

Compiler course

Chapter 6

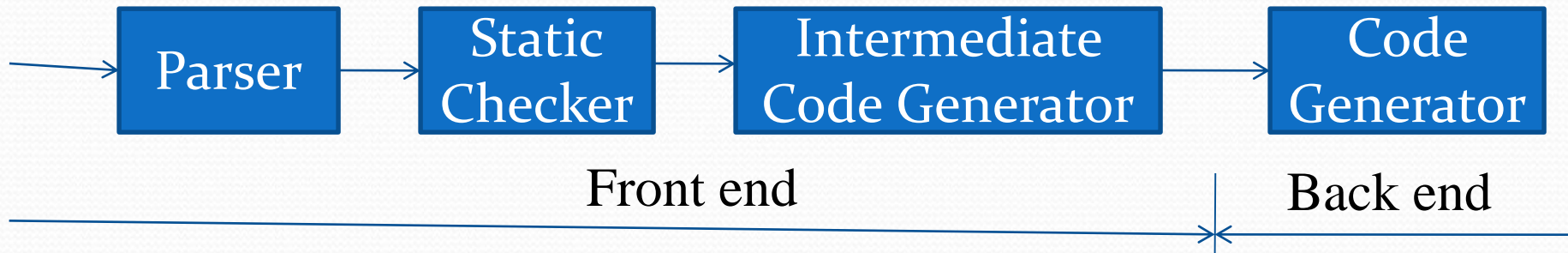
Intermediate Code Generation

Outline

- Variants of Syntax Trees
- Three-address code
- Types and declarations
- Translation of expressions

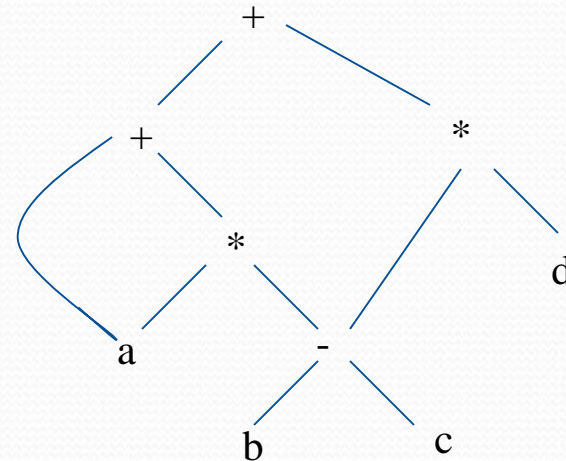
Introduction

- Intermediate code is the interface between front end and back end in a compiler
- Ideally the details of source language are confined to the front end and the details of target machines to the back end (a $m \times n$ model)
- In this chapter we study intermediate representations, static type checking and intermediate code generation



Variants of syntax trees

- It is sometimes beneficial to create a DAG instead of a tree for Expressions.
- This way we can easily show the common sub-expressions and then use that knowledge during code generation
- Example: $a + a * (b - c) + (b - c) * d$



SDD for creating DAG's

Production

- 1) $E \rightarrow E1 + T$
- 2) $E \rightarrow E1 - T$
- 3) $E \rightarrow T$
- 4) $T \rightarrow (E)$
- 5) $T \rightarrow id$
- 6) $T \rightarrow num$

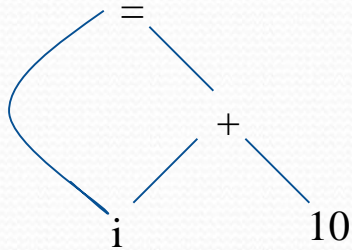
Semantic Rules

- $E.node = \text{new Node}('+', E1.node, T.node)$
 $E.node = \text{new Node}('-', E1.node, T.node)$
 $E.node = T.node$
 $T.node = E.node$
 $T.node = \text{new Leaf}(id, id.entry)$
 $T.node = \text{new Leaf}(num, num.val)$

Example:

- 1) $p1 = \text{Leaf}(id, \text{entry-a})$
- 2) $p2 = \text{Leaf}(id, \text{entry-a}) = p1$
- 3) $p3 = \text{Leaf}(id, \text{entry-b})$
- 4) $p4 = \text{Leaf}(id, \text{entry-c})$
- 5) $p5 = \text{Node}('-', p3, p4)$
- 6) $p6 = \text{Node}('*', p1, p5)$
- 7) $p7 = \text{Node}('+', p1, p6)$
- 8) $p8 = \text{Leaf}(id, \text{entry-b}) = p3$
- 9) $p9 = \text{Leaf}(id, \text{entry-c}) = p4$
- 10) $p10 = \text{Node}('-', p3, p4) = p5$
- 11) $p11 = \text{Leaf}(id, \text{entry-d})$
- 12) $p12 = \text{Node}('*', p5, p11)$
- 13) $p13 = \text{Node}('+', p7, p12)$

Value-number method for constructing DAG's



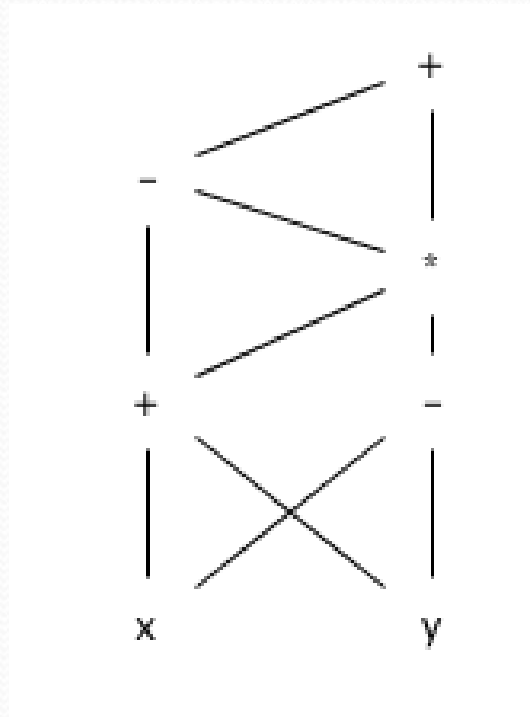
id			→ To entry for i
num	10		
+	1	2	
3	1	3	

Nodes of a DAG for $i=i+10$ allocated in an array

- Algorithm
 - Search the array for a node M with label op, left child l and right child r
 - If there is such a node, return the value number M
 - If not create in the array a new node N with label op, left child l, and right child r and return its value
- We may use a hash table

Exercises

Construct the DAG for the expression
 $((x+y)-((x+y)*(x-y)))+(x+y)*(x-y)$



Exercises

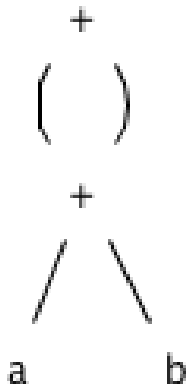
Construct the DAG and identify the value numbers for the subexpressions of the following expressions, assuming + associates from the left.

a. $a+b+(a+b)$

b. $a+b+a+b$

c. $a+a+(a+a+a+(a+a+a+a))$

a. $a+b+(a+b)$



1	id	a	
2	id	b	
3	+	1	2
4	+	3	3

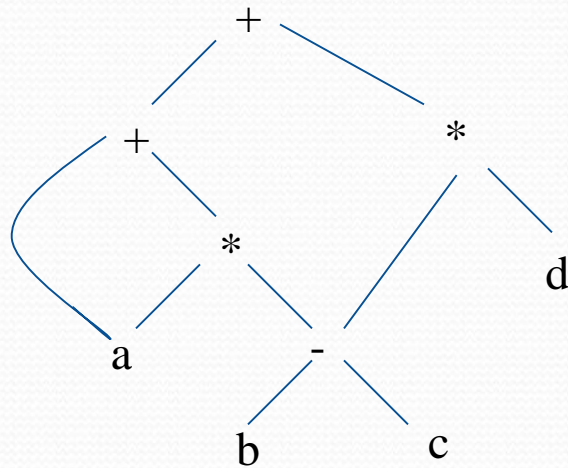
b. $a+b+a+b$



1	id	a	
2	id	b	
3	+	1	2
4	+	3	1
5	+	4	2

Three address code

- In a three address code there is at most one operator at the right side of an instruction
- Example:



$t1 = b - c$

$t2 = a * t1$

$t3 = a + t2$

$t4 = t1 * d$

$t5 = t3 + t4$

Forms of three address instructions

- $x = y \text{ op } z$
- $x = \text{op } y$
- $x = y$
- `goto L`
- `if x goto L and ifFalse x goto L`
- `if x relop y goto L`
- Procedure calls using:
 - `param x`
 - `call p,n`
 - `y = call p,n`
- $x = y[i]$ and $x[i] = y$
- $x = \&y$ and $x = *y$ and $*x = y$

Example

- do $i = i + 1$; while ($a[i] < v$);

```
L:      t1 = i + 1  
        i = t1  
        t2 = i * 8  
        t3 = a[t2]  
        if t3 < v goto L
```

Symbolic labels

```
100:    t1 = i + 1  
101:    i = t1  
102:    t2 = i * 8  
103:    t3 = a[t2]  
104:    if t3 < v goto 100
```

Position numbers

Data structures for three address codes

- Quadruples
 - Has four fields: op, arg1, arg2 and result
- Triples
 - Temporaries are not used and instead references to instructions are made
- Indirect triples
 - In addition to triples we use a list of pointers to triples

Example

- $b * \text{minus } c + b * \text{minus } c$

Three address code

$t1 = \text{minus } c$

$t2 = b * t1$

$t3 = \text{minus } c$

$t4 = b * t3$

$t5 = t2 + t4$

$a = t5$

Quadruples

op	arg1	arg2	result
minus	c		t1
*	b	t1	t2
minus	c		t3
*	b	t3	t4
+	t2	t4	t5
=	t5		a

Triples

	op	arg1	arg2
0	minus	c	
1	*	b	(0)
2	minus	c	
3	*	b	(2)
4	+	(1)	(3)
5	=	a	(4)

Indirect Triples

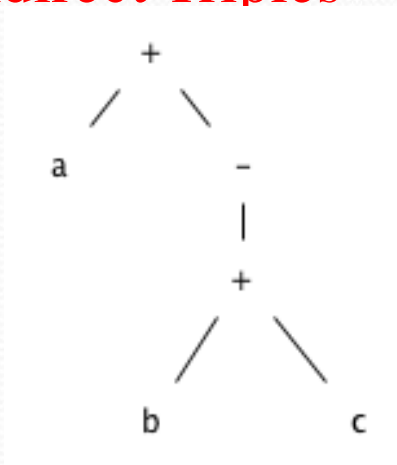
	op		arg1	arg2
35	(0)			
36	(1)			
37	(2)			
38	(3)			
39	(4)			
40	(5)			
0	minus	c		
1	*	b	(0)	
2	minus	c		
3	*	b	(2)	
4	+	(1)	(3)	
5	=	a	(4)	

Exercises

Translate the arithmetic expression $a + -(b + c)$ into

- a. A Syntax tree
- b. Quadruples
- c. Triples
- d. Indirect Triples

a.



c.

	op	arg1	arg2
0	+	b	c
1	minus	(0)	
2	+	a	(1)

d.

	op	arg1	arg2	result
0	+	b	c	t1
1	minus	t1		t2
2	+	a	t2	t3

	op	arg1	arg2	instruction
0	+	b	c	0 (0)
1	minus	(0)		1 (1)
2	+	a	(1)	2 (2)

Exercises

a) $a = b[i] + c[j]$

0)	=[]	b	i	t1
1)	=[]	c	j	t2
2)	+	t1	t2	t3
3)	=	t3		a

0)	=[]	b	i
1)	=[]	c	j
2)	+	(0)	(1)
3)	=	a	(2)

0)	=[]	b	i
1)	=[]	c	j
2)	+	(0)	(1)
3)	=	a	(2)

0)	
1)	
2)	
3)	

b. $a[i] = b*c - b*d$

0)	*	b	c	t1
1)	*	b	d	t2
2)	-	t1	t2	t3
3)	[]=	a	i	t4
4)	=	t3		t4

0)	*	b	c
1)	*	b	d
2)	-	(0)	(1)
3)	[]=	a	i
4)	=	(3)	(2)

0)	*	b	c
1)	*	b	d
2)	-	(0)	(1)
3)	[]=	a	i
4)	=	(3)	(2)

0)	
1)	
2)	
3)	
4)	

Exercises

c. $x = f(y+1) + 2$

0)	+	y	1	t1
1)	param	t1		
2)	call	f	1	t2
3)	+	t2	2	t3
4)	=	t3		x

0)	+	y	1
1)	param	(0)	
2)	call	f	1
3)	+	(2)	2
4)	=	x	(3)

0)	+	y	1
1)	param	(0)	
2)	call	f	1
3)	+	(2)	2
4)	=	x	(3)

0)	
1)	
2)	
3)	
4)	

Static Single-Assignment Form

- Static single-assignment form (SSA) is an intermediate representation that facilitates certain code optimizations.
- Two distinctive aspects distinguish SSA from three-address code.
- The first is that all assignments in SSA are to variables with distinct names; hence the term static single-assignment

```
p = a + b
q = p - c
p = q * d
p = e - p
q = p + q
```

```
p1 = a + b
q1 = p1 - c
p2 = q1 * d
p3 = e - p2
q2 = p3 + q1
```

(a) Three-address code. (b) Static single-assignment form.

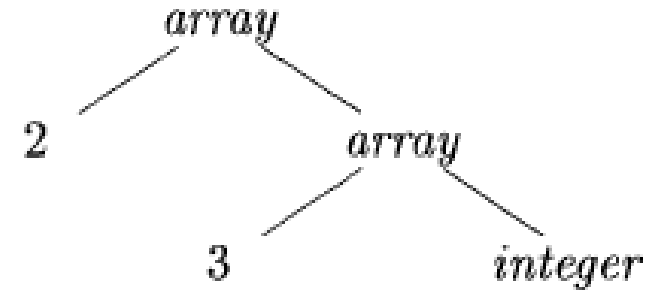
Figure : Intermediate program in three-address code and SSA

Types and Declarations

- The applications of types can be grouped under checking and translation:
 - *Type checking* uses logical rules to reason about the behavior of a program at run time. Specifically, it ensures that the types of the operands match the type expected by an operator.
 - For example, the && operator in Java expects its two operands to be booleans; the result is also of type boolean.
 - *Translation Applications.* From the type of a name, a compiler can determine the storage that will be needed for that name at run time. Type information is also needed to calculate the address denoted by an array reference, to insert explicit type conversions, and to choose the right version of an arithmetic operator, among other things.

Type Expressions

Example: `int[2][3]`
 `array(2,array(3,integer))`



- A basic type is a type expression
- A type name is a type expression
- A type expression can be formed by applying the array type constructor to a number and a type expression.
- A record is a data structure with named field
- A type expression can be formed by using the type constructor \rightarrow for function types
- If s and t are type expressions, then their Cartesian product $s * t$ is a type expression
- Type expressions may contain variables whose values are type expressions

Type Equivalence

- When type expressions are represented by graphs, two types are structurally equivalent if and only if one of the following conditions is true:
 - They are the same basic type.
 - They are formed by applying the same constructor to structurally equivalent types.
 - One is a type name that denotes the other.

Declarations

$$\begin{aligned} D &\rightarrow T \text{ id} ; D \mid \epsilon \\ T &\rightarrow B C \mid \text{record } \{ D \} \\ B &\rightarrow \text{int} \mid \text{float} \\ C &\rightarrow \epsilon \mid [\text{num}] C \end{aligned}$$

- ❑ Nonterminal D generates a sequence of declarations. Nonterminal T generates basic, array, or record types.
- ❑ Nonterminal B generates one of the basic types `int` and `float`. Nonterminal C , for "component," generates strings of zero or more integers, each integer surrounded by brackets.
- ❑ An array type consists of a basic type specified by B , followed by array components specified by nonterminal C .
- ❑ A record type (the second production for T) is a sequence of declarations for the fields of the record, all surrounded by curly braces.

Storage Layout for Local Names

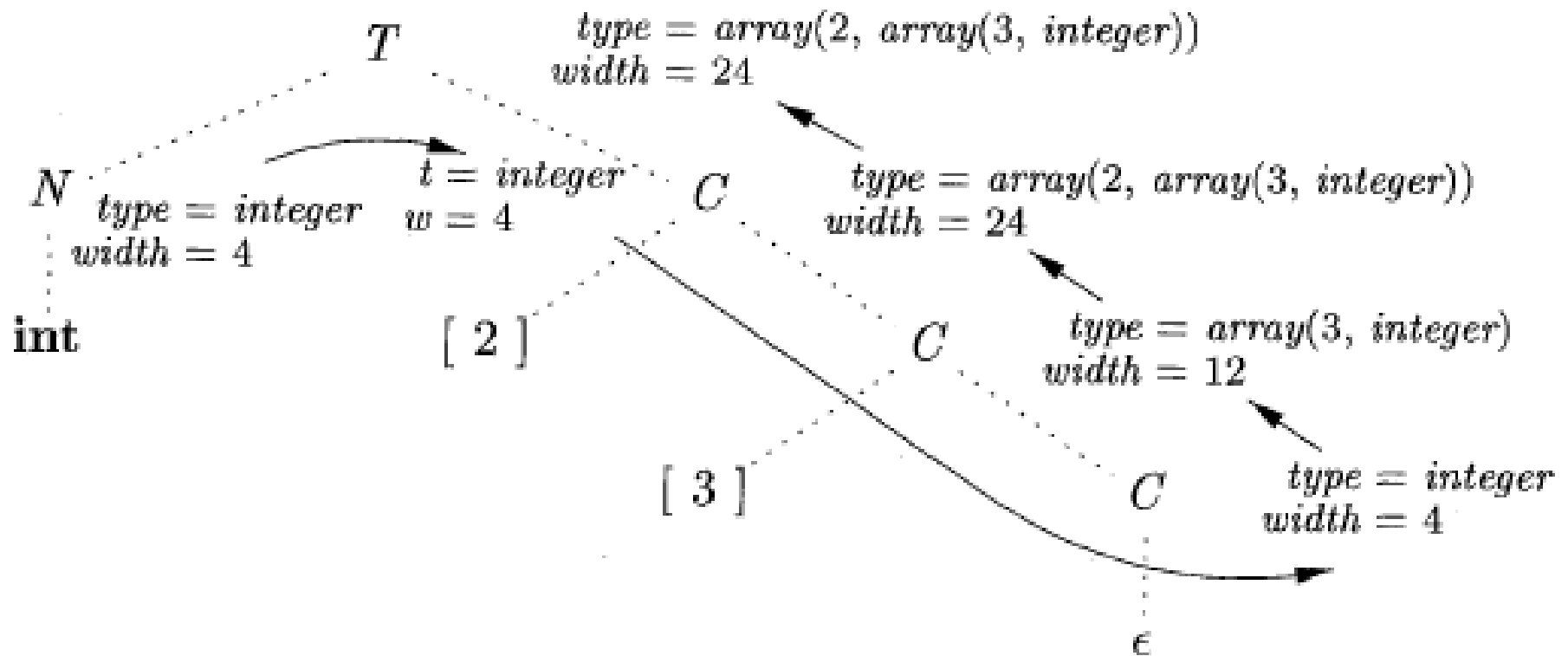
- Suppose that storage comes in blocks of contiguous bytes, where a byte is the smallest unit of addressable memory. Typically, a byte is eight bits, and some number of bytes form a machine word. Multibyte objects are stored in consecutive bytes and given the address of the first byte.
- The *width* of a type is the number of storage units needed for objects of that type. A basic type, such as a character, integer, or float, requires an integral number of bytes. For easy access, storage for aggregates such as arrays and classes is allocated in one contiguous block of bytes.

$$\begin{array}{ll} T \rightarrow \begin{array}{c} B \\ C \end{array} & \{ t = B.type; w = B.width; \} \\ B \rightarrow \text{int} & \{ B.type = integer; B.width = 4; \} \\ B \rightarrow \text{float} & \{ B.type = float; B.width = 8; \} \\ C \rightarrow \epsilon & \{ C.type = t; C.width = w; \} \\ C \rightarrow [\text{num}] C_1 & \{ \text{array}(\text{num.value}, C_1.type); \\ & C.width = \text{num.value} \times C_1.width; \} \end{array}$$

Computing types and their widths

Storage Layout for Local Names

- Syntax-directed translation of array types



Sequences of Declarations

- $$\begin{aligned} P &\rightarrow D \quad \{ \textit{offset} = 0; \} \\ D &\rightarrow T \textit{id} ; \quad \{ \textit{top.put}(\textit{id.lexeme}, T.\textit{type}, \textit{offset}); \\ &\quad \textit{offset} = \textit{offset} + T.\textit{width}; \} \\ D &\rightarrow D_1 \\ D &\rightarrow \epsilon \end{aligned}$$

- Actions at the end:

- $$\begin{aligned} P &\rightarrow M D \\ M &\rightarrow \epsilon \quad \{ \textit{offset} = 0; \} \end{aligned}$$

Fields in Records and Classes

- ```
float x;
record { float x; float y; } p;
record { int tag; float x; float y; } q;
```
- $$\begin{array}{ll} T \rightarrow \text{record } \{ & \{ \text{Env.push}(top); top = \text{new Env}(); \\ & \text{Stack.push}(\text{offset}); \text{offset} = 0; \} \\ D \} & \{ T.type = \text{record}(top); T.width = \text{offset}; \\ & top = \text{Env.pop}(); \text{offset} = \text{Stack.pop}(); \} \end{array}$$



# Translation of Expressions and Statements

- We discussed how to find the types and offset of variables
- We have therefore necessary preparations to discuss about translation to intermediate code
- We also discuss the type checking

# Three-address code for expressions

| PRODUCTION                      | SEMANTIC RULES                                                                                                                |
|---------------------------------|-------------------------------------------------------------------------------------------------------------------------------|
| $S \rightarrow \text{id} = E ;$ | $S.code = E.code \parallel$<br>$gen(top.get(\text{id.lexeme}) \neq E.addr)$                                                   |
| $E \rightarrow E_1 + E_2$       | $E.addr = \text{new Temp}()$<br>$E.code = E_1.code \parallel E_2.code \parallel$<br>$gen(E.addr \neq E_1.addr \neq E_2.addr)$ |
| $  - E_1$                       | $E.addr = \text{new Temp}()$<br>$E.code = E_1.code \parallel$<br>$gen(E.addr \neq \text{'minus'} E_1.addr)$                   |
| $  ( E_1 )$                     | $E.addr = E_1.addr$<br>$E.code = E_1.code$                                                                                    |
| $  \text{id}$                   | $E.addr = top.get(\text{id.lexeme})$<br>$E.code = ''$                                                                         |

# Incremental Translation

$S \rightarrow \text{id} = E ; \quad \{ \text{gen}( \text{top.get}(\text{id.lexeme}) \neq E.\text{addr}); \}$

$E \rightarrow E_1 + E_2 \quad \{ E.\text{addr} = \text{new Temp}();$   
 $\quad \text{gen}(E.\text{addr} \neq E_1.\text{addr} + E_2.\text{addr}); \}$

$| \quad - E_1 \quad \{ E.\text{addr} = \text{new Temp}();$   
 $\quad \text{gen}(E.\text{addr} \neq \text{'minus'} E_1.\text{addr}); \}$

$| \quad ( E_1 ) \quad \{ E.\text{addr} = E_1.\text{addr}; \}$

$| \quad \text{id} \quad \{ E.\text{addr} = \text{top.get}(\text{id.lexeme}); \}$



# Addressing Array Elements

- Layouts for a two-dimensional array:

First row  
Second row

|           |
|-----------|
| $A[1, 1]$ |
| $A[1, 2]$ |
| $A[1, 3]$ |
| $A[2, 1]$ |
| $A[2, 2]$ |
| $A[2, 3]$ |

(a) Row Major

|           |
|-----------|
| $A[1, 1]$ |
| $A[2, 1]$ |
| $A[1, 2]$ |
| $A[2, 2]$ |
| $A[1, 3]$ |
| $A[2, 3]$ |

(b) Column Major

First column  
Second column  
Third column

# Semantic actions for array reference

```

$$\begin{aligned} S &\rightarrow \mathbf{id} = E ; \quad \{ \text{gen}(\text{top.get}(\mathbf{id.lexeme}) \neq E.addr); \} \\ &| L = E ; \quad \{ \text{gen}(L.addr.base '[' L.addr ']' \neq E.addr); \} \\ E &\rightarrow E_1 + E_2 \quad \{ E.addr = \mathbf{new Temp}(); \\ &\quad \text{gen}(E.addr \neq E_1.addr '+' E_2.addr); \} \\ &| \mathbf{id} \quad \{ E.addr = \text{top.get}(\mathbf{id.lexeme}); \} \\ &| L \quad \{ E.addr = \mathbf{new Temp}(); \\ &\quad \text{gen}(E.addr \neq L.array.base '[' L.addr ']); \} \\ L &\rightarrow \mathbf{id} [E] \quad \{ L.array = \text{top.get}(\mathbf{id.lexeme}); \\ &\quad L.type = L.array.type.elem; \\ &\quad L.addr = \mathbf{new Temp}(); \\ &\quad \text{gen}(L.addr \neq E.addr '*' L.type.width); \} \\ &| L_1 [E] \quad \{ L.array = L_1.array; \\ &\quad L.type = L_1.type.elem; \\ &\quad t = \mathbf{new Temp}(); \\ &\quad L.addr = \mathbf{new Temp}(); \\ &\quad \text{gen}(t \neq E.addr '*' L.type.width); \} \\ &\quad \text{gen}(L.addr \neq L_1.addr '+' t); \} \end{aligned}$$

```

# Translation of Array References

Nonterminal  $L$  has three synthesized attributes:

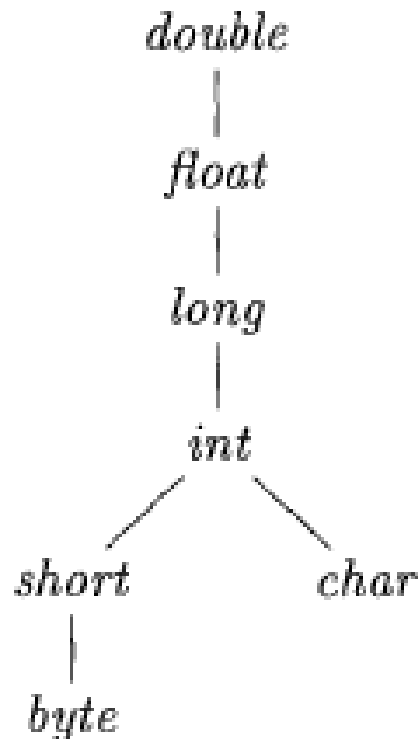
- $L.addr$
- $L.array$
- $L.type$



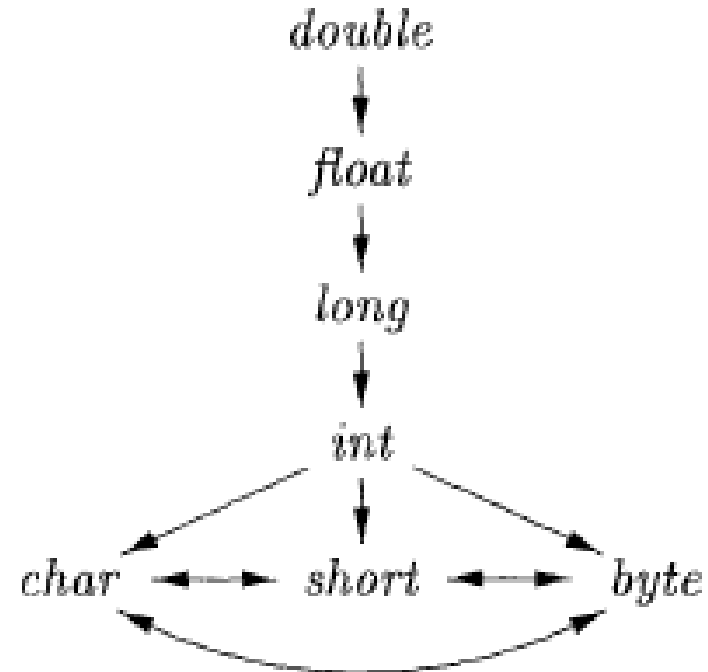


END

# Conversions between primitive types in Java



(a) Widening conversions



(b) Narrowing conversions

# Introducing type conversions into expression evaluation

```

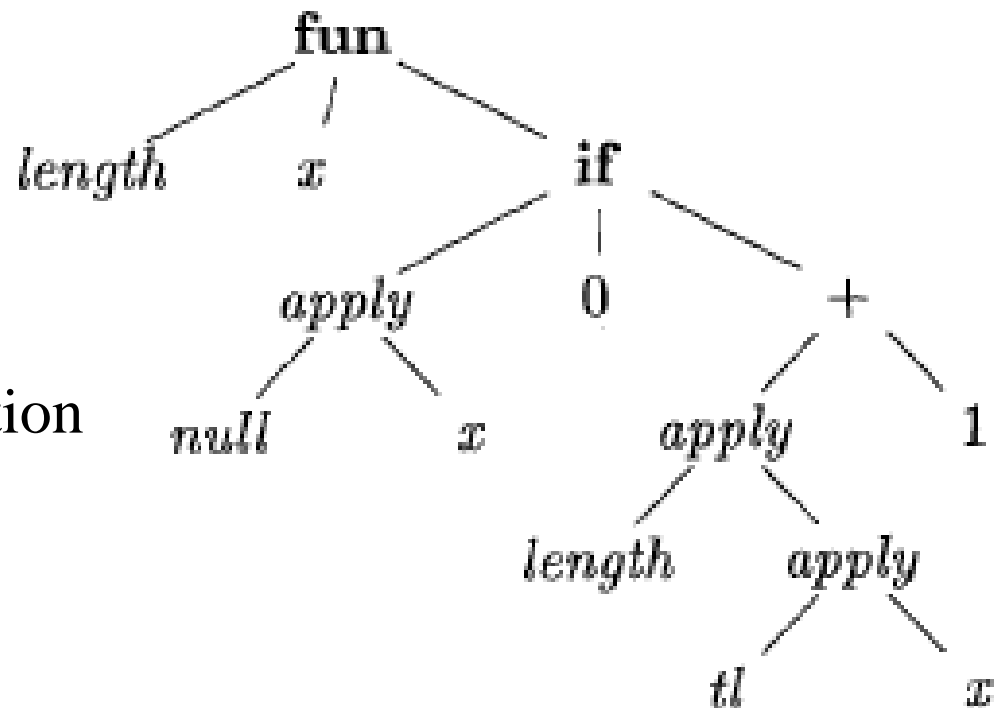
$$E \rightarrow E_1 + E_2 \quad \{ \begin{array}{l} E.type = \max(E_1.type, E_2.type); \\ a_1 = \text{widen}(E_1.addr, E_1.type, E.type); \\ a_2 = \text{widen}(E_2.addr, E_2.type, E.type); \\ E.addr = \text{new Temp}(); \\ \text{gen}(E.addr \text{ '=' } a_1 \text{ '+' } a_2); \end{array} \}$$

```



# Abstract syntax tree for the function definition

fun length(x) =  
 if null(x) then 0 else length(tl(x)+1)



This is a polymorphic function  
in ML language

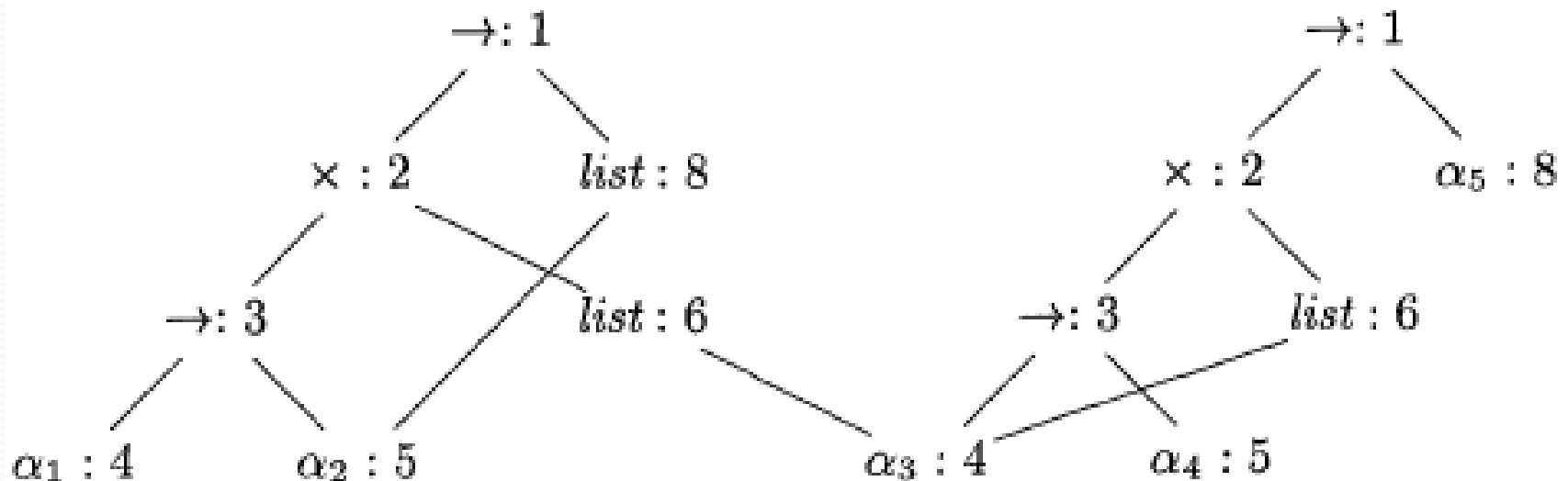
# Inferring a type for the function *length*

| LINE | EXPRESSION : TYPE                                                            | UNIFY                             |
|------|------------------------------------------------------------------------------|-----------------------------------|
| 1)   | $length : \beta \rightarrow \gamma$                                          |                                   |
| 2)   | $x : \beta$                                                                  |                                   |
| 3)   | $\mathbf{if} : boolean \times \alpha_i \times \alpha_i \rightarrow \alpha_i$ |                                   |
| 4)   | $null : list(\alpha_n) \rightarrow boolean$                                  |                                   |
| 5)   | $null(x) : boolean$                                                          | $list(\alpha_n) = \beta$          |
| 6)   | $0 : integer$                                                                | $\alpha_i = integer$              |
| 7)   | $+ : integer \times integer \rightarrow integer$                             |                                   |
| 8)   | $tl : list(\alpha_t) \rightarrow list(\alpha_t)$                             |                                   |
| 9)   | $tl(x) : list(\alpha_t)$                                                     | $list(\alpha_t) = list(\alpha_n)$ |
| 10)  | $length(tl(x)) : \gamma$                                                     | $\gamma = integer$                |
| 11)  | $1 : integer$                                                                |                                   |
| 12)  | $length(tl(x)) + 1 : integer$                                                |                                   |
| 13)  | $\mathbf{if}(\dots) : integer$                                               |                                   |

# Algorithm for Unification

$$((\alpha_1 \rightarrow \alpha_2) \times \text{list}(\alpha_3)) \rightarrow \text{list}(\alpha_2)$$

$$((\alpha_3 \rightarrow \alpha_4) \times \text{list}(\alpha_3)) \rightarrow \alpha_5$$





# Unification algorithm

```
boolean unify (Node m, Node n) {
 s = find(m); t = find(n);
 if (s = t) return true;
 else if (nodes s and t represent the same basic type) return true;
 else if (s is an op-node with children s1 and s2 and
 t is an op-node with children t1 and t2) {
 union(s , t) ;
 return unify(s1, t1) and unify(s2, t2);
 }
 else if s or t represents a variable {
 union(s, t) ;
 return true;
 }
 else return false;
}
```

# Control Flow

boolean expressions are often used to:

- *Alter the flow of control.*
- *Compute logical values.*

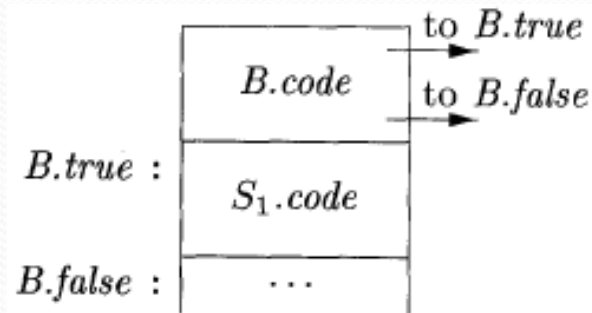
# Short-Circuit Code

- `if ( x < 100 || x > 200 && x != y ) x = 0;`
- - `if x < 100 goto L2`
  - `ifFalse x > 200 goto L1`
  - `ifFalse x != y goto L1`
  - `L2: x = 0`
  - `L1:`

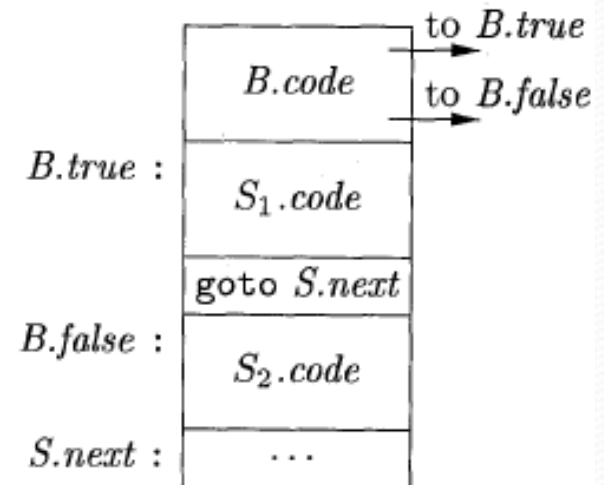


# Flow-of-Control Statements

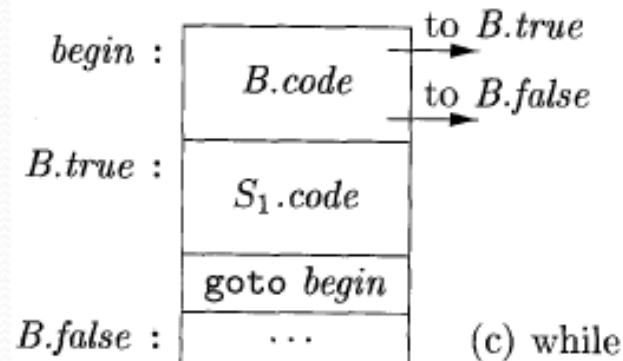
$S \rightarrow \text{if } ( B ) S_1$   
 $S \rightarrow \text{if } ( B ) S_1 \text{ else } S_2$   
 $S \rightarrow \text{while } ( B ) S_1$



(a) if



(b) if-else



(c) while

# Syntax-directed definition

| PRODUCTION                                            | SEMANTIC RULES                                                                                                                                                                                                                            |
|-------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $P \rightarrow S$                                     | $S.next = newlabel()$<br>$P.code = S.code \parallel label(S.next)$                                                                                                                                                                        |
| $S \rightarrow \text{assign}$                         | $S.code = \text{assign.code}$                                                                                                                                                                                                             |
| $S \rightarrow \text{if} ( B ) S_1$                   | $B.true = newlabel()$<br>$B.false = S_1.next = S.next$<br>$S.code = B.code \parallel label(B.true) \parallel S_1.code$                                                                                                                    |
| $S \rightarrow \text{if} ( B ) S_1 \text{ else } S_2$ | $B.true = newlabel()$<br>$B.false = newlabel()$<br>$S_1.next = S_2.next = S.next$<br>$S.code = B.code$<br>$\parallel label(B.true) \parallel S_1.code$<br>$\parallel gen('goto' S.next)$<br>$\parallel label(B.false) \parallel S_2.code$ |
| $S \rightarrow \text{while} ( B ) S_1$                | $begin = newlabel()$<br>$B.true = newlabel()$<br>$B.false = S.next$<br>$S_1.next = begin$<br>$S.code = label(begin) \parallel B.code$<br>$\parallel label(B.true) \parallel S_1.code$<br>$\parallel gen('goto' begin)$                    |
| $S \rightarrow S_1 S_2$                               | $S_1.next = newlabel()$<br>$S_2.next = S.next$<br>$S.code = S_1.code \parallel label(S_1.next) \parallel S_2.code$                                                                                                                        |

# Generating three-address code for booleans

| PRODUCTION                           | SEMANTIC RULES                                                                                                                                                       |
|--------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $B \rightarrow B_1 \parallel B_2$    | $B_1.true = B.true$<br>$B_1.false = newlabel()$<br>$B_2.true = B.true$<br>$B_2.false = B.false$<br>$B.code = B_1.code \parallel label(B_1.false) \parallel B_2.code$ |
| $B \rightarrow B_1 \&\& B_2$         | $B_1.true = newlabel()$<br>$B_1.false = B.false$<br>$B_2.true = B.true$<br>$B_2.false = B.false$<br>$B.code = B_1.code \parallel label(B_1.true) \parallel B_2.code$ |
| $B \rightarrow ! B_1$                | $B_1.true = B.false$<br>$B_1.false = B.true$<br>$B.code = B_1.code$                                                                                                  |
| $B \rightarrow E_1 \text{ rel } E_2$ | $B.code = E_1.code \parallel E_2.code$<br>$\parallel gen('if' E_1.addr \text{ rel } op E_2.addr 'goto' B.true)$<br>$\parallel gen('goto' B.false)$                   |
| $B \rightarrow \text{true}$          | $B.code = gen('goto' B.true)$                                                                                                                                        |
| $B \rightarrow \text{false}$         | $B.code = gen('goto' B.false)$                                                                                                                                       |



# translation of a simple if-statement

- `if( x < 100 || x > 200 && x != y ) x = 0;`

- ```
        if x < 100 goto L2
        goto L3
L3:    if x > 200 goto L4
        goto L1
L4:    if x != y goto L2
        goto L1
L2:    x = 0
L1:
```

Backpatching

- Previous codes for Boolean expressions insert symbolic labels for jumps
- It therefore needs a separate pass to set them to appropriate addresses
- We can use a technique named backpatching to avoid this
- We assume we save instructions into an array and labels will be indices in the array
- For nonterminal B we use two attributes B.truelist and B.falselist together with following functions:
 - makelist(i): create a new list containing only I, an index into the array of instructions
 - Merge(p1,p2): concatenates the lists pointed by p1 and p2 and returns a pointer to the concatenated list
 - Backpatch(p,i): inserts i as the target label for each of the instruction on the list pointed to by p

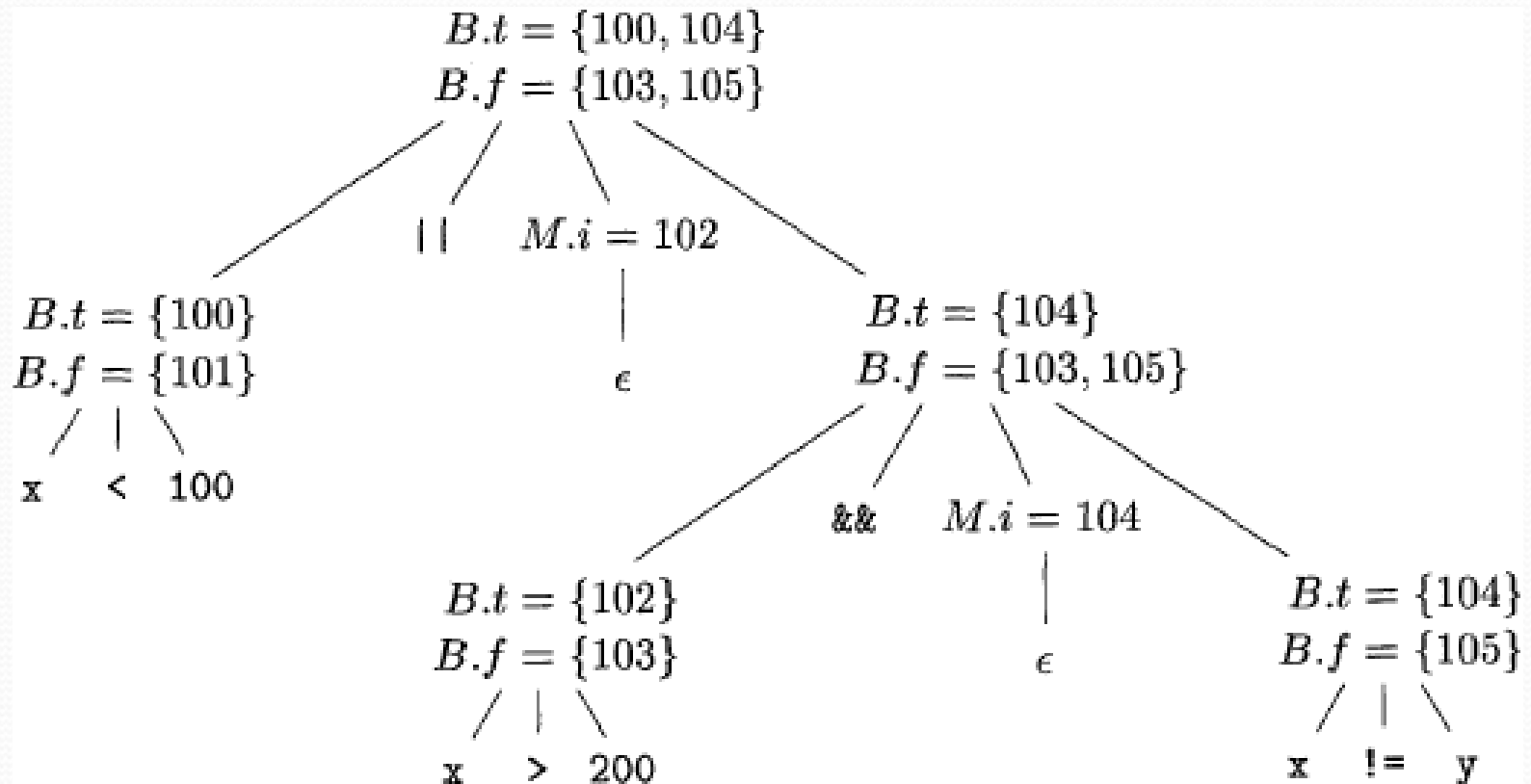
Backpatching for Boolean Expressions

- $B \rightarrow B_1 \mid \mid M B_2 \mid B_1 \&\& M B_2 \mid ! B_1 \mid (B_1) \mid E_1 \text{ rel } E_2 \mid \text{true} \mid \text{false}$
 $M \rightarrow \epsilon$

- 1) $B \rightarrow B_1 \mid \mid M B_2$ { *backpatch*(B_1 .*false*list, M .*instr*);
 B .*true*list = *merge*(B_1 .*true*list, B_2 .*true*list);
 B .*false*list = B_2 .*false*list; }
- 2) $B \rightarrow B_1 \&\& M B_2$ { *backpatch*(B_1 .*true*list, M .*instr*);
 B .*true*list = B_2 .*true*list;
 B .*false*list = *merge*(B_1 .*false*list, B_2 .*false*list); }
- 3) $B \rightarrow ! B_1$ { B .*true*list = B_1 .*false*list;
 B .*false*list = B_1 .*true*list; }
- 4) $B \rightarrow (B_1)$ { B .*true*list = B_1 .*true*list;
 B .*false*list = B_1 .*false*list; }
- 5) $B \rightarrow E_1 \text{ rel } E_2$ { B .*true*list = *makelist*(*nextinstr*);
 B .*false*list = *makelist*(*nextinstr* + 1);
emit('if' E_1 .*addr* *rel.op* E_2 .*addr* 'goto -');
emit('goto -'); }
- 6) $B \rightarrow \text{true}$ { B .*true*list = *makelist*(*nextinstr*);
emit('goto -'); }
- 7) $B \rightarrow \text{false}$ { B .*false*list = *makelist*(*nextinstr*);
emit('goto -'); }
- 8) $M \rightarrow \epsilon$ { M .*instr* = *nextinstr*; }

Backpatching for Boolean Expressions

- Annotated parse tree for $x < 100 \parallel x > 200 \&\& x \neq y$



Flow-of-Control Statements

1) $S \rightarrow \text{if}(B) M S_1 \{ \text{backpatch}(B.\text{truelist}, M.\text{instr});$
 $S.\text{nextlist} = \text{merge}(B.\text{falselist}, S_1.\text{nextlist}); \}$

2) $S \rightarrow \text{if}(B) M_1 S_1 N \text{ else } M_2 S_2$
 $\{ \text{backpatch}(B.\text{truelist}, M_1.\text{instr});$
 $\text{backpatch}(B.\text{falselist}, M_2.\text{instr});$
 $\text{temp} = \text{merge}(S_1.\text{nextlist}, N.\text{nextlist});$
 $S.\text{nextlist} = \text{merge}(\text{temp}, S_2.\text{nextlist}); \}$

3) $S \rightarrow \text{while } M_1 (B) M_2 S_1$
 $\{ \text{backpatch}(S_1.\text{nextlist}, M_1.\text{instr});$
 $\text{backpatch}(B.\text{truelist}, M_2.\text{instr});$
 $S.\text{nextlist} = B.\text{falselist};$
 $\text{emit}(\text{'goto' } M_1.\text{instr}); \}$

$S \rightarrow \text{while } M_1 (B) M_2 S_1$

4) $S \rightarrow \{ L \} \quad \{ S.\text{nextlist} = L.\text{nextlist}; \}$

5) $S \rightarrow A ; \quad \{ S.\text{nextlist} = \text{null}; \}$

6) $M \rightarrow \epsilon \quad \{ M.\text{instr} = \text{nextinstr}; \}$

7) $N \rightarrow \epsilon \quad \{ N.\text{nextlist} = \text{makelist}(\text{nextinstr});$
 $\text{emit}(\text{'goto' } -'); \}$

8) $L \rightarrow L_1 M S \quad \{ \text{backpatch}(L_1.\text{nextlist}, M.\text{instr});$
 $L.\text{nextlist} = S.\text{nextlist}; \}$

9) $L \rightarrow S \quad \{ L.\text{nextlist} = S.\text{nextlist}; \}$

Translation of a switch-statement

<pre> switch (<i>E</i>) { case V_1: S_1 case V_2: S_2 ... case V_{n-1}: S_{n-1} default: S_n } </pre>	<pre> code to evaluate E into t goto test L₁: code for S_1 goto next L₂: code for S_2 goto next ... L_{$n-1$}: code for S_{n-1} goto next L_{n}: code for S_n goto next test: if $t = V_1$ goto L₁ if $t = V_2$ goto L₂ ... if $t = V_{n-1}$ goto L_{$n-1$} goto L_{n} next: </pre>	<pre> code to evaluate E into t if $t \neq V_1$ goto L₁ code for S_1 goto next L₁: if $t \neq V_2$ goto L₂ code for S_2 goto next ... L₂: ... L_{$n-2$}: if $t \neq V_{n-1}$ goto L_{$n-1$} code for S_{n-1} goto next L_{$n-1$}: code for S_n next: </pre>
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Readings

- Chapter 6 of the book