## PERSONAL NOTES

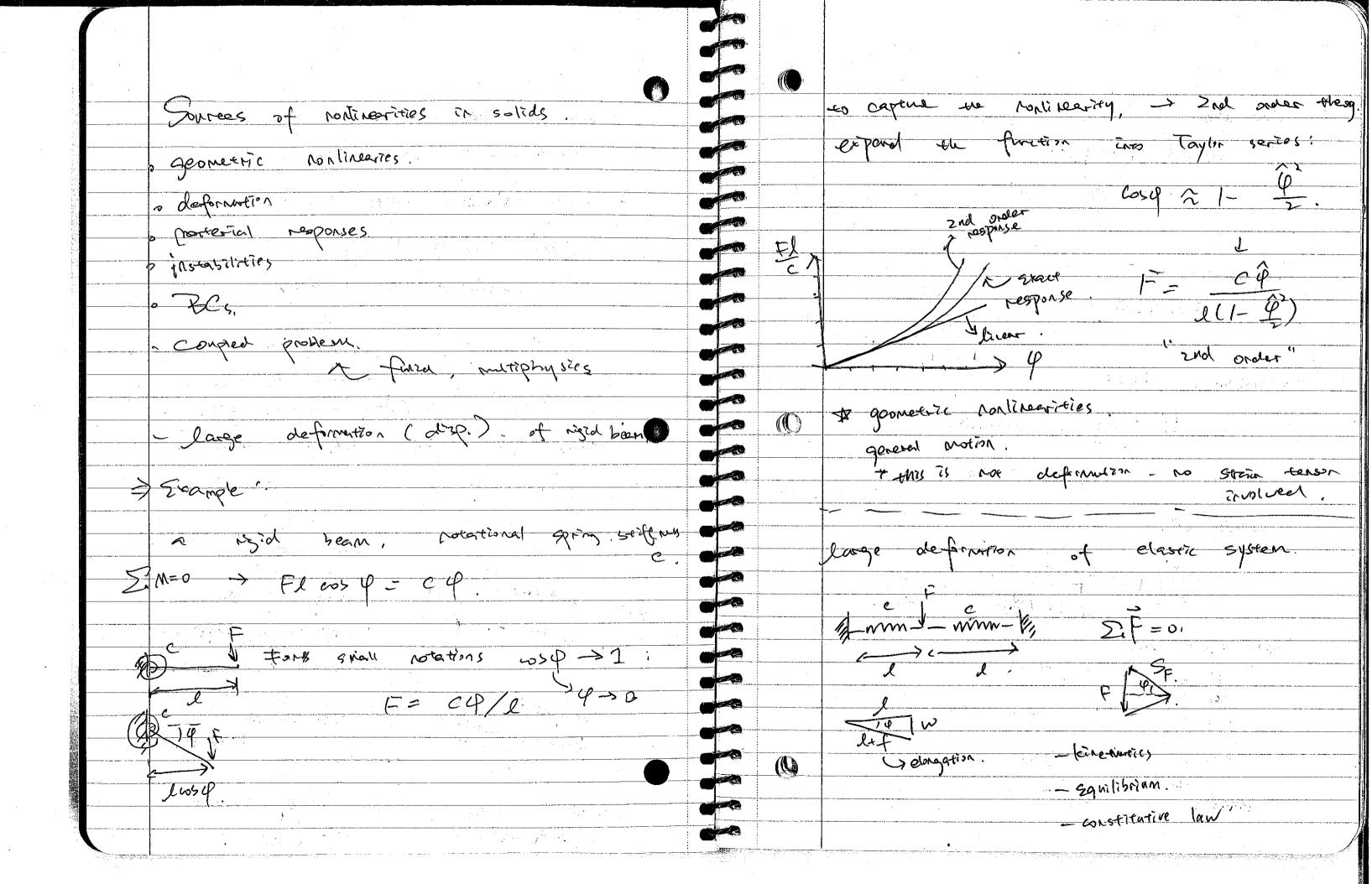
## Nonlinear F.E.A.

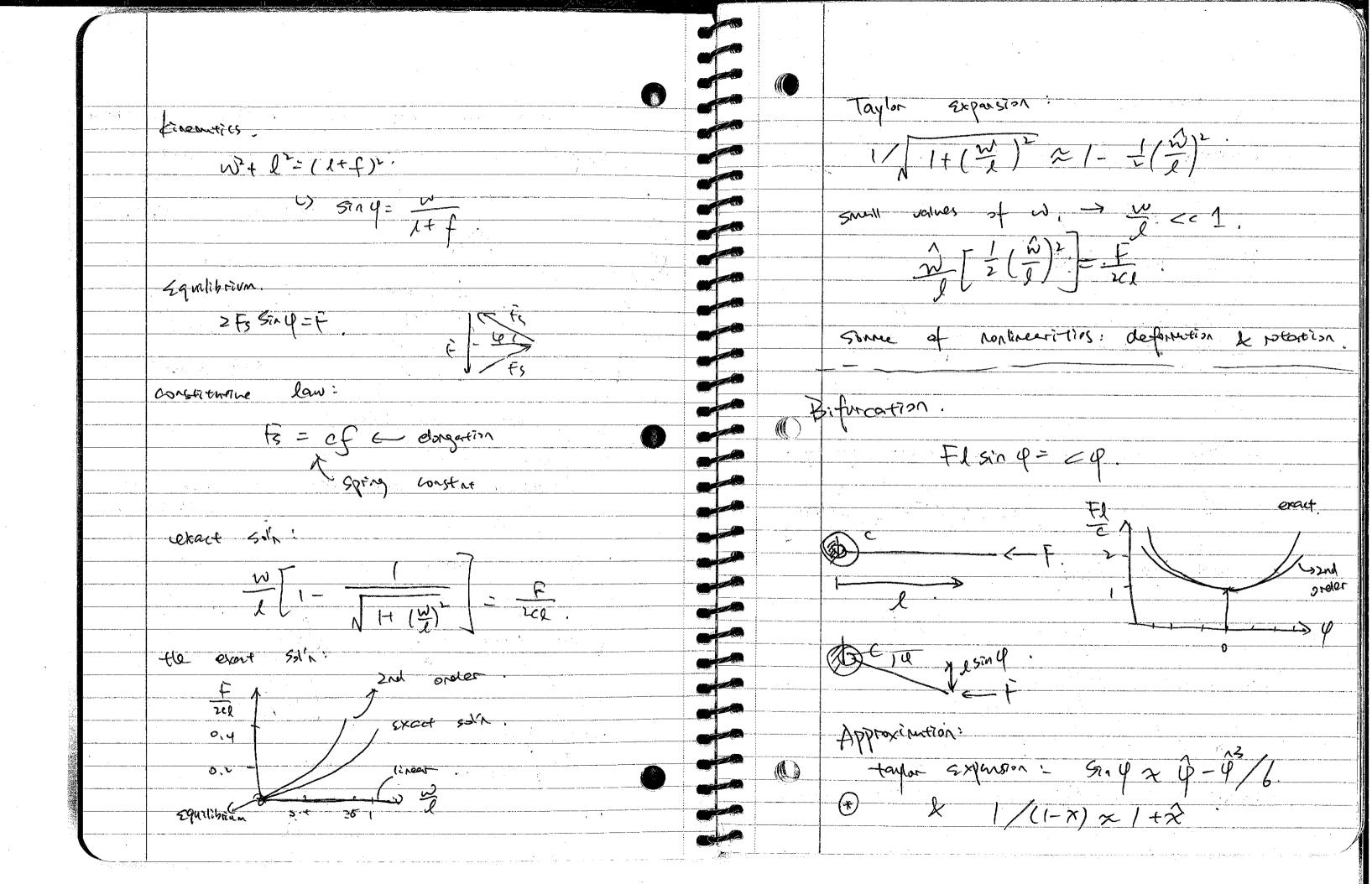
## Hanfeng Zhai

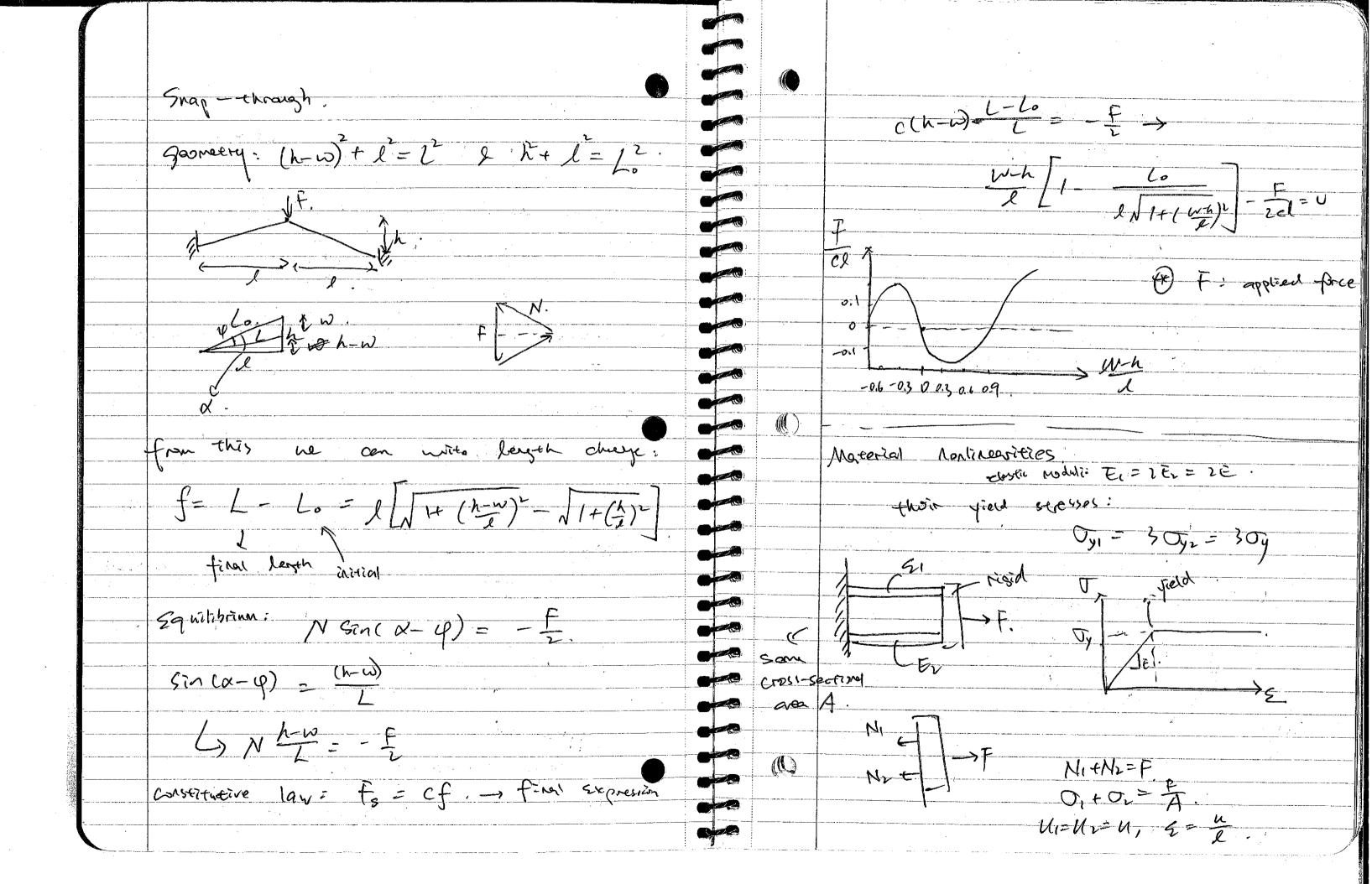
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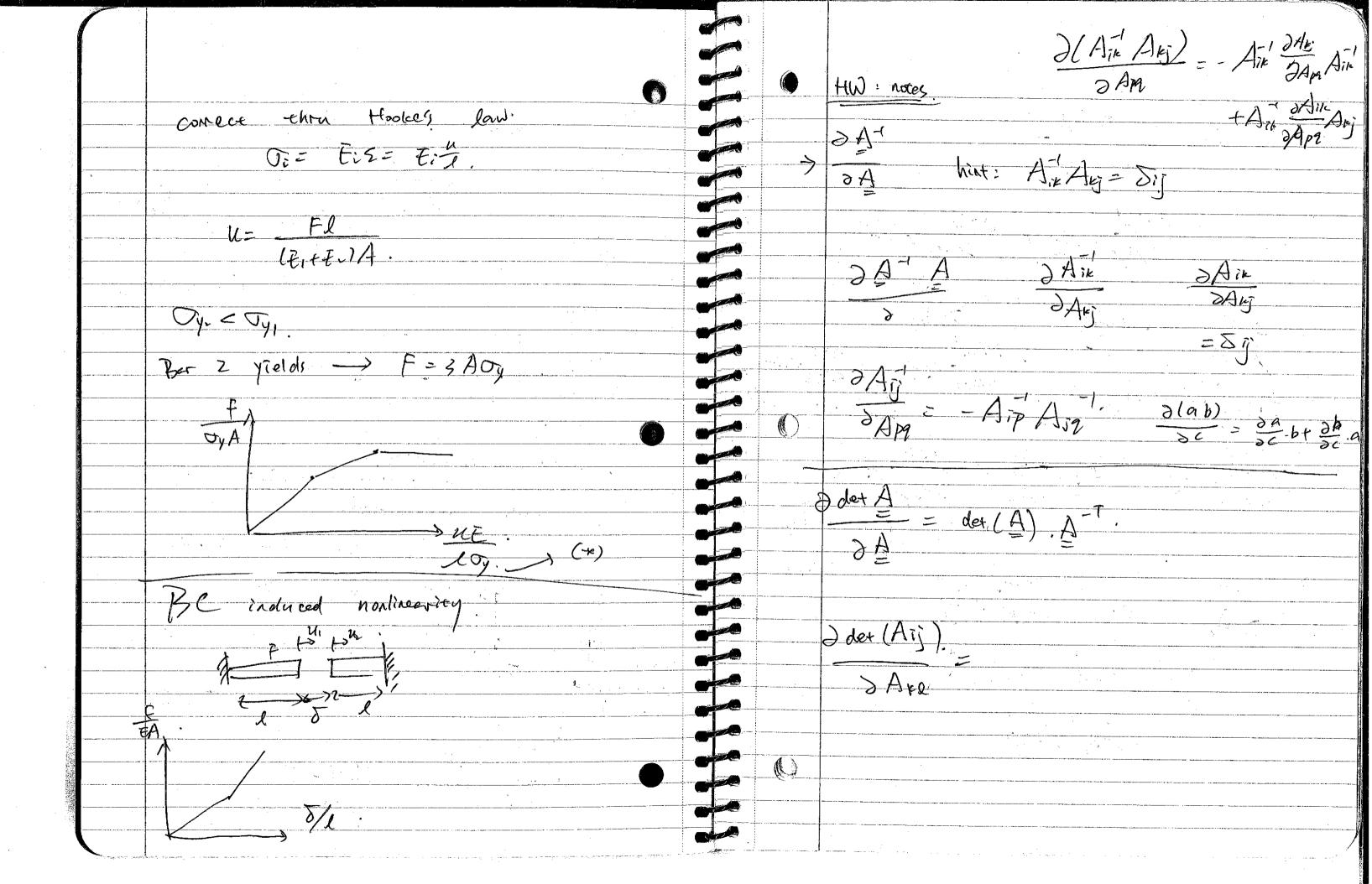
#FEM (Nontinear)

D What 3s FEA -Method to silve PDE. Why Nantinear FEA ? mportant? large deformation. ( linearite the strain). plastic deformain. ( naterial response. hypenelastre, etc.. for linear FEA . - relevant? Seroner form - weak form discretize. Shape function. t Abort-local support. prescribibe bu behavior within interphoners ) - Garss, Quadretine Station a assembly. () yostprocessing. (integration).

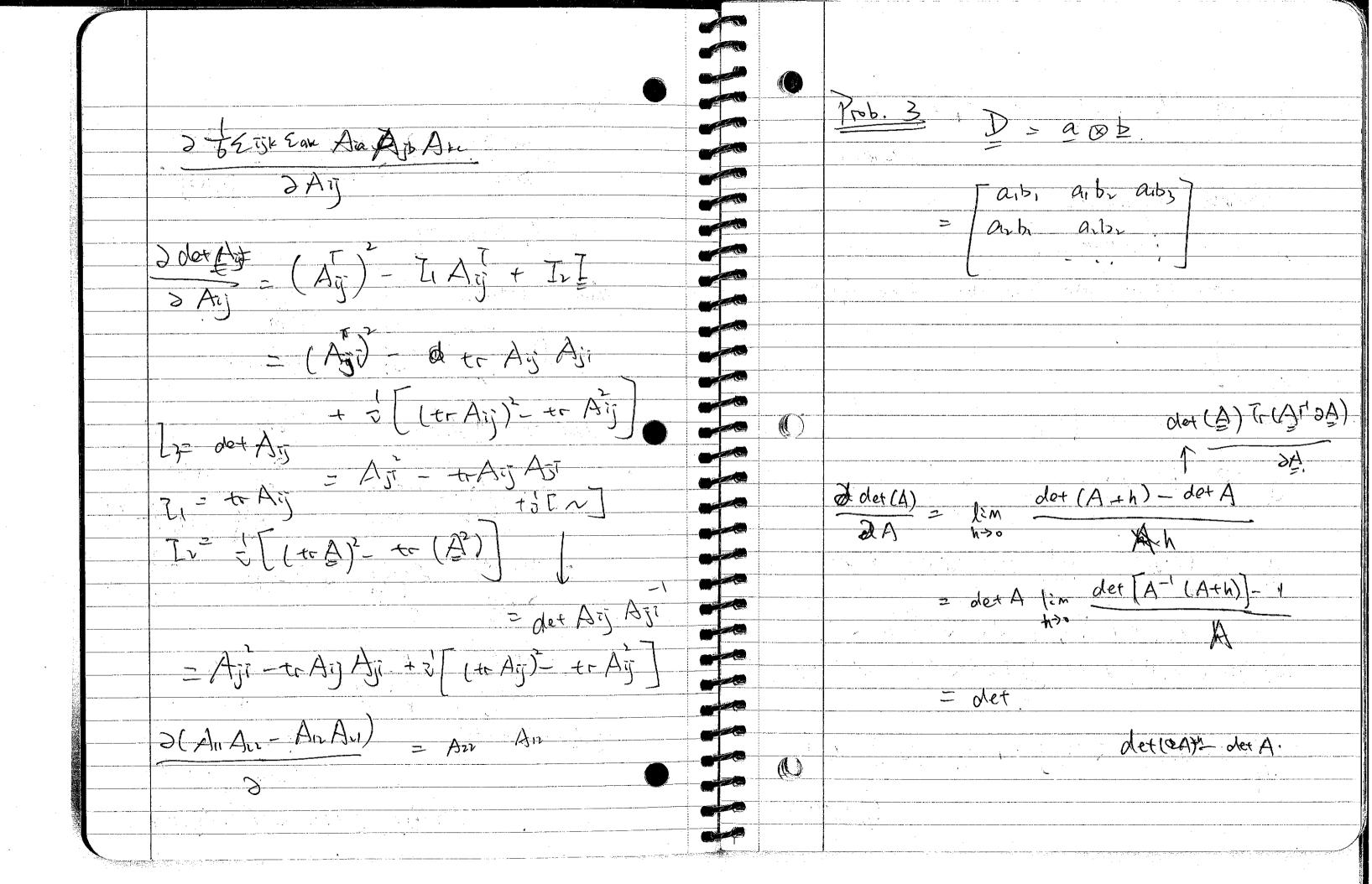




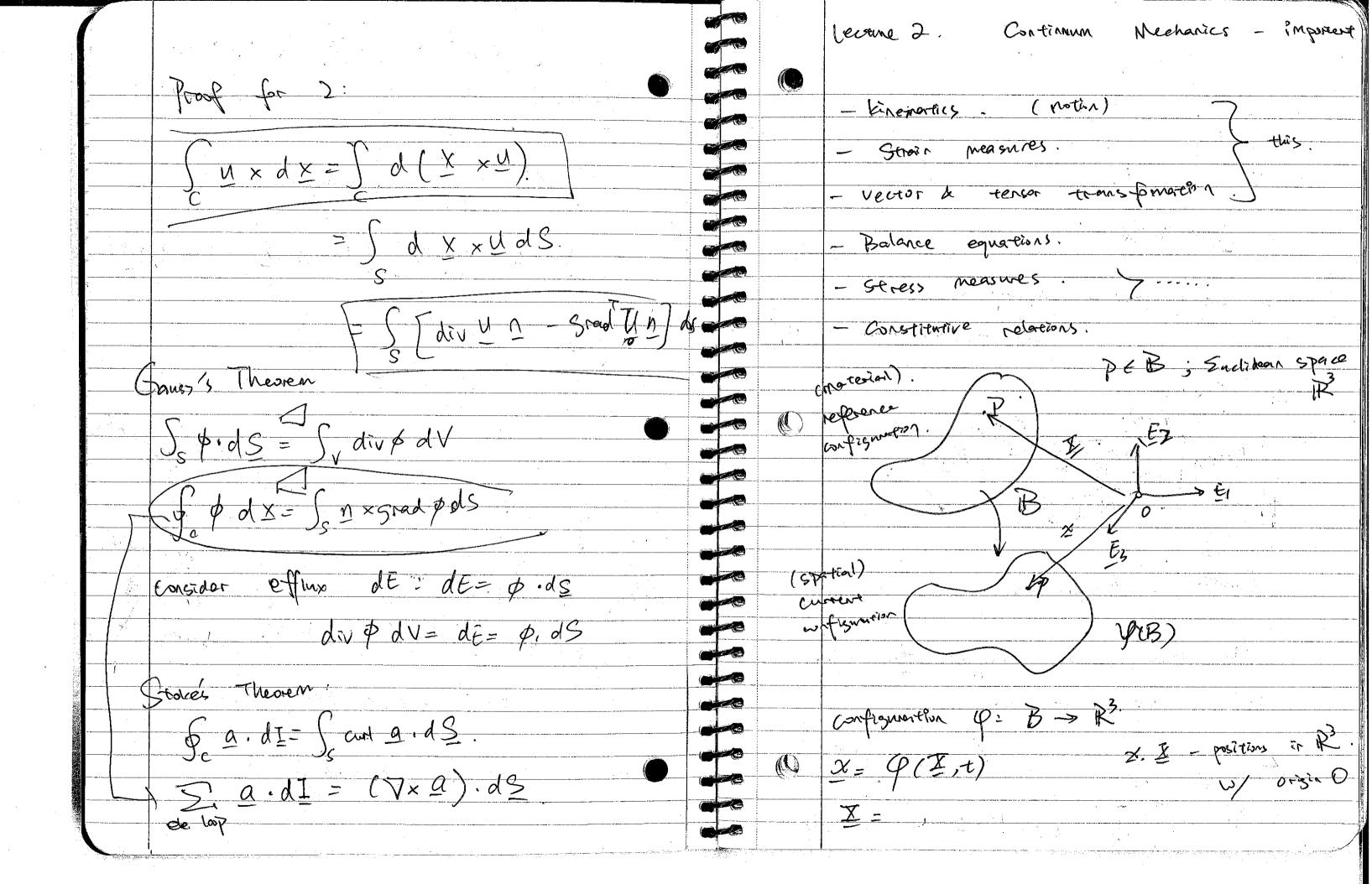


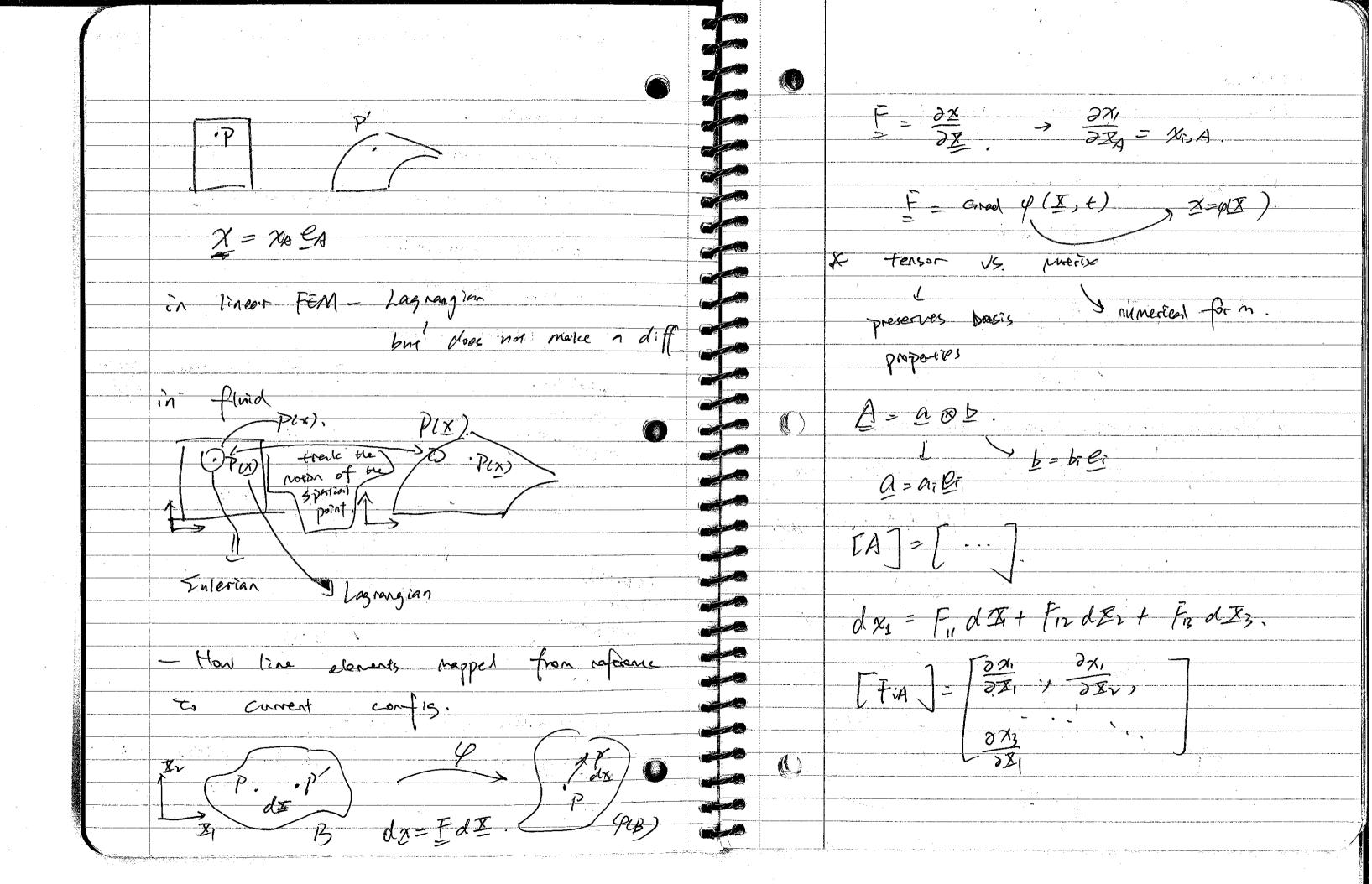


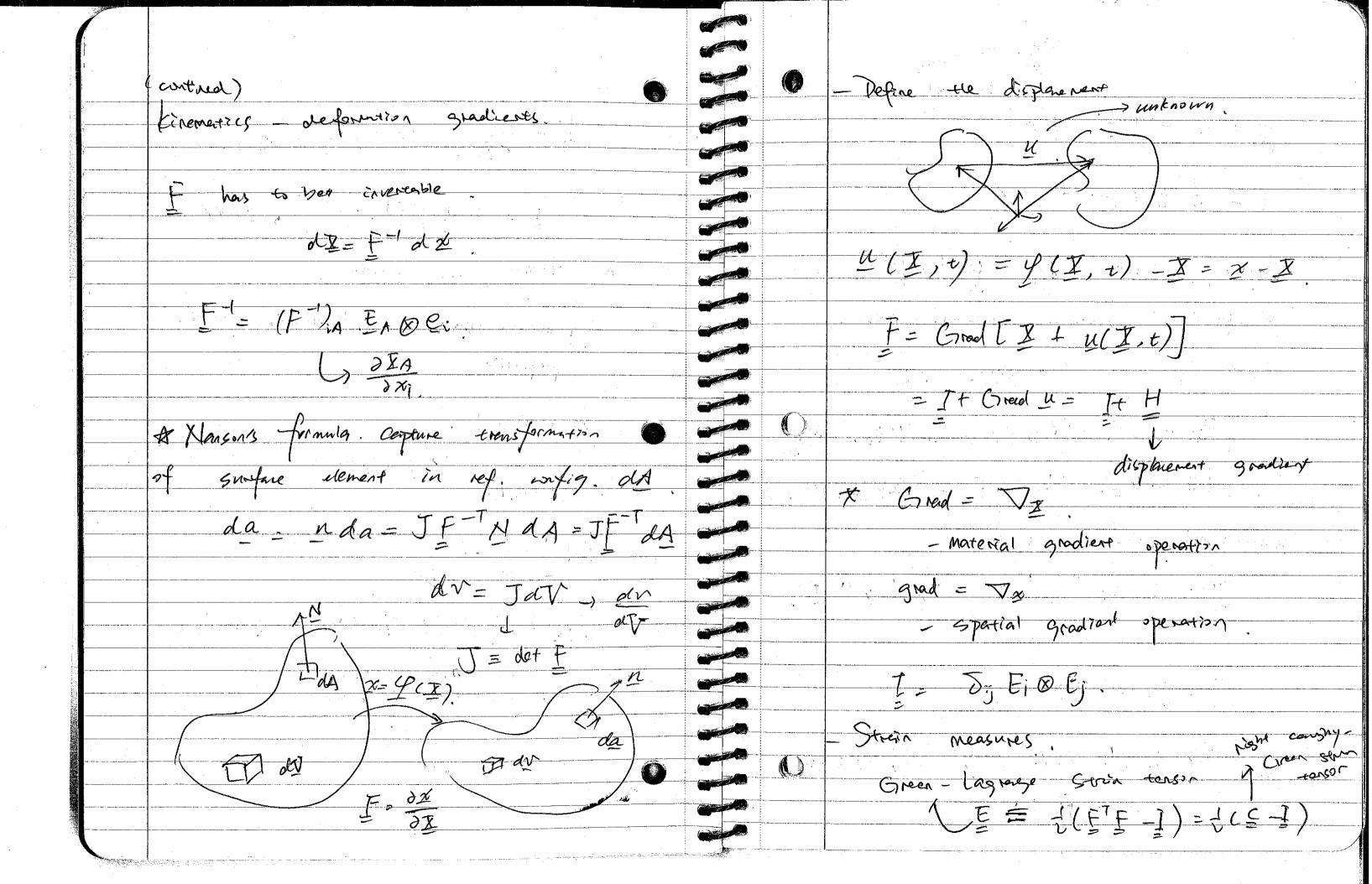
Rob - 2 Prob 1. 2 (Air Aki) a det (A) 2 der (A) 3/42)  $\frac{\partial \delta i}{\partial App}$   $\frac{\partial Ai}{\partial App}$   $\frac{\partial A}{\partial App}$   $\frac{\partial A}$ Notation. det A = det A = 11 Aii11 a det A - Si Gra Dir Jie - Li AT Aij = - Ail DAPR AK J AM and the second of the second o = - Ail Sepoka ki - (A) = def (A). ALAN - ALAN det (A)= { Eijk Ease Aia Aib Ac

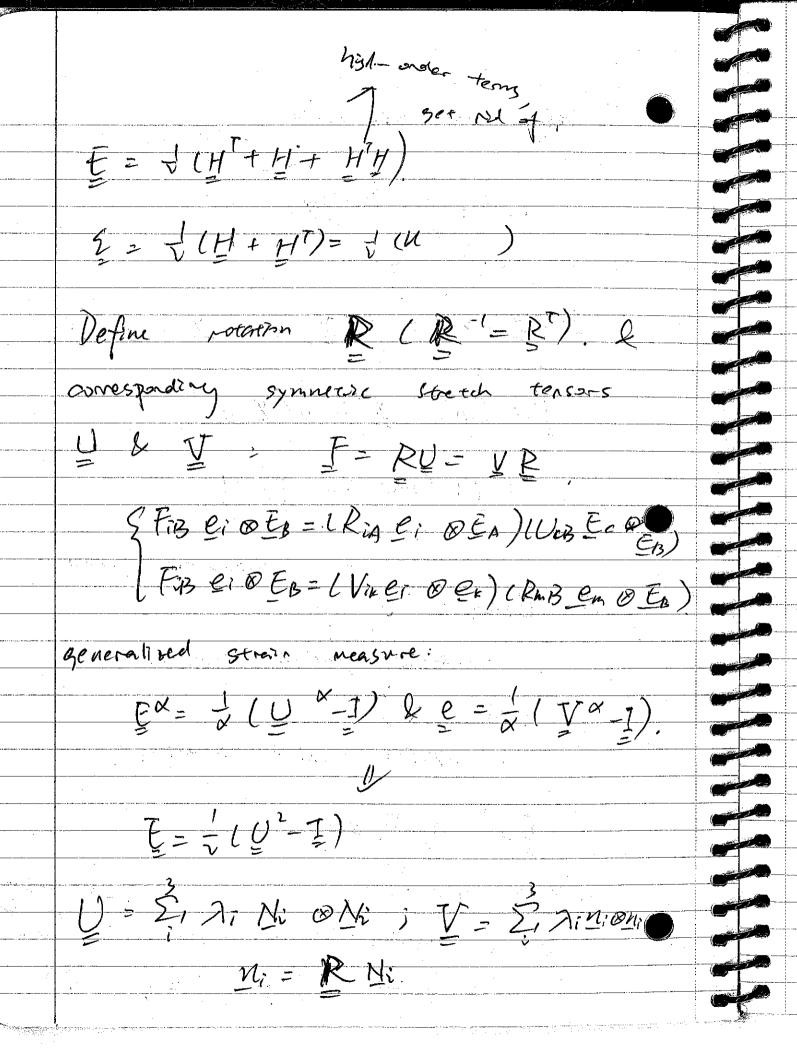


TUXFdI= S(V·F)nds Pob 4. A= a(I - e, oe,)+Bleioer + e20e1) P pdx = Comparte , eigen values. ux dx = ( [ (div u) n - (grad u) n]ds - eigeneurs we can morety form -(6 Q φ d x= on x grad & ids Rob B. - Vector form A.dr = Dx F ds = SS carl F J (x . 3rad 4) div (curl F) of V. (do X . grad p) , φd<u>×</u>= SSS div (curt F) dV = SSS (V.F) dx × gradpdS. M(((D(),F)-V)) dV= ((V,F)) n d5 1 nx good p ds. -55 F.ndS

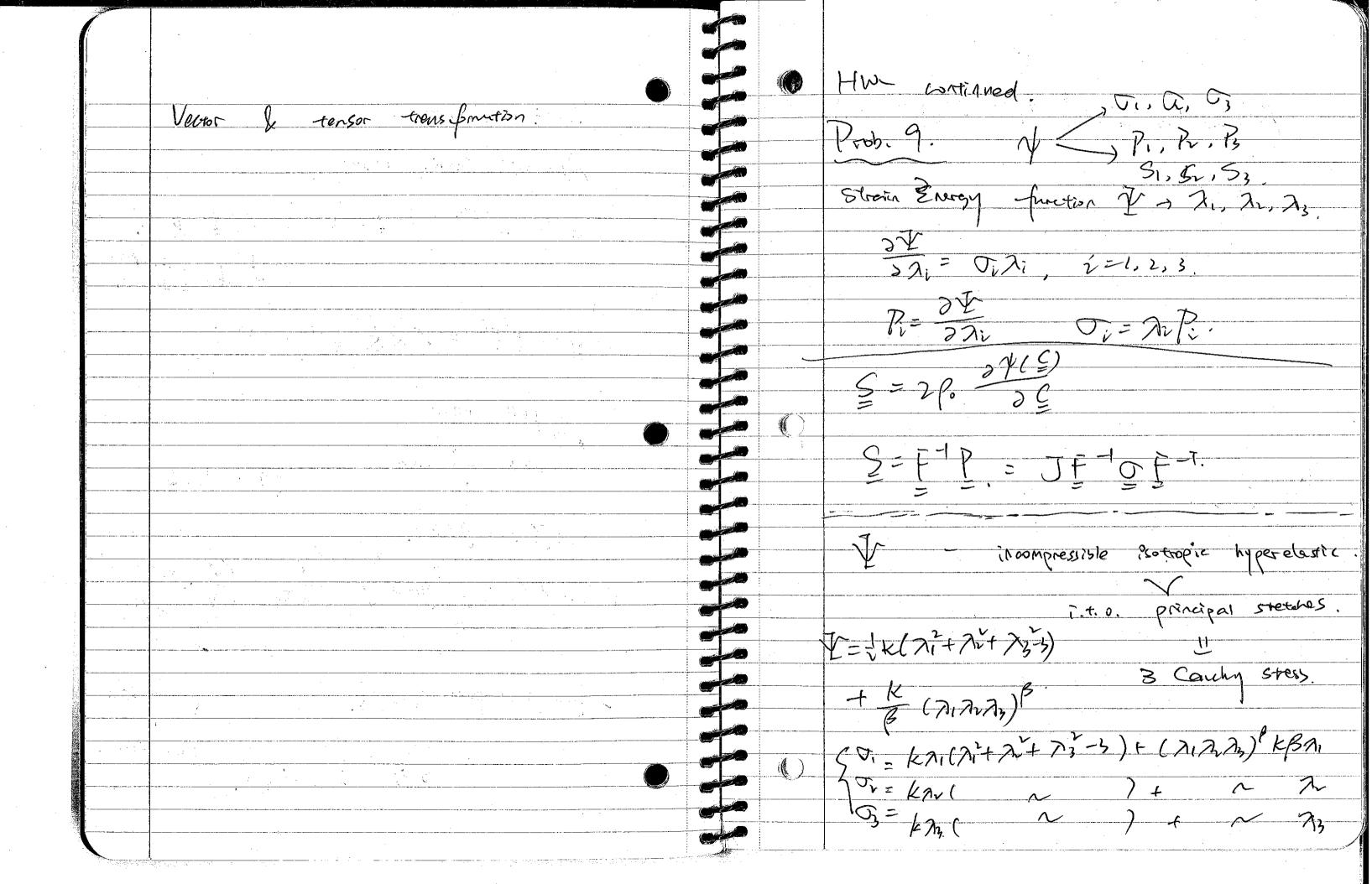


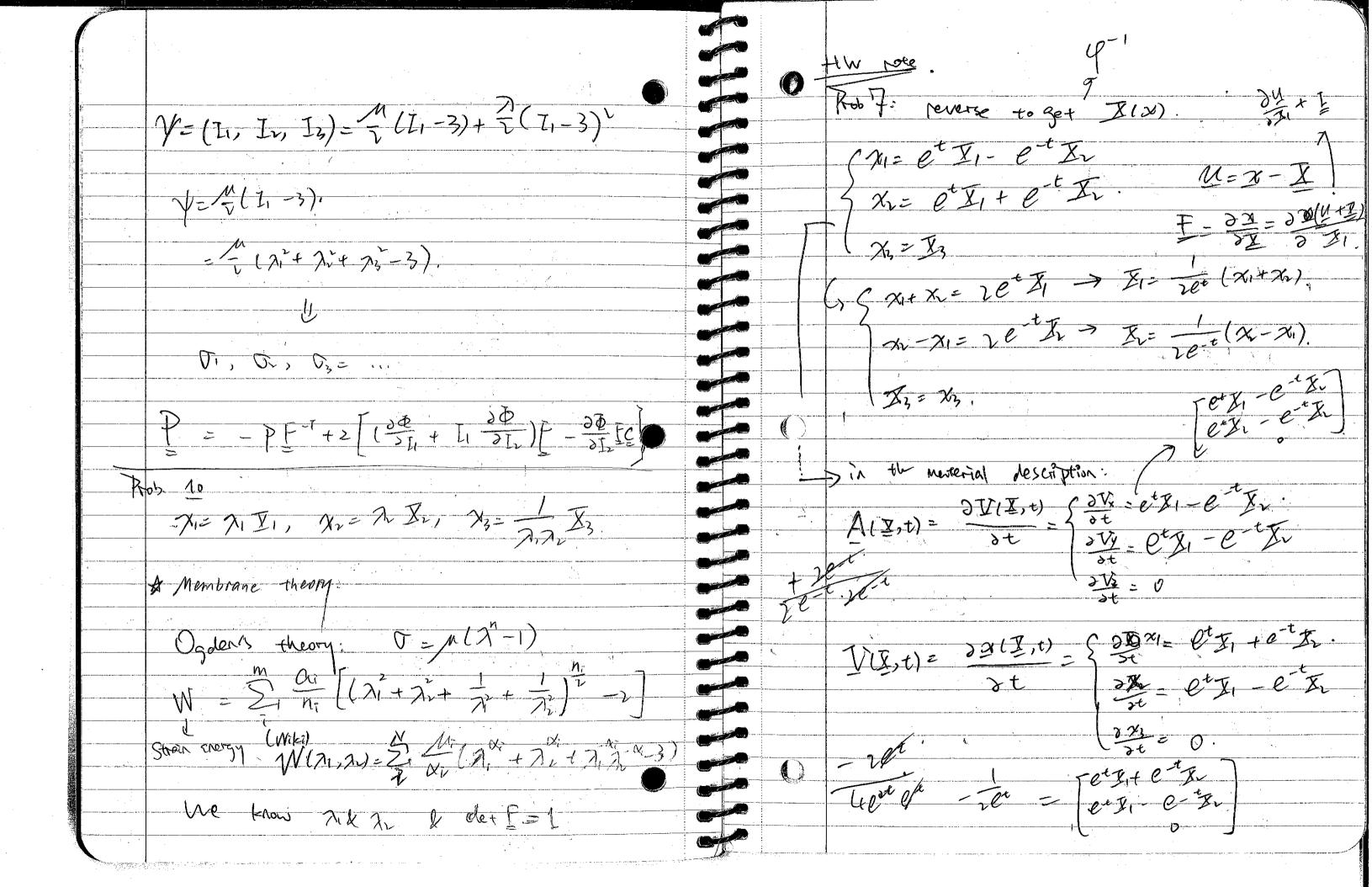


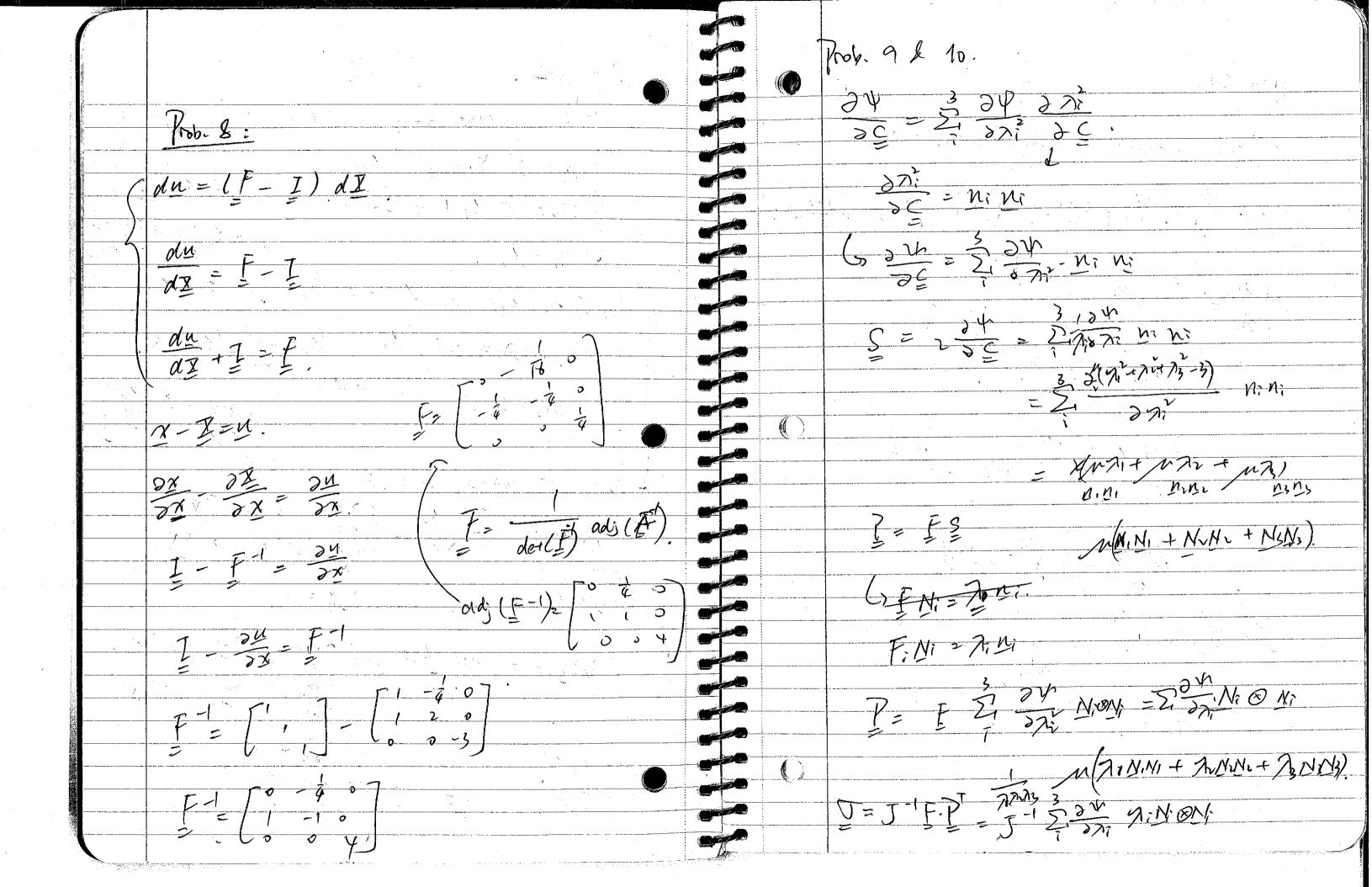


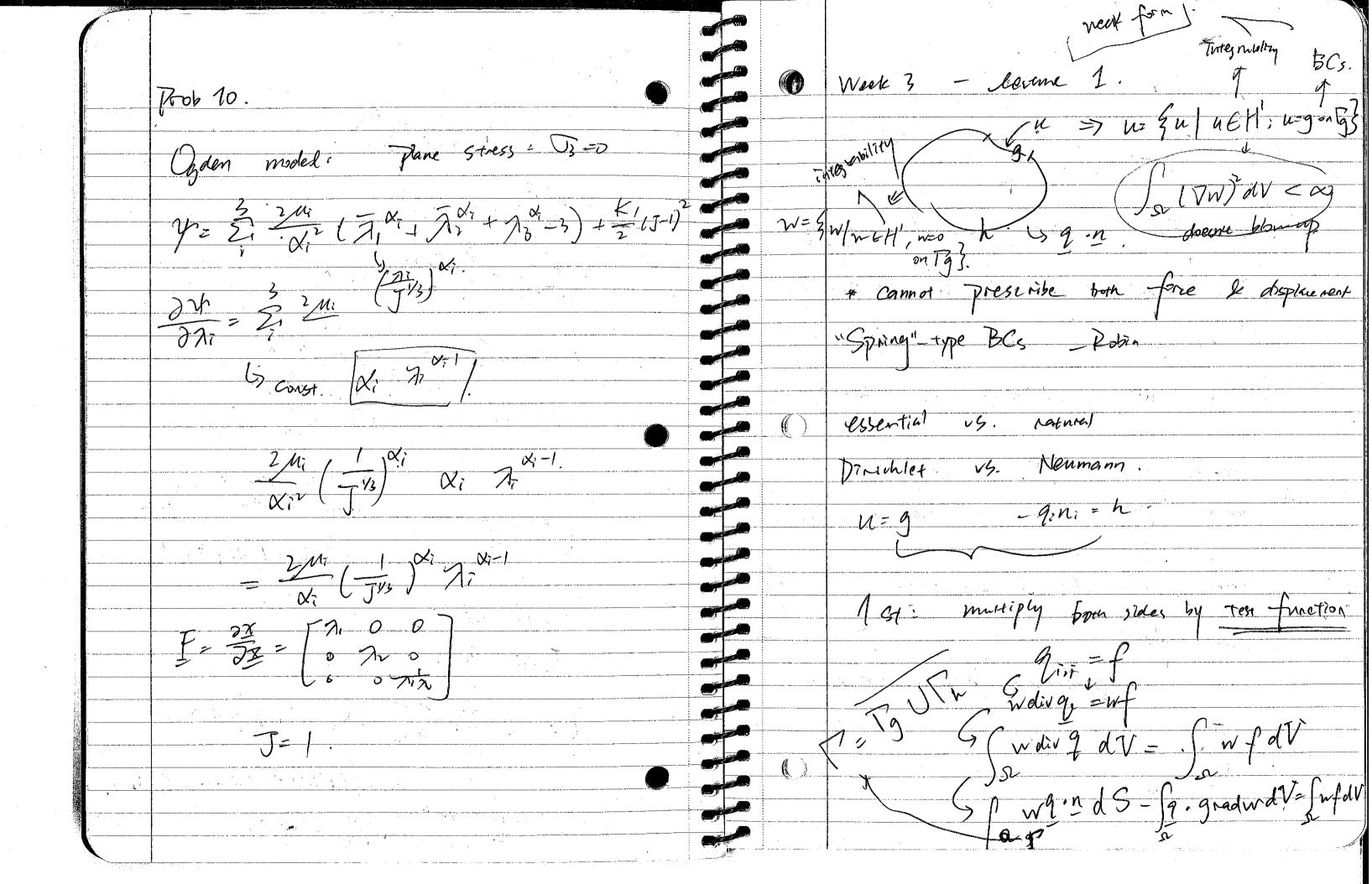


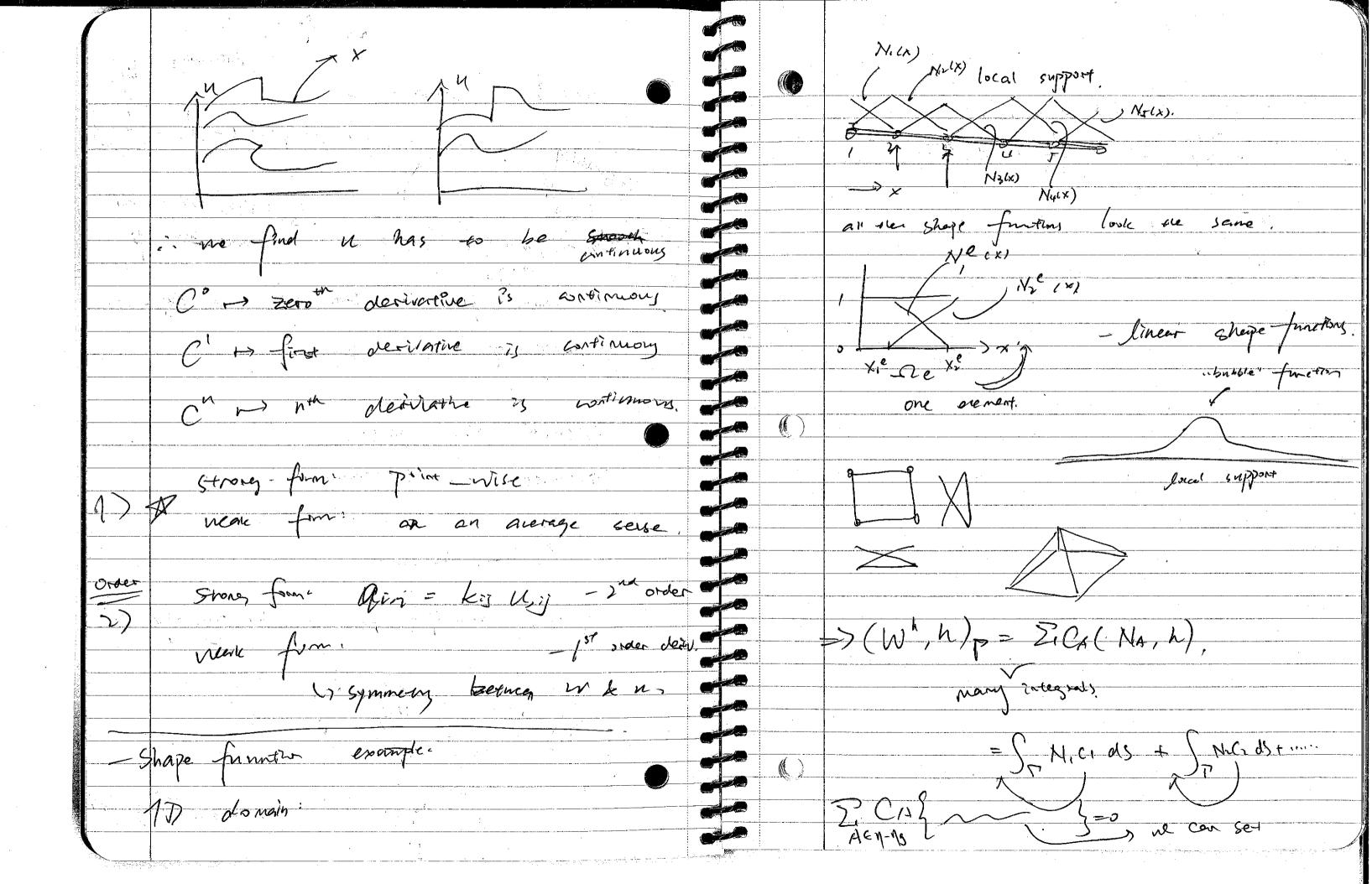
Strain masures. Almansi Grain tenson . e = e(-v) = d(I-V-v) = i(I-b-1).  $= \frac{1}{1} \left( \underline{I} - F \underline{F}^{-1} \right)$ b=FFT=VRRTVT=V C Pull back back G(Z)=g(x). Grad G = F grad g (-) 2G = 3g 2X; pull back. grand g = F-T Grand GT. puch forward







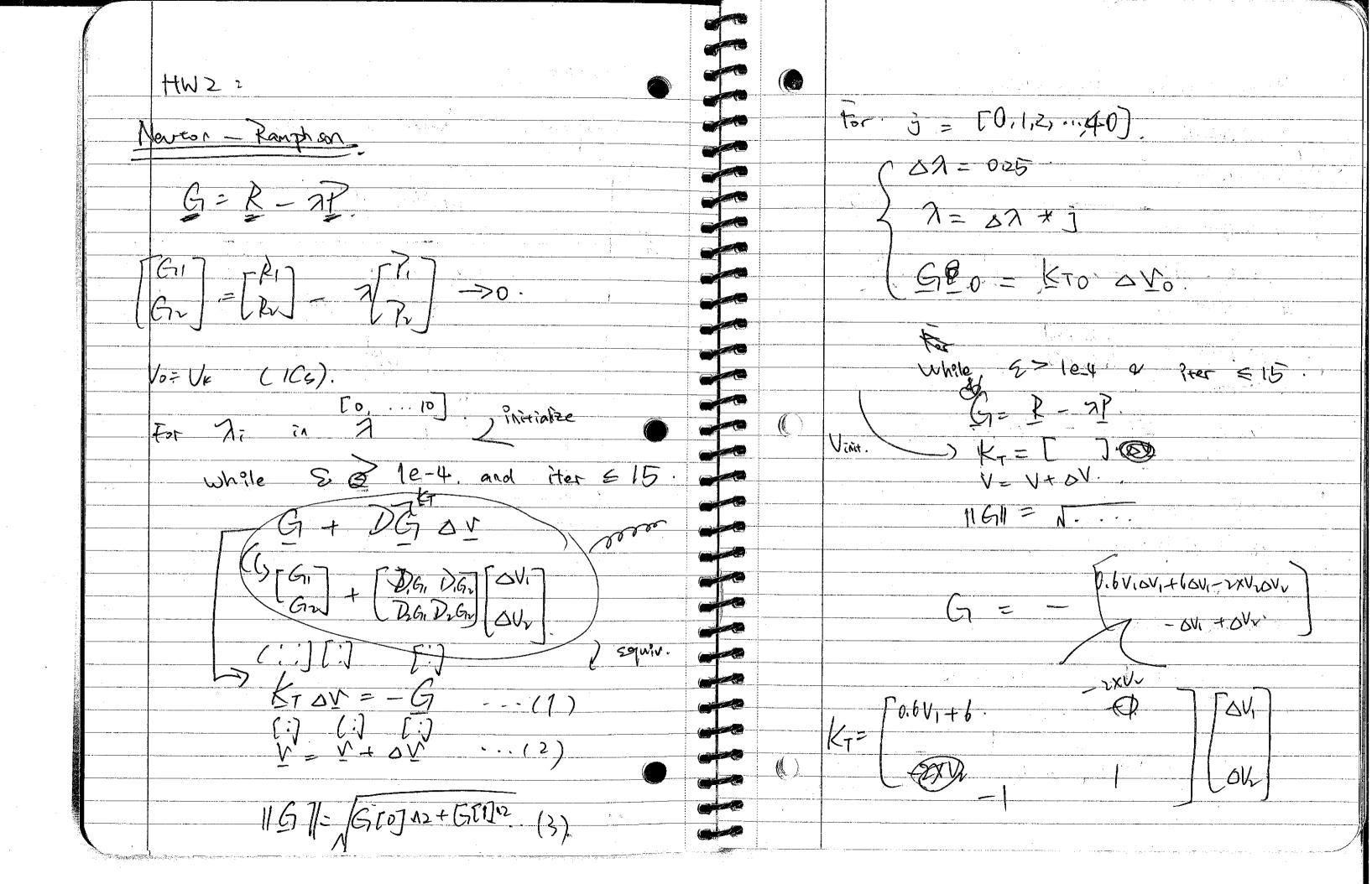


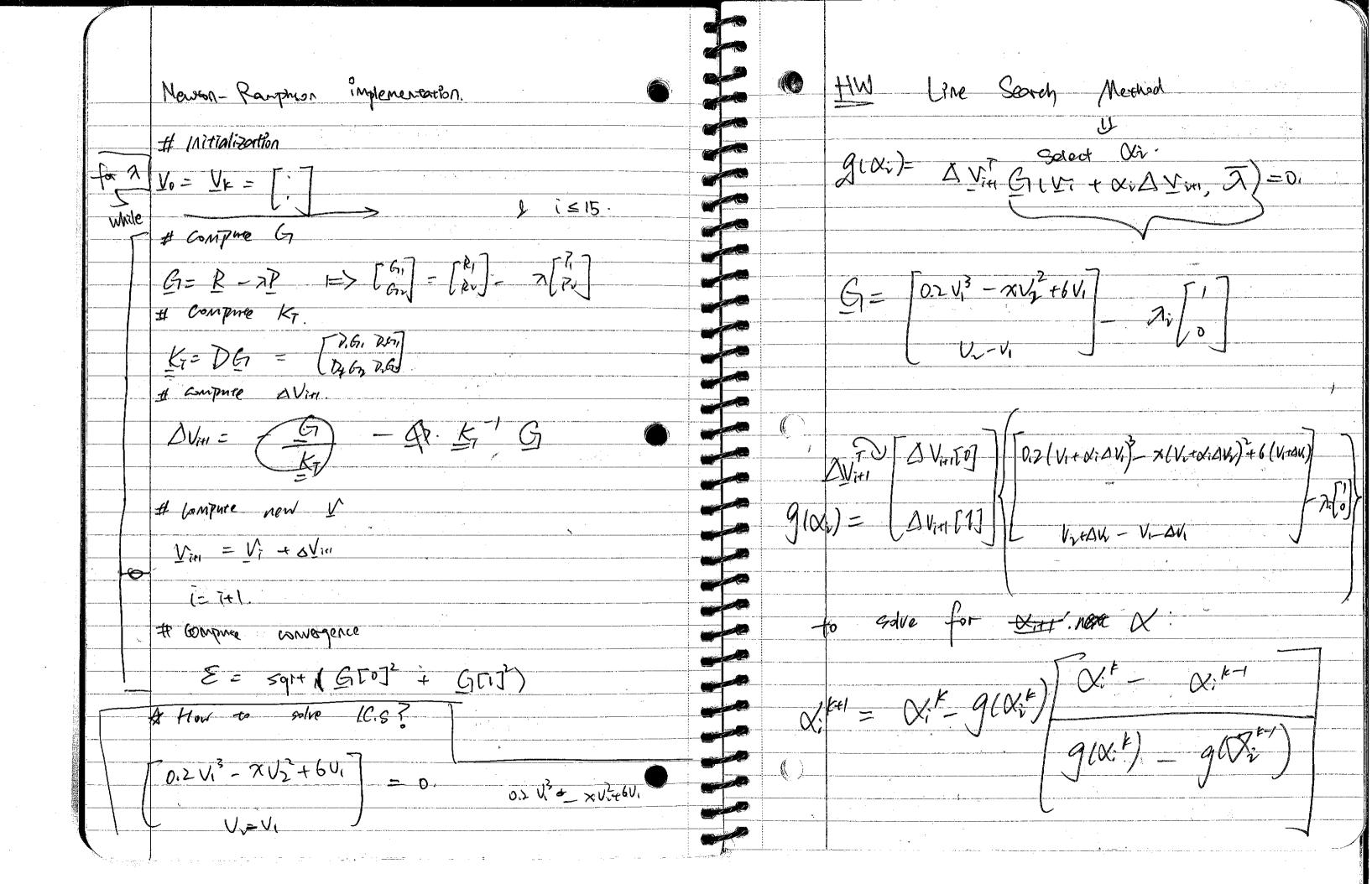


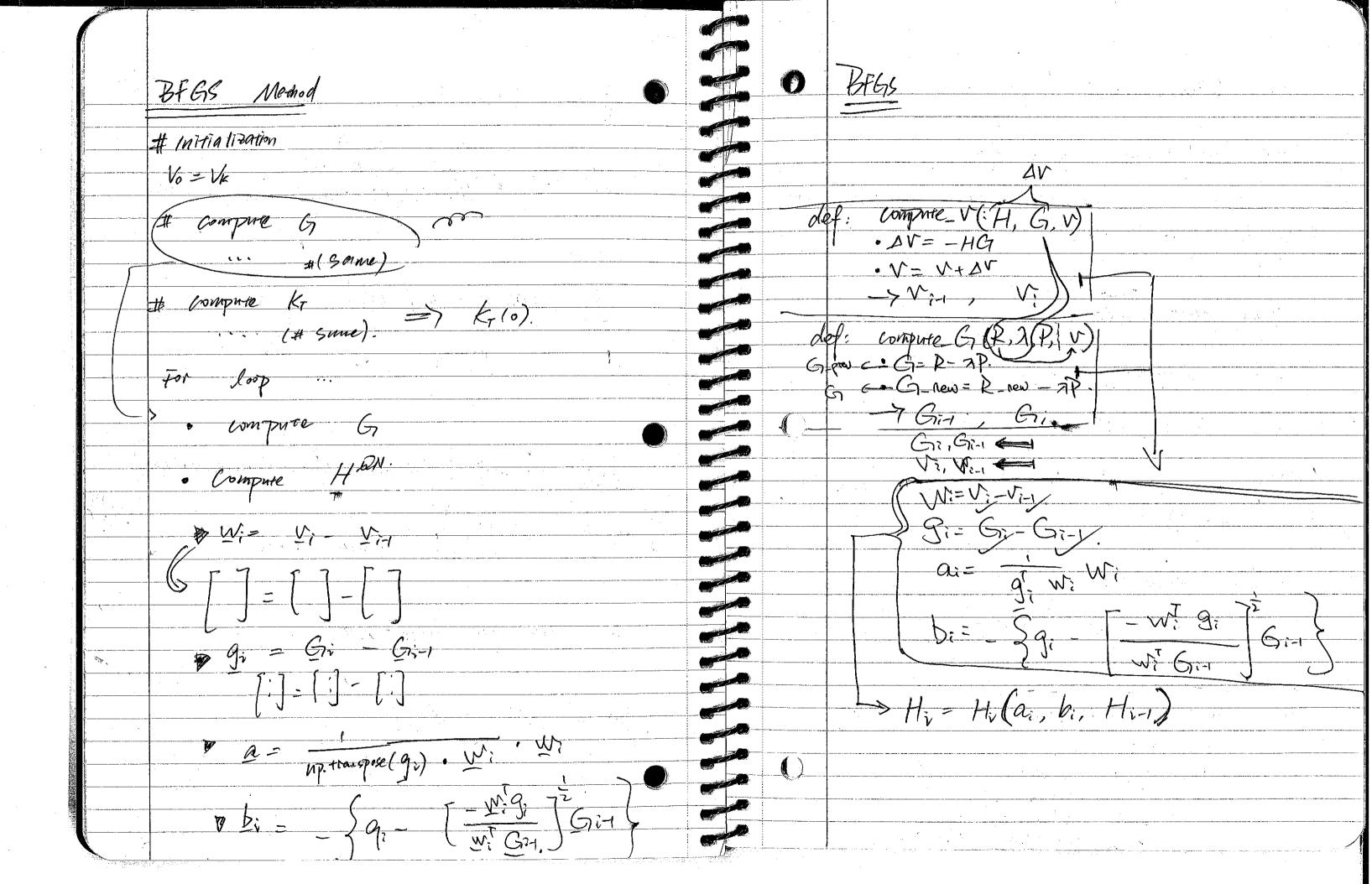
AFEM Week 3 - levene 2. C. U,N, + WN. quadrentic gradietilsample - integration quadrat ~ nerhod Janss

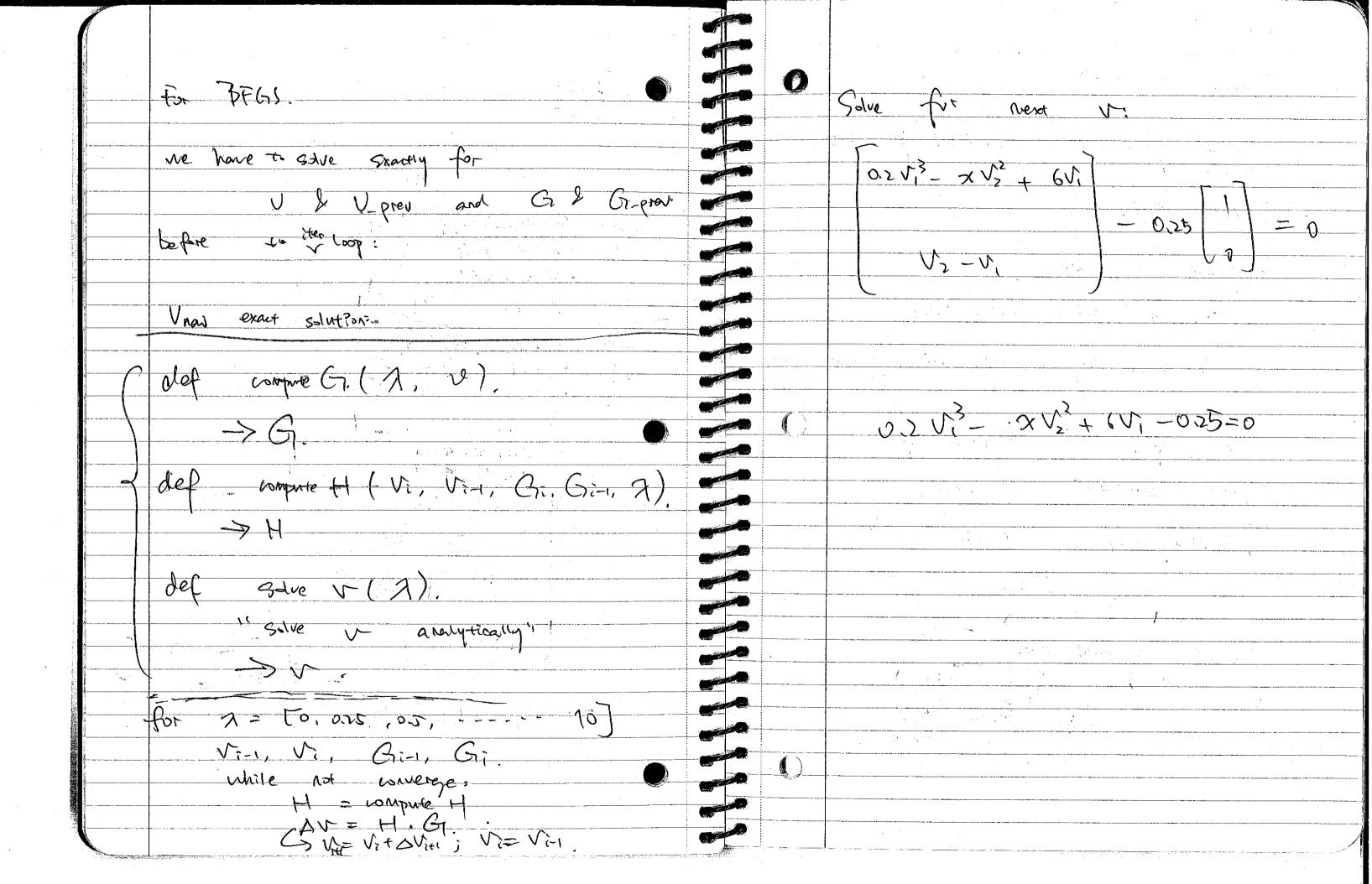
Some Shope furction Wook 4. vevene 1. - Bublior - Galerkin -> same Petrov-Galerkin -> different ( subg. how to some PDE > tune the shape function 6 mend is Riley Rith method Track shape force . Shape function Ne= [N, M] has to be global Co i dériussère hare a jump. definitives in weak form order order continuibles in required

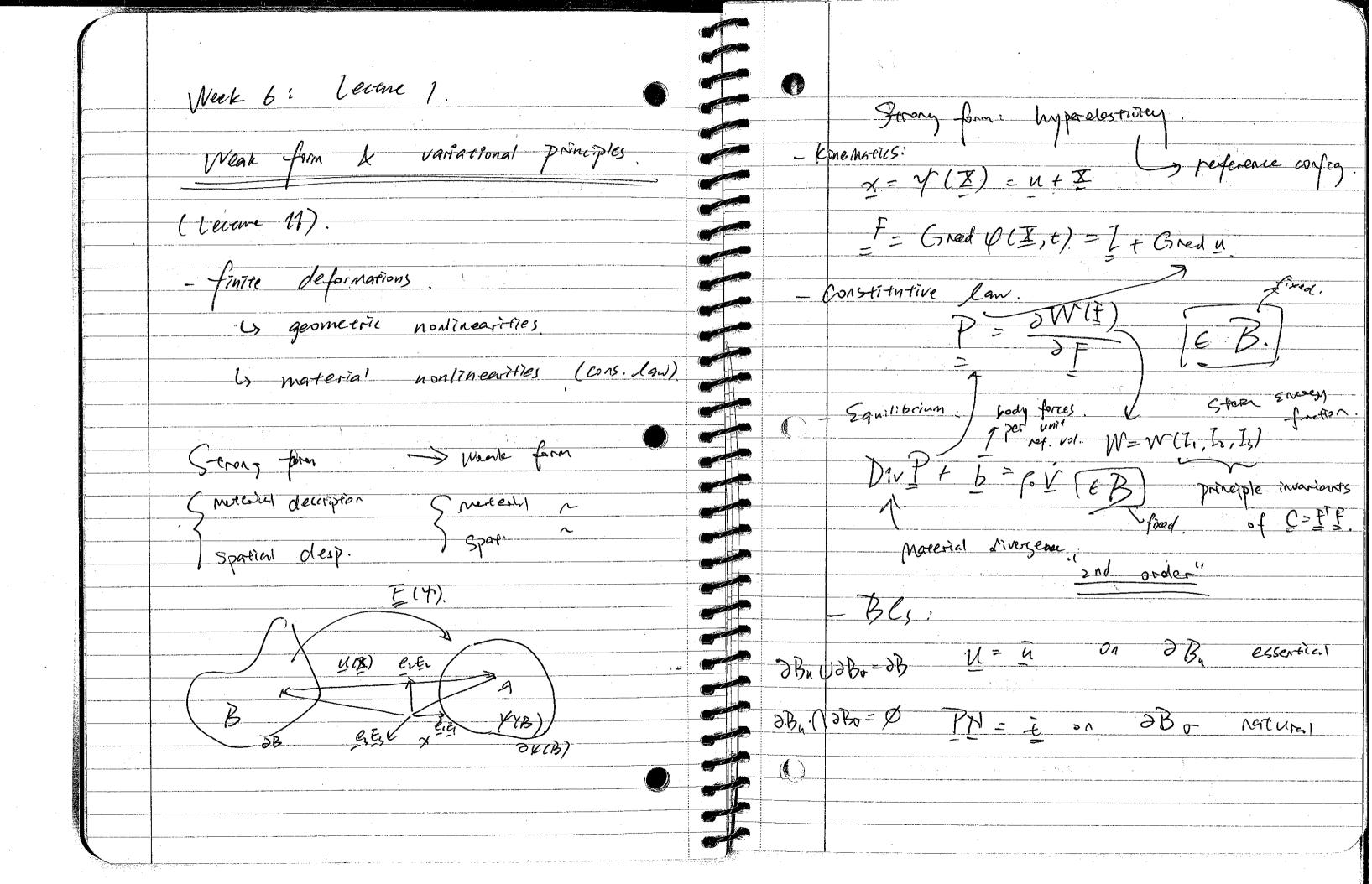
Ceene 2 Week 5, lune 1 Comparion nemed between 7 KT(V.) Get therance " Quadratic Comergenee" 7/ Vkth Way R(Vkth)-R(Vk)

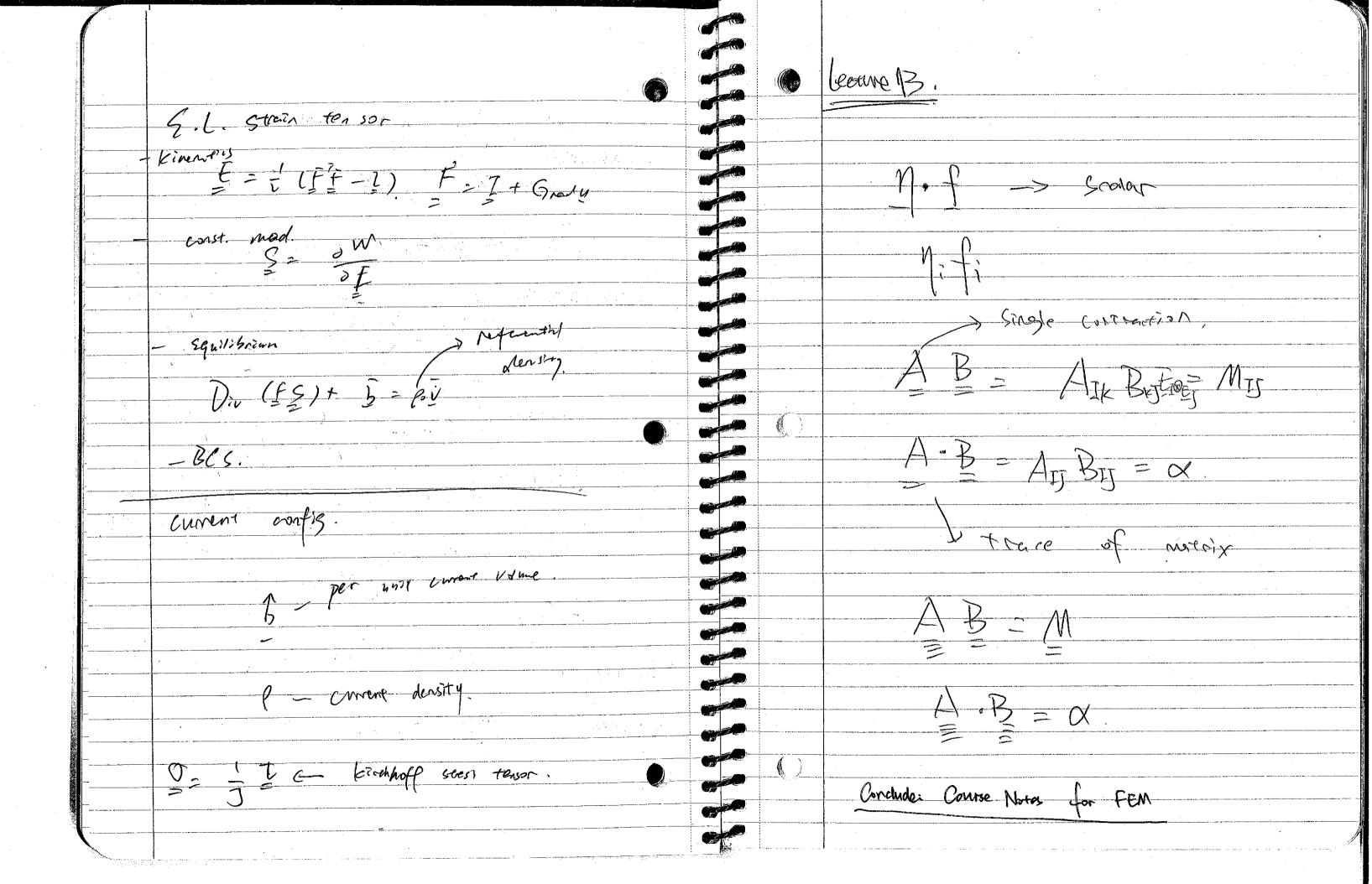




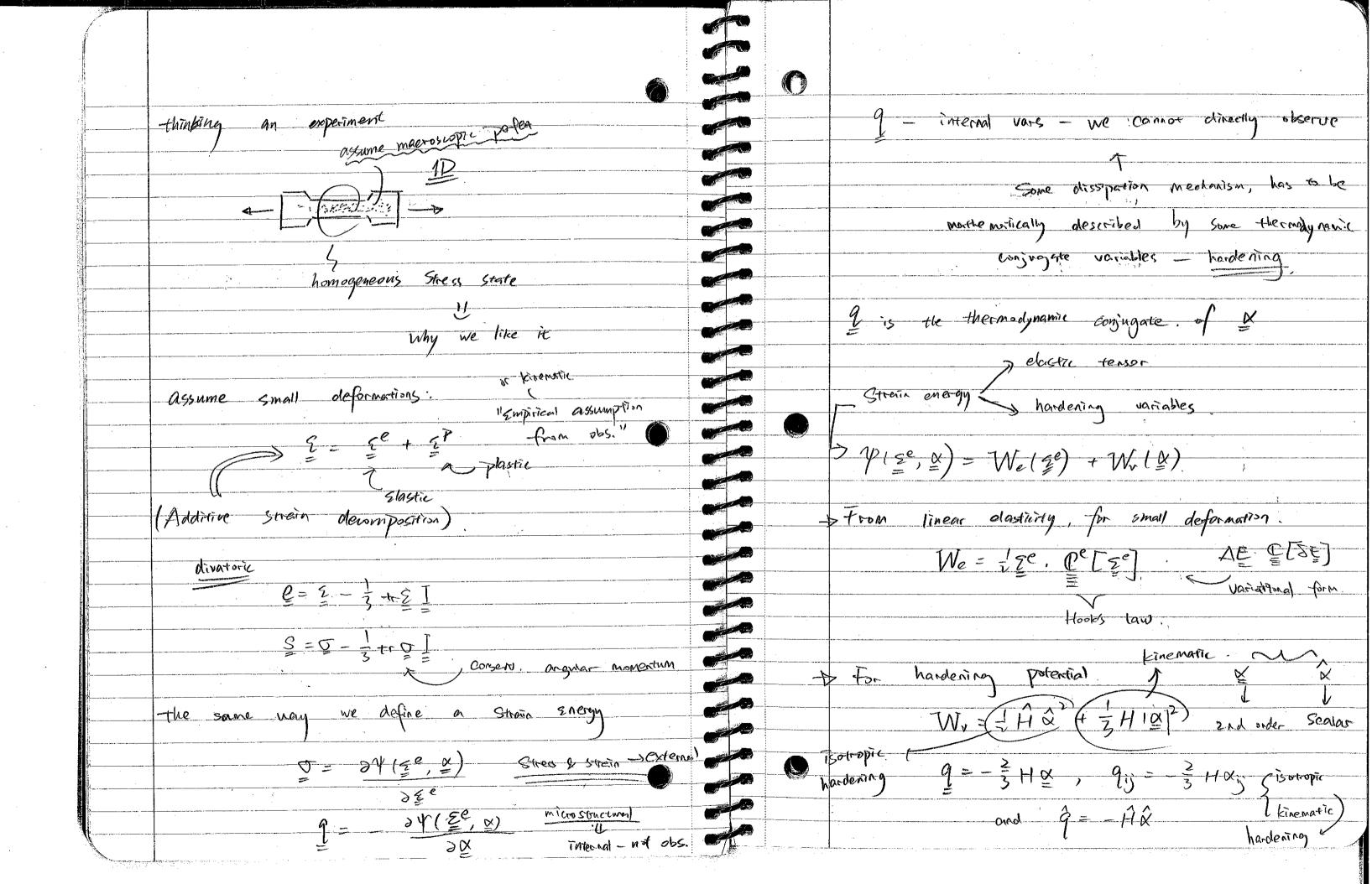


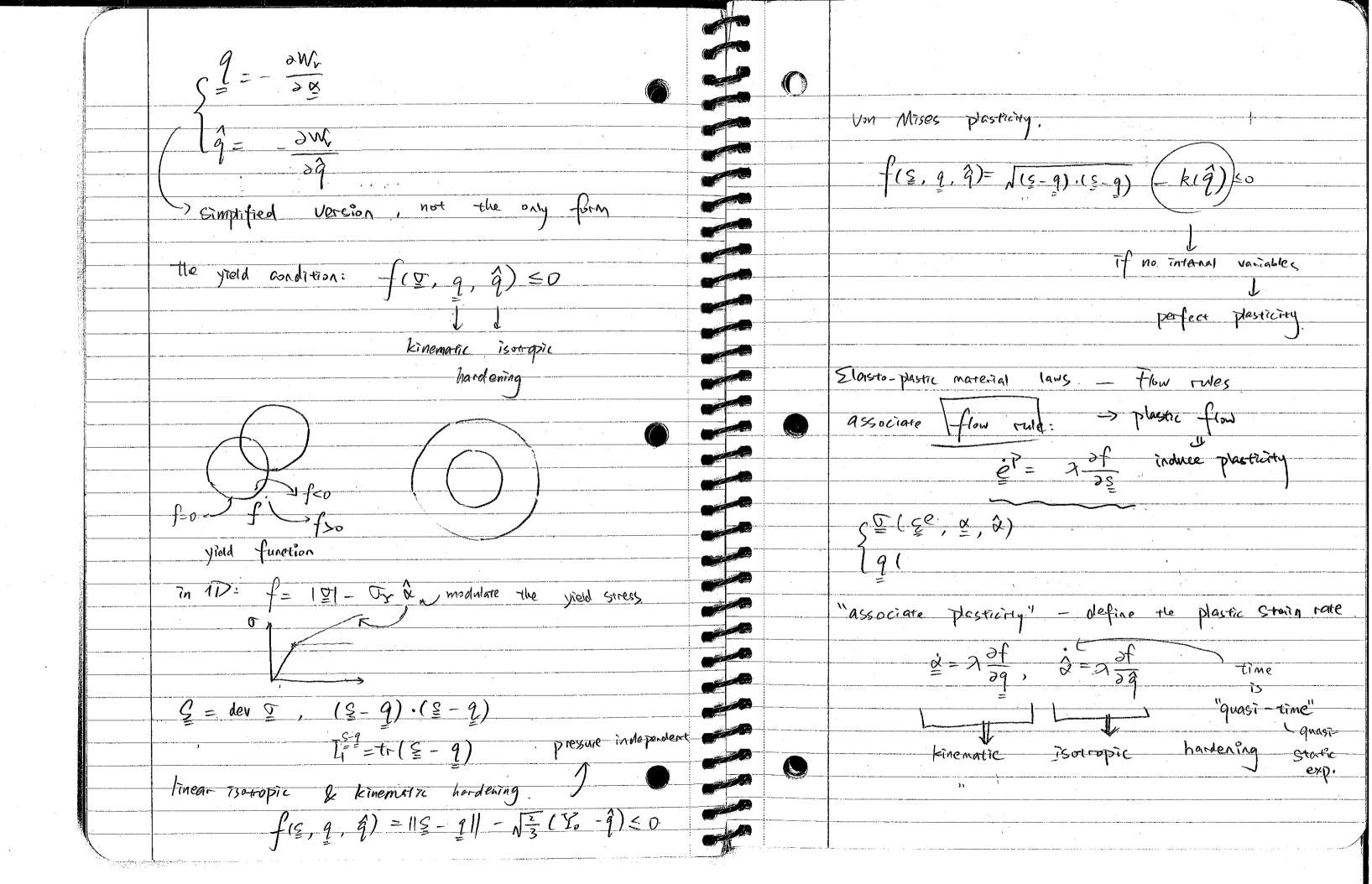


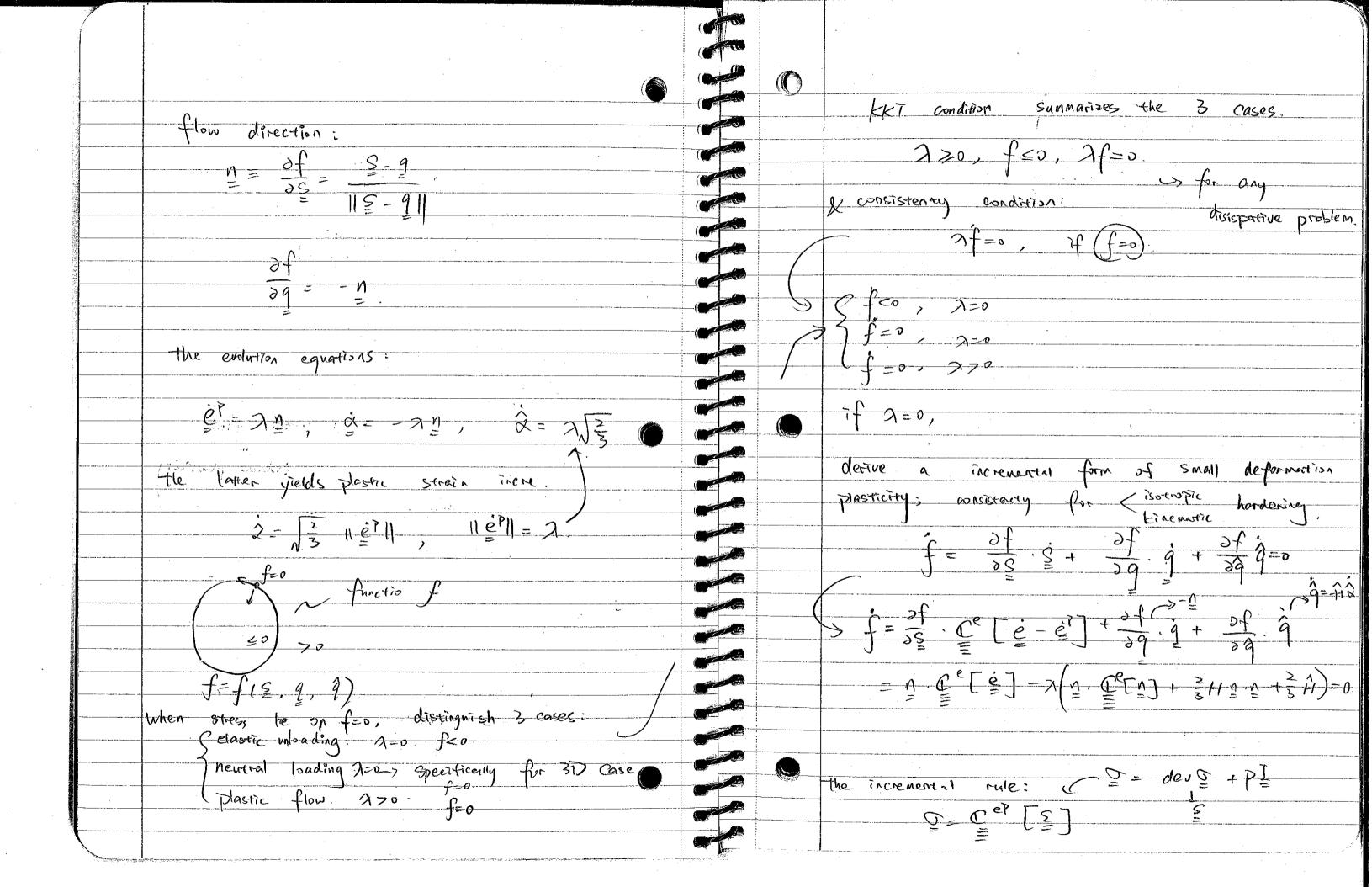




# Additional Notes on Plasticity Plasnoty US. Nyperelasticity hyperelastic yields & Pailure VY 1/00d Give metice kinematic hardening hardening hypadasiticity has one-on-one the stress between Strains Hyperelastic: >> S=V=0 = Y(E) U= U+AU G19,7)+ AG AU 20 Conculate Stresses in this Dasticity - Postost Verston Treese-sibility. deformation. dissipate energy to induce plasic







We can Solve	for plastic	mutipliec:	
	)= A y.	Ce [è]	
linear elasticity	g 'Standard'		
Q= 0 when	to use sp	eific K;	
3 Ru		3	
	V vs. V	?	