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# Simple random sampling

Type I errors (n = 500)

|                                |           |           |           | Re    | jection r | ate   |
|--------------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                           | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                          |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 2         | 0.091 | 0.059     | 0.009 |
| $\operatorname{WaldVCF}$       | 1000      | 1000      | 2         | 0.090 | 0.058     | 0.009 |
| WaldDiag,MM3                   | 1000      | 1000      | 2         | 0.075 | 0.034     | 0.008 |
| Pearson,MM3                    | 1000      | 1000      | 2         | 0.095 | 0.048     | 0.013 |
| RSS,MM3                        | 1000      | 1000      | 2         | 0.096 | 0.046     | 0.013 |
| $\mathrm{Multn}, \mathrm{MM3}$ | 1000      | 1000      | 2         | 0.090 | 0.056     | 0.009 |
| 1F 8V                          |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 1         | 0.098 | 0.053     | 0.014 |
| $\operatorname{WaldVCF}$       | 1000      | 1000      | 1         | 0.095 | 0.051     | 0.014 |
| WaldDiag,MM3                   | 1000      | 1000      | 1         | 0.051 | 0.026     | 0.000 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.099 | 0.047     | 0.012 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.097 | 0.052     | 0.012 |
| Multn, MM3                     | 1000      | 1000      | 1         | 0.085 | 0.046     | 0.014 |
| 1F 15V                         |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 1         | 0.106 | 0.051     | 0.013 |
| $\operatorname{WaldVCF}$       | 1000      | 1000      | 1         | 0.106 | 0.051     | 0.013 |
| WaldDiag,MM3                   | 1000      | 1000      | 1         | 0.092 | 0.051     | 0.007 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.098 | 0.047     | 0.012 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.099 | 0.049     | 0.011 |
| Multn, MM3                     | 1000      | 1000      | 1         | 0.104 | 0.051     | 0.012 |
| 2F 10V                         |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 1         | 0.100 | 0.056     | 0.012 |
| $\operatorname{WaldVCF}$       | 1000      | 1000      | 1         | 0.100 | 0.054     | 0.012 |
| WaldDiag,MM3                   | 1000      | 1000      | 1         | 0.055 | 0.025     | 0.003 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.092 | 0.054     | 0.016 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.095 | 0.061     | 0.015 |
| Multn, MM3                     | 1000      | 1000      | 1         | 0.098 | 0.051     | 0.012 |
| 3F 15V                         |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 23        | 0.116 | 0.068     | 0.009 |
| WaldVCF                        | 1000      | 1000      | 23        | 0.114 | 0.066     | 0.008 |
| WaldDiag,MM3                   | 1000      | 1000      | 23        | 0.094 | 0.046     | 0.008 |
| Pearson,MM3                    | 1000      | 1000      | 23        | 0.111 | 0.050     | 0.007 |
| RSS,MM3                        | 1000      | 1000      | 23        | 0.117 | 0.056     | 0.007 |
| Multn,MM3                      | 1000      | 1000      | 23        | 0.114 | 0.066     | 0.008 |

Type I errors (n = 1000)

|                          |           |           |           | Re    | jection r | ate   |
|--------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                     | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                    |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 1         | 0.094 | 0.044     | 0.011 |
| WaldVCF                  | 1000      | 1000      | 1         | 0.093 | 0.044     | 0.010 |
| ${\it WaldDiag,MM3}$     | 1000      | 1000      | 1         | 0.055 | 0.023     | 0.002 |
| Pearson,MM3              | 1000      | 1000      | 1         | 0.083 | 0.038     | 0.006 |
| RSS,MM3                  | 1000      | 1000      | 1         | 0.085 | 0.037     | 0.007 |
| Multn,MM3                | 1000      | 1000      | 1         | 0.087 | 0.040     | 0.008 |
| 1F 8V                    |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 2         | 0.091 | 0.047     | 0.017 |
| WaldVCF                  | 1000      | 1000      | 2         | 0.088 | 0.047     | 0.01' |
| WaldDiag,MM3             | 1000      | 1000      | 2         | 0.065 | 0.031     | 0.008 |
| Pearson,MM3              | 1000      | 1000      | 2         | 0.087 | 0.042     | 0.009 |
| RSS,MM3                  | 1000      | 1000      | 2         | 0.087 | 0.045     | 0.012 |
| Multn, MM3               | 1000      | 1000      | 2         | 0.087 | 0.045     | 0.01' |
| 1F 15V                   |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 10        | 0.094 | 0.044     | 0.006 |
| $\operatorname{WaldVCF}$ | 1000      | 1000      | 10        | 0.093 | 0.041     | 0.00! |
| WaldDiag,MM3             | 1000      | 1000      | 10        | 0.068 | 0.028     | 0.003 |
| Pearson,MM3              | 1000      | 1000      | 10        | 0.082 | 0.033     | 0.003 |
| RSS,MM3                  | 1000      | 1000      | 10        | 0.074 | 0.036     | 0.004 |
| Multn,MM3                | 1000      | 1000      | 10        | 0.092 | 0.041     | 0.00  |
| 2F 10V                   |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 11        | 0.096 | 0.050     | 0.009 |
| WaldVCF                  | 1000      | 1000      | 11        | 0.092 | 0.044     | 0.009 |
| WaldDiag,MM3             | 1000      | 1000      | 11        | 0.045 | 0.024     | 0.003 |
| Pearson,MM3              | 1000      | 1000      | 11        | 0.100 | 0.044     | 0.000 |
| RSS,MM3                  | 1000      | 1000      | 11        | 0.092 | 0.046     | 0.00! |
| Multn,MM3                | 1000      | 1000      | 11        | 0.088 | 0.039     | 0.009 |
| 3F 15V                   |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 31        | 0.110 | 0.052     | 0.008 |
| WaldVCF                  | 1000      | 1000      | 31        | 0.101 | 0.045     | 0.000 |
| WaldDiag,MM3             | 1000      | 1000      | 31        | 0.059 | 0.027     | 0.00  |
| Pearson,MM3              | 1000      | 1000      | 31        | 0.094 | 0.047     | 0.00  |
| RSS,MM3                  | 1000      | 1000      | 31        | 0.093 | 0.045     | 0.00  |
| m Multn, MM3             | 1000      | 1000      | 31        | 0.091 | 0.043     | 0.00  |

#### Type I errors (n = 2000)

|        |      |           |           |           | Reje | Rejection rate |    |  |
|--------|------|-----------|-----------|-----------|------|----------------|----|--|
| $\sin$ | Name | No. repl. | Converged | Rank def. | 10%  | 5%             | 1% |  |

|        |      |           |           |           | Reje | Rejection rate |    |  |
|--------|------|-----------|-----------|-----------|------|----------------|----|--|
| $\sin$ | Name | No. repl. | Converged | Rank def. | 10%  | 5%             | 1% |  |

Type I errors (n = 5000)

|                          |           |           |           | Re    | ejection r | ate   |
|--------------------------|-----------|-----------|-----------|-------|------------|-------|
| Name                     | No. repl. | Converged | Rank def. | 10%   | 5%         | 1%    |
| 1F 5V                    |           |           |           |       |            |       |
| Wald                     | 1000      | 1000      | 1         | 0.096 | 0.049      | 0.006 |
| WaldVCF                  | 1000      | 1000      | 1         | 0.093 | 0.047      | 0.006 |
| ${\bf WaldDiag, MM3}$    | 1000      | 1000      | 1         | 0.080 | 0.032      | 0.007 |
| Pearson,MM3              | 1000      | 1000      | 1         | 0.084 | 0.042      | 0.005 |
| RSS,MM3                  | 1000      | 1000      | 1         | 0.086 | 0.045      | 0.005 |
| Multn,MM3                | 1000      | 1000      | 1         | 0.092 | 0.047      | 0.006 |
| 1F 8V                    |           |           |           |       |            |       |
| Wald                     | 1000      | 1000      | 1         | 0.092 | 0.046      | 0.006 |
| WaldVCF                  | 1000      | 1000      | 1         | 0.092 | 0.045      | 0.004 |
| WaldDiag,MM3             | 1000      | 1000      | 1         | 0.073 | 0.041      | 0.009 |
| Pearson,MM3              | 1000      | 1000      | 1         | 0.090 | 0.042      | 0.007 |
| RSS,MM3                  | 1000      | 1000      | 1         | 0.093 | 0.043      | 0.010 |
| Multn,MM3                | 1000      | 1000      | 1         | 0.092 | 0.045      | 0.004 |
| 1F 15V                   |           |           |           |       |            |       |
| Wald                     | 1000      | 1000      | 17        | 0.113 | 0.048      | 0.005 |
| $\operatorname{WaldVCF}$ | 1000      | 1000      | 17        | 0.109 | 0.045      | 0.005 |
| WaldDiag,MM3             | 1000      | 1000      | 17        | 0.099 | 0.048      | 0.004 |
| Pearson,MM3              | 1000      | 1000      | 17        | 0.099 | 0.050      | 0.004 |
| RSS,MM3                  | 1000      | 1000      | 17        | 0.105 | 0.049      | 0.003 |
| Multn,MM3                | 1000      | 1000      | 17        | 0.109 | 0.045      | 0.005 |
| 2F 10V                   |           |           |           |       |            |       |
| Wald                     | 1000      | 1000      | 25        | 0.115 | 0.058      | 0.014 |
| WaldVCF                  | 1000      | 1000      | 25        | 0.107 | 0.054      | 0.014 |
| WaldDiag,MM3             | 1000      | 1000      | 25        | 0.098 | 0.045      | 0.007 |
| Pearson,MM3              | 1000      | 1000      | 25        | 0.092 | 0.038      | 0.006 |
| RSS,MM3                  | 1000      | 1000      | 25        | 0.088 | 0.042      | 0.006 |
| Multn,MM3                | 1000      | 1000      | 25        | 0.106 | 0.053      | 0.013 |
| 3F 15V                   |           |           |           |       |            |       |
| Wald                     | 1000      | 1000      | 56        | 0.098 | 0.049      | 0.010 |
| WaldVCF                  | 1000      | 1000      | 56        | 0.087 | 0.043      | 0.008 |
| WaldDiag,MM3             | 1000      | 1000      | 56        | 0.080 | 0.041      | 0.006 |
| Pearson,MM3              | 1000      | 1000      | 56        | 0.097 | 0.043      | 0.013 |
| RSS,MM3                  | 1000      | 1000      | 56        | 0.101 | 0.042      | 0.012 |
| Multn,MM3                | 1000      | 1000      | 56        | 0.087 | 0.042      | 0.007 |

**Type I errors** (n = 10000)

|                             |           |           |           | Re    | jection r | ate   |
|-----------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                        | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 2         | 0.093 | 0.057     | 0.010 |
| WaldVCF                     | 1000      | 1000      | 2         | 0.092 | 0.056     | 0.010 |
| WaldDiag,MM3                | 1000      | 1000      | 2         | 0.088 | 0.049     | 0.009 |
| Pearson,MM3                 | 1000      | 1000      | 2         | 0.105 | 0.053     | 0.013 |
| RSS,MM3                     | 1000      | 1000      | 2         | 0.101 | 0.056     | 0.012 |
| Multn,MM3                   | 1000      | 1000      | 2         | 0.092 | 0.056     | 0.010 |
| 1F 8V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 5         | 0.103 | 0.055     | 0.013 |
| WaldVCF                     | 1000      | 1000      | 5         | 0.102 | 0.055     | 0.013 |
| WaldDiag,MM3                | 1000      | 1000      | 5         | 0.092 | 0.046     | 0.010 |
| Pearson,MM3                 | 1000      | 1000      | 5         | 0.112 | 0.059     | 0.015 |
| RSS,MM3                     | 1000      | 1000      | 5         | 0.104 | 0.055     | 0.015 |
| Multn, MM3                  | 1000      | 1000      | 5         | 0.100 | 0.054     | 0.013 |
| 1F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 37        | 0.106 | 0.054     | 0.011 |
| WaldVCF                     | 1000      | 1000      | 37        | 0.104 | 0.053     | 0.010 |
| WaldDiag,MM3                | 1000      | 1000      | 37        | 0.117 | 0.062     | 0.013 |
| Pearson,MM3                 | 1000      | 1000      | 37        | 0.091 | 0.049     | 0.011 |
| RSS,MM3                     | 1000      | 1000      | 37        | 0.094 | 0.047     | 0.013 |
| Multn,MM3                   | 1000      | 1000      | 37        | 0.104 | 0.053     | 0.010 |
| 2F 10V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 24        | 0.115 | 0.060     | 0.015 |
| WaldVCF                     | 1000      | 1000      | 24        | 0.108 | 0.059     | 0.011 |
| ${\bf WaldDiag,} {\bf MM3}$ | 1000      | 1000      | 24        | 0.104 | 0.052     | 0.010 |
| Pearson,MM3                 | 1000      | 1000      | 24        | 0.106 | 0.051     | 0.015 |
| RSS,MM3                     | 1000      | 1000      | 24        | 0.104 | 0.053     | 0.015 |
| Multn,MM3                   | 1000      | 1000      | 24        | 0.108 | 0.058     | 0.011 |
| 3F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 97        | 0.106 | 0.052     | 0.007 |
| WaldVCF                     | 1000      | 1000      | 97        | 0.088 | 0.043     | 0.006 |
| ${\it WaldDiag,MM3}$        | 1000      | 1000      | 97        | 0.082 | 0.039     | 0.009 |
| Pearson,MM3                 | 1000      | 1000      | 97        | 0.091 | 0.045     | 0.011 |
| RSS,MM3                     | 1000      | 1000      | 97        | 0.090 | 0.043     | 0.008 |
| Multn,MM3                   | 1000      | 1000      | 97        | 0.087 | 0.042     | 0.006 |

Power (n = 500)

|                                |           |           |           | Re    | ejection r | ate   |
|--------------------------------|-----------|-----------|-----------|-------|------------|-------|
| Name                           | No. repl. | Converged | Rank def. | 10%   | 5%         | 1%    |
| 1F 5V                          |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 1         | 0.891 | 0.827      | 0.671 |
| WaldVCF                        | 1000      | 1000      | 1         | 0.890 | 0.827      | 0.670 |
| WaldDiag,MM3                   | 1000      | 1000      | 1         | 0.808 | 0.709      | 0.425 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.902 | 0.844      | 0.688 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.918 | 0.854      | 0.712 |
| Multn,MM3                      | 1000      | 1000      | 1         | 0.890 | 0.826      | 0.668 |
| 1F 8V                          |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 0         | 0.334 | 0.228      | 0.081 |
| WaldVCF                        | 1000      | 1000      | 0         | 0.332 | 0.225      | 0.079 |
| WaldDiag,MM3                   | 1000      | 1000      | 0         | 0.154 | 0.061      | 0.007 |
| Pearson,MM3                    | 1000      | 1000      | 0         | 0.354 | 0.220      | 0.069 |
| RSS,MM3                        | 1000      | 1000      | 0         | 0.357 | 0.236      | 0.075 |
| Multn,MM3                      | 1000      | 1000      | 0         | 0.317 | 0.203      | 0.058 |
| 1F 15V                         |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 5         | 1.000 | 0.999      | 0.996 |
| $\operatorname{WaldVCF}$       | 1000      | 1000      | 5         | 1.000 | 0.999      | 0.996 |
| WaldDiag,MM3                   | 1000      | 1000      | 5         | 0.998 | 0.995      | 0.966 |
| Pearson,MM3                    | 1000      | 1000      | 5         | 0.980 | 0.955      | 0.831 |
| RSS,MM3                        | 1000      | 1000      | 5         | 0.994 | 0.985      | 0.946 |
| Multn,MM3                      | 1000      | 1000      | 5         | 1.000 | 0.998      | 0.996 |
| 2F 10V                         |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 1         | 0.622 | 0.506      | 0.286 |
| WaldVCF                        | 1000      | 1000      | 1         | 0.617 | 0.503      | 0.283 |
| WaldDiag,MM3                   | 1000      | 1000      | 1         | 0.401 | 0.266      | 0.083 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.373 | 0.240      | 0.077 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.441 | 0.322      | 0.129 |
| Multn,MM3                      | 1000      | 1000      | 1         | 0.616 | 0.497      | 0.279 |
| 3F 15V                         |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 11        | 0.995 | 0.990      | 0.957 |
| WaldVCF                        | 1000      | 1000      | 11        | 0.995 | 0.988      | 0.956 |
| WaldDiag,MM3                   | 1000      | 1000      | 11        | 0.983 | 0.968      | 0.871 |
| Pearson,MM3                    | 1000      | 1000      | 11        | 1.000 | 0.998      | 0.995 |
| RSS,MM3                        | 1000      | 1000      | 11        | 1.000 | 1.000      | 0.994 |
| $\mathrm{Multn}, \mathrm{MM3}$ | 1000      | 1000      | 11        | 0.995 | 0.988      | 0.956 |

Power (n = 1000)

|                             |           |           |           | Re    | Rejection rate |       |  |
|-----------------------------|-----------|-----------|-----------|-------|----------------|-------|--|
| Name                        | No. repl. | Converged | Rank def. | 10%   | 5%             | 1%    |  |
| 1F 5V                       |           |           |           |       |                |       |  |
| Wald                        | 1000      | 1000      | 0         | 0.511 | 0.382          | 0.203 |  |
| WaldVCF                     | 1000      | 1000      | 0         | 0.508 | 0.382          | 0.203 |  |
| ${\bf WaldDiag,} {\bf MM3}$ | 1000      | 1000      | 0         | 0.342 | 0.221          | 0.076 |  |
| Pearson,MM3                 | 1000      | 1000      | 0         | 0.545 | 0.422          | 0.229 |  |
| RSS,MM3                     | 1000      | 1000      | 0         | 0.560 | 0.428          | 0.244 |  |
| Multn,MM3                   | 1000      | 1000      | 0         | 0.497 | 0.374          | 0.194 |  |
| 1F 8V                       |           |           |           |       |                |       |  |
| Wald                        | 1000      | 1000      | 1         | 0.904 | 0.832          | 0.658 |  |
| WaldVCF                     | 1000      | 1000      | 1         | 0.901 | 0.831          | 0.657 |  |
| ${\it WaldDiag,MM3}$        | 1000      | 1000      | 1         | 0.768 | 0.653          | 0.374 |  |
| Pearson,MM3                 | 1000      | 1000      | 1         | 0.629 | 0.474          | 0.224 |  |
| RSS,MM3                     | 1000      | 1000      | 1         | 0.762 | 0.639          | 0.365 |  |
| Multn,MM3                   | 1000      | 1000      | 1         | 0.898 | 0.827          | 0.655 |  |
| 1F 15V                      |           |           |           |       |                |       |  |
| Wald                        | 1000      | 1000      | 8         | 0.731 | 0.598          | 0.368 |  |
| WaldVCF                     | 1000      | 1000      | 8         | 0.721 | 0.586          | 0.360 |  |
| WaldDiag,MM3                | 1000      | 1000      | 8         | 0.575 | 0.433          | 0.224 |  |
| Pearson,MM3                 | 1000      | 1000      | 8         | 0.877 | 0.792          | 0.592 |  |
| RSS,MM3                     | 1000      | 1000      | 8         | 0.877 | 0.776          | 0.581 |  |
| Multn,MM3                   | 1000      | 1000      | 8         | 0.720 | 0.582          | 0.361 |  |
| 2F 10V                      |           |           |           |       |                |       |  |
| Wald                        | 1000      | 1000      | 5         | 0.346 | 0.240          | 0.095 |  |
| WaldVCF                     | 1000      | 1000      | 5         | 0.330 | 0.234          | 0.085 |  |
| ${\it WaldDiag,MM3}$        | 1000      | 1000      | 5         | 0.290 | 0.181          | 0.059 |  |
| Pearson, MM3                | 1000      | 1000      | 5         | 0.412 | 0.303          | 0.137 |  |
| RSS,MM3                     | 1000      | 1000      | 5         | 0.431 | 0.332          | 0.164 |  |
| Multn,MM3                   | 1000      | 1000      | 5         | 0.324 | 0.227          | 0.085 |  |
| 3F 15V                      |           |           |           |       |                |       |  |
| Wald                        | 1000      | 1000      | 24        | 0.408 | 0.285          | 0.118 |  |
| WaldVCF                     | 1000      | 1000      | 24        | 0.400 | 0.269          | 0.105 |  |
| ${\it WaldDiag,MM3}$        | 1000      | 1000      | 24        | 0.370 | 0.250          | 0.098 |  |
| Pearson,MM3                 | 1000      | 1000      | 24        | 0.483 | 0.365          | 0.204 |  |
| RSS,MM3                     | 1000      | 1000      | 24        | 0.499 | 0.396          | 0.227 |  |
| Multn,MM3                   | 1000      | 1000      | 24        | 0.386 | 0.262          | 0.096 |  |

|          |           |           |           | recje | Rejection rate |    |  |
|----------|-----------|-----------|-----------|-------|----------------|----|--|
| sim Name | No. repl. | Converged | Rank def. | 10%   | 5%             | 1% |  |

Power (n = 3000)

|        |      |           |           |           | Reje | Rejection rate |    |
|--------|------|-----------|-----------|-----------|------|----------------|----|
| $\sin$ | Name | No. repl. | Converged | Rank def. | 10%  | 5%             | 1% |

Power (n = 5000)

|                           |           |           |           | Re    | jection r | ate   |
|---------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                      | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                     |           |           |           |       |           |       |
| Wald                      | 1000      | 1000      | 1         | 0.986 | 0.979     | 0.938 |
| WaldVCF                   | 1000      | 1000      | 1         | 0.986 | 0.979     | 0.938 |
| ${\bf WaldDiag, MM3}$     | 1000      | 1000      | 1         | 0.982 | 0.950     | 0.836 |
| Pearson,MM3               | 1000      | 1000      | 1         | 0.985 | 0.979     | 0.942 |
| RSS,MM3                   | 1000      | 1000      | 1         | 0.987 | 0.982     | 0.948 |
| Multn,MM3                 | 1000      | 1000      | 1         | 0.986 | 0.978     | 0.938 |
| 1F 8V                     |           |           |           |       |           |       |
| Wald                      | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.000 |
| WaldVCF                   | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3              | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.000 |
| Pearson,MM3               | 1000      | 1000      | 4         | 1.000 | 1.000     | 0.996 |
| RSS,MM3                   | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.000 |
| Multn,MM3                 | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.000 |
| 1F 15V                    |           |           |           |       |           |       |
| Wald                      | 1000      | 1000      | 19        | 1.000 | 1.000     | 1.000 |
| WaldVCF                   | 1000      | 1000      | 19        | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3              | 1000      | 1000      | 19        | 1.000 | 1.000     | 1.000 |
| Pearson,MM3               | 1000      | 1000      | 19        | 1.000 | 1.000     | 1.000 |
| RSS,MM3                   | 1000      | 1000      | 19        | 1.000 | 1.000     | 1.000 |
| Multn,MM3                 | 1000      | 1000      | 19        | 1.000 | 1.000     | 1.000 |
| 2F 10V                    |           |           |           |       |           |       |
| Wald                      | 1000      | 1000      | 12        | 0.801 | 0.730     | 0.598 |
| WaldVCF                   | 1000      | 1000      | 12        | 0.790 | 0.723     | 0.584 |
| ${ m WaldDiag}, { m MM3}$ | 1000      | 1000      | 12        | 0.814 | 0.751     | 0.610 |
| Pearson,MM3               | 1000      | 1000      | 12        | 0.843 | 0.792     | 0.688 |
| RSS,MM3                   | 1000      | 1000      | 12        | 0.862 | 0.823     | 0.720 |
| Multn,MM3                 | 1000      | 1000      | 12        | 0.794 | 0.726     | 0.591 |
| 3F 15V                    |           |           |           |       |           |       |
| Wald                      | 1000      | 1000      | 45        | 0.929 | 0.890     | 0.805 |
| WaldVCF                   | 1000      | 1000      | 45        | 0.923 | 0.885     | 0.796 |
| WaldDiag,MM3              | 1000      | 1000      | 45        | 0.947 | 0.916     | 0.834 |
| Pearson,MM3               | 1000      | 1000      | 45        | 0.959 | 0.926     | 0.857 |
| RSS,MM3                   | 1000      | 1000      | 45        | 0.964 | 0.944     | 0.881 |
| m Multn, MM3              | 1000      | 1000      | 45        | 0.924 | 0.885     | 0.799 |

Power (n = 10000)

|                          |           |           |           | Re    | jection r | ate   |
|--------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                     | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                    |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 0         | 1.000 | 0.999     | 0.995 |
| WaldVCF                  | 1000      | 1000      | 0         | 1.000 | 0.999     | 0.995 |
| ${\bf WaldDiag, MM3}$    | 1000      | 1000      | 0         | 0.999 | 0.996     | 0.989 |
| Pearson,MM3              | 1000      | 1000      | 0         | 1.000 | 0.999     | 0.994 |
| RSS,MM3                  | 1000      | 1000      | 0         | 1.000 | 0.999     | 0.99  |
| Multn,MM3                | 1000      | 1000      | 0         | 1.000 | 0.999     | 0.99  |
| 1F 8V                    |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.000 |
| WaldVCF                  | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.00  |
| WaldDiag,MM3             | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.00  |
| Pearson, MM3             | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.00  |
| RSS,MM3                  | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.00  |
| Multn,MM3                | 1000      | 1000      | 4         | 1.000 | 1.000     | 1.00  |
| 1F 15V                   |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 23        | 1.000 | 1.000     | 1.00  |
| WaldVCF                  | 1000      | 1000      | 23        | 1.000 | 1.000     | 1.00  |
| ${\bf WaldDiag, MM3}$    | 1000      | 1000      | 23        | 1.000 | 1.000     | 1.00  |
| Pearson, MM3             | 1000      | 1000      | 23        | 1.000 | 1.000     | 1.00  |
| RSS,MM3                  | 1000      | 1000      | 23        | 1.000 | 1.000     | 1.00  |
| Multn,MM3                | 1000      | 1000      | 23        | 1.000 | 1.000     | 1.00  |
| 2F 10V                   |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 14        | 0.937 | 0.913     | 0.84  |
| $\operatorname{WaldVCF}$ | 1000      | 1000      | 14        | 0.932 | 0.906     | 0.83  |
| WaldDiag,MM3             | 1000      | 1000      | 14        | 0.945 | 0.921     | 0.84  |
| Pearson,MM3              | 1000      | 1000      | 14        | 0.946 | 0.929     | 0.86  |
| RSS,MM3                  | 1000      | 1000      | 14        | 0.954 | 0.941     | 0.89  |
| Multn,MM3                | 1000      | 1000      | 14        | 0.932 | 0.910     | 0.83  |
| 3F 15V                   |           |           |           |       |           |       |
| Wald                     | 1000      | 1000      | 61        | 0.988 | 0.982     | 0.96  |
| WaldVCF                  | 1000      | 1000      | 61        | 0.987 | 0.981     | 0.96  |
| ${\bf Wald Diag, MM3}$   | 1000      | 1000      | 61        | 0.987 | 0.984     | 0.97  |
| Pearson, MM3             | 1000      | 1000      | 61        | 0.992 | 0.986     | 0.97  |
| RSS,MM3                  | 1000      | 1000      | 61        | 0.992 | 0.991     | 0.98  |
| Multn,MM3                | 1000      | 1000      | 61        | 0.987 | 0.981     | 0.96  |

### Stratified sampling

Type I errors (n = 500)

|                                |           |           |           | Re    | jection r | ate   |
|--------------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                           | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                          |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 1         | 0.142 | 0.083     | 0.020 |
| WaldVCF                        | 1000      | 1000      | 1         | 0.130 | 0.083     | 0.017 |
| ${\bf Wald Diag, MM3}$         | 1000      | 1000      | 1         | 0.119 | 0.055     | 0.016 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.140 | 0.083     | 0.021 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.143 | 0.078     | 0.021 |
| $\mathrm{Multn}, \mathrm{MM3}$ | 1000      | 1000      | 1         | 0.137 | 0.083     | 0.018 |
| 1F 8V                          |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 1         | 0.155 | 0.099     | 0.030 |
| WaldVCF                        | 1000      | 1000      | 1         | 0.126 | 0.073     | 0.019 |
| ${\bf Wald Diag, MM3}$         | 1000      | 1000      | 1         | 0.056 | 0.027     | 0.002 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.109 | 0.060     | 0.009 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.109 | 0.062     | 0.009 |
| ${ m Multn, MM3}$              | 1000      | 1000      | 1         | 0.133 | 0.080     | 0.021 |
| 1F 15V                         |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 6         | 0.178 | 0.106     | 0.030 |
| WaldVCF                        | 1000      | 1000      | 6         | 0.149 | 0.090     | 0.023 |
| WaldDiag,MM3                   | 1000      | 1000      | 6         | 0.121 | 0.070     | 0.012 |
| Pearson,MM3                    | 1000      | 1000      | 6         | 0.156 | 0.088     | 0.022 |
| RSS,MM3                        | 1000      | 1000      | 6         | 0.158 | 0.095     | 0.023 |
| ${ m Multn, MM3}$              | 1000      | 1000      | 6         | 0.169 | 0.104     | 0.029 |
| 2F 10V                         |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 6         | 0.337 | 0.232     | 0.100 |
| WaldVCF                        | 1000      | 1000      | 6         | 0.173 | 0.100     | 0.026 |
| WaldDiag,MM3                   | 1000      | 1000      | 6         | 0.091 | 0.038     | 0.010 |
| Pearson,MM3                    | 1000      | 1000      | 6         | 0.175 | 0.090     | 0.026 |
| RSS,MM3                        | 1000      | 1000      | 6         | 0.157 | 0.096     | 0.024 |
| ${ m Multn, MM3}$              | 1000      | 1000      | 6         | 0.275 | 0.170     | 0.064 |
| 3F 15V                         |           |           |           |       |           |       |
| Wald                           | 1000      | 1000      | 13        | 0.383 | 0.262     | 0.085 |
| WaldVCF                        | 1000      | 1000      | 13        | 0.280 | 0.156     | 0.045 |
| WaldDiag,MM3                   | 1000      | 1000      | 13        | 0.180 | 0.091     | 0.014 |
| Pearson,MM3                    | 1000      | 1000      | 13        | 0.302 | 0.179     | 0.053 |
| RSS,MM3                        | 1000      | 1000      | 13        | 0.308 | 0.187     | 0.055 |
| ${ m Multn, MM3}$              | 1000      | 1000      | 13        | 0.400 | 0.271     | 0.096 |

Type I errors (n = 1000)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.126 | 0.079     | 0.022 |
| WaldVCF      | 1000      | 1000      | 1         | 0.111 | 0.066     | 0.015 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.074 | 0.037     | 0.007 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.099 | 0.051     | 0.019 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.094 | 0.052     | 0.018 |
| Multn, MM3   | 1000      | 1000      | 1         | 0.115 | 0.072     | 0.017 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 2         | 0.261 | 0.162     | 0.052 |
| WaldVCF      | 1000      | 1000      | 2         | 0.185 | 0.108     | 0.027 |
| WaldDiag,MM3 | 1000      | 1000      | 2         | 0.117 | 0.051     | 0.012 |
| Pearson, MM3 | 1000      | 1000      | 2         | 0.173 | 0.103     | 0.029 |
| RSS,MM3      | 1000      | 1000      | 2         | 0.185 | 0.099     | 0.022 |
| Multn,MM3    | 1000      | 1000      | 2         | 0.239 | 0.150     | 0.043 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 12        | 0.620 | 0.501     | 0.267 |
| WaldVCF      | 1000      | 1000      | 12        | 0.333 | 0.203     | 0.057 |
| WaldDiag,MM3 | 1000      | 1000      | 12        | 0.162 | 0.079     | 0.012 |
| Pearson, MM3 | 1000      | 1000      | 12        | 0.286 | 0.173     | 0.051 |
| RSS,MM3      | 1000      | 1000      | 12        | 0.292 | 0.174     | 0.046 |
| Multn, MM3   | 1000      | 1000      | 12        | 0.614 | 0.482     | 0.260 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 10        | 0.294 | 0.202     | 0.068 |
| WaldVCF      | 1000      | 1000      | 10        | 0.221 | 0.134     | 0.032 |
| WaldDiag,MM3 | 1000      | 1000      | 10        | 0.108 | 0.049     | 0.009 |
| Pearson, MM3 | 1000      | 1000      | 10        | 0.199 | 0.123     | 0.023 |
| RSS,MM3      | 1000      | 1000      | 10        | 0.203 | 0.118     | 0.023 |
| Multn, MM3   | 1000      | 1000      | 10        | 0.294 | 0.202     | 0.070 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 44        | 0.543 | 0.406     | 0.180 |
| WaldVCF      | 1000      | 1000      | 44        | 0.335 | 0.210     | 0.069 |
| WaldDiag,MM3 | 1000      | 1000      | 44        | 0.162 | 0.086     | 0.021 |
| Pearson,MM3  | 1000      | 1000      | 44        | 0.236 | 0.143     | 0.037 |
| RSS,MM3      | 1000      | 1000      | 44        | 0.241 | 0.155     | 0.044 |
| Multn,MM3    | 1000      | 1000      | 44        | 0.576 | 0.453     | 0.214 |

Type I errors (n = 2000)

|        |      |           |           |           | Reject | tion rate |    |
|--------|------|-----------|-----------|-----------|--------|-----------|----|
| 1F 5V  |      |           |           |           |        |           |    |
| 1F 8V  |      |           |           |           |        |           |    |
| 1F 15V |      |           |           |           |        |           |    |
| 2F 10V |      |           |           |           |        |           |    |
| 3F 15V |      |           |           |           |        |           |    |
|        | Name | No. repl. | Converged | Rank def. | 10%    | 5%        | 1% |

|        |      |           |           |           | Reject | tion rate |    |
|--------|------|-----------|-----------|-----------|--------|-----------|----|
| 1F 5V  |      |           |           |           |        |           |    |
| 1F 8V  |      |           |           |           |        |           |    |
| 1F 15V |      |           |           |           |        |           |    |
| 2F 10V |      |           |           |           |        |           |    |
| 3F 15V |      |           |           |           |        |           |    |
|        | Name | No. repl. | Converged | Rank def. | 10%    | 5%        | 1% |

Type I errors (n = 5000)

|                         |           |           |           | Re    | jection r | ate   |
|-------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                    | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                   |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 1         | 0.144 | 0.077     | 0.020 |
| WaldVCF                 | 1000      | 1000      | 1         | 0.142 | 0.075     | 0.020 |
| WaldDiag,MM3            | 1000      | 1000      | 1         | 0.126 | 0.061     | 0.012 |
| Pearson,MM3             | 1000      | 1000      | 1         | 0.146 | 0.071     | 0.014 |
| RSS,MM3                 | 1000      | 1000      | 1         | 0.142 | 0.074     | 0.017 |
| $_{\mathrm{Multn,MM3}}$ | 1000      | 1000      | 1         | 0.141 | 0.076     | 0.020 |
| 1F 8V                   |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 6         | 0.211 | 0.115     | 0.028 |
| WaldVCF                 | 1000      | 1000      | 6         | 0.193 | 0.106     | 0.023 |
| WaldDiag,MM3            | 1000      | 1000      | 6         | 0.156 | 0.078     | 0.017 |
| Pearson,MM3             | 1000      | 1000      | 6         | 0.187 | 0.102     | 0.024 |
| RSS,MM3                 | 1000      | 1000      | 6         | 0.201 | 0.110     | 0.026 |
| Multn,MM3               | 1000      | 1000      | 6         | 0.205 | 0.112     | 0.026 |
| 1F 15V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 33        | 0.336 | 0.219     | 0.074 |
| WaldVCF                 | 1000      | 1000      | 33        | 0.284 | 0.174     | 0.044 |
| WaldDiag,MM3            | 1000      | 1000      | 33        | 0.221 | 0.130     | 0.024 |
| Pearson,MM3             | 1000      | 1000      | 33        | 0.305 | 0.202     | 0.068 |
| RSS,MM3                 | 1000      | 1000      | 33        | 0.317 | 0.206     | 0.069 |
| Multn,MM3               | 1000      | 1000      | 33        | 0.349 | 0.227     | 0.078 |
| 2F 10V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 28        | 0.216 | 0.134     | 0.034 |
| WaldVCF                 | 1000      | 1000      | 28        | 0.204 | 0.121     | 0.029 |
| WaldDiag,MM3            | 1000      | 1000      | 28        | 0.167 | 0.080     | 0.023 |
| Pearson,MM3             | 1000      | 1000      | 28        | 0.189 | 0.104     | 0.029 |
| RSS,MM3                 | 1000      | 1000      | 28        | 0.194 | 0.123     | 0.029 |
| Multn,MM3               | 1000      | 1000      | 28        | 0.212 | 0.130     | 0.032 |
| 3F 15V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 59        | 0.357 | 0.242     | 0.078 |
| WaldVCF                 | 1000      | 1000      | 59        | 0.309 | 0.201     | 0.061 |
| WaldDiag,MM3            | 1000      | 1000      | 59        | 0.216 | 0.114     | 0.027 |
| Pearson,MM3             | 1000      | 1000      | 59        | 0.275 | 0.175     | 0.051 |
| RSS,MM3                 | 1000      | 1000      | 59        | 0.294 | 0.181     | 0.057 |
| Multn,MM3               | 1000      | 1000      | 59        | 0.354 | 0.244     | 0.086 |

Type I errors (n = 10000)

|                             |           |           |           | Re    | jection r | ate   |
|-----------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                        | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 4         | 0.154 | 0.077     | 0.011 |
| WaldVCF                     | 1000      | 1000      | 4         | 0.153 | 0.077     | 0.011 |
| WaldDiag,MM3                | 1000      | 1000      | 4         | 0.123 | 0.073     | 0.013 |
| Pearson, MM3                | 1000      | 1000      | 4         | 0.149 | 0.079     | 0.022 |
| RSS,MM3                     | 1000      | 1000      | 4         | 0.153 | 0.081     | 0.020 |
| ${ m Multn, MM3}$           | 1000      | 1000      | 4         | 0.152 | 0.075     | 0.011 |
| 1F 8V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 6         | 0.165 | 0.088     | 0.022 |
| WaldVCF                     | 1000      | 1000      | 6         | 0.158 | 0.082     | 0.021 |
| WaldDiag,MM3                | 1000      | 1000      | 6         | 0.129 | 0.067     | 0.018 |
| Pearson,MM3                 | 1000      | 1000      | 6         | 0.168 | 0.089     | 0.025 |
| RSS,MM3                     | 1000      | 1000      | 6         | 0.172 | 0.099     | 0.026 |
| Multn, MM3                  | 1000      | 1000      | 6         | 0.162 | 0.088     | 0.021 |
| 1F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 44        | 0.291 | 0.176     | 0.055 |
| WaldVCF                     | 1000      | 1000      | 44        | 0.265 | 0.159     | 0.048 |
| ${\it WaldDiag}, {\it MM3}$ | 1000      | 1000      | 44        | 0.205 | 0.118     | 0.033 |
| Pearson,MM3                 | 1000      | 1000      | 44        | 0.309 | 0.203     | 0.075 |
| RSS,MM3                     | 1000      | 1000      | 44        | 0.321 | 0.203     | 0.075 |
| Multn, MM3                  | 1000      | 1000      | 44        | 0.292 | 0.178     | 0.057 |
| 2F 10V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 27        | 0.201 | 0.127     | 0.035 |
| WaldVCF                     | 1000      | 1000      | 27        | 0.190 | 0.117     | 0.033 |
| ${\bf WaldDiag,} {\bf MM3}$ | 1000      | 1000      | 27        | 0.159 | 0.086     | 0.016 |
| Pearson,MM3                 | 1000      | 1000      | 27        | 0.178 | 0.102     | 0.032 |
| RSS,MM3                     | 1000      | 1000      | 27        | 0.184 | 0.112     | 0.034 |
| Multn, MM3                  | 1000      | 1000      | 27        | 0.197 | 0.121     | 0.033 |
| 3F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 87        | 0.333 | 0.212     | 0.070 |
| WaldVCF                     | 1000      | 1000      | 87        | 0.306 | 0.180     | 0.062 |
| ${\bf Wald Diag, MM3}$      | 1000      | 1000      | 87        | 0.234 | 0.135     | 0.036 |
| Pearson, MM3                | 1000      | 1000      | 87        | 0.276 | 0.166     | 0.051 |
| RSS,MM3                     | 1000      | 1000      | 87        | 0.281 | 0.181     | 0.055 |
| Multn, MM3                  | 1000      | 1000      | 87        | 0.326 | 0.205     | 0.067 |

**Power** (n = 500)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 2         | 0.833 | 0.744     | 0.525 |
| WaldVCF      | 1000      | 1000      | 2         | 0.828 | 0.738     | 0.515 |
| WaldDiag,MM3 | 1000      | 1000      | 2         | 0.707 | 0.567     | 0.298 |
| Pearson,MM3  | 1000      | 1000      | 2         | 0.854 | 0.780     | 0.576 |
| RSS,MM3      | 1000      | 1000      | 2         | 0.865 | 0.796     | 0.607 |
| Multn, MM3   | 1000      | 1000      | 2         | 0.829 | 0.738     | 0.514 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 2         | 0.424 | 0.307     | 0.141 |
| WaldVCF      | 1000      | 1000      | 2         | 0.373 | 0.258     | 0.094 |
| WaldDiag,MM3 | 1000      | 1000      | 2         | 0.187 | 0.093     | 0.015 |
| Pearson,MM3  | 1000      | 1000      | 2         | 0.398 | 0.268     | 0.096 |
| RSS,MM3      | 1000      | 1000      | 2         | 0.415 | 0.274     | 0.105 |
| Multn,MM3    | 1000      | 1000      | 2         | 0.368 | 0.242     | 0.084 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 2         | 1.000 | 1.000     | 1.000 |
| WaldVCF      | 1000      | 1000      | 2         | 1.000 | 1.000     | 0.999 |
| WaldDiag,MM3 | 1000      | 1000      | 2         | 1.000 | 0.999     | 0.978 |
| Pearson,MM3  | 1000      | 1000      | 2         | 0.999 | 0.993     | 0.964 |
| RSS,MM3      | 1000      | 1000      | 2         | 1.000 | 1.000     | 0.987 |
| Multn,MM3    | 1000      | 1000      | 2         | 1.000 | 1.000     | 1.000 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.833 | 0.754     | 0.567 |
| WaldVCF      | 1000      | 1000      | 1         | 0.609 | 0.474     | 0.215 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.449 | 0.282     | 0.086 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.491 | 0.317     | 0.116 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.567 | 0.419     | 0.175 |
| Multn,MM3    | 1000      | 1000      | 1         | 0.777 | 0.682     | 0.463 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 13        | 0.996 | 0.992     | 0.957 |
| WaldVCF      | 1000      | 1000      | 13        | 0.992 | 0.973     | 0.910 |
| WaldDiag,MM3 | 1000      | 1000      | 13        | 0.991 | 0.972     | 0.892 |
| Pearson,MM3  | 1000      | 1000      | 13        | 0.999 | 0.999     | 0.995 |
| RSS,MM3      | 1000      | 1000      | 13        | 0.999 | 0.999     | 0.994 |
| Multn,MM3    | 1000      | 1000      | 13        | 0.996 | 0.990     | 0.950 |

Power (n = 1000)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.510 | 0.405     | 0.212 |
| WaldVCF      | 1000      | 1000      | 1         | 0.483 | 0.362     | 0.186 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.361 | 0.236     | 0.079 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.554 | 0.420     | 0.248 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.560 | 0.421     | 0.251 |
| Multn, MM3   | 1000      | 1000      | 1         | 0.482 | 0.364     | 0.188 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.934 | 0.882     | 0.736 |
| WaldVCF      | 1000      | 1000      | 1         | 0.859 | 0.774     | 0.542 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.793 | 0.672     | 0.396 |
| Pearson, MM3 | 1000      | 1000      | 1         | 0.675 | 0.534     | 0.278 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.785 | 0.666     | 0.414 |
| Multn, MM3   | 1000      | 1000      | 1         | 0.916 | 0.855     | 0.697 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 13        | 0.983 | 0.969     | 0.910 |
| WaldVCF      | 1000      | 1000      | 13        | 0.905 | 0.834     | 0.588 |
| WaldDiag,MM3 | 1000      | 1000      | 13        | 0.822 | 0.712     | 0.425 |
| Pearson,MM3  | 1000      | 1000      | 13        | 0.973 | 0.945     | 0.867 |
| RSS,MM3      | 1000      | 1000      | 13        | 0.968 | 0.946     | 0.864 |
| Multn, MM3   | 1000      | 1000      | 13        | 0.971 | 0.950     | 0.859 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 9         | 0.435 | 0.319     | 0.142 |
| WaldVCF      | 1000      | 1000      | 9         | 0.320 | 0.204     | 0.060 |
| WaldDiag,MM3 | 1000      | 1000      | 9         | 0.225 | 0.133     | 0.038 |
| Pearson,MM3  | 1000      | 1000      | 9         | 0.357 | 0.252     | 0.113 |
| RSS,MM3      | 1000      | 1000      | 9         | 0.344 | 0.244     | 0.100 |
| Multn, MM3   | 1000      | 1000      | 9         | 0.402 | 0.291     | 0.116 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 31        | 0.718 | 0.602     | 0.342 |
| WaldVCF      | 1000      | 1000      | 31        | 0.515 | 0.361     | 0.142 |
| WaldDiag,MM3 | 1000      | 1000      | 31        | 0.368 | 0.237     | 0.061 |
| Pearson,MM3  | 1000      | 1000      | 31        | 0.486 | 0.333     | 0.129 |
| RSS,MM3      | 1000      | 1000      | 31        | 0.518 | 0.369     | 0.156 |
| Multn,MM3    | 1000      | 1000      | 31        | 0.750 | 0.633     | 0.387 |

|                          |      |            |           |            | Reject | tion rate |    |
|--------------------------|------|------------|-----------|------------|--------|-----------|----|
| 1F 5V                    |      |            |           |            |        |           |    |
| 1F 8V                    |      |            |           |            |        |           |    |
| 1F 15V                   |      |            |           |            |        |           |    |
| 2F 10V                   |      |            |           |            |        |           |    |
| 3F 15V                   |      |            |           |            |        |           |    |
|                          | Name | No. repl.  | Converged | Rank def.  | 10%    | 5%        | 1% |
| ower $(n=3)$             |      | Tvov Topii | Converged | Tumin deri |        |           |    |
| wer $(n=3)$              |      | Tvov Topii | Converged | Tum der    |        | tion rate |    |
|                          |      | Tvov Topii |           | Tum der    |        |           |    |
| 1F 5V                    |      | Tvor Topa  |           | Tum der    |        |           |    |
| 1F 5V<br>1F 8V           |      |            |           | Tum der    |        |           |    |
| 1F 5V<br>1F 8V<br>1F 15V |      |            |           | Tumin deri |        |           |    |
| 1F 8V                    |      |            |           | Tum der    |        |           |    |

Power (n = 5000)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.938 | 0.892     | 0.749 |
| WaldVCF      | 1000      | 1000      | 0         | 0.938 | 0.892     | 0.747 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.871 | 0.786     | 0.554 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.963 | 0.926     | 0.821 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.964 | 0.930     | 0.829 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.937 | 0.892     | 0.747 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| WaldVCF      | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| RSS,MM3      | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| Multn,MM3    | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 16        | 1.000 | 1.000     | 1.000 |
| WaldVCF      | 1000      | 1000      | 16        | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3 | 1000      | 1000      | 16        | 1.000 | 1.000     | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 16        | 1.000 | 1.000     | 1.000 |
| RSS,MM3      | 1000      | 1000      | 16        | 1.000 | 1.000     | 1.000 |
| Multn,MM3    | 1000      | 1000      | 16        | 1.000 | 1.000     | 1.000 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 13        | 0.928 | 0.875     | 0.706 |
| WaldVCF      | 1000      | 1000      | 13        | 0.918 | 0.857     | 0.675 |
| WaldDiag,MM3 | 1000      | 1000      | 13        | 0.944 | 0.877     | 0.699 |
| Pearson,MM3  | 1000      | 1000      | 13        | 0.964 | 0.933     | 0.813 |
| RSS,MM3      | 1000      | 1000      | 13        | 0.975 | 0.958     | 0.877 |
| Multn,MM3    | 1000      | 1000      | 13        | 0.926 | 0.875     | 0.707 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 45        | 0.999 | 0.998     | 0.987 |
| WaldVCF      | 1000      | 1000      | 45        | 0.998 | 0.997     | 0.974 |
| WaldDiag,MM3 | 1000      | 1000      | 45        | 1.000 | 1.000     | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 45        | 1.000 | 1.000     | 0.989 |
| RSS,MM3      | 1000      | 1000      | 45        | 1.000 | 1.000     | 1.000 |
| Multn,MM3    | 1000      | 1000      | 45        | 1.000 | 0.998     | 0.991 |

Power (n = 10000)

|                   |           |           |           | Re  | ejection 1 | rate  |
|-------------------|-----------|-----------|-----------|-----|------------|-------|
| Name              | No. repl. | Converged | Rank def. | 10% | 5%         | 1%    |
| 1F 5V             |           |           |           |     |            |       |
| Wald              | 1000      | 1000      | 0         | 1   | 1.000      | 0.999 |
| WaldVCF           | 1000      | 1000      | 0         | 1   | 1.000      | 0.999 |
| WaldDiag,MM3      | 1000      | 1000      | 0         | 1   | 0.999      | 0.996 |
| Pearson,MM3       | 1000      | 1000      | 0         | 1   | 1.000      | 1.000 |
| RSS,MM3           | 1000      | 1000      | 0         | 1   | 1.000      | 1.000 |
| Multn,MM3         | 1000      | 1000      | 0         | 1   | 1.000      | 0.999 |
| 1F 8V             |           |           |           |     |            |       |
| Wald              | 1000      | 1000      | 3         | 1   | 1.000      | 1.000 |
| WaldVCF           | 1000      | 1000      | 3         | 1   | 1.000      | 1.000 |
| WaldDiag,MM3      | 1000      | 1000      | 3         | 1   | 1.000      | 1.000 |
| Pearson,MM3       | 1000      | 1000      | 3         | 1   | 1.000      | 1.000 |
| RSS,MM3           | 1000      | 1000      | 3         | 1   | 1.000      | 1.000 |
| m Multn, MM3      | 1000      | 1000      | 3         | 1   | 1.000      | 1.000 |
| 1F 15V            |           |           |           |     |            |       |
| Wald              | 1000      | 1000      | 18        | 1   | 1.000      | 1.000 |
| WaldVCF           | 1000      | 1000      | 18        | 1   | 1.000      | 1.000 |
| WaldDiag,MM3      | 1000      | 1000      | 18        | 1   | 1.000      | 1.000 |
| Pearson,MM3       | 1000      | 1000      | 18        | 1   | 1.000      | 1.000 |
| RSS,MM3           | 1000      | 1000      | 18        | 1   | 1.000      | 1.000 |
| ${ m Multn, MM3}$ | 1000      | 1000      | 18        | 1   | 1.000      | 1.000 |
| 2F 10V            |           |           |           |     |            |       |
| Wald              | 1000      | 1000      | 7         | 1   | 1.000      | 1.000 |
| WaldVCF           | 1000      | 1000      | 7         | 1   | 1.000      | 1.000 |
| WaldDiag,MM3      | 1000      | 1000      | 7         | 1   | 1.000      | 1.000 |
| Pearson,MM3       | 1000      | 1000      | 7         | 1   | 1.000      | 1.000 |
| RSS,MM3           | 1000      | 1000      | 7         | 1   | 1.000      | 1.000 |
| Multn,MM3         | 1000      | 1000      | 7         | 1   | 1.000      | 1.000 |
| 3F 15V            |           |           |           |     |            |       |
| Wald              | 1000      | 1000      | 77        | 1   | 0.999      | 0.992 |
| WaldVCF           | 1000      | 1000      | 77        | 1   | 0.999      | 0.992 |
| WaldDiag,MM3      | 1000      | 1000      | 77        | 1   | 1.000      | 0.999 |
| Pearson,MM3       | 1000      | 1000      | 77        | 1   | 1.000      | 1.000 |
| RSS,MM3           | 1000      | 1000      | 77        | 1   | 1.000      | 1.000 |
| Multn,MM3         | 1000      | 1000      | 77        | 1   | 0.999      | 0.993 |

Cluster sampling

Type I errors (n = 500)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 4         | 0.115 | 0.057     | 0.015 |
| WaldVCF      | 1000      | 1000      | 4         | 0.109 | 0.052     | 0.014 |
| WaldDiag,MM3 | 1000      | 1000      | 4         | 0.082 | 0.039     | 0.008 |
| Pearson,MM3  | 1000      | 1000      | 4         | 0.103 | 0.061     | 0.010 |
| RSS,MM3      | 1000      | 1000      | 4         | 0.105 | 0.052     | 0.010 |
| Multn,MM3    | 1000      | 1000      | 4         | 0.111 | 0.054     | 0.014 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 4         | 0.129 | 0.072     | 0.031 |
| WaldVCF      | 1000      | 1000      | 4         | 0.095 | 0.048     | 0.009 |
| WaldDiag,MM3 | 1000      | 1000      | 4         | 0.031 | 0.012     | 0.000 |
| Pearson,MM3  | 1000      | 1000      | 4         | 0.068 | 0.030     | 0.004 |
| RSS,MM3      | 1000      | 1000      | 4         | 0.070 | 0.027     | 0.004 |
| Multn,MM3    | 1000      | 1000      | 4         | 0.102 | 0.057     | 0.011 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 3         | 0.150 | 0.082     | 0.025 |
| WaldVCF      | 1000      | 1000      | 3         | 0.123 | 0.063     | 0.019 |
| WaldDiag,MM3 | 1000      | 1000      | 3         | 0.112 | 0.061     | 0.020 |
| Pearson,MM3  | 1000      | 1000      | 3         | 0.110 | 0.066     | 0.015 |
| RSS,MM3      | 1000      | 1000      | 3         | 0.109 | 0.064     | 0.016 |
| Multn,MM3    | 1000      | 1000      | 3         | 0.139 | 0.078     | 0.023 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 6         | 0.344 | 0.233     | 0.117 |
| WaldVCF      | 1000      | 1000      | 6         | 0.127 | 0.070     | 0.018 |
| WaldDiag,MM3 | 1000      | 1000      | 6         | 0.063 | 0.029     | 0.004 |
| Pearson,MM3  | 1000      | 1000      | 6         | 0.076 | 0.032     | 0.006 |
| RSS,MM3      | 1000      | 1000      | 6         | 0.083 | 0.033     | 0.005 |
| Multn,MM3    | 1000      | 1000      | 6         | 0.251 | 0.160     | 0.057 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 25        | 0.244 | 0.153     | 0.049 |
| WaldVCF      | 1000      | 1000      | 25        | 0.149 | 0.073     | 0.014 |
| WaldDiag,MM3 | 1000      | 1000      | 25        | 0.113 | 0.057     | 0.006 |
| Pearson,MM3  | 1000      | 1000      | 25        | 0.100 | 0.052     | 0.007 |
| RSS,MM3      | 1000      | 1000      | 25        | 0.105 | 0.049     | 0.007 |
| Multn, MM3   | 1000      | 1000      | 25        | 0.260 | 0.167     | 0.057 |

Type I errors (n = 1000)

|                        |           |           |           | Re    | jection r | ate   |
|------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                   | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                  |           |           |           |       |           |       |
| Wald                   | 1000      | 1000      | 1         | 0.117 | 0.068     | 0.012 |
| WaldVCF                | 1000      | 1000      | 1         | 0.102 | 0.061     | 0.011 |
| WaldDiag,MM3           | 1000      | 1000      | 1         | 0.070 | 0.027     | 0.003 |
| Pearson,MM3            | 1000      | 1000      | 1         | 0.086 | 0.052     | 0.007 |
| RSS,MM3                | 1000      | 1000      | 1         | 0.087 | 0.051     | 0.009 |
| Multn, MM3             | 1000      | 1000      | 1         | 0.108 | 0.060     | 0.011 |
| 1F 8V                  |           |           |           |       |           |       |
| Wald                   | 1000      | 1000      | 3         | 0.196 | 0.126     | 0.039 |
| WaldVCF                | 1000      | 1000      | 3         | 0.130 | 0.071     | 0.012 |
| WaldDiag,MM3           | 1000      | 1000      | 3         | 0.094 | 0.047     | 0.007 |
| Pearson, MM3           | 1000      | 1000      | 3         | 0.107 | 0.048     | 0.010 |
| RSS,MM3                | 1000      | 1000      | 3         | 0.111 | 0.051     | 0.007 |
| Multn, MM3             | 1000      | 1000      | 3         | 0.172 | 0.107     | 0.033 |
| 1F 15V                 |           |           |           |       |           |       |
| Wald                   | 1000      | 1000      | 18        | 0.504 | 0.396     | 0.208 |
| WaldVCF                | 1000      | 1000      | 18        | 0.175 | 0.092     | 0.014 |
| WaldDiag,MM3           | 1000      | 1000      | 18        | 0.107 | 0.047     | 0.006 |
| Pearson,MM3            | 1000      | 1000      | 18        | 0.094 | 0.044     | 0.008 |
| RSS,MM3                | 1000      | 1000      | 18        | 0.097 | 0.041     | 0.004 |
| Multn,MM3              | 1000      | 1000      | 18        | 0.499 | 0.374     | 0.197 |
| 2F 10V                 |           |           |           |       |           |       |
| Wald                   | 1000      | 1000      | 13        | 0.191 | 0.113     | 0.031 |
| WaldVCF                | 1000      | 1000      | 13        | 0.117 | 0.062     | 0.010 |
| WaldDiag,MM3           | 1000      | 1000      | 13        | 0.063 | 0.026     | 0.003 |
| Pearson, MM3           | 1000      | 1000      | 13        | 0.083 | 0.039     | 0.007 |
| RSS,MM3                | 1000      | 1000      | 13        | 0.088 | 0.041     | 0.006 |
| Multn, MM3             | 1000      | 1000      | 13        | 0.193 | 0.113     | 0.036 |
| 3F 15V                 |           |           |           |       |           |       |
| Wald                   | 1000      | 1000      | 35        | 0.288 | 0.183     | 0.057 |
| WaldVCF                | 1000      | 1000      | 35        | 0.139 | 0.067     | 0.012 |
| ${\bf Wald Diag, MM3}$ | 1000      | 1000      | 35        | 0.062 | 0.028     | 0.005 |
| Pearson,MM3            | 1000      | 1000      | 35        | 0.096 | 0.046     | 0.010 |
| RSS,MM3                | 1000      | 1000      | 35        | 0.092 | 0.048     | 0.006 |
| Multn,MM3              | 1000      | 1000      | 35        | 0.371 | 0.250     | 0.109 |

Type I errors (n = 2000)

|        |      |           |           |           | Reject | Rejection rate |    |  |
|--------|------|-----------|-----------|-----------|--------|----------------|----|--|
| 1F 5V  |      |           |           |           |        |                |    |  |
| 1F 8V  |      |           |           |           |        |                |    |  |
| 1F 15V |      |           |           |           |        |                |    |  |
| 2F 10V |      |           |           |           |        |                |    |  |
| 3F 15V |      |           |           |           |        |                |    |  |
|        | Name | No. repl. | Converged | Rank def. | 10%    | 5%             | 1% |  |

|        |      |           |           |           | Reject | Rejection rate |    |  |
|--------|------|-----------|-----------|-----------|--------|----------------|----|--|
| 1F 5V  |      |           |           |           |        |                |    |  |
| 1F 8V  |      |           |           |           |        |                |    |  |
| 1F 15V |      |           |           |           |        |                |    |  |
| 2F 10V |      |           |           |           |        |                |    |  |
| 3F 15V |      |           |           |           |        |                |    |  |
|        | Name | No. repl. | Converged | Rank def. | 10%    | 5%             | 1% |  |

Type I errors (n = 5000)

|                         |           |           |           | Re    | jection r | ate   |
|-------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                    | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                   |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 1         | 0.087 | 0.037     | 0.005 |
| WaldVCF                 | 1000      | 1000      | 1         | 0.083 | 0.037     | 0.003 |
| WaldDiag,MM3            | 1000      | 1000      | 1         | 0.077 | 0.042     | 0.006 |
| Pearson,MM3             | 1000      | 1000      | 1         | 0.082 | 0.040     | 0.005 |
| RSS,MM3                 | 1000      | 1000      | 1         | 0.083 | 0.043     | 0.004 |
| Multn,MM3               | 1000      | 1000      | 1         | 0.083 | 0.037     | 0.003 |
| 1F 8V                   |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 3         | 0.140 | 0.072     | 0.015 |
| WaldVCF                 | 1000      | 1000      | 3         | 0.126 | 0.068     | 0.012 |
| WaldDiag,MM3            | 1000      | 1000      | 3         | 0.115 | 0.057     | 0.012 |
| Pearson,MM3             | 1000      | 1000      | 3         | 0.101 | 0.055     | 0.006 |
| RSS,MM3                 | 1000      | 1000      | 3         | 0.109 | 0.048     | 0.007 |
| $_{\mathrm{Multn,MM3}}$ | 1000      | 1000      | 3         | 0.135 | 0.072     | 0.013 |
| 1F 15V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 25        | 0.183 | 0.104     | 0.026 |
| WaldVCF                 | 1000      | 1000      | 25        | 0.141 | 0.070     | 0.017 |
| WaldDiag,MM3            | 1000      | 1000      | 25        | 0.130 | 0.077     | 0.014 |
| Pearson,MM3             | 1000      | 1000      | 25        | 0.110 | 0.055     | 0.003 |
| RSS,MM3                 | 1000      | 1000      | 25        | 0.111 | 0.057     | 0.005 |
| Multn,MM3               | 1000      | 1000      | 25        | 0.191 | 0.110     | 0.029 |
| 2F 10V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 23        | 0.154 | 0.084     | 0.025 |
| WaldVCF                 | 1000      | 1000      | 23        | 0.137 | 0.076     | 0.019 |
| WaldDiag,MM3            | 1000      | 1000      | 23        | 0.105 | 0.063     | 0.013 |
| Pearson,MM3             | 1000      | 1000      | 23        | 0.116 | 0.055     | 0.013 |
| RSS,MM3                 | 1000      | 1000      | 23        | 0.119 | 0.063     | 0.013 |
| Multn,MM3               | 1000      | 1000      | 23        | 0.151 | 0.084     | 0.024 |
| 3F 15V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 46        | 0.152 | 0.083     | 0.022 |
| WaldVCF                 | 1000      | 1000      | 46        | 0.122 | 0.061     | 0.018 |
| WaldDiag,MM3            | 1000      | 1000      | 46        | 0.119 | 0.051     | 0.011 |
| Pearson,MM3             | 1000      | 1000      | 46        | 0.098 | 0.056     | 0.011 |
| RSS,MM3                 | 1000      | 1000      | 46        | 0.101 | 0.048     | 0.010 |
| Multn,MM3               | 1000      | 1000      | 46        | 0.160 | 0.087     | 0.026 |

Type I errors (n = 10000)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.112 | 0.053     | 0.009 |
| WaldVCF      | 1000      | 1000      | 1         | 0.109 | 0.053     | 0.008 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.103 | 0.054     | 0.008 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.100 | 0.054     | 0.008 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.102 | 0.051     | 0.010 |
| Multn, MM3   | 1000      | 1000      | 1         | 0.109 | 0.053     | 0.008 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 6         | 0.128 | 0.067     | 0.011 |
| WaldVCF      | 1000      | 1000      | 6         | 0.119 | 0.061     | 0.011 |
| WaldDiag,MM3 | 1000      | 1000      | 6         | 0.117 | 0.058     | 0.015 |
| Pearson,MM3  | 1000      | 1000      | 6         | 0.090 | 0.043     | 0.013 |
| RSS,MM3      | 1000      | 1000      | 6         | 0.099 | 0.043     | 0.012 |
| Multn,MM3    | 1000      | 1000      | 6         | 0.125 | 0.063     | 0.011 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 40        | 0.143 | 0.081     | 0.017 |
| WaldVCF      | 1000      | 1000      | 40        | 0.126 | 0.066     | 0.015 |
| WaldDiag,MM3 | 1000      | 1000      | 40        | 0.123 | 0.062     | 0.014 |
| Pearson,MM3  | 1000      | 1000      | 40        | 0.109 | 0.044     | 0.008 |
| RSS,MM3      | 1000      | 1000      | 40        | 0.102 | 0.046     | 0.012 |
| Multn,MM3    | 1000      | 1000      | 40        | 0.147 | 0.084     | 0.018 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 25        | 0.124 | 0.066     | 0.017 |
| WaldVCF      | 1000      | 1000      | 25        | 0.114 | 0.057     | 0.015 |
| WaldDiag,MM3 | 1000      | 1000      | 25        | 0.096 | 0.052     | 0.009 |
| Pearson,MM3  | 1000      | 1000      | 25        | 0.081 | 0.042     | 0.011 |
| RSS,MM3      | 1000      | 1000      | 25        | 0.099 | 0.044     | 0.010 |
| Multn,MM3    | 1000      | 1000      | 25        | 0.118 | 0.061     | 0.016 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 116       | 0.128 | 0.074     | 0.020 |
| WaldVCF      | 1000      | 1000      | 116       | 0.112 | 0.063     | 0.018 |
| WaldDiag,MM3 | 1000      | 1000      | 116       | 0.103 | 0.057     | 0.008 |
| Pearson,MM3  | 1000      | 1000      | 116       | 0.106 | 0.051     | 0.019 |
| RSS,MM3      | 1000      | 1000      | 116       | 0.099 | 0.053     | 0.014 |
| Multn,MM3    | 1000      | 1000      | 116       | 0.125 | 0.073     | 0.020 |

**Power** (n = 500)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.875 | 0.788     | 0.580 |
| WaldVCF      | 1000      | 1000      | 0         | 0.870 | 0.783     | 0.564 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.754 | 0.613     | 0.327 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.871 | 0.775     | 0.564 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.894 | 0.817     | 0.623 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.872 | 0.783     | 0.570 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.286 | 0.195     | 0.078 |
| WaldVCF      | 1000      | 1000      | 1         | 0.242 | 0.154     | 0.048 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.104 | 0.042     | 0.005 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.237 | 0.147     | 0.050 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.249 | 0.156     | 0.049 |
| Multn,MM3    | 1000      | 1000      | 1         | 0.241 | 0.151     | 0.048 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 3         | 1.000 | 0.999     | 0.997 |
| WaldVCF      | 1000      | 1000      | 3         | 0.999 | 0.999     | 0.994 |
| WaldDiag,MM3 | 1000      | 1000      | 3         | 0.997 | 0.996     | 0.950 |
| Pearson,MM3  | 1000      | 1000      | 3         | 0.993 | 0.978     | 0.872 |
| RSS,MM3      | 1000      | 1000      | 3         | 0.997 | 0.993     | 0.957 |
| Multn,MM3    | 1000      | 1000      | 3         | 1.000 | 0.999     | 0.997 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 2         | 0.728 | 0.623     | 0.451 |
| WaldVCF      | 1000      | 1000      | 2         | 0.428 | 0.292     | 0.090 |
| WaldDiag,MM3 | 1000      | 1000      | 2         | 0.279 | 0.139     | 0.026 |
| Pearson,MM3  | 1000      | 1000      | 2         | 0.274 | 0.154     | 0.041 |
| RSS,MM3      | 1000      | 1000      | 2         | 0.352 | 0.207     | 0.061 |
| Multn,MM3    | 1000      | 1000      | 2         | 0.646 | 0.544     | 0.325 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 13        | 1.000 | 0.999     | 0.978 |
| WaldVCF      | 1000      | 1000      | 13        | 0.999 | 0.988     | 0.953 |
| WaldDiag,MM3 | 1000      | 1000      | 13        | 0.995 | 0.985     | 0.934 |
| Pearson,MM3  | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| RSS,MM3      | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| Multn,MM3    | 1000      | 1000      | 13        | 1.000 | 0.999     | 0.978 |

Power (n = 1000)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.466 | 0.357     | 0.157 |
| WaldVCF      | 1000      | 1000      | 0         | 0.444 | 0.329     | 0.134 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.308 | 0.195     | 0.049 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.432 | 0.320     | 0.138 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.477 | 0.351     | 0.167 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.450 | 0.337     | 0.141 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.934 | 0.902     | 0.766 |
| WaldVCF      | 1000      | 1000      | 0         | 0.882 | 0.798     | 0.549 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.702 | 0.563     | 0.266 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.684 | 0.507     | 0.228 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.792 | 0.681     | 0.400 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.927 | 0.893     | 0.747 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 9         | 0.900 | 0.816     | 0.629 |
| WaldVCF      | 1000      | 1000      | 9         | 0.588 | 0.444     | 0.195 |
| WaldDiag,MM3 | 1000      | 1000      | 9         | 0.486 | 0.352     | 0.120 |
| Pearson,MM3  | 1000      | 1000      | 9         | 0.868 | 0.779     | 0.561 |
| RSS,MM3      | 1000      | 1000      | 9         | 0.847 | 0.749     | 0.525 |
| Multn, MM3   | 1000      | 1000      | 9         | 0.851 | 0.751     | 0.540 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 13        | 0.492 | 0.365     | 0.179 |
| WaldVCF      | 1000      | 1000      | 13        | 0.368 | 0.254     | 0.098 |
| WaldDiag,MM3 | 1000      | 1000      | 13        | 0.401 | 0.273     | 0.105 |
| Pearson,MM3  | 1000      | 1000      | 13        | 0.589 | 0.472     | 0.255 |
| RSS,MM3      | 1000      | 1000      | 13        | 0.573 | 0.467     | 0.242 |
| Multn, MM3   | 1000      | 1000      | 13        | 0.471 | 0.347     | 0.155 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 34        | 0.755 | 0.621     | 0.360 |
| WaldVCF      | 1000      | 1000      | 34        | 0.525 | 0.371     | 0.143 |
| WaldDiag,MM3 | 1000      | 1000      | 34        | 0.589 | 0.430     | 0.181 |
| Pearson,MM3  | 1000      | 1000      | 34        | 0.787 | 0.668     | 0.435 |
| RSS,MM3      | 1000      | 1000      | 34        | 0.793 | 0.678     | 0.436 |
| Multn,MM3    | 1000      | 1000      | 34        | 0.801 | 0.683     | 0.435 |

|  |      |           |            |            | Reject | tion rate |    |
|--|------|-----------|------------|------------|--------|-----------|----|
| 1F 5V  |      |           |            |            |        |           |    |
| 1F 8V  |      |           |            |            |        |           |    |
| 1F 15V                                       |      |           |            |            |        |           |    |
| 2F 10V                                       |      |           |            |            |        |           |    |
| 3F 15V                                       |      |           |            |            |        |           |    |
|  | Name | No. repl. | Converged  | Rank def.  | 10%    | 5%        | 1% |
| ower $(n=3)$                                 |      | 2.0. 252  | 001101604  | Tumin deri |        |           |    |
| wer $(n=3)$                                  |      |           | 0011101604 | Tumin deri |        | tion rate |    |
|  |      |           | 0011,01804 | Tumin deri |        |           |    |
| 1F 5V  |      |           | 0011101604 | Tumin deri |        |           |    |
| 1F 5V<br>1F 8V                               |      |           | 0011101800 | Tumin deri |        |           |    |
| 1F 5V<br>1F 8V<br>1F 15V                     |      |           | 0011,01804 | Tumin deri |        |           |    |
| 1F 5V<br>1F 8V<br>1F 15V<br>2F 10V<br>3F 15V |      |           | 0011,01804 | Tumin deri |        |           |    |

Power (n = 5000)

|                         |           |           |           | Re    | jection r | ate   |
|-------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                    | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                   |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 2         | 0.995 | 0.983     | 0.935 |
| WaldVCF                 | 1000      | 1000      | 2         | 0.995 | 0.983     | 0.934 |
| WaldDiag,MM3            | 1000      | 1000      | 2         | 0.975 | 0.948     | 0.809 |
| Pearson,MM3             | 1000      | 1000      | 2         | 0.996 | 0.993     | 0.955 |
| RSS,MM3                 | 1000      | 1000      | 2         | 0.996 | 0.994     | 0.966 |
| Multn,MM3               | 1000      | 1000      | 2         | 0.994 | 0.983     | 0.935 |
| 1F 8V                   |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| WaldVCF                 | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3            | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| Pearson,MM3             | 1000      | 1000      | 0         | 1.000 | 1.000     | 0.982 |
| RSS,MM3                 | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| $_{\mathrm{Multn,MM3}}$ | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| 1F 15V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| WaldVCF                 | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3            | 1000      | 1000      | 13        | 1.000 | 1.000     | 0.998 |
| Pearson,MM3             | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| RSS,MM3                 | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| $_{\mathrm{Multn,MM3}}$ | 1000      | 1000      | 13        | 1.000 | 1.000     | 1.000 |
| 2F 10V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 12        | 0.701 | 0.573     | 0.329 |
| WaldVCF                 | 1000      | 1000      | 12        | 0.671 | 0.546     | 0.289 |
| WaldDiag,MM3            | 1000      | 1000      | 12        | 0.700 | 0.558     | 0.305 |
| Pearson,MM3             | 1000      | 1000      | 12        | 0.871 | 0.791     | 0.586 |
| RSS,MM3                 | 1000      | 1000      | 12        | 0.872 | 0.816     | 0.635 |
| $_{ m Multn,MM3}$       | 1000      | 1000      | 12        | 0.695 | 0.567     | 0.328 |
| 3F 15V                  |           |           |           |       |           |       |
| Wald                    | 1000      | 1000      | 41        | 1.000 | 1.000     | 0.991 |
| WaldVCF                 | 1000      | 1000      | 41        | 1.000 | 0.999     | 0.984 |
| WaldDiag,MM3            | 1000      | 1000      | 41        | 1.000 | 1.000     | 0.998 |
| Pearson,MM3             | 1000      | 1000      | 41        | 0.990 | 0.981     | 0.887 |
| RSS,MM3                 | 1000      | 1000      | 41        | 0.999 | 0.997     | 0.982 |
| Multn,MM3               | 1000      | 1000      | 41        | 1.000 | 1.000     | 0.996 |

Power (n = 10000)

|              |           |           |           | Re  | jection | rate  |
|--------------|-----------|-----------|-----------|-----|---------|-------|
| Name         | No. repl. | Converged | Rank def. | 10% | 5%      | 1%    |
| 1F 5V        |           |           |           |     |         |       |
| Wald         | 1000      | 1000      | 0         | 1   | 1       | 1.000 |
| WaldVCF      | 1000      | 1000      | 0         | 1   | 1       | 1.000 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 1   | 1       | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 0         | 1   | 1       | 1.000 |
| RSS,MM3      | 1000      | 1000      | 0         | 1   | 1       | 1.000 |
| Multn,MM3    | 1000      | 1000      | 0         | 1   | 1       | 1.000 |
| 1F 8V        |           |           |           |     |         |       |
| Wald         | 1000      | 1000      | 1         | 1   | 1       | 1.000 |
| WaldVCF      | 1000      | 1000      | 1         | 1   | 1       | 1.000 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 1   | 1       | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 1         | 1   | 1       | 1.000 |
| RSS,MM3      | 1000      | 1000      | 1         | 1   | 1       | 1.000 |
| Multn, MM3   | 1000      | 1000      | 1         | 1   | 1       | 1.000 |
| 1F 15V       |           |           |           |     |         |       |
| Wald         | 1000      | 1000      | 16        | 1   | 1       | 1.000 |
| WaldVCF      | 1000      | 1000      | 16        | 1   | 1       | 1.000 |
| WaldDiag,MM3 | 1000      | 1000      | 16        | 1   | 1       | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 16        | 1   | 1       | 1.000 |
| RSS,MM3      | 1000      | 1000      | 16        | 1   | 1       | 1.000 |
| Multn, MM3   | 1000      | 1000      | 16        | 1   | 1       | 1.000 |
| 2F 10V       |           |           |           |     |         |       |
| Wald         | 1000      | 1000      | 18        | 1   | 1       | 1.000 |
| WaldVCF      | 1000      | 1000      | 18        | 1   | 1       | 0.999 |
| WaldDiag,MM3 | 1000      | 1000      | 18        | 1   | 1       | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 18        | 1   | 1       | 1.000 |
| RSS,MM3      | 1000      | 1000      | 18        | 1   | 1       | 1.000 |
| Multn, MM3   | 1000      | 1000      | 18        | 1   | 1       | 0.999 |
| 3F 15V       |           |           |           |     |         |       |
| Wald         | 1000      | 1000      | 57        | 1   | 1       | 1.000 |
| WaldVCF      | 1000      | 1000      | 57        | 1   | 1       | 1.000 |
| WaldDiag,MM3 | 1000      | 1000      | 57        | 1   | 1       | 1.000 |
| Pearson,MM3  | 1000      | 1000      | 57        | 1   | 1       | 1.000 |
| RSS,MM3      | 1000      | 1000      | 57        | 1   | 1       | 1.000 |
| Multn,MM3    | 1000      | 1000      | 57        | 1   | 1       | 1.000 |

### Strat-clust sampling

Type I errors (n = 500)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 0.116 | 0.063     | 0.012 |
| WaldVCF      | 1000      | 1000      | 1         | 0.111 | 0.062     | 0.010 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.096 | 0.045     | 0.005 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.110 | 0.062     | 0.013 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.102 | 0.065     | 0.011 |
| Multn, MM3   | 1000      | 1000      | 1         | 0.112 | 0.062     | 0.011 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.130 | 0.076     | 0.019 |
| WaldVCF      | 1000      | 1000      | 0         | 0.099 | 0.053     | 0.008 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.041 | 0.014     | 0.001 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.086 | 0.040     | 0.005 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.083 | 0.039     | 0.005 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.109 | 0.060     | 0.010 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 4         | 0.148 | 0.083     | 0.019 |
| WaldVCF      | 1000      | 1000      | 4         | 0.122 | 0.066     | 0.010 |
| WaldDiag,MM3 | 1000      | 1000      | 4         | 0.095 | 0.048     | 0.010 |
| Pearson,MM3  | 1000      | 1000      | 4         | 0.124 | 0.060     | 0.011 |
| RSS,MM3      | 1000      | 1000      | 4         | 0.122 | 0.066     | 0.012 |
| Multn, MM3   | 1000      | 1000      | 4         | 0.142 | 0.082     | 0.014 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.272 | 0.177     | 0.070 |
| WaldVCF      | 1000      | 1000      | 0         | 0.115 | 0.058     | 0.013 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.052 | 0.019     | 0.004 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.120 | 0.054     | 0.013 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.113 | 0.054     | 0.007 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.209 | 0.120     | 0.044 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 20        | 0.267 | 0.176     | 0.050 |
| WaldVCF      | 1000      | 1000      | 20        | 0.189 | 0.105     | 0.026 |
| WaldDiag,MM3 | 1000      | 1000      | 20        | 0.127 | 0.070     | 0.011 |
| Pearson,MM3  | 1000      | 1000      | 20        | 0.175 | 0.106     | 0.025 |
| RSS,MM3      | 1000      | 1000      | 20        | 0.181 | 0.105     | 0.021 |
| Multn,MM3    | 1000      | 1000      | 20        | 0.286 | 0.190     | 0.061 |

Type I errors (n = 1000)

|                                |           |           |           | Re    | ejection r | ate   |
|--------------------------------|-----------|-----------|-----------|-------|------------|-------|
| Name                           | No. repl. | Converged | Rank def. | 10%   | 5%         | 1%    |
| 1F 5V                          |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 1         | 0.119 | 0.067      | 0.023 |
| WaldVCF                        | 1000      | 1000      | 1         | 0.111 | 0.059      | 0.018 |
| WaldDiag,MM3                   | 1000      | 1000      | 1         | 0.071 | 0.038      | 0.005 |
| Pearson,MM3                    | 1000      | 1000      | 1         | 0.115 | 0.063      | 0.013 |
| RSS,MM3                        | 1000      | 1000      | 1         | 0.117 | 0.068      | 0.014 |
| Multn, MM3                     | 1000      | 1000      | 1         | 0.112 | 0.059      | 0.022 |
| 1F 8V                          |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 4         | 0.206 | 0.117      | 0.029 |
| WaldVCF                        | 1000      | 1000      | 4         | 0.134 | 0.070      | 0.014 |
| WaldDiag,MM3                   | 1000      | 1000      | 4         | 0.089 | 0.042      | 0.006 |
| Pearson,MM3                    | 1000      | 1000      | 4         | 0.133 | 0.067      | 0.011 |
| RSS,MM3                        | 1000      | 1000      | 4         | 0.135 | 0.063      | 0.009 |
| Multn, MM3                     | 1000      | 1000      | 4         | 0.183 | 0.104      | 0.022 |
| 1F 15V                         |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 12        | 0.429 | 0.308      | 0.139 |
| WaldVCF                        | 1000      | 1000      | 12        | 0.172 | 0.095      | 0.013 |
| ${\bf WaldDiag,} {\bf MM3}$    | 1000      | 1000      | 12        | 0.079 | 0.031      | 0.004 |
| Pearson,MM3                    | 1000      | 1000      | 12        | 0.145 | 0.071      | 0.013 |
| RSS,MM3                        | 1000      | 1000      | 12        | 0.149 | 0.077      | 0.007 |
| $\mathrm{Multn}, \mathrm{MM3}$ | 1000      | 1000      | 12        | 0.424 | 0.298      | 0.130 |
| 2F 10V                         |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 10        | 0.202 | 0.123      | 0.044 |
| WaldVCF                        | 1000      | 1000      | 10        | 0.142 | 0.084      | 0.022 |
| ${\bf WaldDiag,} {\bf MM3}$    | 1000      | 1000      | 10        | 0.072 | 0.034      | 0.006 |
| Pearson,MM3                    | 1000      | 1000      | 10        | 0.119 | 0.067      | 0.016 |
| RSS,MM3                        | 1000      | 1000      | 10        | 0.120 | 0.066      | 0.020 |
| Multn, MM3                     | 1000      | 1000      | 10        | 0.208 | 0.131      | 0.044 |
| 3F 15V                         |           |           |           |       |            |       |
| Wald                           | 1000      | 1000      | 33        | 0.347 | 0.250      | 0.087 |
| WaldVCF                        | 1000      | 1000      | 33        | 0.195 | 0.105      | 0.028 |
| ${\it WaldDiag,MM3}$           | 1000      | 1000      | 33        | 0.091 | 0.042      | 0.009 |
| Pearson,MM3                    | 1000      | 1000      | 33        | 0.155 | 0.081      | 0.018 |
| RSS,MM3                        | 1000      | 1000      | 33        | 0.154 | 0.086      | 0.017 |
| Multn, MM3                     | 1000      | 1000      | 33        | 0.397 | 0.283      | 0.111 |

Type I errors (n = 2000)

| -      |      |           |           |           | Reject | Rejection rate |    |  |
|--------|------|-----------|-----------|-----------|--------|----------------|----|--|
| 1F 5V  |      |           |           |           |        |                |    |  |
| 1F 8V  |      |           |           |           |        |                |    |  |
| 1F 15V |      |           |           |           |        |                |    |  |
| 2F 10V |      |           |           |           |        |                |    |  |
| 3F 15V |      |           |           |           |        |                |    |  |
|        | Name | No. repl. | Converged | Rank def. | 10%    | 5%             | 1% |  |

|        |      |           |           |           | Reject | Rejection rate |    |  |
|--------|------|-----------|-----------|-----------|--------|----------------|----|--|
| 1F 5V  |      |           |           |           |        |                |    |  |
| 1F 8V  |      |           |           |           |        |                |    |  |
| 1F 15V |      |           |           |           |        |                |    |  |
| 2F 10V |      |           |           |           |        |                |    |  |
| 3F 15V |      |           |           |           |        |                |    |  |
|        | Name | No. repl. | Converged | Rank def. | 10%    | 5%             | 1% |  |

Type I errors (n = 5000)

|                         |           |           |           | Re    | ejection r | ate   |
|-------------------------|-----------|-----------|-----------|-------|------------|-------|
| Name                    | No. repl. | Converged | Rank def. | 10%   | 5%         | 1%    |
| 1F 5V                   |           |           |           |       |            |       |
| Wald                    | 1000      | 1000      | 1         | 0.127 | 0.062      | 0.018 |
| WaldVCF                 | 1000      | 1000      | 1         | 0.124 | 0.061      | 0.017 |
| WaldDiag,MM3            | 1000      | 1000      | 1         | 0.102 | 0.052      | 0.012 |
| Pearson,MM3             | 1000      | 1000      | 1         | 0.121 | 0.062      | 0.017 |
| RSS,MM3                 | 1000      | 1000      | 1         | 0.127 | 0.065      | 0.015 |
| $_{\mathrm{Multn,MM3}}$ | 1000      | 1000      | 1         | 0.124 | 0.062      | 0.018 |
| 1F 8V                   |           |           |           |       |            |       |
| Wald                    | 1000      | 1000      | 4         | 0.131 | 0.076      | 0.010 |
| WaldVCF                 | 1000      | 1000      | 4         | 0.125 | 0.068      | 0.009 |
| WaldDiag,MM3            | 1000      | 1000      | 4         | 0.113 | 0.059      | 0.008 |
| Pearson,MM3             | 1000      | 1000      | 4         | 0.149 | 0.075      | 0.018 |
| RSS,MM3                 | 1000      | 1000      | 4         | 0.140 | 0.081      | 0.017 |
| Multn,MM3               | 1000      | 1000      | 4         | 0.129 | 0.076      | 0.010 |
| 1F 15V                  |           |           |           |       |            |       |
| Wald                    | 1000      | 1000      | 26        | 0.195 | 0.112      | 0.028 |
| WaldVCF                 | 1000      | 1000      | 26        | 0.164 | 0.084      | 0.018 |
| WaldDiag,MM3            | 1000      | 1000      | 26        | 0.126 | 0.061      | 0.014 |
| Pearson,MM3             | 1000      | 1000      | 26        | 0.168 | 0.089      | 0.018 |
| RSS,MM3                 | 1000      | 1000      | 26        | 0.169 | 0.095      | 0.020 |
| Multn,MM3               | 1000      | 1000      | 26        | 0.206 | 0.127      | 0.032 |
| 2F 10V                  |           |           |           |       |            |       |
| Wald                    | 1000      | 1000      | 18        | 0.151 | 0.079      | 0.015 |
| WaldVCF                 | 1000      | 1000      | 18        | 0.132 | 0.071      | 0.012 |
| WaldDiag,MM3            | 1000      | 1000      | 18        | 0.099 | 0.046      | 0.010 |
| Pearson,MM3             | 1000      | 1000      | 18        | 0.127 | 0.064      | 0.020 |
| RSS,MM3                 | 1000      | 1000      | 18        | 0.133 | 0.067      | 0.017 |
| Multn,MM3               | 1000      | 1000      | 18        | 0.149 | 0.076      | 0.014 |
| 3F 15V                  |           |           |           |       |            |       |
| Wald                    | 1000      | 1000      | 64        | 0.193 | 0.119      | 0.035 |
| WaldVCF                 | 1000      | 1000      | 64        | 0.169 | 0.094      | 0.025 |
| WaldDiag,MM3            | 1000      | 1000      | 64        | 0.134 | 0.069      | 0.018 |
| Pearson,MM3             | 1000      | 1000      | 64        | 0.179 | 0.096      | 0.029 |
| RSS,MM3                 | 1000      | 1000      | 64        | 0.168 | 0.099      | 0.028 |
| Multn,MM3               | 1000      | 1000      | 64        | 0.200 | 0.117      | 0.039 |

Type I errors (n = 10000)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 2         | 0.104 | 0.054     | 0.016 |
| WaldVCF      | 1000      | 1000      | 2         | 0.102 | 0.054     | 0.015 |
| WaldDiag,MM3 | 1000      | 1000      | 2         | 0.087 | 0.050     | 0.010 |
| Pearson,MM3  | 1000      | 1000      | 2         | 0.108 | 0.051     | 0.020 |
| RSS,MM3      | 1000      | 1000      | 2         | 0.112 | 0.056     | 0.018 |
| Multn,MM3    | 1000      | 1000      | 2         | 0.101 | 0.054     | 0.016 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 11        | 0.130 | 0.074     | 0.011 |
| WaldVCF      | 1000      | 1000      | 11        | 0.122 | 0.072     | 0.010 |
| WaldDiag,MM3 | 1000      | 1000      | 11        | 0.111 | 0.058     | 0.011 |
| Pearson, MM3 | 1000      | 1000      | 11        | 0.117 | 0.064     | 0.017 |
| RSS,MM3      | 1000      | 1000      | 11        | 0.129 | 0.071     | 0.019 |
| Multn,MM3    | 1000      | 1000      | 11        | 0.126 | 0.074     | 0.011 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 44        | 0.189 | 0.107     | 0.023 |
| WaldVCF      | 1000      | 1000      | 44        | 0.165 | 0.097     | 0.018 |
| WaldDiag,MM3 | 1000      | 1000      | 44        | 0.147 | 0.074     | 0.018 |
| Pearson, MM3 | 1000      | 1000      | 44        | 0.186 | 0.102     | 0.035 |
| RSS,MM3      | 1000      | 1000      | 44        | 0.180 | 0.110     | 0.028 |
| Multn,MM3    | 1000      | 1000      | 44        | 0.191 | 0.111     | 0.024 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 28        | 0.150 | 0.085     | 0.032 |
| WaldVCF      | 1000      | 1000      | 28        | 0.134 | 0.082     | 0.028 |
| WaldDiag,MM3 | 1000      | 1000      | 28        | 0.135 | 0.071     | 0.015 |
| Pearson,MM3  | 1000      | 1000      | 28        | 0.160 | 0.083     | 0.019 |
| RSS,MM3      | 1000      | 1000      | 28        | 0.162 | 0.088     | 0.020 |
| Multn,MM3    | 1000      | 1000      | 28        | 0.142 | 0.084     | 0.031 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 97        | 0.176 | 0.095     | 0.020 |
| WaldVCF      | 1000      | 1000      | 97        | 0.156 | 0.075     | 0.013 |
| WaldDiag,MM3 | 1000      | 1000      | 97        | 0.135 | 0.067     | 0.013 |
| Pearson, MM3 | 1000      | 1000      | 97        | 0.140 | 0.078     | 0.019 |
| RSS,MM3      | 1000      | 1000      | 97        | 0.153 | 0.082     | 0.013 |
| Multn,MM3    | 1000      | 1000      | 97        | 0.169 | 0.088     | 0.018 |

**Power** (n = 500)

|              |           |           |           | Re    | jection r | ate   |
|--------------|-----------|-----------|-----------|-------|-----------|-------|
| Name         | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V        |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.955 | 0.922     | 0.799 |
| WaldVCF      | 1000      | 1000      | 0         | 0.952 | 0.920     | 0.790 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.896 | 0.798     | 0.545 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.973 | 0.953     | 0.879 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.974 | 0.955     | 0.886 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.952 | 0.920     | 0.792 |
| 1F 8V        |           |           |           |       |           |       |
| Wald         | 1000      | 999       | 3         | 0.425 | 0.304     | 0.142 |
| WaldVCF      | 1000      | 999       | 3         | 0.386 | 0.258     | 0.101 |
| WaldDiag,MM3 | 1000      | 999       | 3         | 0.168 | 0.074     | 0.009 |
| Pearson,MM3  | 1000      | 999       | 3         | 0.436 | 0.301     | 0.118 |
| RSS,MM3      | 1000      | 999       | 3         | 0.452 | 0.310     | 0.130 |
| Multn, MM3   | 1000      | 999       | 3         | 0.382 | 0.250     | 0.100 |
| 1F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 1         | 1.000 | 1.000     | 0.999 |
| WaldVCF      | 1000      | 1000      | 1         | 1.000 | 1.000     | 0.999 |
| WaldDiag,MM3 | 1000      | 1000      | 1         | 0.999 | 0.999     | 0.990 |
| Pearson,MM3  | 1000      | 1000      | 1         | 0.996 | 0.981     | 0.901 |
| RSS,MM3      | 1000      | 1000      | 1         | 0.999 | 0.998     | 0.984 |
| Multn, MM3   | 1000      | 1000      | 1         | 1.000 | 1.000     | 0.999 |
| 2F 10V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 0         | 0.843 | 0.751     | 0.549 |
| WaldVCF      | 1000      | 1000      | 0         | 0.586 | 0.432     | 0.184 |
| WaldDiag,MM3 | 1000      | 1000      | 0         | 0.416 | 0.251     | 0.066 |
| Pearson,MM3  | 1000      | 1000      | 0         | 0.440 | 0.286     | 0.097 |
| RSS,MM3      | 1000      | 1000      | 0         | 0.545 | 0.398     | 0.161 |
| Multn, MM3   | 1000      | 1000      | 0         | 0.780 | 0.689     | 0.436 |
| 3F 15V       |           |           |           |       |           |       |
| Wald         | 1000      | 1000      | 11        | 0.994 | 0.991     | 0.950 |
| WaldVCF      | 1000      | 1000      | 11        | 0.989 | 0.977     | 0.913 |
| WaldDiag,MM3 | 1000      | 1000      | 11        | 0.977 | 0.958     | 0.879 |
| Pearson,MM3  | 1000      | 1000      | 11        | 1.000 | 1.000     | 0.997 |
| RSS,MM3      | 1000      | 1000      | 11        | 1.000 | 1.000     | 0.995 |
| Multn,MM3    | 1000      | 1000      | 11        | 0.993 | 0.990     | 0.949 |

Power (n = 1000)

|                             |           |           |           | Re    | jection r | ate   |
|-----------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                        | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 1         | 0.506 | 0.379     | 0.188 |
| WaldVCF                     | 1000      | 1000      | 1         | 0.485 | 0.357     | 0.165 |
| ${\it WaldDiag}, {\it MM3}$ | 1000      | 1000      | 1         | 0.340 | 0.213     | 0.053 |
| Pearson,MM3                 | 1000      | 1000      | 1         | 0.510 | 0.376     | 0.167 |
| RSS,MM3                     | 1000      | 1000      | 1         | 0.525 | 0.403     | 0.192 |
| Multn, MM3                  | 1000      | 1000      | 1         | 0.485 | 0.364     | 0.168 |
| 1F 8V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 1         | 0.955 | 0.908     | 0.756 |
| WaldVCF                     | 1000      | 1000      | 1         | 0.894 | 0.804     | 0.560 |
| WaldDiag,MM3                | 1000      | 1000      | 1         | 0.737 | 0.579     | 0.278 |
| Pearson, MM3                | 1000      | 1000      | 1         | 0.726 | 0.568     | 0.292 |
| RSS,MM3                     | 1000      | 1000      | 1         | 0.820 | 0.712     | 0.442 |
| Multn, MM3                  | 1000      | 1000      | 1         | 0.947 | 0.891     | 0.746 |
| 1F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 10        | 0.942 | 0.889     | 0.726 |
| WaldVCF                     | 1000      | 1000      | 10        | 0.726 | 0.588     | 0.321 |
| WaldDiag,MM3                | 1000      | 1000      | 10        | 0.642 | 0.478     | 0.224 |
| Pearson, MM3                | 1000      | 1000      | 10        | 0.916 | 0.848     | 0.678 |
| RSS,MM3                     | 1000      | 1000      | 10        | 0.912 | 0.832     | 0.666 |
| Multn, MM3                  | 1000      | 1000      | 10        | 0.906 | 0.845     | 0.644 |
| 2F 10V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 8         | 0.453 | 0.312     | 0.132 |
| WaldVCF                     | 1000      | 1000      | 8         | 0.318 | 0.193     | 0.069 |
| WaldDiag,MM3                | 1000      | 1000      | 8         | 0.266 | 0.160     | 0.040 |
| Pearson, MM3                | 1000      | 1000      | 8         | 0.363 | 0.246     | 0.103 |
| RSS,MM3                     | 1000      | 1000      | 8         | 0.384 | 0.268     | 0.110 |
| Multn, MM3                  | 1000      | 1000      | 8         | 0.420 | 0.280     | 0.120 |
| 3F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 28        | 0.662 | 0.526     | 0.287 |
| WaldVCF                     | 1000      | 1000      | 28        | 0.464 | 0.319     | 0.129 |
| WaldDiag,MM3                | 1000      | 1000      | 28        | 0.392 | 0.267     | 0.094 |
| Pearson,MM3                 | 1000      | 1000      | 28        | 0.607 | 0.461     | 0.231 |
| RSS,MM3                     | 1000      | 1000      | 28        | 0.653 | 0.517     | 0.288 |
| Multn,MM3                   | 1000      | 1000      | 28        | 0.688 | 0.567     | 0.329 |

|                          |      |            |           |           | Reject | tion rate |    |
|--------------------------|------|------------|-----------|-----------|--------|-----------|----|
| 1F 5V                    |      |            |           |           |        |           |    |
| 1F 8V                    |      |            |           |           |        |           |    |
| 1F 15V                   |      |            |           |           |        |           |    |
| 2F 10V                   |      |            |           |           |        |           |    |
| 3F 15V                   |      |            |           |           |        |           |    |
|                          | Name | No. repl.  | Converged | Rank def. | 10%    | 5%        | 1% |
| ower $(n=3)$             |      | 1,0,10p.   | 33        |           |        |           |    |
| wer $(n=3)$              |      | 1,0,10p.   |           |           |        | tion rate |    |
|                          |      | 7.0. 10p.: | 33        |           |        | tion rate |    |
| 1F 5V                    |      | 7.0. 10p.: |           |           |        | tion rate |    |
| 1F 5V<br>1F 8V           |      | 7,0,10p.   |           |           |        | tion rate |    |
| 1F 5V<br>1F 8V<br>1F 15V |      | 7.0. 10p.: |           |           |        | tion rate |    |
| 1F 8V                    |      |            |           |           |        | tion rate |    |

Power (n = 5000)

|                             |           |           |           | Re    | jection r | ate   |
|-----------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                        | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 1         | 0.993 | 0.990     | 0.945 |
| WaldVCF                     | 1000      | 1000      | 1         | 0.993 | 0.990     | 0.944 |
| WaldDiag,MM3                | 1000      | 1000      | 1         | 0.985 | 0.960     | 0.879 |
| Pearson, MM3                | 1000      | 1000      | 1         | 0.997 | 0.995     | 0.965 |
| RSS,MM3                     | 1000      | 1000      | 1         | 0.999 | 0.995     | 0.972 |
| Multn, MM3                  | 1000      | 1000      | 1         | 0.993 | 0.989     | 0.944 |
| 1F 8V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 3         | 1.000 | 1.000     | 1.000 |
| WaldVCF                     | 1000      | 1000      | 3         | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3                | 1000      | 1000      | 3         | 1.000 | 1.000     | 1.000 |
| Pearson,MM3                 | 1000      | 1000      | 3         | 1.000 | 1.000     | 1.000 |
| RSS,MM3                     | 1000      | 1000      | 3         | 1.000 | 1.000     | 1.000 |
| Multn, MM3                  | 1000      | 1000      | 3         | 1.000 | 1.000     | 1.000 |
| 1F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 12        | 1.000 | 1.000     | 1.000 |
| WaldVCF                     | 1000      | 1000      | 12        | 1.000 | 1.000     | 1.000 |
| ${\it WaldDiag}, {\it MM3}$ | 1000      | 1000      | 12        | 1.000 | 1.000     | 1.000 |
| Pearson,MM3                 | 1000      | 1000      | 12        | 1.000 | 1.000     | 1.000 |
| RSS,MM3                     | 1000      | 1000      | 12        | 1.000 | 1.000     | 1.000 |
| Multn, MM3                  | 1000      | 1000      | 12        | 1.000 | 1.000     | 1.000 |
| 2F 10V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 9         | 0.832 | 0.738     | 0.523 |
| WaldVCF                     | 1000      | 1000      | 9         | 0.797 | 0.691     | 0.459 |
| ${\bf WaldDiag,} {\bf MM3}$ | 1000      | 1000      | 9         | 0.865 | 0.793     | 0.553 |
| Pearson,MM3                 | 1000      | 1000      | 9         | 0.923 | 0.873     | 0.729 |
| RSS,MM3                     | 1000      | 1000      | 9         | 0.949 | 0.904     | 0.785 |
| Multn, MM3                  | 1000      | 1000      | 9         | 0.825 | 0.728     | 0.506 |
| 3F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 46        | 0.902 | 0.848     | 0.682 |
| WaldVCF                     | 1000      | 1000      | 46        | 0.875 | 0.795     | 0.605 |
| ${\bf Wald Diag, MM3}$      | 1000      | 1000      | 46        | 0.938 | 0.889     | 0.763 |
| Pearson, MM3                | 1000      | 1000      | 46        | 0.960 | 0.942     | 0.853 |
| RSS,MM3                     | 1000      | 1000      | 46        | 0.970 | 0.947     | 0.881 |
| Multn, MM3                  | 1000      | 1000      | 46        | 0.904 | 0.844     | 0.687 |

Power (n = 10000)

|                             |           |           |           | Re    | jection r | ate   |
|-----------------------------|-----------|-----------|-----------|-------|-----------|-------|
| Name                        | No. repl. | Converged | Rank def. | 10%   | 5%        | 1%    |
| 1F 5V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| WaldVCF                     | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3                | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| Pearson,MM3                 | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| RSS,MM3                     | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| Multn, MM3                  | 1000      | 1000      | 0         | 1.000 | 1.000     | 1.000 |
| 1F 8V                       |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 1         | 1.000 | 1.000     | 1.000 |
| WaldVCF                     | 1000      | 1000      | 1         | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3                | 1000      | 1000      | 1         | 1.000 | 1.000     | 1.000 |
| Pearson, MM3                | 1000      | 1000      | 1         | 1.000 | 1.000     | 1.000 |
| RSS,MM3                     | 1000      | 1000      | 1         | 1.000 | 1.000     | 1.000 |
| Multn, MM3                  | 1000      | 1000      | 1         | 1.000 | 1.000     | 1.000 |
| 1F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 27        | 1.000 | 1.000     | 1.000 |
| WaldVCF                     | 1000      | 1000      | 27        | 1.000 | 1.000     | 1.000 |
| WaldDiag,MM3                | 1000      | 1000      | 27        | 1.000 | 1.000     | 1.000 |
| Pearson,MM3                 | 1000      | 1000      | 27        | 1.000 | 1.000     | 1.000 |
| RSS,MM3                     | 1000      | 1000      | 27        | 1.000 | 1.000     | 1.000 |
| Multn, MM3                  | 1000      | 1000      | 27        | 1.000 | 1.000     | 1.000 |
| 2F 10V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 26        | 0.864 | 0.785     | 0.567 |
| WaldVCF                     | 1000      | 1000      | 26        | 0.845 | 0.764     | 0.527 |
| WaldDiag,MM3                | 1000      | 1000      | 26        | 0.927 | 0.862     | 0.673 |
| Pearson, MM3                | 1000      | 1000      | 26        | 0.896 | 0.842     | 0.631 |
| RSS,MM3                     | 1000      | 1000      | 26        | 0.908 | 0.868     | 0.700 |
| Multn, MM3                  | 1000      | 1000      | 26        | 0.860 | 0.781     | 0.560 |
| 3F 15V                      |           |           |           |       |           |       |
| Wald                        | 1000      | 1000      | 70        | 0.807 | 0.714     | 0.480 |
| WaldVCF                     | 1000      | 1000      | 70        | 0.774 | 0.672     | 0.434 |
| ${\it WaldDiag}, {\it MM3}$ | 1000      | 1000      | 70        | 0.870 | 0.783     | 0.537 |
| Pearson,MM3                 | 1000      | 1000      | 70        | 0.920 | 0.856     | 0.707 |
| RSS,MM3                     | 1000      | 1000      | 70        | 0.920 | 0.877     | 0.728 |
| Multn,MM3                   | 1000      | 1000      | 70        | 0.802 | 0.712     | 0.478 |