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Semester-2

Section = CSE

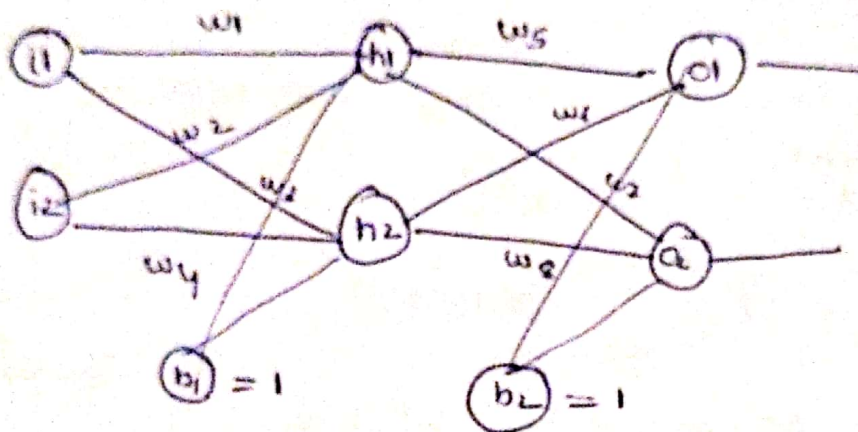
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Assignment = 4



Phase-I Feed Forward Phase

Total net input for h_1

$$\text{net}_{h_1} = w_1 * i_1 + w_2 * i_2 + b_1 * 1$$

$$\text{out}_{h_1} = \frac{1}{1 + e^{-\text{net}_{h_1}}}$$

$$\text{net}_{h_2} = w_3 * i_1 + w_4 * i_2 + b_1 * 1$$

$$\text{out}_{h_2} = \frac{1}{1 + e^{-\text{net}_{h_2}}}$$

$$\text{net}_{o_1} = w_5 * \text{out}_{h_1} + w_6 * \text{out}_{h_2} + b_2 * 1$$

$$\text{out}_{o_1} = \frac{1}{1 + e^{-\text{net}_{o_1}}}$$

$$\text{net } o_2 = w_7 \text{ out } h_1 + w_8 \text{ out } h_2 + b_2 + 1$$

$$\text{out } o_2 = \frac{1}{1 + e^{-\text{net } o_2}}$$

$$E_{\text{total}} = \sum \frac{1}{2} (\text{target} - \text{output})^2$$

$$E_{o_1} = \frac{1}{2} (\text{target } o_1 - \text{out } o_1)^2$$

$$E_{o_2} = \frac{1}{2} (\text{target } o_2 - \text{out } o_2)^2$$

$$E_{\text{total}} = E_{o_1} + E_{o_2}$$

Phase II: Back Propagation of Error ~~and~~ calculate

Phase III Weight & bias updation

$\frac{\partial E_{\text{total}}}{\partial w_5}$ by applying chain rule

$$w_5 (\text{new}) = w_5 (\text{old}) - \eta \left(\frac{\partial E_{\text{total}}}{\partial w_5} \right) \quad [\eta = \text{learning rate}]$$

similarly ~~Partial~~ ~~derivative~~ ~~of~~ ~~error~~ ~~with~~ ~~respect~~ ~~to~~ ~~weight~~ ~~and~~ ~~bias~~

uplating w_1

$$\frac{\partial E_{\text{total}}}{\partial w_1} = \frac{\partial \text{total}}{\partial \text{out } h_1} \times \frac{\partial \text{out } h_1}{\partial \text{net } h_1} \times \frac{\partial \text{net } h_1}{\partial w_1}$$

$$w_1 (\text{new}) = w_1 (\text{old}) - \eta \frac{\partial E_{\text{total}}}{\partial w_1}$$

similarly ~~the~~ ~~derivative~~ ~~of~~ ~~error~~ ~~with~~ ~~respect~~ ~~to~~ ~~weight~~ ~~and~~ ~~bias~~ for w_2, w_3 and w_4

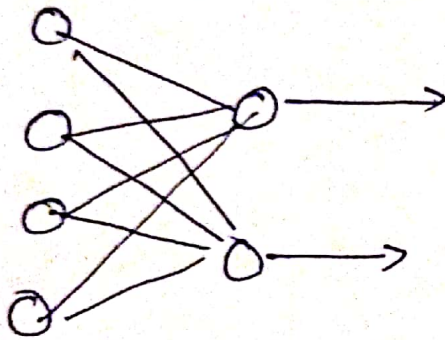
as decomposed as:-

$$\frac{\partial L}{\partial w_{\text{old}}} = \left(\frac{\partial L}{\partial o_2} \right) \left(\frac{\partial o_2}{\partial z_3} \right) \left(\frac{\partial z_3}{\partial w_{\text{old}}} \right)$$

$$\frac{\partial (y - \hat{y})^2}{\partial o_2} = \frac{\partial (y - o_2)^2}{\partial o_2} \quad \frac{\partial (y - \hat{y})^2}{\partial o_2} = \frac{\partial (y - o_2)^2}{\partial o_2} \quad \frac{\partial z_3}{\partial w_{\text{old}}} = \frac{\partial (o_{11} w_5 + o_{12} w_6 + b_2)}{\partial w_{\text{old}}}$$

Single Layer Neural Network model

- Has only 2 layer input layer and output layer
- single layer perceptron
- Activation function used = limiting function
- has connection between input and output layer.
- No hidden layer



input layer

output layer

Activation function: $f(x) = \begin{cases} 0 & x \leq 0 \\ 1 & x > 0 \end{cases}$

where $x = wa + b$

w - weight

a - input

b - bias

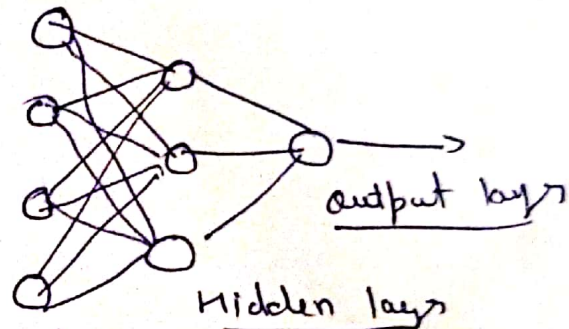
Multi Layer Neural Network model

has more than 2 input and output layer

multi layer perceptron

Activation f^n = sigmoid activation

→ has connection between input and hidden layer, hidden layer and output layer



input layer

sigmoid

Activation function

$$f(x) = \frac{1}{1 + e^{-x}} \begin{cases} 1 & \text{if } f(x) > 0.5 \\ 0 & \text{if } f(x) < 0.5 \end{cases}$$

where $x = wa + b$

w ← weights

a ← input

b ← bias