

a)

1	$A \wedge B$	PR
2	B	$\wedge E 1$

b)

1	A	PR
2	$A \vee B$	$\vee I 1$

c)

1	$C \wedge (B \rightarrow \neg F)$	PR
2	C	$\wedge E 1$

d)

1	$A \wedge B$	PR
2	A	$\wedge E 1$
3	B	$\wedge E 1$
4	$B \wedge A$	$\wedge I 2,3$

e)

1	$A \vee B$	PR
2	A	AS
3	$A \vee B$	$\vee I 2$
4	B	AS
5	$A \vee B$	$\vee I 4$
6	$A \vee B$	$\vee E 1,2,3,4,5$

f)

1	$(A \wedge C) \vee (B \wedge A)$	PR
2	$A \wedge C$	AS
3	A	$\wedge E 2$
4	$B \wedge A$	AS
5	A	$\wedge E 4$
6	A	$\vee E 1,2,3,4,5$

g)

1	$A \rightarrow B$	PR
2	$B \rightarrow C$	PR
3	A	AS
4	B	$\rightarrow E 1,3$
5	C	$\rightarrow E 2,4$
6	$A \rightarrow C$	$\rightarrow I 3-5$

h)

1	A	PR
2	$A \rightarrow B$	PR
3	B	$\rightarrow E 1,2$
4	$B \vee C$	$\vee I 3$

i)

1	$A \leftrightarrow B$	PR
2	A	AS
3	B	$\leftrightarrow E 1,2$
4	B	AS
5	A	$\leftrightarrow E 1,4$
6	$B \leftrightarrow A$	$\leftrightarrow I 1,2,3,4,5$

j)

1	$A \leftrightarrow (B \wedge C)$	PR
2	C	PR
3	$B \wedge D$	PR
4	B	$\wedge E 3$
5	$B \wedge C$	$\wedge I 2,4$
6	A	$\leftrightarrow E 1,5$

k)

1	$(A \vee B) \rightarrow C$	PR
2	$A \wedge D$	PR
3	$A$	$\wedge E 2$
4	$A \vee B$	$\vee I 3$
5	$C$	$\rightarrow E 1, 4$

l)

1	$(A \vee B) \rightarrow C$	PR
2	$A$	AS
3	$B$	AS
4	$A \wedge B$	$\wedge I 2, 3$
5	$C$	$\rightarrow E 1, 4$
6	$B \rightarrow C$	$\rightarrow I 3-5$
7	$A \rightarrow (B \rightarrow C)$	$\rightarrow I 2-6$

m)

1	$B \rightarrow A$	PR
2	$B \vee (D \wedge E)$	PR
3	$D \rightarrow A$	PR
4	$B$	AS
5	$A$	$\rightarrow E 4, 1$
6	$D \wedge E$	AS
7	$D$	$\wedge E 6$
8	$A$	$\rightarrow E 3, 7$
9	$A$	$\vee E 2, 4-5, 6-8$
10	$A \vee E$	$\vee I 9$

n)

1	$(A \rightarrow B) \vee (A \rightarrow C)$	PR
2	$A$	AS
3	$A \rightarrow B$	AS
4	$B$	$\rightarrow E 2, 3$
5	$B \vee C$	$\vee I 4$
6	$A \rightarrow C$	AS
7	$C$	$\rightarrow E 2, 6$
8	$B \vee C$	$\vee I 7$
9	$B \vee C$	$\vee E 1, 3-5, 6-8$
10	$A \rightarrow (B \vee C)$	$\rightarrow I 2-9$