

Find Push Down Automata that accepts the Context-free Grammar:

$$P: \begin{cases} S \rightarrow XY, \\ X \rightarrow aX \mid bX \mid a, \\ Y \rightarrow Ya \mid Yb \mid a \end{cases}$$

$$G = (\{S, X, Y\}, \{a, b\}, P, S)$$

$$\hookrightarrow M = (\{S, \epsilon\}, \{a, b\}, \{S, X, Y, a, b\}, \{S, \epsilon, S, \phi\})$$

$$\begin{aligned} S \Rightarrow XY &\Rightarrow aXY \Rightarrow \underset{\uparrow}{a} \underset{\uparrow}{a} \underset{\uparrow}{Y} \Rightarrow \underset{\uparrow}{a} \underset{\uparrow}{a} \underset{\uparrow}{b} \\ &\Rightarrow \underset{\uparrow}{a} \underset{\uparrow}{a} \underset{\uparrow}{b} \end{aligned}$$

rule 1:  $\delta(\underline{\epsilon}, \underline{A}, \underline{A}) = \{\underline{(\epsilon, A)} \mid A \rightarrow a\}$  (for each variable)

rule 2:  $\delta(\underline{\epsilon}, \underline{a}, \underline{a}) = \{\underline{(\epsilon, a)}\}$  (for each terminal)

$\checkmark$  rule 3:  $\delta(\underline{\epsilon}, \underline{\epsilon}, \underline{S}) = \{\underline{(\epsilon, XY)} \mid S \rightarrow XY\}$

$$R_1: \delta(\underline{\epsilon}, \underline{\epsilon}, \underline{S}) = \{\underline{(\epsilon, XY)} \mid S \rightarrow XY\}$$

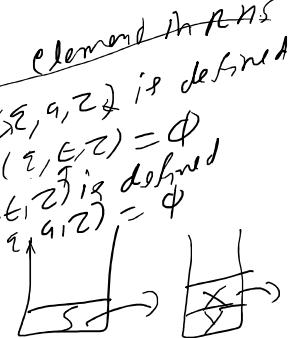
$$R_2: \delta(\underline{\epsilon}, \underline{a}, \underline{X}) = \{\underline{(\epsilon, ax)}, \underline{(\epsilon, bx)}, \underline{(\epsilon, a)} \mid a, b \in \{a, b\}\}$$

$$R_3: \delta(\underline{\epsilon}, \underline{\epsilon}, \underline{Y}) = \{\underline{(\epsilon, Ya)}, \underline{(\epsilon, Yb)}, \underline{(\epsilon, a)} \mid a, b \in \{a, b\}\}$$

$$R_4: \delta(\underline{\epsilon}, \underline{a}, \underline{a}) = \{\underline{(\epsilon, a)}\}$$

$$R_5: \delta(\underline{\epsilon}, \underline{b}, \underline{b}) = \{\underline{(\epsilon, b)}\}$$

Consider  $w = aabb$  for validation



$$(\underline{\epsilon}, \underline{aabb}, \underline{S}) \vdash (\underline{\epsilon}, \underline{aabb}, \underline{XY}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{XY}) \in \delta(\underline{\epsilon}, \underline{S}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{aab}, \underline{aXY}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{aX}) \in \delta(\underline{\epsilon}, \underline{E}, \underline{X}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{aab}, \underline{XY}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{E}) \in \delta(\underline{\epsilon}, \underline{a}, \underline{a}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{ab}, \underline{aY}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{a}) \in \delta(\underline{\epsilon}, \underline{E}, \underline{X}) \text{ ]}$$

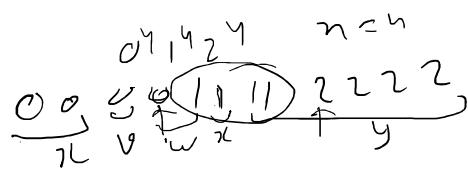
$$\vdash (\underline{\epsilon}, \underline{ab}, \underline{Y}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{E}) \in \delta(\underline{\epsilon}, \underline{a}, \underline{a}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{ab}, \underline{Yb}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{Yb}) \in \delta(\underline{\epsilon}, \underline{E}, \underline{Y}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{ab}, \underline{b}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{a}) \in \delta(\underline{\epsilon}, \underline{E}, \underline{Y}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{b}, \underline{b}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{E}) \in \delta(\underline{\epsilon}, \underline{a}, \underline{a}) \text{ ]}$$

$$\vdash (\underline{\epsilon}, \underline{b}, \underline{b}) \quad \text{[ } \vdash (\underline{\epsilon}, \underline{E}) \in \delta(\underline{\epsilon}, \underline{b}, \underline{b}) \text{ ]}$$



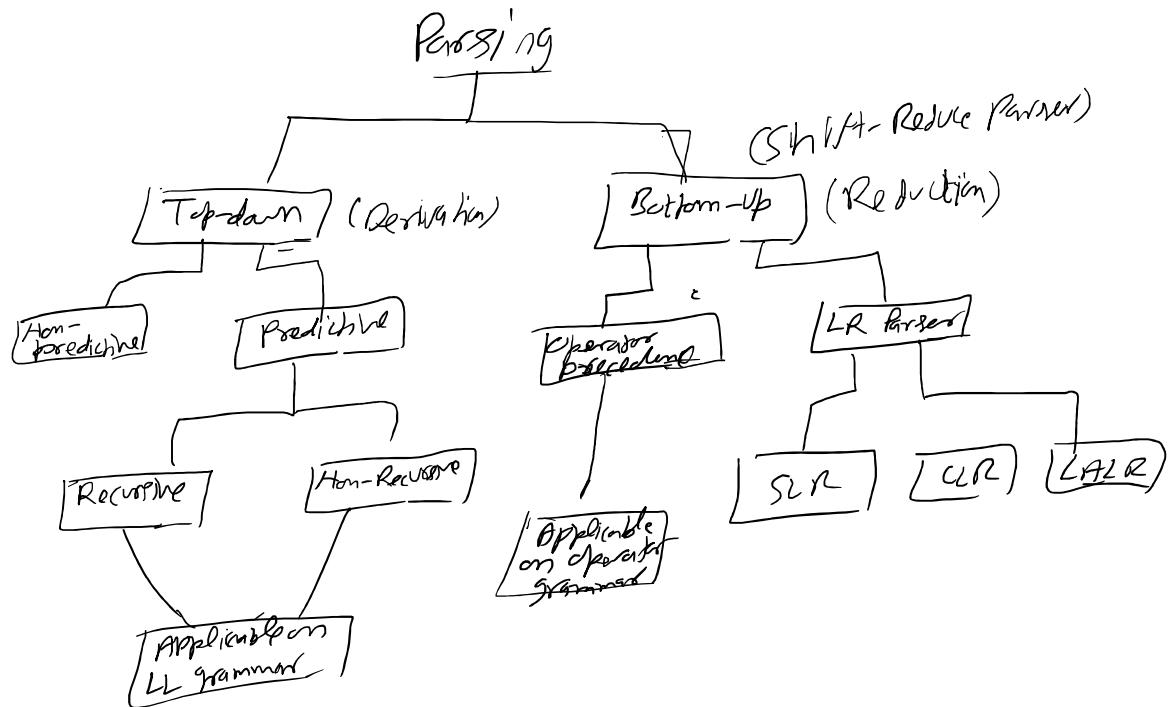
$$n = 4$$

$$n = 4$$

U U V T W X Y

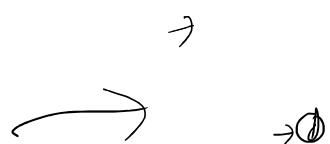
$$|VWXY|=n$$

## Module $\rightarrow$ : Parsing



### Non-predictive Topdown Parsing :

$$\begin{aligned} S &\rightarrow cAd \\ A &\rightarrow ab \mid a \end{aligned}$$



$$w = \underline{\underline{cad}}$$

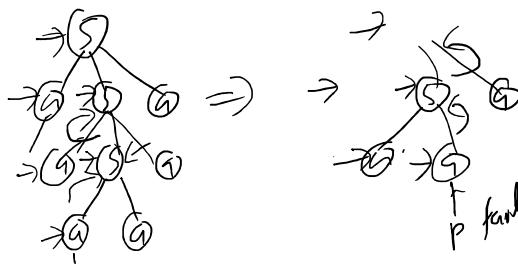
cad

P.T.  $S \rightarrow aSa \mid a$  generates strings  $cba$ ,  $aaba$  but not generate  $aabaaa$  using non-predictive top down parsing.

$$S \Rightarrow a \underline{S} a \Rightarrow a \underline{a} \underline{S} a \Rightarrow \cancel{a} \cancel{a} \cancel{S} a \Rightarrow \cancel{a} \cancel{a} \cancel{a} \cancel{a} \cancel{a}$$

$s \Rightarrow a \underline{sa} \Rightarrow a \underline{a} a \underline{a} \Rightarrow \cancel{aa}$

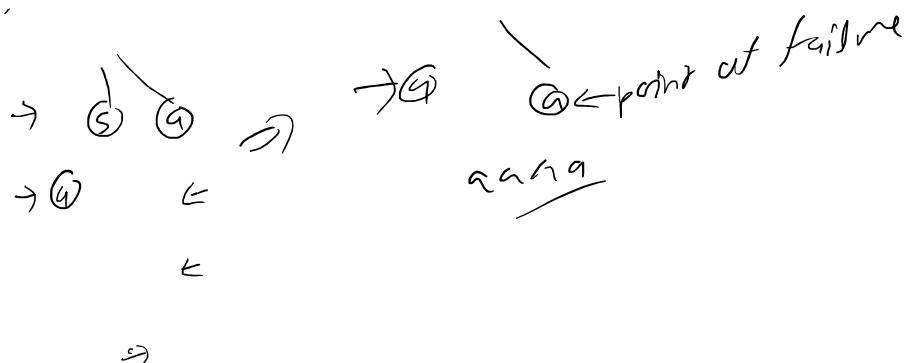
(I)  $a \underline{a} \underline{a}$



$\rightarrow 6 \rightarrow$

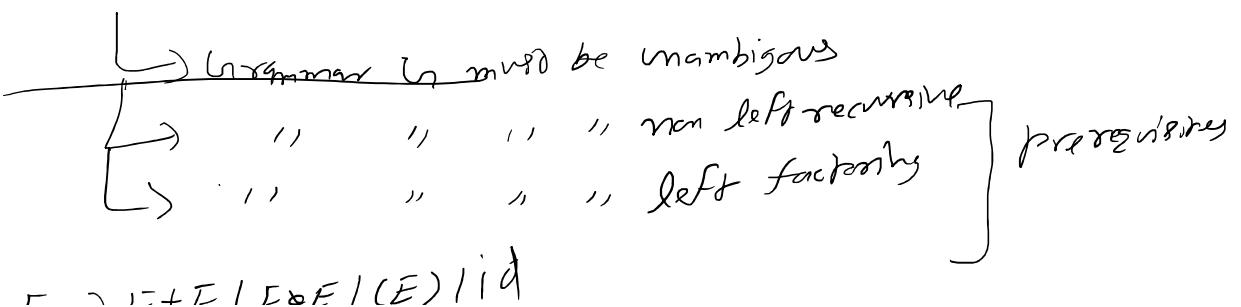
(II)  $a \underline{a} a \underline{a}$

(III)  $a \underline{a} a \underline{a} a \underline{a} a \underline{a}$



$\uparrow \uparrow \uparrow \uparrow$  ↑  
point of failure

Predictive Top down Parsing



$$\begin{array}{c}
 E \rightarrow E+E \mid E \cdot E \mid (E) \mid id \\
 \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\
 id + id \cdot id
 \end{array}$$

$\Rightarrow E \Rightarrow E+E \Rightarrow id + E \Rightarrow id + E \cdot E \Rightarrow id + id \cdot id \quad (\text{LMD})$   
 $E \Rightarrow E \cdot E \Rightarrow E+E \cdot E \Rightarrow id + id \cdot E \Rightarrow id + id \cdot id \quad (\text{LMD})$   
 $E \Rightarrow E+T \Rightarrow T+T \Rightarrow F+T \Rightarrow id + T \Rightarrow id + T \cdot F \Rightarrow$   
 $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$   
 $E \rightarrow E+T \mid T$   
 $T \rightarrow T \cdot F \mid F$   
 $F \rightarrow (id) \mid id$

$\underbrace{id + id \cdot id}_{+} \Rightarrow +$   
 $(2+3)+4 \quad (2 \times 3) \times 4 = 6 \times 4 = 24$   
 $+,-,\times,/ \quad - \text{left association}$   
 $,,= \quad - \text{right association}$   
 $\underbrace{2+3+4}_{\leftarrow} \Rightarrow 2^8$

$$w = xyz \in L$$

$$\rightarrow x^i y^j z \in L \quad \text{if } i \geq 0$$

$$z \in L \quad |z| \geq n$$

$n$  is any positive constant

$$\begin{array}{c}
 z = uuvwxy \\
 \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\
 |vwx| \geq 1 \quad |vwx| \leq n \quad vwx \neq \epsilon
 \end{array}$$

$uv^i w^j x^y \in L \neq \emptyset$   
 $T \rightarrow T_0$  where  $L$  is not CFL, find  $i$  such that  
 $uv^i w^j x^y \notin L$

$$z = uvwxy$$

Consider the grammar given below to construct a predictive parser

$$E \rightarrow E+E \mid E \cdot E \mid (E) \mid id \quad (\text{Ambiguous})$$



$$\begin{array}{l}
 E \rightarrow E+T \mid T \\
 T \rightarrow T \cdot F \mid F
 \end{array} \quad (\text{Unambiguous})$$

$E \rightarrow E + T \mid T$   
 $T \rightarrow T * F \mid F$  (Unambiguous)  
 $F \rightarrow (E) \mid id$   
 $\Downarrow A \rightarrow \alpha \alpha / \beta \Rightarrow A \rightarrow \beta A' \text{, } A' \rightarrow \alpha A' \mid \epsilon$

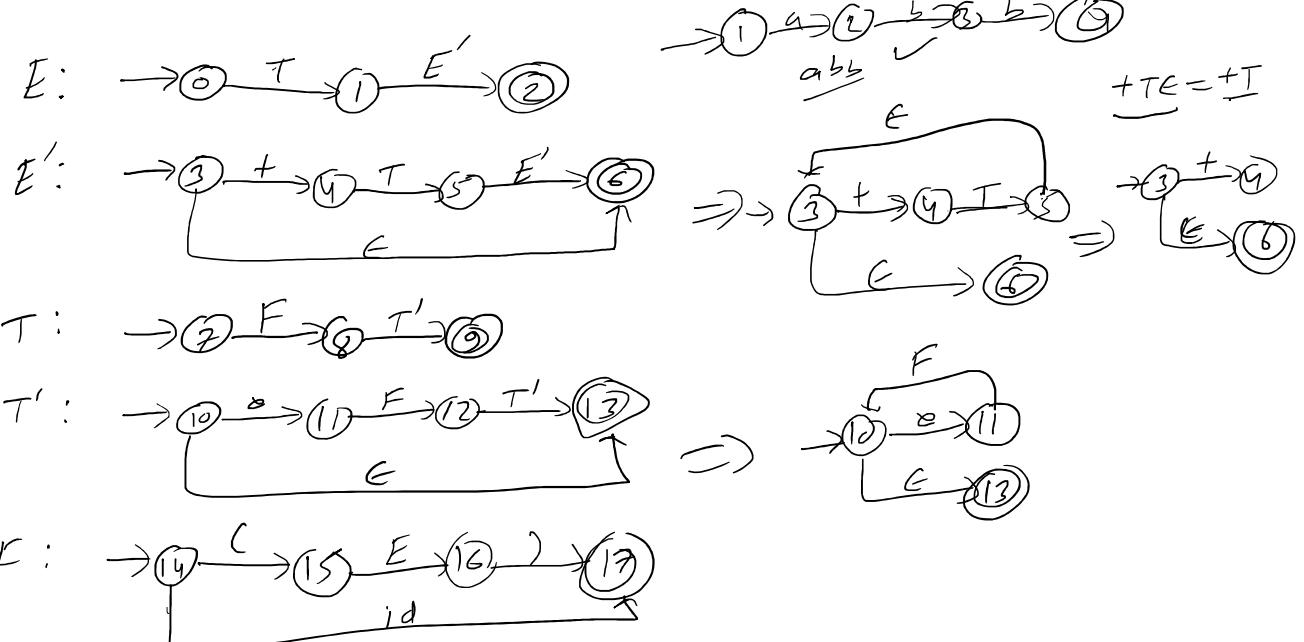
$E \rightarrow E + T \mid T$   
 $A = E, \alpha = +T, \beta = T$

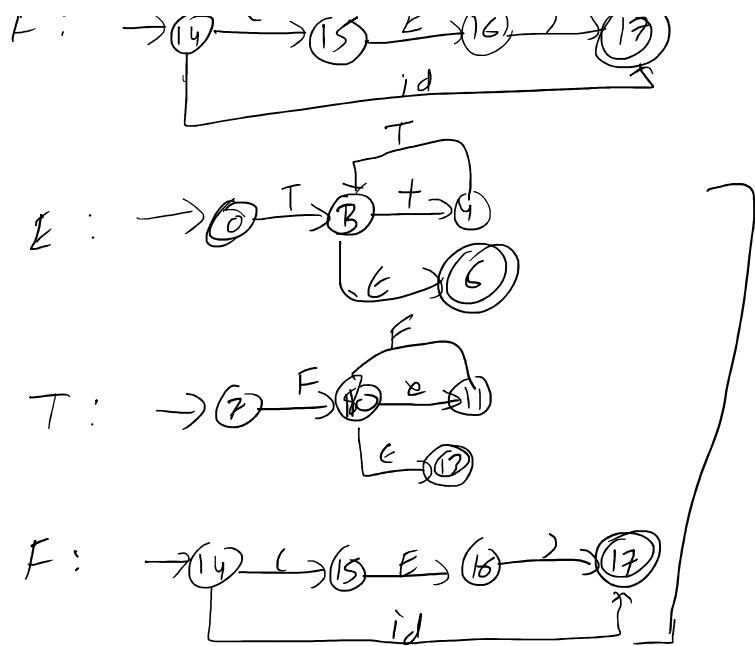
$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow T * F \mid F$   
 $A = T, \alpha = *F, \beta = F$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

### Recursive Predictive Parsing

$E \rightarrow TE'$   
 $E' \rightarrow +TE' \mid \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' \mid \epsilon$   
 $F \rightarrow (E) \mid id$

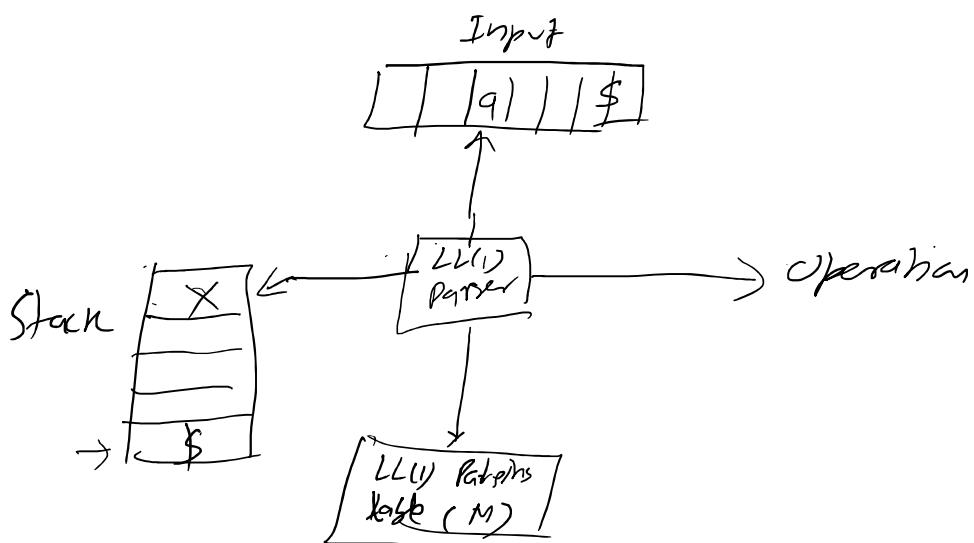
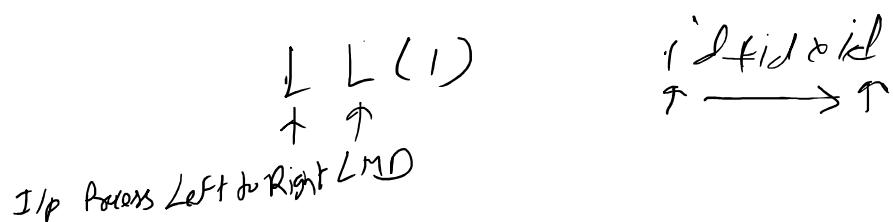




$$w = id + id \times id$$

$\uparrow \quad \uparrow \quad \uparrow$

### Non-recursing Predictive Parsing (LL(1) Parsing)



(1)  $X = a = \$$  Success (i.e. string is syntactically valid)  
 n . . . n -> a move I/p

- (I)  $X = a = \$$  Success (i.e. string is syntactically valid)
- (II)  $X = a \neq \$$  Pop top element from the stack & move I/P pointer to next I/P element
- (III)  $X \neq a$  Unsuccess i.e. given string is syntactically invalid string
- (IV) if  $X$  is variable then refer entry in Parsing table  $M[X, a]$   
 $\rightarrow$   $X \rightarrow \text{word}$ , pop  $X$  from the stack & push word.
- (V) if  $X$  is variable &  $M[X, a]$  is blank (error entry)  
string is invalid

Ex

$$E \rightarrow E+E \mid E \cdot E \mid (E) \mid \text{id} \quad (\text{Ambiguous})$$

$\Downarrow$

$$\begin{array}{l} E \rightarrow E+T \mid T \\ T \rightarrow T \cdot F \mid F \quad (\text{Unambiguous}) \\ F \rightarrow (E) \mid \text{id} \\ \Downarrow \end{array}$$

$A \Rightarrow A\alpha / \beta \Rightarrow \begin{cases} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' / \epsilon \end{cases}$

$$\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow +TE' \mid \epsilon \\ T \rightarrow FT' \\ T' \rightarrow *FT' \mid \epsilon \\ F \rightarrow (E) \mid \text{id} \end{array} \quad (\text{non left-recursive})$$

$B \rightarrow \epsilon$

(Already left factored)

$$X = a \underline{B} C = a \epsilon C = a \underset{=} \epsilon = a$$

$\text{FIRST}(X)$ :

(1) if  $X$  starts with a terminal  $a$ , then  
 $a$  included in  $\text{FIRST}(X)$

(2) if  $X \xrightarrow{*} \epsilon$ , then  $\epsilon$  will be included in  $\text{FIRST}(X)$  if  $\epsilon = \frac{BC}{\uparrow \uparrow} \xrightarrow{*} \epsilon$   
 $\epsilon$  included in  $\text{FIRST}(X)$

if

.. .. ✓

Included in FIRST(x)

(3)  $X \rightarrow x_1 x_2 \dots x_i x_{i+1} \dots x_n$

$x_1 \xrightarrow{\epsilon} \epsilon, x_2 \xrightarrow{\epsilon} \epsilon \dots x_i \xrightarrow{\epsilon} \epsilon \quad x_{i+1} \not\xrightarrow{\epsilon}$

FIRST( $\underbrace{x_{i+1} \dots x_n}_{\not\xrightarrow{\epsilon}}$ ) will be included in FIRST(x)

- Follow(B) :
- (1) if B is right symbol then \$ will be included in Follow(B)
  - (2) if  $A \rightarrow \alpha B \beta$ , then FIRST(\$) will be included in Follow(B) except \$\epsilon\$
  - (3) if  $A \rightarrow \alpha B \beta$ ,  $\beta \xrightarrow{\epsilon} \epsilon$  then Follow(A) will be included in Follow(B)

$$E \rightarrow TE' \checkmark$$

$$E' \rightarrow +TE' | \epsilon \checkmark$$

$$\text{FIRST}(E) \cap \text{Follow}(E) = \emptyset$$

$$\text{FIRST}(T') \cap \text{Follow}(T') = \emptyset$$

$$T \rightarrow FT' \checkmark$$

$$T' \rightarrow *ET' | \epsilon \checkmark$$

$$F \rightarrow (E) | id \checkmark$$

$$X = \begin{cases} TE' & \text{FIRST}(T) \neq \emptyset \\ \epsilon & \text{otherwise} \end{cases}$$

$$\text{FIRST}(E) = \text{FIRST}(TE') = \{ (, id \} \}$$

$$\text{FIRST}(E') = \text{FIRST}(+TE') \cup \text{FIRST}(E) = \{ +, \epsilon \}$$

$$\text{FIRST}(T) = \text{FIRST}(FT') = \{ (, id \} \}$$

$$\text{FIRST}(T') = \text{FIRST}(*ET') \cup \text{FIRST}(E) = \{ *, \epsilon \}$$

$$\text{FIRST}(F) = \text{FIRST}(E) \cup \text{FIRST}(id) = \{ (, id \} \}$$

$$\text{Follow}(E) = \{ \$, ) \}$$

$$\text{Follow}(E) = \{\$, )\}$$

$$\text{Follow}(E') = \{\$, )\}$$

$$\text{Follow}(T) = \{+, \$, )\}$$

$$\text{Follow}(T') = \{+, \$, )\}$$

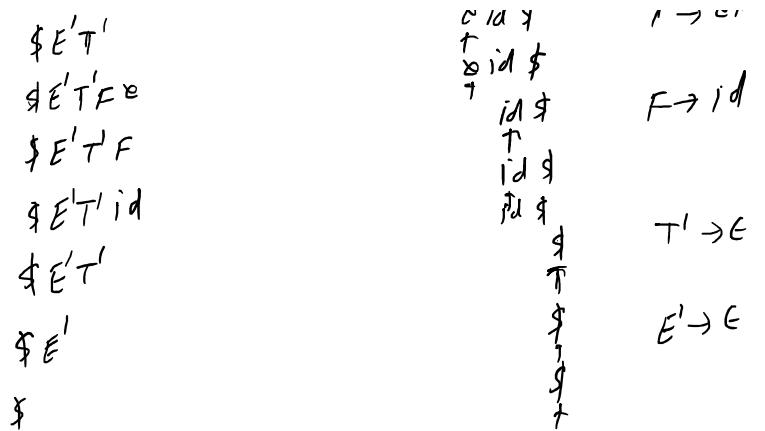
$$\text{Follow}(F) = \{\&, +, \$, )\}$$

|                  | $\downarrow$          | $\downarrow$         | $\downarrow$        | $\downarrow$ | $\downarrow$        | $\downarrow$       | $\downarrow$       |
|------------------|-----------------------|----------------------|---------------------|--------------|---------------------|--------------------|--------------------|
|                  | +                     | *                    | (                   | )            | id                  | \$                 |                    |
| $\rightarrow E$  |                       |                      | $E \rightarrow TE'$ |              | $E \rightarrow TE'$ |                    |                    |
| $\rightarrow E'$ | $E' \rightarrow +TE'$ |                      |                     |              |                     |                    | $E' \rightarrow E$ |
| $\rightarrow T$  |                       |                      | $T \rightarrow FT'$ |              |                     |                    |                    |
| $\rightarrow T'$ | $T' \rightarrow E$    | $T' \rightarrow FT'$ |                     |              | $T' \rightarrow E$  |                    | $T' \rightarrow E$ |
| $\rightarrow F$  |                       |                      | $F \rightarrow (E)$ |              |                     | $F \rightarrow id$ |                    |

$\text{LL(1)}$

Stack      Input      Production      Tree

|            |                    |                       |                 |
|------------|--------------------|-----------------------|-----------------|
| $\$E$      | $id + id \& id \$$ | $E \rightarrow TE'$   |                 |
| $\$E'T$    | $id + id \& id \$$ | $T \rightarrow FT'$   |                 |
| $\$E'T'F$  | $id + id \& id \$$ | $F \rightarrow id$    |                 |
| $\$E'T'id$ | $id + id \& id \$$ | $T' \rightarrow E$    |                 |
| $\$E'T'$   | $+ id \& id \$$    | $E' \rightarrow +TE'$ |                 |
| $\$E'$     | $+ id \& id \$$    |                       |                 |
| $\$E'T+$   | $id \& id \$$      | $T \rightarrow FT'$   | $id + id \& id$ |
| $\$E'T$    | $id \& id \$$      | $F \rightarrow id$    |                 |
| $\$E'T'F$  | $id \& id \$$      |                       |                 |
| $\$E'T'id$ | $+ id \& id \$$    | $T' \rightarrow FT'$  |                 |
| $\$E'T'$   | $+ id \& id \$$    |                       |                 |
| $\$E'T'F*$ | $+ id \& id \$$    | $C \rightarrow id$    |                 |



$\text{FIRST}(E)$

Consider the grammar:

$$S \rightarrow iCtSA|a$$

$$A \rightarrow eS|e$$

$$C \rightarrow b$$

Test whether it is LL(1) grammar and construct the predictive parsing table for it.

|                              |                                |
|------------------------------|--------------------------------|
| $\text{FIRST}(S) = \{i, a\}$ | $\text{Follow}(S) = \{\$, e\}$ |
| $\text{FIRST}(A) = \{e, e\}$ | $\text{Follow}(A) = \{\$, e\}$ |
| $\text{FIRST}(C) = \{b\}$    | $\text{Follow}(C) = \{t\}$     |

Prove that it is not LL(1)

$$A \rightarrow eS \in$$

$$\text{FIRST}(A) \cap \text{Follow}(A) = \{e, e\} \cap \{\$, e\} = \{e\} \neq \emptyset$$

So, grammar is not LL(1)

|   | i                     | t | q                 | e                  | b                 | \$                |
|---|-----------------------|---|-------------------|--------------------|-------------------|-------------------|
| S | $S \rightarrow iCtSA$ |   | $S \rightarrow q$ |                    |                   |                   |
| A |                       |   |                   | $A \rightarrow eS$ |                   | $A \rightarrow G$ |
| C |                       |   |                   |                    | $C \rightarrow b$ |                   |

### Bottom-Up Parser (Shift-Reduce Parser)

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T \& F \mid F$$

$$F \rightarrow (E) \mid id$$

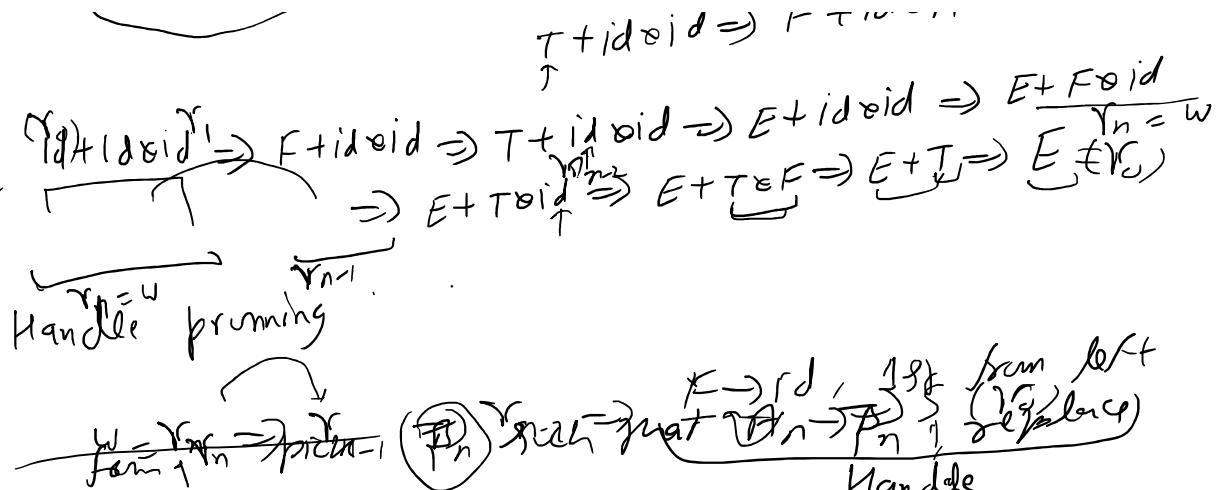
RMD

$$id + id \& id$$

$$T + id \& id \Rightarrow F + id \& id \Rightarrow id + id \& id$$

RMD

RMP



(reduction)

$P_n \rightarrow A_n$  to get  $V_{n-1}$

$A_{n-1} \rightarrow P_{n-1}$

$A_{n-2} \rightarrow P_{n-2} \rightarrow P_{n-3}$

and so on

| Stack      | Input      | operation                    |
|------------|------------|------------------------------|
| \$         | id id \$   | shift id                     |
| \$ id      | + id \$    | Reduce by $I \rightarrow id$ |
| \$ F       | + id id \$ | Reduce by $T \rightarrow F$  |
| \$ T       | + id id \$ | Reduce by $E \rightarrow T$  |
| \$ E       | + id id \$ | Shift +                      |
| \$ E +     | id \$      | Shift id                     |
| \$ E + id  | id \$      | Reduce by $C \rightarrow id$ |
| \$ E + F   | id \$      | Reduce by $T \rightarrow F$  |
| \$ E + T   | id \$      | Shift *                      |
| \$ E + T * | id \$      | Shift id                     |
| ...        |            | $\vdots \rightarrow id$      |

$\boxed{id + id \cdot id}$

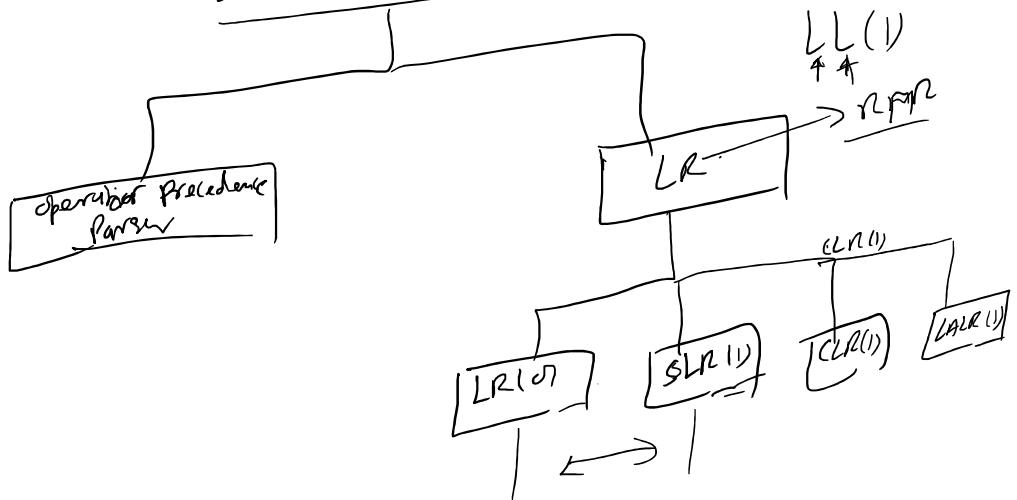
\$ E \$

$\$ \rightarrow T$   
 $\$ \rightarrow E + T$   
 $\$ \rightarrow E + T \rightarrow id$   
 $\$ \rightarrow E + T \rightarrow F$   
 $\$ \rightarrow E + T \rightarrow J$   
 $\$ \rightarrow E$

$\$ \rightarrow F$   
 $\$ \rightarrow T$   
 $\$ \rightarrow T$   
 $\$ \rightarrow T$   
 $\$ \rightarrow T$

Shift - id  
 Reduce  $F \rightarrow id$   
 Reduce  $T \rightarrow T \rightarrow F$   
 Reduce  $T \rightarrow E + T$

Bottom-up Parsing (Shift-Reduce Parser)



SLR(1) Parser (Simple LR)

Items       $A \rightarrow \underline{XYZ}$  (production)  
 $A \rightarrow \cdot XYZ$   
 $A \rightarrow X \cdot YZ$   
 $A \rightarrow XY \cdot Z$   
 $A \rightarrow XYZ \cdot$  (Items)

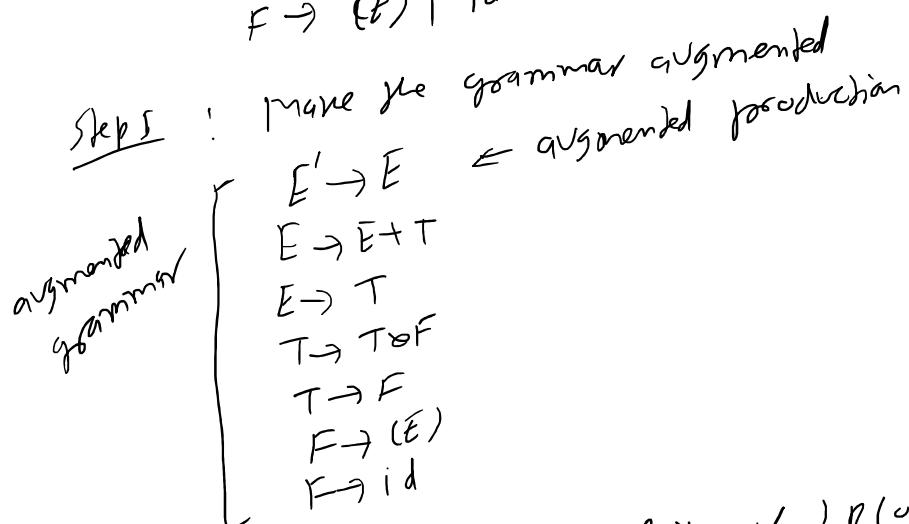
>Note - Shifting dot (.) one position ahead

Closure - If after dot variable appears then explore all the productions of that variable and place dot at first position in all the productions.

Example

$E \rightarrow E + T \mid T$   
 $T \rightarrow T \otimes F \mid F$

$F \rightarrow (E) \mid id$



Step II Complete Canonical Collection of LR(0) Items

$$I_0 = \{ E' \rightarrow \cdot E \quad \checkmark \\ E \rightarrow \cdot E + T \quad \checkmark \\ E \rightarrow \cdot T \\ T \rightarrow \cdot T * F \\ T \rightarrow \cdot F \\ F \rightarrow \cdot (E) \\ F \rightarrow \cdot id \}$$

$\{ E, T, F, (, id \}$

$$L_{\text{NT}}(I_0, E) = I_1 = \{ E' \rightarrow E \cdot \\ E \rightarrow E \cdot + T \quad \checkmark \quad \{ + \} \\ \}$$

$$L_{\text{NT}}(I_0, T) = I_2 = \{ E \rightarrow T \cdot \quad \{ \cdot \} \\ T \rightarrow T \cdot * F \}$$

$$\text{FIRST}(E) \cap \text{Follow}(E) = \emptyset \\ \{ \$, +, ) \} = \emptyset$$

$$L_{\text{NT}}(I_0, F) = I_3 = \{ T \rightarrow F \cdot \}$$

$$L_{\text{NT}}(I_0, ()) = I_4 = \{ F \rightarrow (\cdot E) \\ E \rightarrow \cdot E + T \\ E \rightarrow \cdot T \\ T \rightarrow \cdot T * F \\ T \rightarrow \cdot F \\ F \rightarrow \cdot (E) \\ F \rightarrow \cdot id \}$$

$\{ E \rightarrow T \cdot \\ \{ T \rightarrow T \cdot * F \} \}$

... r. T)

$$\text{not}_0(I_0, \text{id}) = I_5 = \begin{cases} F \rightarrow \text{id} \\ F \rightarrow \text{id.} \end{cases}$$

$$\text{not}_0(I_1, +) = I_6 = \begin{cases} E \rightarrow E + \cdot T \\ T \rightarrow \cdot T \otimes F \\ T \rightarrow \cdot F \\ F \rightarrow \cdot (E) \\ F \rightarrow \cdot \text{id} \end{cases} \quad \{ \stackrel{2}{+}, \stackrel{1}{F}, \stackrel{1}{(}, \stackrel{1}{\text{id}} \}$$

$$\text{not}_0(I_2, \otimes) = I_7 = \begin{cases} T \rightarrow T \otimes \cdot F \\ F \rightarrow \cdot (F) \\ F \rightarrow \cdot \text{id} \end{cases} \quad \{ \stackrel{1}{F}, \stackrel{1}{(}, \stackrel{1}{\text{id}} \}$$

$$\text{not}_0(I_4, E) = I_8 = \begin{cases} F \rightarrow (E \cdot) \\ E \rightarrow E \cdot + T \end{cases} \quad \{ \stackrel{1}{)}, \stackrel{1}{+} \}$$

$$\text{not}_0(I_4, T) = I_2$$

$$\text{not}_0(I_4, F) = I_3$$

$$\text{not}_0(I_4, ()) = I_4$$

$$\text{not}_0(I_4, \text{id}) = I_5$$

$$\text{not}_0(I_6, T) = I_9 = \begin{cases} E \rightarrow E + T \cdot \\ T \rightarrow T \cdot \otimes F \end{cases} \quad \{ \stackrel{1}{\otimes} \}$$

$$\text{not}_0(I_6, F) = I_3$$

$$\text{not}_0(I_6, ()) = I_4$$

$$\text{not}_0(I_6, \text{id}) = I_5$$

$$\text{not}_0(I_7, F) = I_{10} = \begin{cases} T \rightarrow T \otimes F \cdot \end{cases}$$

$$\text{not}_0(I_7, ()) = I_4$$

$$\text{not}_0(I_7, \text{id}) = I_5$$

$$\text{funst}(\otimes F) \cap \text{Follow}(B) = \emptyset$$

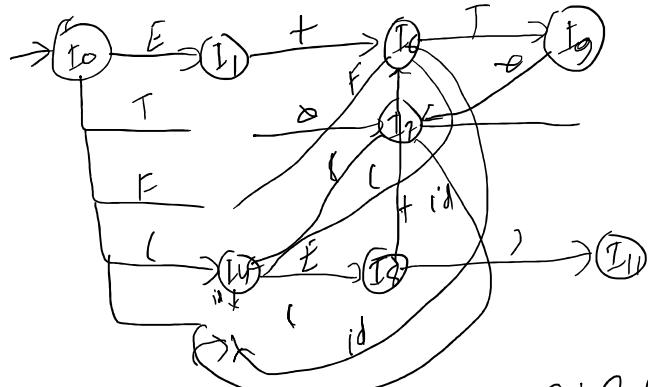
$$\{ \otimes \cap \{ , +, () \} = \emptyset$$

$$L_{\text{To}}(I_8, \cdot) = I_{11} = \left\{ F \Rightarrow (E) \right.$$

↓

$$L_{\text{To}}(I_8, +) = I_6$$

$$L_{\text{To}}(I_9, \alpha) = I_7$$



SLR(1) Parsing table

| States          | Action         |                |                |                |                 |                | Lookaheads |    |   |
|-----------------|----------------|----------------|----------------|----------------|-----------------|----------------|------------|----|---|
|                 | +              | *              | (              | )              | id              | \$             | E          | T  | F |
| I <sub>0</sub>  |                |                | S <sub>4</sub> |                | S <sub>5</sub>  |                | +          | 2  | 3 |
| I <sub>1</sub>  | S <sub>6</sub> |                |                |                |                 | accept         |            |    |   |
| I <sub>2</sub>  | R <sub>2</sub> | S <sub>7</sub> | L              | R <sub>2</sub> |                 | R <sub>2</sub> |            |    |   |
| I <sub>3</sub>  | R <sub>4</sub> | R <sub>4</sub> | S <sub>4</sub> | R <sub>4</sub> | R <sub>4</sub>  | R <sub>4</sub> |            |    |   |
| I <sub>4</sub>  |                |                | S <sub>4</sub> |                | S <sub>5</sub>  |                | 8          | 2  | 3 |
| I <sub>5</sub>  | R <sub>6</sub> | R <sub>6</sub> | R <sub>6</sub> |                |                 | R <sub>6</sub> |            |    |   |
| I <sub>6</sub>  |                |                | S <sub>4</sub> |                | S <sub>8</sub>  |                | 9          | 3  |   |
| I <sub>7</sub>  |                |                | S <sub>4</sub> |                | S <sub>5</sub>  |                |            | 10 |   |
| I <sub>8</sub>  | S <sub>6</sub> |                |                |                | S <sub>11</sub> |                |            |    |   |
| I <sub>9</sub>  | R <sub>1</sub> | S <sub>7</sub> |                | R <sub>1</sub> |                 | R <sub>1</sub> |            |    |   |
| I <sub>10</sub> | R <sub>3</sub> | R <sub>3</sub> |                | R <sub>3</sub> |                 | R <sub>3</sub> |            |    |   |
| I <sub>11</sub> | R <sub>5</sub> | R <sub>5</sub> |                | R <sub>5</sub> |                 | R <sub>5</sub> |            |    |   |

Shift  
Reduce  
Accept

$$\textcircled{1} E \rightarrow E + T$$

$$\text{Follow}(E) = \{ \$, +, ) \}$$

$$\textcircled{2} E \rightarrow T$$

$$\text{Follow}(T) = \{ \$, +, ), \alpha \}$$

- ①  $T \rightarrow T \& F$
- ②  $T \rightarrow F$
- ③  $F \rightarrow (E)$
- ④  $F \rightarrow id$

$$Follow(F) = \{ \$, +, ), \}, \Rightarrow \}$$

For LR(0) (LR-  
without referring follow  
we reduce entries  $(r_1, r_2, -r_6)$ )

~~Parity~~

| Stack                 | Input              |
|-----------------------|--------------------|
| 0                     | $id + id \& id \$$ |
| 0 id \$               | $+ id \& id \$$    |
| 0 F 3                 | $+ id \& id \$$    |
| 0 T 2                 | $+ id \& id \$$    |
| 0 E 1                 | $+ id \& id \$$    |
| 0 E 1 + 6             | $id \& id \$$      |
| 0 E 1 + 6 id \$       | $\& id \$$         |
| 0 E 1 + 6 F 3         | $\& id \$$         |
| 0 E 1 + (T)           | $\& id \$$         |
| 0 E 1 + (T) & 7       | $\& id \$$         |
| 0 E 1 + (T) & 7 id \$ | $\$$               |
| 0 E 1 + (T) & 7 F 10  | $\$$               |
| 0 E 1 + (T) & 7 F 10  | $\$$               |
| 0 E 1 + (T) & 7 F 10  | $\$$               |
| 0 E 4                 | <u>accept</u>      |

[ P.T. given grammar is  
not SLR(1) ]

→ Prove that there exists  
Shift-Reduce conflict to prove  
grammar is not SLR(1) ]

$$I_{\beta} : \begin{cases} A \rightarrow \alpha \cdot \beta & (\text{shift}) \\ \beta \rightarrow \gamma \cdot & (\text{reduce}) \end{cases}$$

$$FIRST(\beta) \cap FOLLOW(B) \neq \emptyset$$

(Shift-reduce conflict) ✓

$E' \rightarrow E$   
 $E \rightarrow E + E$      $E \& E$      $(E) / id$  (Ambiguity)

$$L : E \rightarrow E + E$$

To

$$S_F : E \rightarrow E^*$$

$$\begin{aligned} & FIRST(+E) \cup FIRST(\& E) \\ & \{ +, \& \} \cap \{ \$, +, \&, ) \} \quad \checkmark \\ & (2 \& 3)^* \quad \checkmark \\ & \text{Follow}(E) = \{ \$, +, \&, ) \} \quad \checkmark \end{aligned}$$

$E \xrightarrow{?+?^*} \{+, -, /\}$   
 $\text{Syntax Reduced } E = \{ \$, +, *, /\} \}$   
 $\downarrow S \quad \downarrow T \quad \downarrow$   
 $(S_0 / S_1) (S_0 / S_1)$   
 $(S_0 / S_1) (S_0 / S_1)$

## CLR(1) (Canonical LR)

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid \text{id}$$

Step  
 augmented grammar  
 $E' \rightarrow E$   
 $E' \rightarrow E + T$   
 $T \rightarrow F$   
 $F \rightarrow (E)$   
 $F \rightarrow \text{id}$

Complete Canonical collection of LR(1) items  
 Skip if

$E' \rightarrow \cdot E, \$$  → (null part)  
 $E' \rightarrow \cdot E + T, \$ \mid +$  → Lookahead part

$\checkmark E' \rightarrow \cdot T, \$ \mid +$   
 $\checkmark E' \rightarrow \cdot T * F, \$ \mid + \mid *$

$\checkmark T \rightarrow \cdot F, \$ \mid + \mid *$

$\checkmark F \rightarrow \cdot (E), \$ \mid + \mid *$

$\checkmark F \rightarrow \cdot \text{id}, \$ \mid + \mid *$

$$\text{LR}(1) = \{ + \}$$

$$\{ E, T, F, \cdot, \mid, \text{id} \}$$

$$+ \cup \{ \cdot \} = \{ + \}$$

$$\{ E, T, F, \cdot, \mid, \text{id} \}$$

$I_1 : E' \rightarrow E \cdot, \$$   
 $E \rightarrow E \cdot + T, \$ \mid +$

$I_2 : E \rightarrow T \cdot, \$ \mid +$   
 $T \rightarrow T \cdot * F, \$ \mid + \mid *$

$I_3 : F \rightarrow F \cdot, \$ \mid + \mid *$

$I_4 : F \rightarrow (\cdot E)$

Construct CLR(1)  
 $S \rightarrow CC$   
 $C \rightarrow C \mid d$

Q. Design CLR(1) Parser for the following grammar

$$S \rightarrow CC$$

$$C \rightarrow cC \mid d$$

Step I

more grammar augmented

$$S' \rightarrow S \leftarrow \text{augmented production}$$

augmented  
grammar

$$\begin{array}{l} S \rightarrow CC \\ C \rightarrow cC \\ C \rightarrow d \end{array}$$

Step II Compute canonical collection of LR(1) items

$$\begin{array}{ll} I_0 = & \overbrace{S' \rightarrow \cdot S, \$}^{\text{FIRST}(E\$) = \text{FIRST}(\$) = \{\$\}} \\ & S \rightarrow \cdot SC, \$ \\ & \quad \quad \quad \text{FIRST}(CS) = \{c\} \\ & \vee C \rightarrow \cdot cC, c \mid d \\ & \vee C \rightarrow \cdot d, \quad c \mid d \quad \quad \quad \{S, C, c, d\} \end{array}$$

$$I_1 = S' \rightarrow S \cdot, \$$$

$$\begin{array}{ll} I_2 = S \rightarrow C \cdot C, \$ & \text{FIRST}(C\$) = \{c\} \\ & C \rightarrow \cdot cC, \$ \\ & \quad \quad \quad \{C, c\} \\ & C \rightarrow \cdot d, \$ \end{array}$$

$$\begin{array}{ll} I_3 = C \rightarrow C \cdot C, c \mid d & \{C, c, d\} \\ C \rightarrow \cdot cC, c \mid d \\ C \rightarrow \cdot d, c \mid d \end{array}$$

$$I_4 = C \rightarrow \cdot d, c \mid d$$

$$I_5 = S \rightarrow CC \cdot, \$$$

$$I_6 = \overbrace{C \rightarrow C \cdot C, \$}^{\{C, c, d\}}$$

$$\begin{array}{l} I_0 \\ I_1 \\ I_2 \\ I_3 \\ I_4 \\ I_5 \\ I_6 \\ I_7 \\ I_8 \end{array}$$

$$\begin{array}{l} C \rightarrow \cdot cC, c \mid d \\ \quad \quad \quad \times \end{array}$$

$I_6 = \overbrace{C \rightarrow c.C, \$}^{C \rightarrow c.C, \$}$        $\overbrace{C, c, d\$}^{C, c, d\$}$        $\overbrace{C \rightarrow c.C, \$}^{C \rightarrow c.C, \$}$   
 $C \rightarrow c.C, \$$   
 $C \rightarrow .d, \$$

$I_7 = C \rightarrow d., \$$

$I_8 = C \rightarrow c.C, cd$

$I_9 = C \rightarrow c.C, \$$

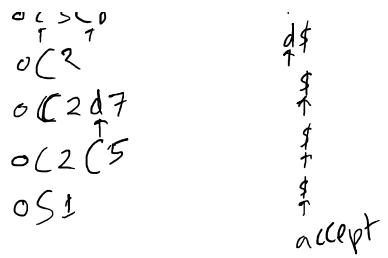
| States | Action |       |        | Go To |   |
|--------|--------|-------|--------|-------|---|
|        | c      | d     | \$     | S     | C |
| $I_0$  | $s_3$  | $s_4$ |        | 1     | 2 |
| $I_1$  |        |       | accept |       |   |
| $I_2$  | $s_6$  | $s_7$ |        |       | 5 |
| $I_3$  | $s_3$  | $s_4$ |        |       | 8 |
| $I_4$  | $r_3$  | $r_3$ |        |       |   |
| $I_5$  |        |       | $r_1$  |       |   |
| $I_6$  | $s_6$  | $s_7$ |        |       | 9 |
| $I_7$  |        |       | $r_3$  |       |   |
| $I_8$  | $r_2$  | $r_2$ |        |       |   |
| $I_9$  |        |       | $r_2$  |       |   |

- ①  $S \rightarrow CC$
- ②  $C \rightarrow cC$
- ③  $C \rightarrow d$

$S \Rightarrow CC \Rightarrow cCC \Rightarrow cdC \Rightarrow \underline{cd}$

Printings

| Stack | Input  |
|-------|--------|
| 0     | cd\\$  |
| 0C3   | +dd\\$ |
| 0C3d4 | d\\$   |
| 0C3C8 | d\\$   |
| 0C2   | d\\$   |
| -r>17 | \$     |



### LALR(1) (LookAhead LR) (LLR(1))

$S \rightarrow CC$   
 $C \rightarrow CC$   
 $C \rightarrow d$   
Step I      more grammar augmented

$S' \rightarrow S$   
 $S \rightarrow CC$   
 $C \rightarrow CC$   
 $C \rightarrow d$   
Step II      Compute Canonical Collection of LR(1) Items

I<sub>0</sub>       $S' \rightarrow \cdot S, \$$       {  $S, C, c, d$  }  
 ~  $S \rightarrow \cdot CC, \$$   
 $C \rightarrow \cdot CC, cld$   
 $C \rightarrow \cdot d, cld$

I<sub>1</sub>       $S' \rightarrow S, \$$       {  $C, c, d$  }  
 I<sub>2</sub>       $S \rightarrow C \cdot C, \$$       {  $C, c, d$  }  
 $C \rightarrow \cdot CC, \$$   
 $C \rightarrow \cdot d, \$$

I<sub>3</sub>       $C \rightarrow C \cdot C, cld$       {  $C, c, d$  }  
 $C \rightarrow \cdot CC, cld$   
 $C \rightarrow \cdot d, cld$

I<sub>4</sub>       $C \rightarrow d, cld$

I<sub>5</sub>       $S \rightarrow C \cdot C, \$$

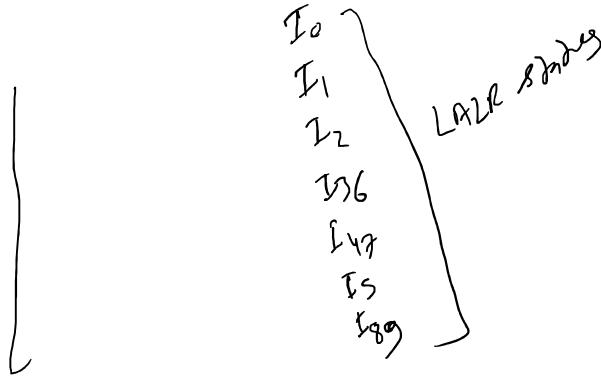
I<sub>6</sub>       $C \rightarrow C \cdot C, \$$       {  $C, c, d$  }  
 $C \rightarrow \cdot CC, \$$   
 $C \rightarrow \cdot d, \$$

I<sub>7</sub>       $C \rightarrow d, \$$   
 $\dots \dots , cld$

I<sub>0</sub> }

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$I_7 : C \rightarrow d\cdot, \$$   
 $I_8 : C \rightarrow cC\cdot, c|d$   
 $I_9 : C \rightarrow cC\cdot, \emptyset$   
 $I_{36} : C \rightarrow c\cdot C, c|d|\$$   
 $C \rightarrow 'cC, c|d|\$$   
 $C \rightarrow .d, c|d|\$$



$I_{47} : C \rightarrow d\cdot, c|d|\$$   
 $I_{89} : C \rightarrow cC\cdot, c|d|\$$

- (1)  $S \rightarrow CC$
- (2)  $C \rightarrow cC$
- (3)  $C \rightarrow d$

| S States | Action   |          |        | Up To |    |
|----------|----------|----------|--------|-------|----|
|          | c        | d        | \$     | S     | C  |
| $I_0$    | $s_{36}$ | $s_{47}$ |        | 1     | 2  |
| $I_1$    |          |          | accept |       |    |
| $I_2$    | $s_{36}$ | $s_{47}$ |        |       |    |
| $I_{36}$ | $s_{36}$ | $s_{47}$ |        |       | 5  |
| $I_{47}$ | $r_3$    | $r_3$    | $r_3$  |       | 89 |
| $I_5$    |          |          | $r_1$  |       |    |
| $I_{89}$ | $r_2$    | $r_2$    | $r_2$  |       |    |

RYBMS  
 Ed d  
 $I_{36}, I_6, I_9$   
 $I_{369}$

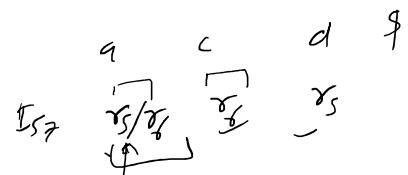
P.T. given grammar is not LA2R(1)

Soln: Prove that there exists Reduce-Reduce Conflict (R-R)

$I_5 : A \rightarrow C\cdot, a$   
 $B \rightarrow d\cdot, c$

$I_7 : A \rightarrow C\cdot, a$   
 $B \rightarrow d\cdot, a$

$I_{57} : \check{A} \rightarrow C\cdot, \check{a}\check{d}$   
 $\check{B} \rightarrow d\cdot, \check{a}\check{c}$



↑  
 Reduce-Reduce Conflict

$I_{S7}$ :  $\cup A \rightarrow C$ ,  $\frac{a|d}{\cup B \rightarrow d}$ ,  $\frac{a|c}{\cup}$

Reduce-Reduce Conflict

$r_s, r_6$

$I_S$        $A \rightarrow C$ ,  $a$   
 $B \rightarrow d$ ,  $b$

$a \quad b \quad c \quad d \quad \$$

$I_T$        $A \rightarrow C$ ,  $d$   
 $B \rightarrow d$ ,  $c$

$I_{S7}$        $\frac{r_s \quad r_6}{(A \rightarrow C, d)}$

(A is conflict)

$I_{S7}$        $A \rightarrow C$ ,  $a|d$   
 $B \rightarrow d$ ,  $b|c$