost half (47%) of these dwellings are owned by a private homeowner. An equal portion is owned by social housing associations and about 6% is rented in the private sector.

## 4. Literature study

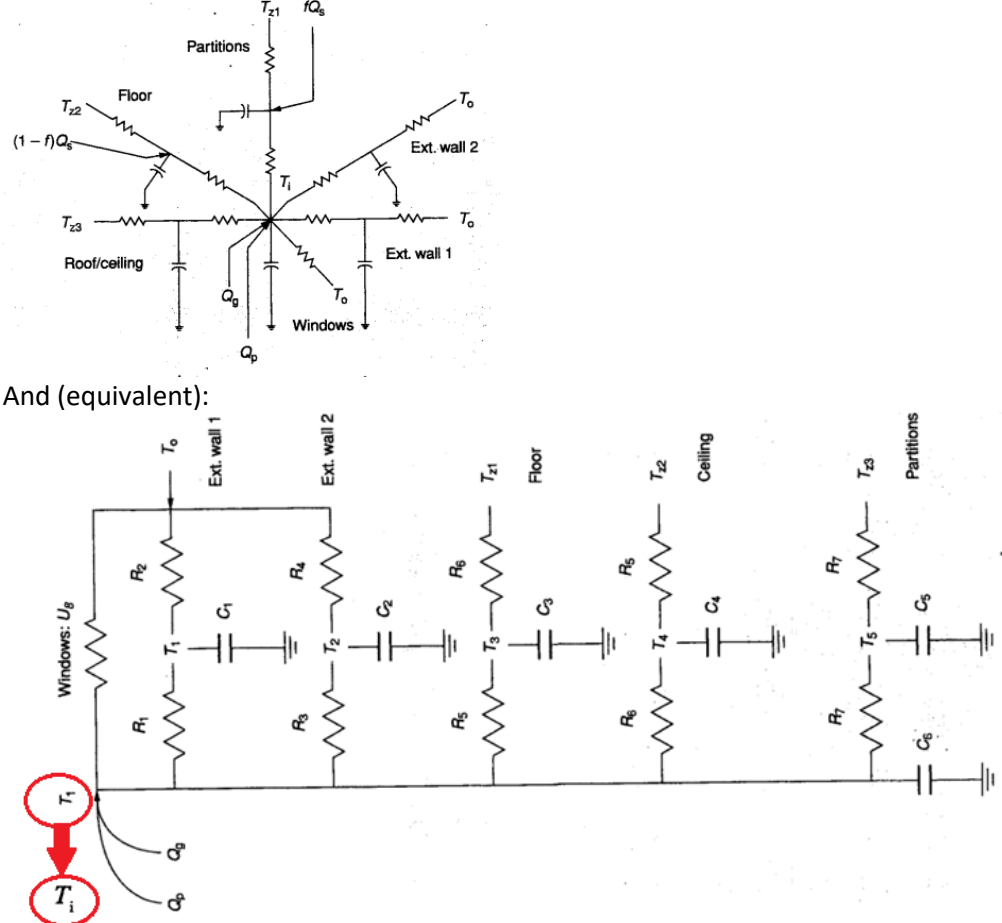
The following literature study focuses on previous RC models, form, parameters and main findings (which could lead to guidelines and simplifications for the HAN model). Particular attention goes to the modelling of the effect of the thermal mass (and related representation in the model through the heat capacitance C).

9 publications (4 papers, 4 conference articles and 1 doctorate thesis) have been selected (*the selected literatures are presented in the order of how the research as evolved over time; the numbering 1 to 9 doesn't follow the numerical order as these publications have been found and selected in different moments. A number has been given at the moment of selection*):

- Ref. 9 (conference): Low-order model for the simulation of a building and its heating system. Older publication, (Gouda et al., 2000). **Note: Precursor of the 'lumped' capacity and resistance modelling method.** Named in Ref.7, 8 which are at the base of Ref.2,3. Particularly interesting is the way in which the equations used are specified in a simple way for the different components (building and emission system).
- Ref.1 (Doctorate thesis): Design and analysis of optimal multi-layer walls for time-varying thermal excitation (Bond, 2006)
- Ref.8 (Journal): Quality of grey-box models and identified parameters as function of the accuracy of input and observation signals (G. Reynders et al., 2014). **Note: The accuracy of different RC models is modelled and compared with a dynamic 'white-box' model. May 2014.** Glenn Reynders, same author in Ref. 6,7,8.
- Ref.7 (conference): Bottom-up modeling of the belgian residential building stock: Influence of model complexity (Glenn Reynders et al., 2014). **Note: December 2014 → Ref.7 is a follow-up of Ref8. where a night zone is added.** Glenn Reynders, same author as in Ref. 6,7,8
- Ref.6 (Journal): Impact of the Heat Emission System on the Identification of Grey-box Models for Residential Buildings (Glenn Reynders et al., 2015). **Note: Ref.6 is a follow-up of Ref7,8. where focus is on the difference in dynamic behaviour between slow floor heating and fast radiators as the heating emissions systems.** Glenn Reynders, same author as in Ref. 6,7,8
- Ref.3 (conference): Bottom-up Modeling of Residential Heating Systems for Demand Side Management in District Energy System Analysis and Distribution Grid Planning (Kramer et al., 2017).
- Ref.2 (conference): Validation of RC Building Models for Applications in Energy and Demand Side Management (Kuniyoshi et al., 2018). **Note: Kremer is author of both Ref. 2&3. Its research is based on the work of Glenn Reynders Ref. 6,7,8**
- Ref.5 (Journal): Energy embodied in, and transmitted through, walls of different type when accounting for the dynamic effects of thermal mass (Reilly et al., 2020). **Note: not directly about RC modelling, interesting for the dynamic effect of thermal mass.**
- Ref.4 (Journal): Grey-box modeling and application for building energy simulations – A critical review (Li et al., 2021).

## Literature study summary

- **Ref9** - Low-order model for the simulation of a building and its heating system. Older publication, (Gouda et al., 2000).

<p><b>RC model used</b></p>	 <p>And (equivalent):</p> <p>The above RC model is simulated and <b>compared with one week of empirical</b> measurements in an equivalent example space. The red circled temperature is used to highlight a mistake in the publication (<math>T_1</math> should be the indoor air temperature <math>T_i</math>).</p> <p style="text-align: right;">Figure 13 Model realisation for the selected example space</p>
<p><b>Notes:</b></p>	<p><b>Precursor research of the ‘lumped’ capacity and resistance modelling method.</b> This research is named in Ref.7, 8 which are then used as a starting point for Ref.2,3.</p>
<p><b>Order of the model</b></p>	<p>6<sup>th</sup> (2 external walls, floor, roof, partitions, indoor air)</p>
<p><b>Description of the (main) parameters</b></p>	<p>6<sup>th</sup> order model:</p> <ul style="list-style-type: none"> <li><math>C_1</math> Thermal capacity of the first layer (<math>\text{J K}^{-1} \text{m}^{-2}</math>)</li> <li><math>C_6</math> Thermal capacity of the indoor air (<math>\text{J K}^{-1}</math>)</li> <li><math>T_g</math> Earth temperature (<math>^{\circ}\text{C}</math>)</li> <li><math>T_i</math> Room air temperature (<math>^{\circ}\text{C}</math>)</li> <li><math>T_j</math> Temperature of the <math>j</math>th room element (<math>^{\circ}\text{C}</math>)</li> <li><math>U_i</math> Overall thermal transmittance of the <math>i</math>th room element (<math>\text{W m}^{-2} \text{K}^{-1}</math>)</li> </ul> <p>The air capacity <math>C_6</math> is placed in series with the capacity of the indoor partitions <math>C_5</math>.  <u>The following state equations are used:</u></p>



$$\begin{aligned}
C_1 \dot{T}_1 &= U_1(T_i - T_1) + U_2(T_0 - T_1) \\
C_2 \dot{T}_2 &= U_3(T_1 - T_2) + U_4(T_0 - T_2) \\
C_3 \dot{T}_3 &= U_5(T_1 - T_3) + U_6(T_{z1} - T_3) + Q_s \\
C_4 \dot{T}_4 &= U_6(T_1 - T_4) + U_5(T_{z2} - T_4) \\
C_5 \dot{T}_5 &= U_7(T_i - T_5) + U_7(T_{z3} - T_5) \\
C_6 \dot{T}_i &= U_1(T_i - T_1) + U_3(T_2 - T_i) + U_5(T_3 - T_i) \\
&+ U_6(T_4 - T_i) + U_7(T_5 - T_i) + U_8(T_0 - T_i) \\
&+ Q_p + Q_g
\end{aligned}$$

A 1<sup>st</sup> order lumped model (one capacity) is also described:

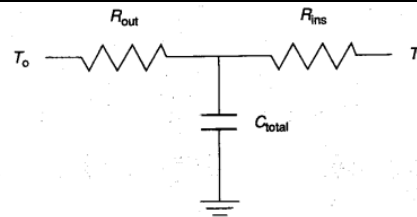


Figure 4 'Lumped parameter' construction element

$R_{ins}$  Area-integrated inner region thermal resistance  
(K W<sup>-1</sup>)

$R_{out}$  Area-integrated outer region thermal resistance  
(K W<sup>-1</sup>)

$C_{total}$  includes the indoor air capacity.

$R_{ins}$  \*includes the internal surface resistance and the resistance of part of the envelope (possibly the part from the center of the insulation layer, facing indoor).

$R_{out}$  \*includes the external surface resistance and the resistance of part of the envelope (possibly the part from the center of the insulation layer, facing outdoor).

Infiltrations and ventilation are not specified.

*\*To determine this the Lorenz and Masy method has been used of which it has been proven difficult to find further specific information.*

Equations used to 'lump' R and C in the 1<sup>st</sup> order model (one capacity):

$$R_{total} = \left( r_{si} + r_{so} + r_a + \sum_{i=1}^L \frac{x_i}{k_i} \right) / A_{total} \quad (1)$$

$$C_{total} = A_{total} \times \left( \sum_{i=1}^L x_i \times \rho_i \times c_{pi} \right) \quad (2)$$

$R_{ins}$  and  $R_{out}$  can be calculated from the following equations, using the method prescribed by Lorenz and Masy<sup>(11)</sup>:

$$R_{ins} = \alpha \times R_{total} \quad (3)$$

$$R_{out} = (1 - \alpha) \times R_{total} \quad (4)$$

The 'accessibility factor',  $\alpha$ , can be calculated for the external construction elements using the following equations:

$$\alpha = 1 - \left[ \frac{\sum_{k=1}^L R_k^* \times C_k}{R_{total} \times C_{total}} \right] \quad (5)$$

where

$$R_k^* = \sum_{i=1}^{i=L-1} R_i + \frac{R_k}{2} \quad (6)$$

N. of zones

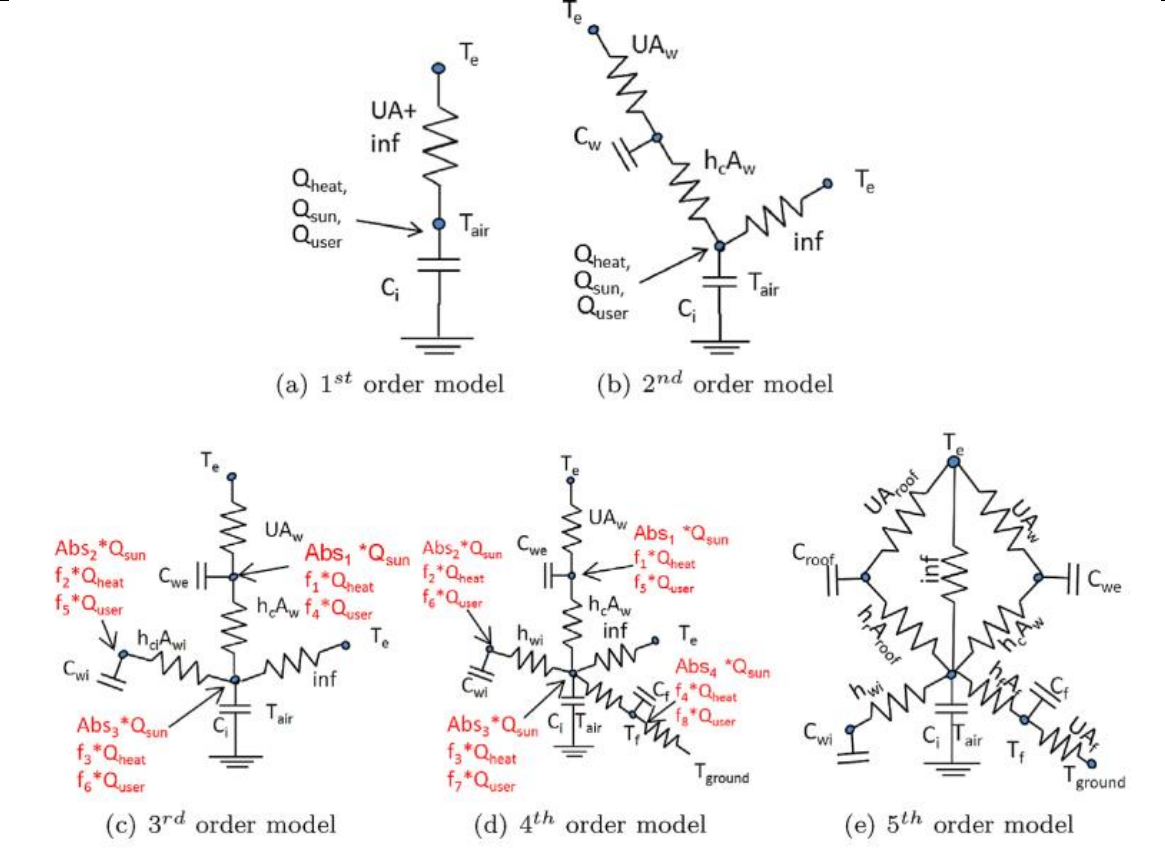
1

Year of publication

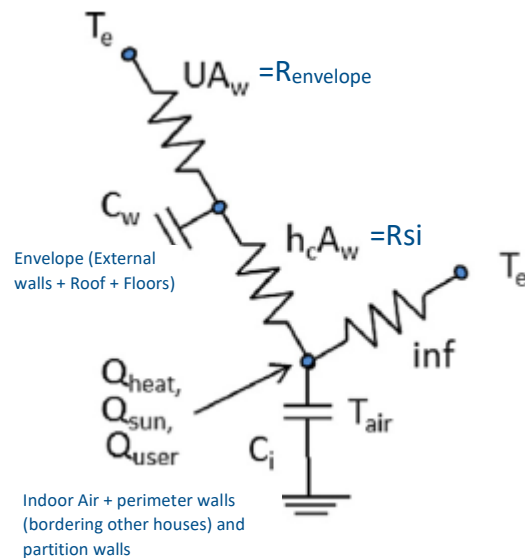
2000 (conference paper)

<p><b>Takeaways:</b></p>	<ul style="list-style-type: none"> <li>• Simplified 'lumped' RC models have sufficient accuracy to be used in the design and selection of heating generation/emission systems and related control systems strategies, for buildings with high thermal capacity.</li> <li>• Having just one C (total 'lumped' thermal capacity) doesn't allow for a distinction between the fast dynamics of the indoor air and the slow dynamics of the structural mass.</li> </ul> <p>Others:</p> <ul style="list-style-type: none"> <li>• This publication contains useful descriptions of possible equations to model convection heat transfer from radiators as emission system.</li> <li>• A solar algorithm is implemented using Simulink in Matlab.</li> <li>• The impact of solar radiation is not validated in their model.</li> <li>• The impact of light buildings (low thermal mass) is not validated.</li> <li>• Validation is done with data from a short period of time (i.e., one week).</li> </ul> <p>A screenshot from the research conclusion paragraph in support of the above takeaways:</p> <p><b>6 Conclusions</b></p> <p>The development of a simplified approach to modelling a building space and heating system has been investigated for the specific purpose of the short time scale simulation of relevance to control system synthesis and design. A building is complex to control, owing to the large time delays, time-variant parameters and plant uncertainties involved. Many simulation programs have been used to simulate the thermal behaviour of the building and its heating system, such as TRNSYS and DOE. These programs have found widespread acceptance as tools for energy analysis or thermal design of buildings but are generally unsuitable for control system simulation over the short term.</p> <p>The model developed in this work represents the building as a low-order linear state-space realisation with a lumped-parameter non-linear heating system description. A solar algorithm has been included and the resulting model has been implemented using Simulink in the Matlab environment. Excellent agreement has been found between the model and results from field monitoring of a building. However, these results apply to a building with a high thermal capacity facing north (with, consequently, low solar radiation). Nevertheless, it may be concluded that the model is simple, computationally efficient and sufficiently accurate to have potential for applications to short time scale simulations appropriate to control system analysis. Further work needs to be done to evaluate the model's performance in situations involving periodic casual heat gains, substantial solar radiation exchange and low building thermal capacity.</p>
--------------------------	--

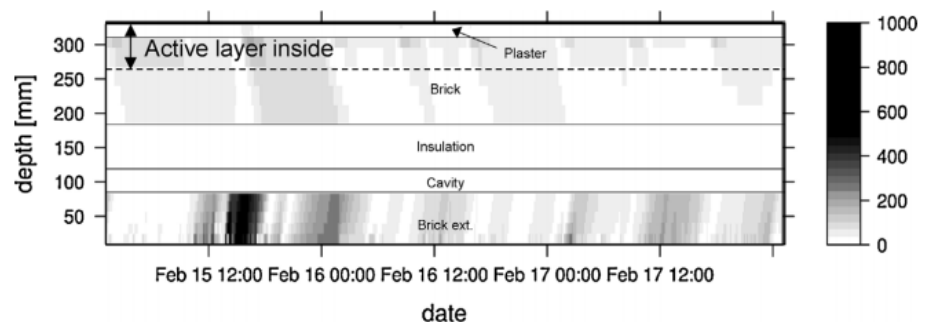
- **Ref8** - Quality of grey-box models and identified parameters as function of the accuracy of input and observation signals (G. Reynders et al., 2014)

<b>RC model used</b>	 <p>(a) 1<sup>st</sup> order model      (b) 2<sup>nd</sup> order model</p> <p>(c) 3<sup>rd</sup> order model      (d) 4<sup>th</sup> order model      (e) 5<sup>th</sup> order model</p>
<b>Notes:</b>	The accuracy of different RC models (1 <sup>st</sup> to 5 <sup>th</sup> order) is modelled and compared with another dynamic 'white-box' simulated model. Glenn Reynders, same author in Ref. 6,7,8.
<b>Order of the model</b>	From 1 <sup>st</sup> to 5 <sup>th</sup>  4 <sup>th</sup> order model: capacities $C_w, C_i, C_{wi}$ and $C_f$ 3 <sup>rd</sup> order: simplified by ground floor and envelope capacities 2 <sup>nd</sup> order: simplifies further combining air and internal walls capacity 1 <sup>st</sup> order: all capacities together
<b>Description of the (main) parameters</b>	$C_w$ = Thermal capacity for the exterior walls + roof $C_f$ = the ground floor $C_{wi}$ = the internal walls $C_i$ = the indoor air The outdoor temperature ( $T_e$ ) and the ground temperature ( $T_g$ ) are used as boundary conditions.
<b>N. of zones</b>	1
<b>Year of publication</b>	May 2014.
<b>Takeaways:</b>	<ul style="list-style-type: none"> <li>• <b>4<sup>th</sup> order models had the best results</b> (5<sup>th</sup> order showed some improvements for well insulated buildings, but not substantial). In particular, it allows: <ol style="list-style-type: none"> <li>1) to simulate separately the capacity of the indoor walls and air</li> <li>2) to simulate the ground temperature for the floor heat transfer: it extends the 3rd order model by including a separate state for the floor. This state is included because the floor is not in direct contact with the outdoor environment at a temperature <math>T_e</math>, but with the ground at a temperature <math>T_{ground}</math></li> </ol> </li> </ul>

- As a rule of thumb, the active thermal mass of the envelope corresponds to the thermal mass of the material layers within the insulation barrier\*. This means that the **thermal mass of materials before the insulation (facing outdoor) could be neglected**.  
*The  $C_w$  then becomes (just) the thermal mass of the material layers within the insulation barrier.*
- Using **at least two thermal capacities C (2<sup>nd</sup> order models)** a distinction can be made between the slow dynamics of the structural mass  $C_1$  and the fast dynamics of the indoor air  $C_2$ , leading to higher accuracy. **For the HAN model, this could be implemented applying the schematic shown below:**



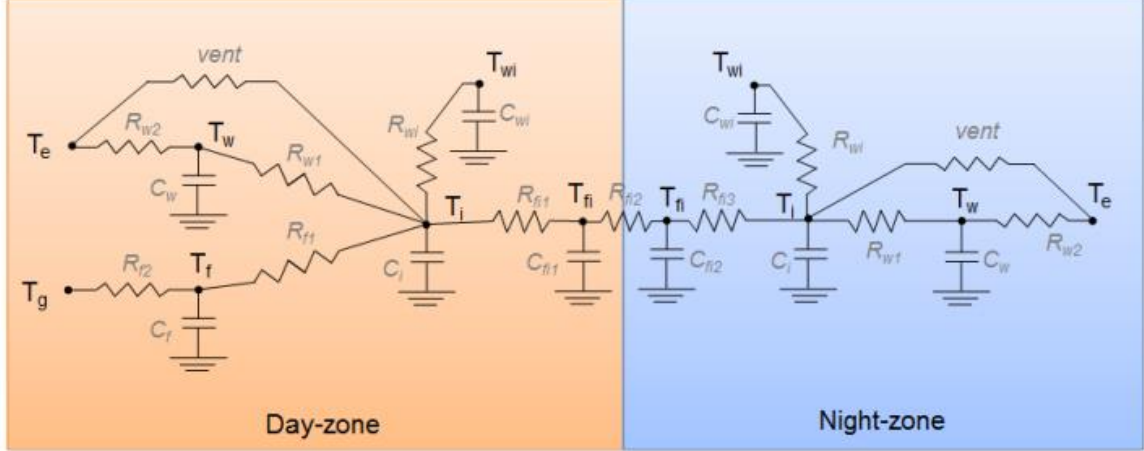
*\*inner layer of construction has been proven to be the most 'active' in absorbing and releasing heat. See fig. 7 from Ref.8:*



**Fig. 7.** Absolute value of the heat absorption [W] throughout the thickness of the wall as function of time.

- Additionally, the accuracy of the control strategies for the modelled RC networks have not been satisfactory which highlights the research gap in this area and justifies the choice to focus on the analysis of control strategies with the HAN model.
- If a light-weight structure is used for part of the building (i.e., the pitched roof in this publication) dynamics can be expected to differ significantly from the heavy-weight of (here brick) walls, a potential improvement of the model could be achieved by separating the dynamics of the light and heavy structures (i.e., separate the capacities by increasing the order of the model, adding a 'C').
- The small differences in model structure between a well-insulated and an uninsulated building indicate that *only few model types are needed to represent the majority of buildings*.

- **Ref7** - Bottom-up modeling of the Belgian residential building stock: Influence of model complexity (Glenn Reynders et al., 2014)

<b>RC model used</b>	 <p><i>Figure 2: Structure of the 2-zone reduced order models. The day-zone is modeled as a 5-state model with states for the indoor air (<math>T_i</math>), the exterior walls (<math>T_w</math>), the interior walls (<math>T_{wi}</math>), the ground floor (<math>T_f</math>) and the floor between day- and night-zone (<math>T_{fi}</math>). A 4-state model is used for the night zone with states for the indoor air (<math>T_i</math>), the exterior walls (<math>T_w</math>), the interior walls (<math>T_{wi}</math>) and the floor between day- and night-zone (<math>T_{fi}</math>). Note that the gain inputs and the related parameters are not shown.</i></p>
<b>Notes:</b>	<p>Glenn Reynders, same author as in Ref. 6,7,8.</p> <p><b>Follow-up of Ref8. where a night zone is added (the focus of this publication is on modelling 2 zones).</b> Terraced dwellings are simulated.</p>
<b>Order of the model</b>	<p>5<sup>th</sup> X2 (day and night zones)</p>
<b>Description of the (main) parameters</b>	<p>The day-zone is modelled with a thermal capacity for the exterior walls (<math>C_w</math>), the ground floor (<math>C_f</math>), the internal walls (<math>C_{wi}</math>) and the indoor air (<math>C_i</math>). The thermal mass of the night-zone is lumped to a capacity for the envelope (roof + walls) (<math>C_w</math>), the internal walls (<math>C_{wi}</math>) and the indoor air (<math>C_i</math>). Both zones are linked by the internal floor which is modelled by 2 thermal capacities (<math>C_{fi1}</math>) and (<math>C_{fi2}</math>). The outdoor temperature (<math>T_e</math>) and the ground temperature (<math>T_g</math>) are used as boundary conditions. The thermal resistance of the interior walls is <math>R_{wi}</math>. The thermal resistance for the envelope is <math>R_w</math>.</p> <p><b>The internal resistance (<math>R_{w1}</math>) is defined as the thermal resistance between the indoor environment and the middle of the material layers within the insulation layer, taking into account also standard heat transfer coefficients at the surface (including <math>R_{si}</math>). <math>R_{w2}</math> is then defined as the thermal resistance between the middle of the layers within the insulation barrier and the outdoor environment (including <math>R_{se}</math>).</b></p> <p><b><math>C_w</math> (envelope and the ground floor) corresponds to the thermal mass of ONLY the material layers within the insulation barrier* accordingly to Ref.8 (G. Reynders et al., 2014)</b></p> <p><i>*Thermal mass of materials before the insulation (facing outdoor) are neglected.</i></p> <p><b><u>For the HAN model (2<sup>nd</sup> order) this could be implemented in such diagram:</u></b></p>

	<p> <math>T_{air}</math> indoor  <math>C_i</math> C of indoor air + indoor partitions walls + perimeter walls bordering with other houses  <math>R_{w,1}</math> Including <math>R_{si}</math>  <math>R_{w,2}</math> Including <math>R_{se}</math>  <math>T_e</math> outdoor  <math>C_w</math> C of the envelope after the insulation (i.e., possible load bearing structure if after insulation + internal side of the envelope 15-25mm plaster layer)          Insulation          Outdoor, <math>R_{w2}</math> Indoor, <math>R_{w1}</math> </p>
Number of zones	2
Year of publication	December 2014
Takeaways:	<ul style="list-style-type: none"> <li>The 5 and 4 state model resulted in the best results for respectively the day and night-zone.</li> <li>A night zone led to overestimated energy consumption especially for well-insulated buildings (built after 2005)</li> <li>The thermal resistance and capacity of the internal partition (between day and night zones) should be reduced in case of 2-zones models.</li> <li>Reynders et al. suggest to only take into account the material layers within the insulation barrier for the heat capacitance <math>C</math>, since only the first centimeters of an envelope wall are excited by a heating system.</li> </ul>

- **Ref6** - Impact of the Heat Emission System on the Identification of Grey-box Models for Residential Buildings (Glenn Reynders et al., 2015)

RC model used	
Notes:	<p><b>Latest of the 3 researches selected from</b> Glenn Reynders et al., same author as in Ref. 6,7,8.</p> <p><b>In this research, focus</b> is on the difference in dynamic <b>behaviour between slow floor heating and fast radiators</b> as the heating emissions systems.</p>

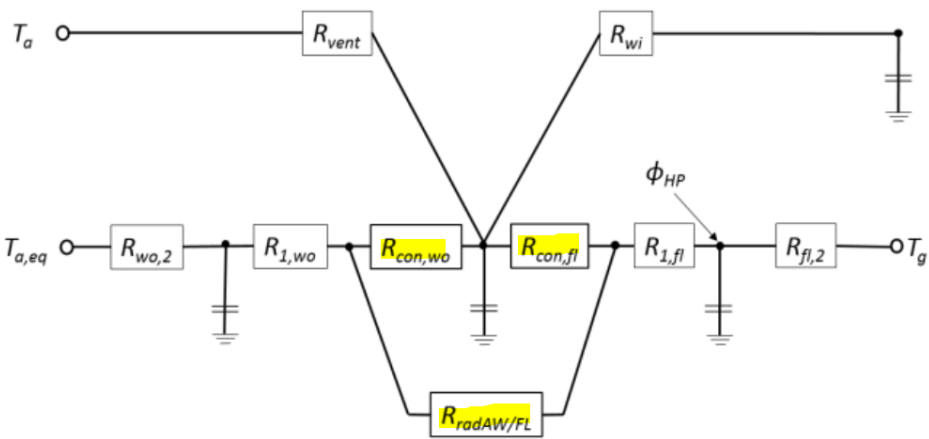
<b>Order of the model</b>	4 <sup>th</sup>
<b>Description of the (main) parameters</b>	RC representation of the 4th order grey-box model. $C_i$ , $C_w$ , $C_{wi}$ , $C_f$ are respectively the indoor air, external wall, internal wall and floor capacity. $T_e$ and $T_g$ are the air and ground temperature used as input for the model. The solar gains and heating input are not show
<b>Number of zones</b>	1
<b>Year of publication</b>	2015
<b>Takeaways:</b>	<ul style="list-style-type: none"> <li>• 1st order model could be sufficient to model floor heating (slow, mostly radiative heat exchange) due to the low-pass filtering effect of the high thermal mass, even a single capacitance model can provide a good approximation in the case of floor heating systems.</li> <li>• 2nd order is necessary to model radiators (different C is needed for the air, because heat transfer is mostly convective).</li> <li>• 3<sup>rd</sup> order showed the best results (smallest RMSE) but it showed over-parameterization issues.</li> <li>• Not only the lay-out of the RC-network, but also the way that heating and solar gains are introduced have a significant impact on the reliability of the models and the estimated parameters</li> </ul>

- **Ref.3** - Bottom-up Modeling of Residential Heating Systems for Demand Side Management in District Energy System Analysis and Distribution Grid Planning (Kramer et al., 2017).
- **Ref.2** - Validation of RC Building Models for Applications in Energy and Demand Side Management (Kuniyoshi et al., 2018).

Kremer is author of both publications. They are here presented together.

<p>RC model used</p>	<p>Main analysed 6R4C model:</p>



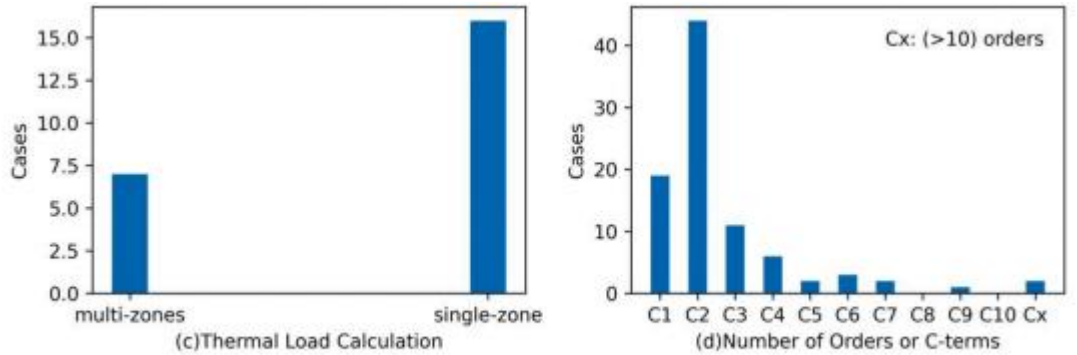
	 <p><math>R_{radAW/FL}</math> is added to represent the long-wave radiation.  <math>R_{radAW/FL}</math> is calculated as <math>1/(\alpha_{str} \cdot A_{FL})</math> with a radiant heat transfer coefficient <math>\alpha_{str} = 5 \text{ W/m}^2\text{K}</math> and the area of the floor <math>A_{FL} [\text{m}^2]</math> based on the VDI 6007.  Also the convective superficial resistances are separated from the envelope and floor resistances:</p> $R_{con} = \frac{1}{\alpha_{con} \cdot A}$ <p><math>\alpha_{con}</math> = convective coefficient. An internal convective coefficient of <math>2.7 \text{ W/(m}^2\text{K)}</math> is adopted.</p>
<b>Notes:</b>	<ul style="list-style-type: none"> <li>• The main aim is to investigate the accuracy of RC models for the simulation of large districts energy demand to support the management of district energy systems (such as Smart Grid and District Heating).</li> <li>• These models are based on the German standard VDI 6007, international Standard 13790: 2008 and on the work of Glenn Reynnders (Ref. 6,7,8).</li> <li>• In Ref.2 the focus is on the simulation of floor heating for a standalone, well insulated house.</li> <li>• Ref.3 focuses on model predictive control strategies for energy management. For that 4 representative typologies for the German building stock of standalone houses are modelled.</li> <li>• Inter-model comparison with EnergyPlus is used for validation.</li> </ul>
<b>Order of the model</b>	<b>4<sup>th</sup></b>

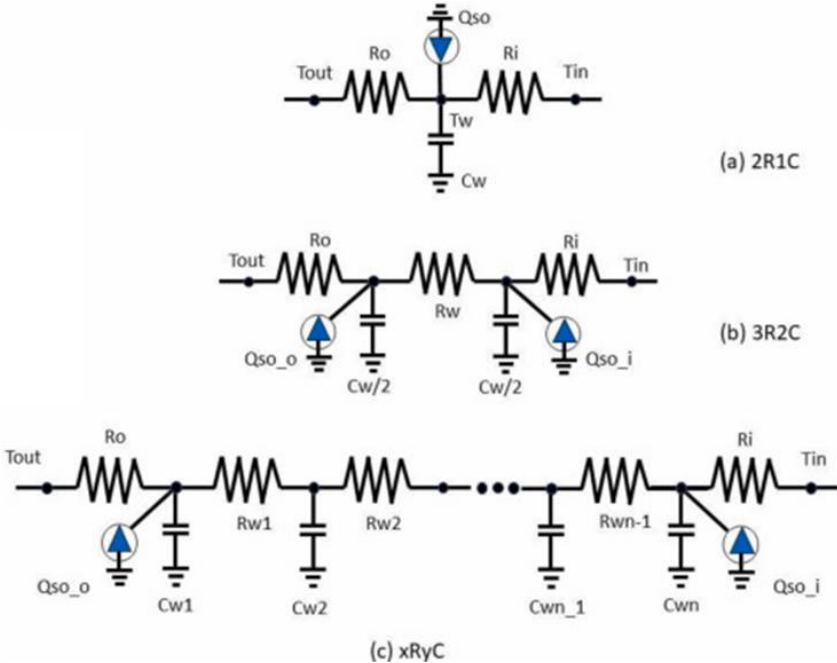


Description of the (main) parameters	Description
$R_{wo,1}$	resistance of the inner side of the outer components (outer walls, roof, windows, and door)
$R_{wo,2}$	resistance of the outer side of the outer components
$R_{fl,1}$	resistance of the inner side of the floor
$R_{fl,2}$	resistance of the outer side of the floor
$R_{wi}$	resistance of the inner walls.
$R_{vent}$	thermal resistance for the air exchange with the ambient air due to ventilation, infiltration and thermal bridges
$C_z, C_{wi}, C_{wo}, C_{fl}$	heat capacitances of each temperature node (zone air, inner walls, outer components and floor)
$\varphi_{sg}$	internal solar gain coming through the windows
$\varphi_{HP}$	heat gain from the heating system
$S_z, S_{wi}, S_{wo}, S_{fl}$	distribution factors of internal solar gain for each temperature node
$f_z, f_{wi}, f_{wo}, f_{fl}$	distribution factors of heat gain from the heating system for each temperature node
$T_a$ = Ambient temperature = T. outdoor on the external surface	
$T_z$ = Zone temperature = Air T. indoor	
$T_g$ is assumed to be 10 °C.	
The shortwave radiation from the sun absorbed by the external surfaces of the building components is considered by introducing a modified equivalent ambient temperature $T_{a,eq}$	
$T_{a,eq} = T_a + \sum_v \left[ \frac{U_v A_v}{\sum_v U_v A_v} (I_{dir,v} + I_{diff,v}) \frac{\alpha_F}{\alpha_A} \right]$	
Other temperatures are derived in such a way:	
$\dot{T}_z = \frac{1}{R_{vent} C_z} (T_a - T_z) + \frac{1}{R_{wi} C_z} (T_{wi} - T_z) + \frac{1}{R_{wo,1} C_z} (T_{wo} - T_z) + \frac{1}{R_{fl,1} C_z} (T_{fl} - T_z) + \frac{S_z}{C_z} \varphi_{sg} + \frac{f_z}{C_z} \varphi_{HP}$	
$\dot{T}_{wi} = \frac{1}{R_{wi} C_{wi}} (T_z - T_{wi}) + \frac{S_{wi}}{C_{wi}} \varphi_{sg} + \frac{f_{wi}}{C_{wi}} \varphi_{HP}$	
$\dot{T}_{wo} = \frac{1}{R_{wo,2} C_{wo}} (T_{a,eq} - T_{wo}) + \frac{1}{R_{wo,1} C_{wo}} (T_z - T_{wo}) + \frac{S_{wo}}{C_{wo}} \varphi_{sg} + \frac{f_{wo}}{C_{wo}} \varphi_{HP}$	
$\dot{T}_{fl} = \frac{1}{R_{fl,2} C_{fl}} (T_g - T_{fl}) + \frac{1}{R_{fl,1} C_{fl}} (T_z - T_{fl}) + \frac{S_{fl}}{C_{fl}} \varphi_{sg} + \frac{f_{fl}}{C_{fl}} \varphi_{HP}$	
The heat losses due to ventilation and infiltration are calculated as follows:	
$Q = c_{air} V_{zone} (\eta_{vent} + \eta_{inf} + \eta_{mec} (1 - \varepsilon)) \cdot (T_a - T_z),$	
where $c_{air}$ is the volumetric specific heat of air [J/m <sup>3</sup> K], $V_{zone}$ is the volume of the zone air [m <sup>3</sup> ], $\eta$ are the ACH (volume air change rates per hour) [1/h] for natural ventilation, infiltration and mechanical ventilation and $\varepsilon$ is the efficiency of heat recovery of a mechanical ventilation system [-].	
$\eta_{vent} + \eta_{inf} = 0,5$ [1/h]	

	$\eta_{mec} = 0,55 \text{ [1/h]}$ Efficiency of heat recovery = 0,84%
<b>Number of zones</b>	<b>1 (single)</b>
<b>Year of publication</b>	<b>2017 and 2018</b>
<b>Takeaways:</b>	<ul style="list-style-type: none"> <li>Envelope resistances are spitted into 2 (as suggested by G. Reynders et al., 2014)</li> <li>RC models ('grey-box') have good potential in the support of district energy management by predicting energy demand dynamically.</li> <li>(Ref 2) Increasing the number of thermal resistances gives better results (a similar conclusion is in Ref. 4). In this publication the added resistance has a focus on the floor heating accuracy.</li> <li>Additional insight about modelling floor heating can be found in Ref.2.</li> </ul>

- **Ref4 - Grey-box modeling and application for building energy simulations – A critical review** (Li et al., 2021)

<b>RC model used</b>	N.A.
<b>Notes:</b>	This research is <b>a literature review on its own</b> . With <b>many interesting insights</b> on the overall RC modelling context and possibilities. Worth reading especially for the developers of the mathematical approach used to solve the target simulation values, modelling language and control systems.
<b>Order of the model</b>	<p>N.A. Based on this literature review, 2<sup>nd</sup> order grey-box modelling is the top pick of previous researchers.</p>  <p style="text-align: center;">Fig. 15. Grey-box modeling statistics.</p> <p>Sample text and image about some analysed researches for single-zones models:</p> <p>"[...] The 5R1C model according to ISO13790 was used to model a residential building. The hourly cooling and heating load agreed well with EnergyPlus simulation results [77]. Analytical solutions were proposed for simplified RC building models with a set of different orders: 5R2C, 4R2C, 2R2C, and 1R2C [78]. The results showed that the proposed solutions had good agreement with the measurement data and EnergyPlus results. A comparison was performed between 5R1C and 7R2C models to a residential building based on ISO13790 and German Guideline VDI 6007, respectively. The results showed that the 7R2C model had better accuracy and was acceptable for heating and cooling load prediction [79] [...]"</p>

	 <p>(a) 2R1C</p> <p>(b) 3R2C</p> <p>(c) xRyC</p>
<b>Description of the (main) parameters</b>	<p>Structure of the discussed paragraphs in this literature review article:</p> <ul style="list-style-type: none"> <li>1 Introduction</li> <li>2 RC modeling fundamentals             <ul style="list-style-type: none"> <li>2.1 RC model structure                 <ul style="list-style-type: none"> <li>2.1.1 RC modeling for envelope</li> <li>2.1.2 RC modeling for zone air</li> <li>2.1.3 RC modeling for zone internal mass</li> <li>2.1.4 RC modeling for internal heat gains</li> <li>2.1.5 RC modeling for infiltration</li> <li>2.1.6 RC modeling for a single zone</li> <li>2.1.7 RC modeling for multi-zones or whole building</li> <li>2.1.8 RC modeling diagram representation</li> </ul> </li> <li>2.2 RC model creation and parameter estimation                 <ul style="list-style-type: none"> <li>2.2.1 Forward approach</li> <li>2.2.2 Inverse approach</li> <li>2.2.3 RC model order reduction</li> </ul> </li> </ul> </li> <li>3 RC model applications             <ul style="list-style-type: none"> <li>3.1 Heat dynamics analysis</li> <li>3.2 Thermal load calculation</li> <li>3.3 Building control and optimization</li> <li>3.4 District/urban energy modeling</li> <li>3.5 Building grid integration</li> </ul> </li> <li>4 RC modeling toolbox</li> <li>5 Conclusions</li> <li>Declaration of competing interest</li> <li>Acknowledgments</li> <li>References</li> </ul>
<b>Number of zones</b>	<p>N.A.</p>
<b>Year of publication</b>	<p>2021</p>
<b>Takeaways:</b>	<ul style="list-style-type: none"> <li>• Several RC models are analysed and compared.</li> <li>• Most model use 2 capacities with good results (small error).</li> </ul>

	<ul style="list-style-type: none"> <li>• To increase the accuracy, the number of thermal resistances could be increased without affecting the computational effort required. (A similar conclusion in Ref. 2).</li> <li>• Many of the analysed researches used the International Standard <b>ISO13790</b> [Energy performance of buildings] and the German Guideline <b>VDI 6007</b> as a reference when preparing RC models. Note that ISO13790: 2008 has been replaced by <b>ISO 52016:2017</b></li> </ul>
--	--

## 5. Literature study - Takeaways Summary

Based on literature studies, there are numerous representations of RC models. RC models are usually formatted into xRyC, in which x is the number of thermal resistances, and y is the number of thermal capacitances. RC models are normally quantified by their 'order', the order is often defined by the number of capacities in the model. So e.g., a 1<sup>st</sup>-order model will have just one capacity.

Some of the literature study main findings are below summarized into a list which includes possible simplifications and rules of thumb for RC modelling:

- Use at least two thermal capacities C (2<sup>nd</sup> order models) so that a distinction can be made between the slow dynamics of the structural mass C1 and the fast dynamics of the indoor air C2 (leading to higher accuracy).
- A minimum of 2 capacities (2<sup>nd</sup> order model) is suggested, up to 4 (more than 4 seem not be particularly relevant, causing over-parameterization issues (Ref 6, 7, 8). It could have some benefit to increase the HAN model to the 3<sup>rd</sup> order (3 capacities) but that would increase the computational effort (as the number of C defines the order of the differential equations). On the other hand, increasing the number of R could allow a higher degree of accuracy without compromising the low computational effort as suggested in Ref. 4 (Li et al., 2021). It could be beneficial, for instance, to introduce a separate resistance in parallel for the ground floor (see 'Step 3' as in 'Possible implementations for the HAN model').
- As a rule of thumb, the active thermal mass of the envelope corresponds to the thermal mass of the material layers within the insulation barrier (since only the first centimeters of an envelope wall are excited by a heating system). This means that the thermal mass of materials before the insulation (facing outdoor) could be neglected.  
Source: Ref.7 and 8. (G. Reynders et al., 2014)
- It is suggested to divide in two parts the internal resistance of the envelope (facades' walls, ground floor and roof). The two resulting resistances could be: 1) the thermal resistance between the indoor environment and the middle of the insulation material layer (including Rsi) and 2) the between the middle of the insulation layer and the outdoor environment (including Rse).
- Only few model types are needed to represent the majority of buildings. (G. Reynders et al., 2014) (Ref. 8).
- In case of mixed light and heavy envelope components, it could be beneficial to separate them into two different capacities (G. Reynders et al., 2014) (Ref. 8).

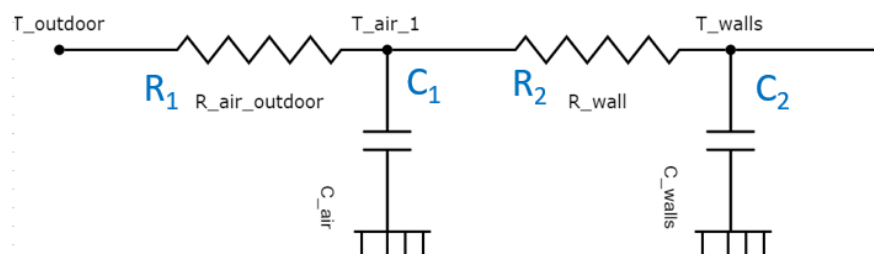
- Not only the lay-out of the RC-network, but also the way that heating and solar gains are introduced have a significant impact on the reliability of the models and the estimated parameters (Ref. 6).
- RC modelling can be of good support in the analysis of demand-side management of energy networks for large scale renovation projects (such as heating generation when provided by heat pumps and connected to a smart grid) or district heating, due to the lower computational effort.
- The International Standard **ISO13790** (Energy performance of buildings: 7.2.2 Simple hourly method) and the German Guideline **VDI 6007** both could be used to improve the model as both were cited multiple times and describe procedures for RC modelling to simulate the thermal behaviour (copy of ISO13790:2008 can be found at <https://www.nen.nl/en/nen-en-iso-13790-2008-en-122104>). Note that ISO13790:2008 has been replaced by **ISO 52016:2017** (copy can be found at <https://www.nen.nl/en/nen-en-iso-52016-1-2017-en-236338>. See: '7.3 Hourly method: validation in case of specific alternative calculation procedures'. And **calculations described in 6.5.6.3**). Note also that, in case alternative models are used, ISO 52016:2017 provides a verification case for validation "[...] Alternative options for the subdivision of each construction elements into a number of nodes of thermal resistances and capacitances are allowed, provided that the verification cases in 7.2 are applied to validate the method [...]".
- Validation of RC models has often been done through inter-model comparison and in fewer cases through empirical data comparison. In the first case, a 'grey-box' RC model is compared with a 'white-box' model with same characteristics (materials, form, environmental bordering conditions etc.).

## 6. HAN Model - Analysis of the main (current) parameters

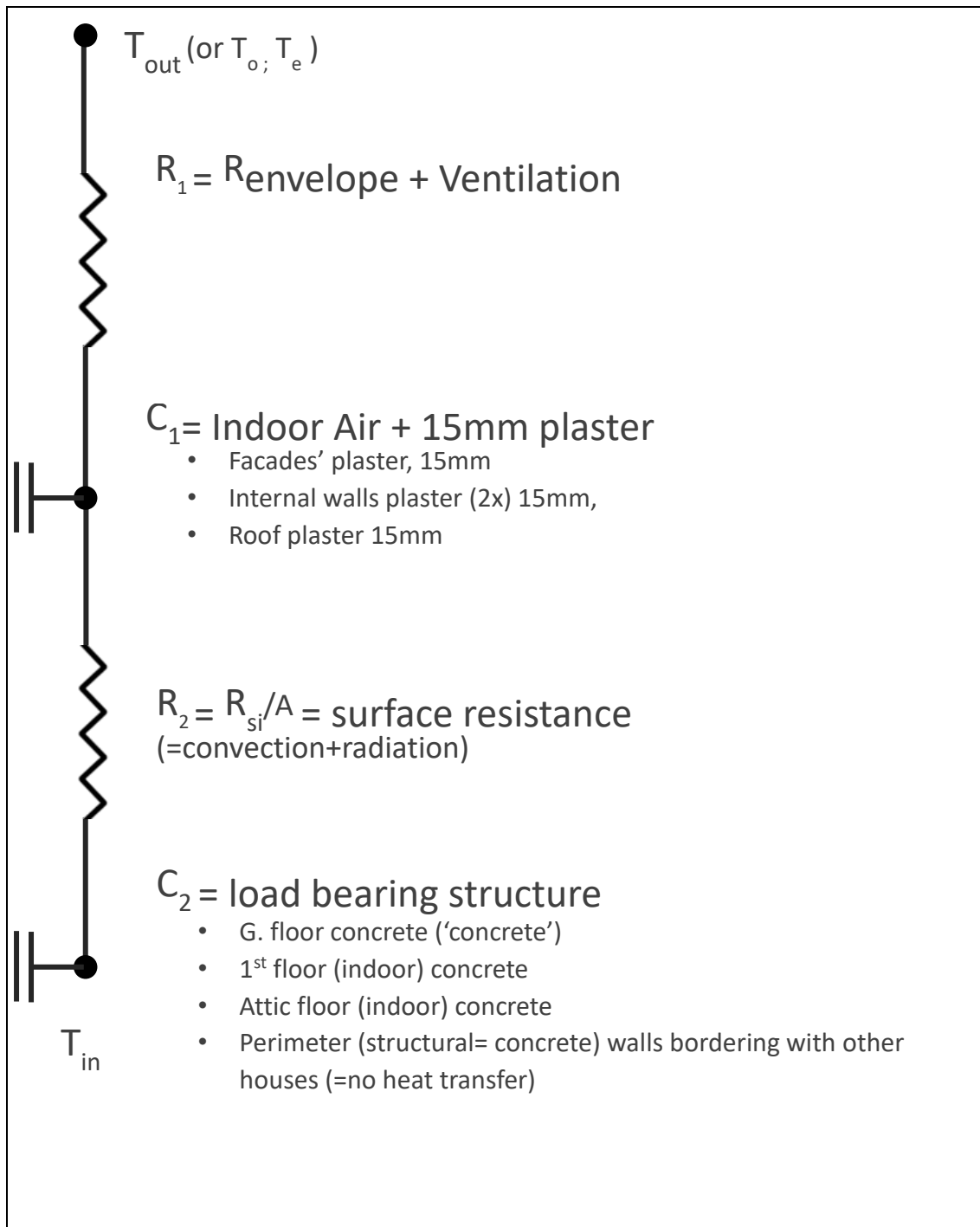
The following analysis is based on the Excel 'Tussenwoning' used as a tool for preparing the HAN Model ('grey-box') RC parameters for the dynamic simulation.

### 4. Current RC model

RC layout:



RC layout explanation based on analysed Excel (insights are presented in the below tables):



Summary table of the R-C parameters:

Name:	Description:	Unit
R <sub>air outdoor</sub> <b>R1</b>	Lumped' Resistance includes:	K/W
	• Windows	
	• Façade walls (including insulation)	
	• Roof (including insulation)	
	• Ground floor (including insulation)	
	• Ventilation (with heat recovery)	
	• Air infiltrations (infiltration and natural ventilation together)	
$= \frac{1}{\left( \frac{A_{windows}}{R_{windows}} + \frac{A_{facades}}{R_{facade}} + \frac{A_{roof}}{R_{roof}} + \frac{A_{floor}}{R_{groundfl.}} \right) + (m_{air\_ven} * (1 - \eta_{WTW}) + m_{air\_inf}) * c_{p\_air}}$		
<b>Note:</b> <ul style="list-style-type: none"> <li>• <i>R<sub>so</sub> currently is not considered (see paragraph 'Rc-waarde, R<sub>si</sub>, R<sub>se</sub> and U-waarde: a brief explanation' for more information)</i></li> <li>• <i>I suggest separating the ventilation losses</i></li> </ul>		
C <sub>air</sub> <b>C1</b>	• Indoor air capacity (for the indoor volume of air)	J/K
	• + Capacity of the internal side of the envelope (roof+façade walls 15mm plaster layer).	
	• + internal partition walls (2x15mm plaster)	
	$(A_{facade\_no-windows} + A_{interior\_walls} + A_{roof}) * c_{plaster\_15mm} + V_{volume\_indoor} * D_{density\_air} * c_{air}$	
<ul style="list-style-type: none"> <li>• <i>If this is the internal capacity, why is it located before R2 (R<sub>si</sub>, internal surface resistance) and C2 (structural materials capacity)?</i></li> </ul>		
R <sub>wall</sub> <b>R2</b>	= R <sub>si</sub> /A (Inside surfaces resistance. Taking into account convection and radiation on surface)	K/W
<b>Note:</b> <ul style="list-style-type: none"> <li>• <i>Missing the area of the facades-walls (instead wall bordering with other houses are used)</i></li> <li>• <i>Missing area of roof (instead 2xAttic is used)</i></li> <li>• <i>Areas of interior partitions (such as attic, floor between g.f. and 1st-floor and walls bordering with other houses, could be considered adiabatic and neglected)</i></li> <li>• <i>The used R<sub>si</sub> (=0,13 m2K/W) is valid only for horizontal heat transfer (i.e., vertical walls. See paragraph 'Rc-waarde, R<sub>si</sub>, R<sub>se</sub> and U-waarde: a brief explanation' for more information). Here it is applied also for vertical heat exchange (i.e., floor and roof). But this should lead to minor effect as R<sub>si</sub> for roof is normally 0,1.</i></li> </ul>		
$= \frac{R_{si}}{A_{ground\_floor} + 2 * A_{intermediate\_indoor\_floor} + 2 * A_{Attic\_floor} + 2 * A_{Perimeter-wallsbordering-other-houses}}$		
C <sub>wall</sub> <b>C2</b>	Thermal capacity of load-bearing construction, including:	J/k
	• Ground floor	
	• Intermediate floor (between ground and 1st floor)	
	• Attic floor	
	• Perimeter-wall, bordering other houses (so not insulated and without heat transfer as not bordering with outdoor temperature T <sub>e</sub> but with another heated environment)	
	$= c_{p\_concrete} * D_{density\_concrete} * (A_{ground\_floor} * d_{Thickness\_groundfloor} + A_{intermediate\_indoor\_floor} * d_{Thickness\_floor} + A_{Attic\_floor} * d_{Thickness\_Attic-floor} + 2 * A_{Perimeter-walls\_bordering-other-houses} * d_{Thickness\_Perimeter-walls})$	

- This should be placed before (from outdoor to indoor) C1 (internal air and walls capacity). Currently the effect of the thermal resistance of the envelope is not perceived by this capacity (for suggestions, see paragraph 'Possible implementations for the HAN model').

Detailed table about the R-C parameters a in the Excel 'Tussenwoning':

Term C1	Formula as in Excel	'Sheet'Cell	unit
Capacity C1	= 'Prepare_Data' !B31	'YAML_XLS'D2 5	J/K
Warmtecapaciteit intern C1	=( (B29+B12) *B30)+(B36*Referentie_data !B3*Referentie_data!B4)  Add missing parenthesis.	'Prepare_Data' !B31	kJ/K → J/K Correct unit  Check: $m^2 * \frac{J}{m^2 K} = \frac{J}{K}$ $+ m^3 * \frac{kg}{m^3} * \frac{J}{kg K} = \frac{J}{K}$
$(A_{\text{facade\_no-windows}} + A_{\text{interior\_walls}} + A_{\text{roof}}) \cdot C_{\text{plaster\_15mm}} + V_{\text{indoor}} \cdot \text{Density\_air} \cdot C_{\text{air}}$			
Totaal oppervlak wanden <i>Total surface of walls (it includes the indoor surfaces of both partition walls and facade walls)</i>	=B10 + B26*2+B27*2  =A <sub>facade\_no-windows</sub> + 2*A <sub>interior\_walls\_1st-floor</sub> + 2*A <sub>interior\_walls\_ground-floor</sub>	'Prepare_Data' !B29	m2
Roof surface = A <sub>roof</sub>	value	'Prepare_Data' !B12	m2
Heat capacity surface internal walls (15 mm plaster)	value	'Prepare_Data' !B30	J/m2K
Net air volume (indoor volume)	value	'Prepare_Data' !B36	m3
Density air	value	Referentie_data !B3	kg/m3
Specific heat capacity air	value	Referentie_data !B4	J/kgK
Term C2	Formula as in Excel	'Sheet'Cell	unit
Capacity C2	= 'Prepare_Data' !B50	'YAML_XLS'D2 9	J/K
Warmtecapaciteit constructie (C2)	=B49*B48*B46	'Prepare_Data' !B50	J/K  Check: $\frac{J}{kg K} * \frac{kg}{m^3} * m^3 = \frac{J}{K}$
$= C_{p\_concrete} * \text{Density\_concrete} * (A_{\text{ground\_floor}} * d_{\text{Thickness\_groundfloor}} + A_{\text{intermediate\_indoor-floor}} * d_{\text{Thickness\_foor}} + A_{\text{attic\_floor}} * d_{\text{Thickness\_Attic-foor}} + 2 * A_{\text{Perimeter-walls\_bordering-other-houses}} * d_{\text{Thickness\_Perimeter-walls}})$			
Specifieke warmte <i>Specific heat capacity = C<sub>p</sub> (of concrete)</i>	value	'Prepare_Data' !B49	J/kgK



Dichtheid <i>Density (of concrete)</i>	value	'Prepare_Data' '!B48	Kg/m3
totaal volume <i>(of load-bearing materials)</i>	=B37*B38+B39*B40+B41*B42+ 2*B43*B44  =A <sub>ground_floor</sub> * d <sub>Thickness_groundfloor</sub> + A <sub>intermediate_indoor-floor</sub> * d <sub>Thickness_foor</sub> + A <sub>attic_floor</sub> * d <sub>Thickness_Attic-foor</sub> + 2*A <sub>Perimeter-walls_bordering-other-houses</sub> * d <sub>Thickness_</sub> Perimeter-walls	'Prepare_Data' '!B46	m3
<b>Term R1</b>	<b>Formula as in Excel</b>	<b>'Sheet'Cell</b>	<b>unit</b>
Conductance 1/R1 (R1=Resistance)	=1/'Prepare_Data '!B24	'YAML_XLS'D2 4	W/K
Warmteweerstand schil R1 <i>(Heat Resistance envelope + Air infiltration and ventilation)</i>	=1/((B7/B9+B10/B11+B12/B13+B14/B15) +((B17*(1- B21)+B22)*Referentie_data!B2*Referentie_data! B4))  Referentie_data!B2 should be removed & 2 missing parenthesis	'Prepare_Data' '!B24	K/W  Check: $\frac{1}{\frac{m^2}{m^2K/W} + \frac{kg}{s} * \frac{J}{Kg K}} = \frac{K}{W}$
$= \frac{1}{\left( \frac{A_{windows}}{R_{windows}} + \frac{A_{facades}}{R_{facade}} + \frac{A_{roof}}{R_{roof}} + \frac{A_{floor}}{R_{groundfl.}} \right) + (m_{air\_ven} * (1 - \eta_{WTW}) + m_{air\_inf}) * c_{p\_air}}$			
Totaal glasoppervlak <i>(total glass area)</i>	value	'Prepare_Data' '!B7	m2
Rc-waarde glas	value	'Prepare_Data' '!B9	m2K/W
Totaal gesloten oppervlak gevel <i>Total surface façade (façade – windows area)</i>	value	'Prepare_Data' '!B10	m2
Rc-waarde gevel = R <sub>walls</sub> <i>façade, including insulation (when present).</i>	value	'Prepare_Data' '!B11	m2K/W
Roof surface	value	'Prepare_Data' '!B12	m2
Rc-waarde dak	value	'Prepare_Data' '!B13	m2K/W
Oppervlak vloer <i>Groundfloor Area</i>	value	'Prepare_Data' '!B14	m2
Rc vloer	value	'Prepare_Data' '!B15	m2K/W
Ventilatie <i>(mechanical Ventilation)</i>	=B16/3600*Referentie_data!B3 = m3/hr/3600*kg/m3=m3/s*kg/m3=kg/s  Value (basic mech. ventilation) =100m3/h= 0,36 ACH (= 100 [m3/h]/275,6[m3]). In line with <a href="#">ASHRAE recommendation (min 0,35 ACH)</a>	'Prepare_Data' '!B17	Kg/s

Warmteterugwining bij gekozen ventilatiesysteem <i>efficiency heat recovery mech. Vent.</i>	value	'Prepare_Data'!B21	-
Infiltrations of air Including natural ventilation? Probably yes, since it is equivalent to 1 ACH.	=INDEX(Referentie_data!B11:B12,B19)*INDEX(Referentie_data!B15:B18,B18)/(10*1000)*B28*Referentie_data!B3  =0,09kg/s =0,09[kg/s]*3600/1,2[kg/m3]=270m3/h =1ACH (270[m3/h]/275,6[m3]).	'Prepare_Data'!B22	Kg/s
Specific heat capacity air	value	Referentie_data!B4	J/kgK
<b>Term R2</b>	<b>Formula as in Excel</b>	<b>'Sheet'Cell</b>	<b>unit</b>
Conductance 1/R1 (R1=Resistance)	=1/'Prepare_Data'!B51	'YAML_XLS'D28	W/K
Weerstand tussen intern woning en bouwmassa (R2) <i>Rsi inner layer superfical resistance</i>	=1/('Prepare_Data'!B\$45*Referentie_data!B\$7)	'Prepare_Data'!B51	K/W Check: $\frac{1}{m^2 \cdot \frac{W}{m^2K}} = \frac{K}{W}$
$\frac{1}{\left( A_{ground\_floor} + 2 \cdot A_{intermediate\_indoor\_floor} + 2 \cdot A_{Attic\_floor} + 2 \cdot A_{Perimeter-walls\_bordering-other-house} \right) \cdot R_{si}}$ $= \frac{R_{si}}{A_{ground\_floor} + 2 \cdot A_{intermediate\_indoor\_floor} + 2 \cdot A_{Attic\_floor} + 2 \cdot A_{Perimeter-walls\_bordering-other-house}}$			
Totaal oppervlak (total area)	=B37+2*B39+2*B41+2*B43 = A <sub>ground_floor</sub> +2* A <sub>intermediate_indoor-floor</sub> +2* A <sub>Attic_floor</sub> +2* A <sub>Perimeter-walls_bordering-other-houses</sub>  <ul style="list-style-type: none"> <li>Missing the area of the facades-walls (instead walls bordering with other houses are used).</li> <li>Missing area of roof (instead attic and GF/1<sup>st</sup> floor - =interior floors - are used).</li> <li>Areas of interior partitions (such as A<sub>Attic</sub>, floor between g.f. and 1<sup>st</sup>-floor and walls bordering with other houses, can be considered adiabatic and so neglected).</li> </ul>	'Prepare_Data'!B\$45	m2
Warmte overdrachtscoëfficiënt tussen intern woning en muur =1/R <sub>si</sub>	Value = 1/R <sub>si_Horizontal</sub> = 1/0,13 = 7,7 <ul style="list-style-type: none"> <li>Approximated to 8</li> <li>R<sub>si</sub>=0,13 is valid just for horizontal heat transfer (i.e., vertical walls)</li> </ul>	Referentie_data!B\$7	W/m2.K
R <sub>si</sub>			m2K/W

## 7. Possible implementations for the HAN model

Maintaining 2<sup>nd</sup> order (2 capacities):

- 1) 2<sup>nd</sup> order (2R2C = 2 capacities and 2 resistances). **Drawback:** both thermal mass of load bearing structure and plaster layer (on top of air and interior partition walls capacity) are located after (facing indoor) the resistance which includes the insulation layer. **This could lead to over estimation of the effect of the thermal mass.**

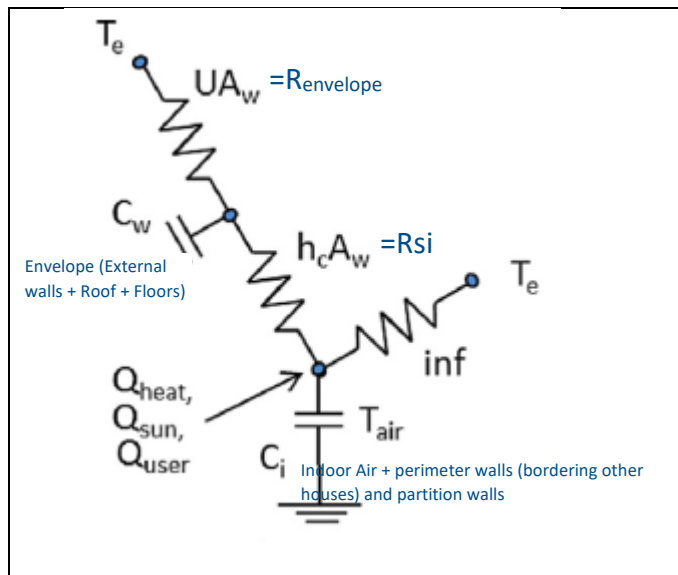
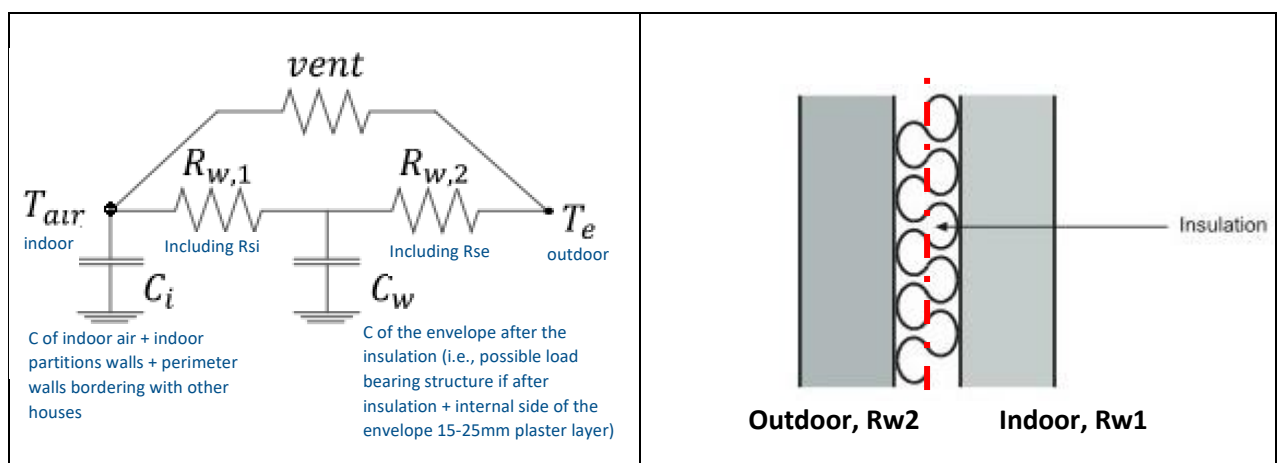


Fig. Based on Ref.8. (G. Reynders et al., 2014) literature study findings.

- 2) 2<sup>nd</sup> order (2R2C). **Improvement from previous network:** The thermal mass of the envelope can be divided between the most active part (after the insulation, facing indoor) and the less active. This is done by splitting the thermal resistance of the envelope into 2. This should result in **more realistic effect of the thermal mass.**

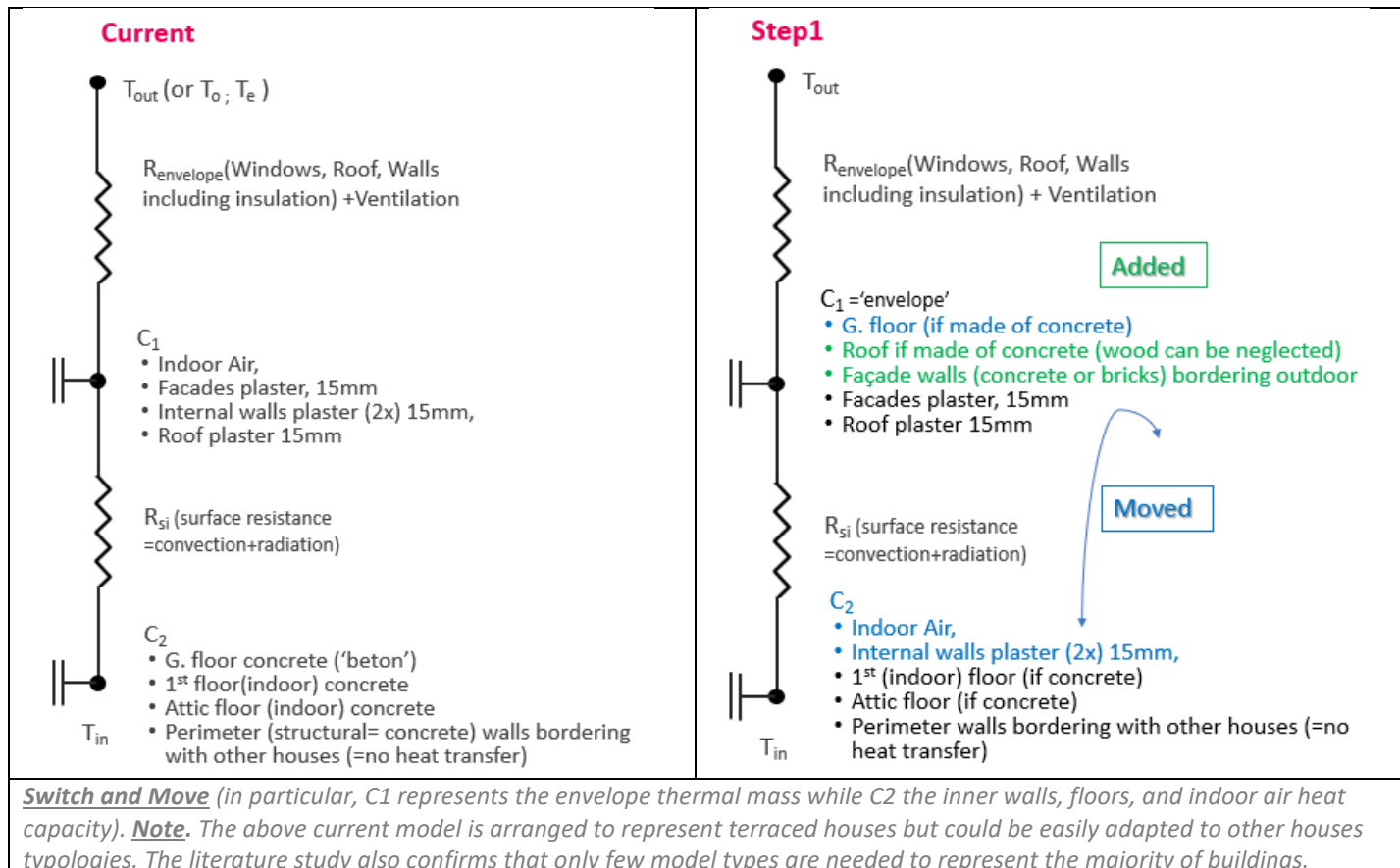
**Possible drawback (in order of importance):**

- I. Ground floor heat transfer cannot be simulated independently with a bordering  $T_{ground}$  (so either neglected or overestimated using bordering  $T_{environment}$ ).
- II. Not possible to separate day and night zones.
- III. Not possible to separate the capacity of the indoor air from that of the indoor partition (i.e., internal floors and walls).



Based on Ref.7 (Glenn Reynders et al., 2014) and Ref.6 (Glenn Reynders et al., 2015) lit. study findings. **The internal resistance ( $R_{w1}$ ) is defined as the thermal resistance between the indoor environment and the middle of the material layers within the insulation layer (including  $R_{si}$ ).  $R_{w2}$  is then defined as the thermal resistance between the middle of the layers within the insulation barrier and the outdoor environment (including  $R_{se}$ ).**

The above approach is suggested and specified in the steps below:  
(see the ppt 'possible RC changes' for the modifiable images files)



<p><b>Step2</b></p> <p><b>Ventilation</b></p> <p><math>T_{out}</math></p> <p><math>\frac{1}{2} R_{envelope} \text{ (including } R_{se})</math>  <math>= \frac{1}{2} R_{C-Waarde} + R_{se}</math></p> <p><math>C_1 = \text{'envelope'}</math></p> <ul style="list-style-type: none"> <li>• G. floor (if made of concrete)</li> <li>• Roof if made of concrete (wood can be neglected)</li> <li>• Façade walls (concrete or bricks) bordering outdoor</li> <li>• Facades' plaster, 15mm</li> <li>• Roof plaster 15mm</li> </ul> <p><math>\frac{1}{2} R_{envelope} \text{ (including } R_{se})</math>  <math>= \frac{1}{2} R_{C-Waarde} + R_{se}</math></p> <p><math>C_2 = \text{'internal'}</math></p> <ul style="list-style-type: none"> <li>• Indoor Air,</li> <li>• Internal walls plaster (2x) 15mm,</li> <li>• 1<sup>st</sup> (indoor) floor (if concrete)</li> <li>• Attic floor (if concrete)</li> <li>• Perimeter walls bordering with other houses (=no heat transfer)</li> </ul> <p><math>T_{in}</math></p>	<p>Divide the heat transfer resistance of the envelope in two parts, where the point of separation is at the middle of the insulation layer.</p> <p>Separate the ventilation heat losses from the envelope resistance.</p>
<p><b>Step3 (optional)</b></p> <p><b>Ventilation</b></p> <p><math>T_{out}</math></p> <p><math>\frac{1}{2} R_{envelope} \text{ (including } R_{se})</math></p> <p><math>C_1 = \text{'envelope'}</math></p> <ul style="list-style-type: none"> <li>• G. floor (if made of concrete)</li> <li>• Roof if made of concrete (wood can be neglected)</li> <li>• Façade walls (concrete or bricks) bordering outdoor</li> <li>• Facades' plaster, 15mm</li> <li>• Roof plaster 15mm</li> </ul> <p><math>\frac{1}{2} R_{envelope} \text{ (including } R_{se})</math></p> <p><math>C_2 = \text{'internal'}</math></p> <ul style="list-style-type: none"> <li>• Indoor Air,</li> <li>• Internal walls plaster (2x) 15mm,</li> <li>• 1<sup>st</sup> (indoor) floor (if concrete)</li> <li>• Attic floor (if concrete)</li> <li>• Perimeter walls bordering with other houses (=no heat transfer)</li> </ul> <p><math>T_g</math></p> <p><math>R_{ground\_floor}</math></p> <p><math>T_{in}</math></p>	<p>(Optional) Separate the resistance of the ground. Ground temperature can so be separated from the outdoor environment temperature. As simplification, ground temperature could be set as a constant (average ground T).</p>

The above scheme could be duplicated to simulate separately a day and night zone (see an example in the RC-model of Ref. 7).

#### Increasing the order to 3<sup>rd</sup> order

A 3<sup>rd</sup> order model could also be implemented (adding a capacity) in the HAN model for buildings where there is a **mixed use of heavy and light elements** in the envelope (i.e., light roof and heavy walls, or heavy ground floor and light walls+roof). Whether adding a capacity is necessary could be verified through comparison with dynamic ‘white-box’ simulations. An example from Ref. 6 where the capacity of the ground floor (‘f’) is separated from that of the envelope (‘w’):

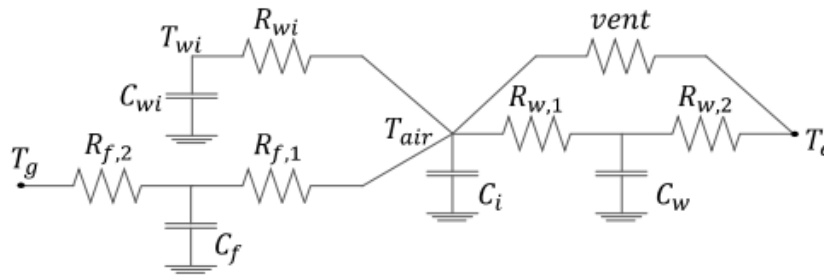


Fig. R6C4 example from reference 6 (Glenn Reynders et al., 2015).

This could be relevant for the ‘doorzonwoning’ with a mix of light and heavy construction elements, where possibly the external wall could be considered as **light envelope structure (C0)**, the **roof, ground floor as heavy envelope structure (C1)** and **internal partitions (floors, walls) plus the indoor air as internal capacity (C2)**.

**NOTE:** that if the ‘doorzonwoning’ envelope is all made of a light-weight structure (both light facades and roof) the capacity could be reduce to the **1<sup>st</sup> order (1C model)**. Where all the thermal mass is of the internal walls and floor is coupled with that of the indoor air. While the thermal mass of façade and roof could be possibly neglected. This 1C possible option requires further investigation (possibly through inter-model validation as suggested in the ‘Follow-up future research steps’ paragraph).

## 8. Rc-waarde, Rsi, Rse and U-waarde: a brief explanation

The U-value of a component is calculated by

$$U = \frac{1}{R_T} = \frac{1}{R_{se} + \frac{d_1}{\lambda_1} + \frac{d_2}{\lambda_2} + \dots + R_{si}}$$

$U$ : heat transfer coefficient in  $W / (K \cdot m^2)$

$R_T$ : thermal resistance in  $(K \cdot m^2) / W$

$R_{se}$ : external heat transfer resistance in  $(K \cdot m^2) / W$

$d_i$ : thickness of the layer number  $i$  in m

$\lambda_i$ : specific thermal conductivity of this layer in  $W / (K \cdot m)$

$1 / R_{\lambda} = \lambda_{sub,i,i}$ : the specific heat resistance of the  $i$ -th layer in  $(K \cdot m) / W$

$d_i / \lambda_{sub,i,i}$ : the thermal resistance of this layer in  $(K \cdot m^2) / W$

$R_{si}$ : internal heat transfer resistance in  $(K \cdot m^2) / W$

Surface Film Thermal Resistances  $R_{si}$  and  $R_{se}$  [ $m^2 K/W$ ]:

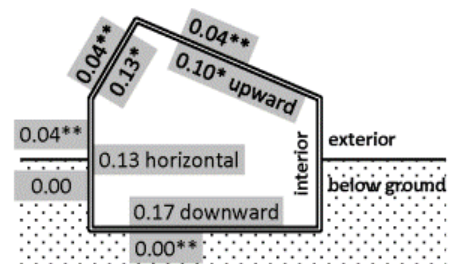


Image source: <https://www.ecomerchant.co.uk/news/u-values-for-dummies/>

$R_{si}$  and  $R_{se}$  accordingly, to EN ISO 6946 : 2007 (see):

Surface Resistance	Direction of heat flow		
( $m^2 K / W$ )	Upwards	Horizontal	Downwards
$R_{si}$	0.10	0.13	0.17
$R_{se}$	0.04	0.04	0.04

When using values of RC-waarde from the Dutch Building regulation ('Bouwbesluit' or NEN1068), Rsi and Rse are already included in the 'Rc-waarde' values, used in HAN model R1. See:

Om te voldoen aan de eisen van het Bouwbesluit 2015 kan de RC-waarde als volgt worden berekend:

$$R_c = \frac{\sum R_m + R_{si} + R_{se}}{1 + \alpha} - R_{si} - R_{se}$$

Uitleg symbolen:

Rc – Warmteweerstand van de constructie in m<sup>2</sup> K/W.

Rm – Warmteweerstand van de afzonderlijke lagen in de constructie in m<sup>2</sup> K/W.

Rsi – Warmte-overgangsweerstand binnen (si staat voor surface interior)

Rse – Warmte-overgangsweerstand buiten (se staat voor surface exterior)

α – Correctiefactor (onder meer convectie en onnauwkeurigheden in de verwerking)

*\*Voor de Rsi en Rse worden de waarden gehanteerd zoals opgenomen in het Bouwbesluit.*

Image source: <https://www.takkenkamp.com/kennisbank/rc-waarde/>

See also: [http://lanten.nl/bouwbesluit\\_2012/rc-waarde-berekenen/](http://lanten.nl/bouwbesluit_2012/rc-waarde-berekenen/)

The correction factor alpha is normally set at 5% (<https://www.isover.nl/beng-website/de-optimale-rc-waarden-voor-in-de-gevel.html>)

## 9. Follow-up future research steps

The next suggested step should include the validation of the suggested simplified RC model (see 'Possible implementations for the HAN model') for different building typology and the quantification (i.e., magnitude) of the effect of the simplifications.

First, additional research about the envelope (especially which components can be expected as light or heavy) of the main Dutch building typologies (i.e., terraced houses) is necessary in order to possibly decide to implement a 3<sup>rd</sup> order (3 capacities) model (see previous paragraph 'Relevant construction characteristics' and 'Possible implementations for the HAN model').

The xRyC, selected models have to be implemented in the HAN model software. Note that calculations for the "subdivision of each construction element into a number of nodes of thermal resistances and capacitances" are described in 6.5.6.3 of ISO 52016:2017. This could also be of support in the further development of the HAN model.

Then a validation of the model can be performed.



“

Validation is essential for improvement in the quality of a model<sup>(19)</sup> since it increases confidence in the predicted result. The increasing use of thermal models requires that their accuracy be assessed regularly. Validation is therefore an integral part of model development. Bowman and Lomas identify three validation methods<sup>(20)</sup>:

- analytical verification
- inter-model comparison
- empirical validation.

In analytical verification, the model predictions are compared with known exact solutions. Within a limited scope of application, this technique is useful for investigating errors in algorithms, but generating exact solutions is highly problematical.

In inter-model comparison, results from an identical problem are generated using two or more programs and the results are compared. However, favourable comparisons of results do not necessarily mean that these results are correct. Hence this method's usefulness is restricted to checking the consistency of predictive algorithms.

Empirical validation, on the other hand, compares a program's predictions with experimental data usually based on field measurements. In principle, this method gives 'real world' results, restricted only by the reliability and comprehensiveness of the measurements.

”

[Text cited from Ref9 (Gouda et al., 2000)]

From the three above cited validation method, I suggest the **inter-model comparison** for validating the RC configurations implemented in the HAN model. Some of the reasons of this suggestion are:

- the large availability nowadays of dynamic simulation software which one can clearly explain how they behave ('white-box' models), with high degree of reliability.
- the lack (or burdensome to implement) of an available experimental setup.

Some examples of available commercial 'white-box' software with a dynamic simulation module as a reference: Designbuilder (EnergyPlus interface), IESVE, IDA-ice, TRNSYS, Rhino (with Ladybug and Grasshopper), Vabi.

The choice of the software is often related to its use and level of complexity.

I suggest Designbuilder, an EnergyPlus interface. This is often the choice for researchers and lecturers of building physics and services when the primary goal is to simulate the integrated behaviour of building envelope, installations (i.e. generation) and other heat gains. See as an example this discussion in ResearchGate: <https://www.researchgate.net/post/Which-software-is-best-for-performing-building-energy-analysis>. Additionally, this software come with a discounted fare for students, and it has a visual interface which makes easier to build the model.

ISO 52016:2017 also provides a verification case for validation “[...] *Alternative options for the subdivision of each construction elements into a number of nodes of thermal resistances and capacitances are allowed, provided that the verification cases in 7.2 are applied to validate the method [...]*”. This could also be applied in the validation process. In that case, I suggest using the input parameters (such as geometry, materials properties, ventilation ACH etc.) described in 7.2 from the beginning, both in the HAN model and in the ('white-box') EnergyPlus (Designbuilder) model.



Finally, I suggest to cross reference the order of magnitude of the results from the different RC networks implemented in the HAN model with national statistical data such as (Delf University of Technology, n.d.) and (Agentschap NL, 2011a).

## **10. Discussion**

RC modelling can be of great support in the analysis of demand-side management of energy networks such as for large scale renovation projects concerning energy saving measures, due to its lower computational effort.

In particular, with the transition of heating systems to electrical heat pumps, models that can accurately predict heat demand with minimum computational effort are increasingly useful to guarantee a reliable power supply from smart grids.

HAN house model could be also used to quantify the impact of Future Factory large scale renovations within a smart grid and possibly contribute to real-time predictions of demands to match the smart grid supply. For this, the model should possibly reach a higher level of accuracy.

### **Pending internal (HAN meet- en regeltechniek group) questions**

- How 'easy' is to implement to a higher order the HAN RC model?
- Is in the interest of the HAN model (based on its future applications) to be able to simulate separate day and night zones?
- Is Future Factory and/or our research group interested in modelling also apartments as typology?

## 11. References

- Agentschap NL. (2011a). *Voorbeeldwoningen 2011 Bestaande bouw. Publicatie-nr. 2KPWB1034*. [www.voorbeeldwoningen.nl](http://www.voorbeeldwoningen.nl).
- Agentschap NL. (2011b). *Voorbeeldwoningen 2011 Onderzoeksverantwoording. Publicatie-nr. 2KPWB1036*, 38.
- Bond, D. E. M. (2006). *DESIGN AND ANALYSIS OF OPTIMAL MULTI-LAYER WALLS FOR TIME-VARYING THERMAL EXCITATION*.
- cbs. (2019). *Energy consumption private dwellings; type of dwelling and regions*. [https://www.cbs.nl/en-gb/figures/detail/81528ENG?q=parts of the country](https://www.cbs.nl/en-gb/figures/detail/81528ENG?q=parts%20of%20the%20country)
- Delf University of Technology. (n.d.). *TABULA project - Housing typologies Netherlands*. Retrieved October 20, 2021, from <https://episcopes.eu/building-typology/country/nl.html>
- Gouda, M. M., Danaher, S., & Underwood, C. P. (2000). Low-order model for the simulation of a building and its heating system. *Building Services Engineering Research and Technology*, 21(3), 199–208. <https://doi.org/10.1177/014362440002100308>
- Herwin Sap, Ronald Rovers, M. V. (2014). *the “Existing district of tomorrow”; a concept for quick an clean passive house renovation for mass housing in the Netherlands*. [https://www.researchgate.net/publication/262399331\\_the\\_Existing\\_district\\_of\\_tomorrow\\_a\\_concept\\_for\\_quick\\_an\\_clean\\_passive\\_house\\_renovation\\_for\\_mass\\_housing\\_in\\_the\\_Netherlands](https://www.researchgate.net/publication/262399331_the_Existing_district_of_tomorrow_a_concept_for_quick_an_clean_passive_house_renovation_for_mass_housing_in_the_Netherlands)
- Kramer, M., Jambagi, A., & Cheng, V. (2017). *Bottom-up Modeling of Residential Heating Systems for Demand Side Management in District Energy System Analysis and Distribution Grid Planning*. <https://doi.org/10.26868/25222708.2017.183>
- Kuniyoshi, R., Kramer, M., & Lindauer, M. (2018). *Validation of RC Building Models for Applications in Energy and Demand Side Management*.
- Li, Y., O'Neill, Z., Zhang, L., Chen, J., Im, P., & DeGraw, J. (2021). Grey-box modeling and application for building energy simulations - A critical review. *Renewable and Sustainable Energy Reviews*, 146, 111174. <https://doi.org/10.1016/J.RSER.2021.111174>
- Reilly, A., Kinnane, O., & O'hegarty, R. (2020). Energy embodied in, and transmitted through, walls of different types when accounting for the dynamic effects of thermal mass. *Journal of Green Building*, 15(4), 43–66. <https://doi.org/10.3992/JGB.15.4.43>
- Reynders, G., Diriken, J., & Saelens, D. (2014). Quality of grey-box models and identified parameters as function of the accuracy of input and observation signals. *Energy and Buildings*, 82, 263–274. <https://doi.org/10.1016/J.ENBUILD.2014.07.025>
- Reynders, Glenn, Diriken, J., & Saelens, D. (2014). *Bottom-up modeling of the belgian residential building stock: Influence of model complexity*. [https://www.researchgate.net/publication/303750596\\_Bottom-up\\_modeling\\_of\\_the\\_belgian\\_residential\\_building\\_stock\\_Influence\\_of\\_model\\_complexity](https://www.researchgate.net/publication/303750596_Bottom-up_modeling_of_the_belgian_residential_building_stock_Influence_of_model_complexity)
- Reynders, Glenn, Diriken, J., & Saelens, D. (2015). Impact of the Heat Emission System on the Identification of Grey-box Models for Residential Buildings. *Energy Procedia*, 78, 3300–3305. <https://doi.org/10.1016/J.EGYPRO.2015.11.740>
- van Oorschot, J. (2016). *HOUSING TYPOLOGY ASSESSMENT MORE-CONNECT WP3.1*. [https://www.more-connect.eu/wp-content/uploads/2019/07/MORE-CONNECT\\_WP3\\_D3.1-Overview-of-main-building-types.pdf](https://www.more-connect.eu/wp-content/uploads/2019/07/MORE-CONNECT_WP3_D3.1-Overview-of-main-building-types.pdf)