

1. a) A: Det snør
B: Det blåser

| A B | A ∧ B |
|-----|-------|
| T T | T |
| T F | F |
| F T | F |
| F F | F |

kontingent

b) ~~B~~ $B \vee \neg B$

| B | B ∨ ¬ B |
|---|---------|
| T | T |
| F | T |

tautologi

- c) $(A \rightarrow (A \wedge \neg B))$

| A B | A → (A ∧ ¬ B) |
|-----|---------------|
| T T | F |
| T F | T |
| F T | T |
| F F | T |

kontingent

- d) ~~$(A \wedge B)$~~

$$((A \wedge B) \wedge (\neg A \vee \neg B))$$

| A B | (A ∧ B) ∧ (¬ A ∨ ¬ B) |
|-----|-----------------------|
| T T | F |
| T F | F |
| F T | F |
| F F | F |

kontradiksjon

- e) A: Det er godt
B: Vi strør fortanet

$$(A \wedge (B \rightarrow \neg A))$$

| A B | A ∧ (B → ¬ A) |
|-----|---------------|
| T T | F |
| T F | T |
| F T | F |
| F F | T |

kontingent

2. a) $(A \wedge \neg A) \Leftrightarrow (A \rightarrow A)$?

| A | $A \wedge \neg A$ | $A \rightarrow A$ |
|---|-------------------|-------------------|
| T | F | T |
| F | F | T |

ikke ekvivalente.

b) $(A \rightarrow B) \Leftrightarrow (\neg A \vee B)$?

| A | B | $A \rightarrow B$ | $\neg A \vee B$ |
|---|---|-------------------|-----------------|
| T | T | T | T |
| T | F | F | F |
| F | T | T | T |
| F | F | T | T |

ekvivalente

c) $(A \wedge (B \wedge C)) \Leftrightarrow (A \rightarrow (B \rightarrow \neg C))$?

| A | B | C | $A \wedge (B \wedge C)$ | $A \rightarrow (B \rightarrow \neg C)$ |
|---|---|---|-------------------------|--|
| T | T | T | T | F |
| T | T | F | F | T |
| T | F | T | F | T |
| T | F | F | F | T |
| F | T | T | F | T |
| F | T | F | F | T |
| F | F | T | F | T |
| F | F | F | F | T |

ikke ekvivalente

d) $(A \rightarrow (B \vee C)) \Leftrightarrow (\neg A \vee (\neg B \rightarrow C))$

| A | B | C | $A \rightarrow (B \vee C)$ | $\neg A \vee (\neg B \rightarrow C)$ |
|---|---|---|----------------------------|--------------------------------------|
| T | T | T | T | T |
| T | T | F | T | T |
| T | F | T | T | T |
| T | F | F | F | F |
| F | T | T | T | T |
| F | T | F | T | T |
| F | F | T | T | T |
| F | F | F | T | T |

ekvivalente

3 a) $A \rightarrow B$
 A
 $\therefore B$

| AB | $A \rightarrow B$ |
|----|-------------------|
| TT | T |
| TF | F |
| FT | T |
| FF | T |

← gyldig

b) $A \vee B$
 $\neg A$
 $\therefore B$

| AB | $A \vee B$ | $\neg A$ |
|----|------------|----------|
| TT | T | F |
| TF | T | F |
| FT | T | T |
| FF | F | T |

← gyldig

c) B
 $B \rightarrow A$
 $\therefore \neg \neg A$

| AB | $B \rightarrow A$ | $\neg \neg A$ |
|----|-------------------|---------------|
| TT | T | TF |
| TF | T | TF |
| FT | F | FT |
| FF | T | FT |

← gyldig

d) $A \vee \neg A$
 $A \rightarrow B$
 $\neg A \rightarrow B$
 $\therefore B$

| AB | $A \vee \neg A$ | $A \rightarrow B$ | $\neg A \rightarrow B$ |
|----|-----------------|-------------------|------------------------|
| TT | TF | T | F T |
| TF | TF | F | F T |
| FT | TT | T | T T |
| FF | TT | T | T F |

← gyldig

e) A
 $\neg(A \wedge \neg B)$
 $\therefore B$

| AB | $\neg(A \wedge \neg B)$ |
|----|-------------------------|
| TT | T FF |
| TF | F TT |
| FT | T FF |
| FF | T FT |

← gyldig

f) gyldig, men gyldigheten kan ikke bevistes i setningslogik.

| ABC |
|-----|
| TTT |
| TTF |
| ... |
| ... |
| ... |
| ... |
| ... |

4. a) $(A \vee B)$
 $\neg B$
 $\therefore (A \rightarrow B)$

| AB | $A \vee B$ | $\neg B$ | $A \rightarrow B$ |
|-----|------------|----------|-------------------|
| T T | T | F | T |
| T F | T | T | F |
| F T | T | F | T |
| F F | F | T | T |

← ikke gyldig

b) $(\neg A \rightarrow B)$
 $\therefore (A \rightarrow B)$

| AB | $\neg A \rightarrow B$ | $A \rightarrow B$ |
|-----|------------------------|-------------------|
| T T | F T | T |
| T F | F T | F |
| F T | T T | T |
| F F | T F | T |

← ikke gyldig

c) $(A \rightarrow B)$
 $(B \rightarrow C)$
 $\neg C$
 $\therefore \neg A$

| ABC | $A \rightarrow B$ | $B \rightarrow C$ | $\neg C$ | $\neg A$ |
|-------|-------------------|-------------------|----------|----------|
| T T T | T | T | F | F |
| T T F | T | F | T | F |
| T F T | F | T | F | F |
| T F F | F | T | T | F |
| F T T | T | T | F | T |
| F T F | T | F | T | T |
| F F T | T | T | F | T |
| F F F | T | T | T | T |

← gyldig

5. a) ~~$(A \vee ((A \wedge B) \vee \neg(A \vee B)))$~~ ikke tautologi

| ABC | $(A \wedge B) \vee \neg(A \vee B)$ |
|-----|------------------------------------|
| T F | T F F |
| F F | F F T T F |

b) ~~$((A \rightarrow B) \wedge \neg(A \wedge B))$~~ ikke kontradiksjon

| AB | $(A \rightarrow B) \wedge \neg(A \wedge B)$ |
|-----|---|
| F F | F T F T F F F |

c) ~~$(A \leftrightarrow B) \Leftrightarrow (\neg A \wedge \neg B)$~~

| AB | $A \leftrightarrow B$ | $\neg A \wedge \neg B$ |
|-----|-----------------------|------------------------|
| T T | T T T | F T F F T |

d) ~~$((A \vee B) \rightarrow (C \wedge \neg B))$~~
 ~~$(\neg C \rightarrow (A \vee (\neg B \rightarrow \neg A)))$~~
 ~~$\therefore C$~~

| ABC |
|-------|
| T T T |
| T T F |
| T F T |
| T F F |
| F T T |
| F T F |
| F F T |
| F F F |

← gyldig

~~$ABC | (A \vee B) \rightarrow (C \wedge \neg B) | \neg C \rightarrow$~~

5.

a) $\neq ((A \wedge B) \vee \neg(A \vee B))$

| AB | $(A \wedge B)$ | \vee | $\neg(A \vee B)$ |
|----|----------------|--------|------------------|
| TF | F | F | T |
| TF | F | F | T |
| TF | F | F | T |

\equiv

b) $((A \rightarrow B) \wedge \neg(A \wedge B)) \neq \perp$

| AB | $(A \rightarrow B)$ | \wedge | $\neg(A \wedge B)$ |
|----|---------------------|----------|--------------------|
| FF | T | T | T |
| FF | T | T | T |
| FF | T | T | T |

\equiv

c) $(A \leftrightarrow B) \not\leftrightarrow (\neg A \wedge \neg B)$

| AB | $A \leftrightarrow B$ | $\neg A \wedge \neg B$ |
|----|-----------------------|------------------------|
| TT | T | F |
| TT | T | F |
| TT | T | F |

\equiv

d) $((A \vee B) \rightarrow (C \vee B))$
 $(\neg C \rightarrow (A \wedge (\neg B \rightarrow \neg A)))$

i. C

ikke gyldig

| ABC | $(A \vee B) \rightarrow (C \vee B)$ | $\neg C \rightarrow (A \wedge (\neg B \rightarrow \neg A))$ |
|-----|-------------------------------------|---|
| TTT | T | T |
| TTT | T | T |
| TTT | T | T |

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