

# Huggett (1996) Model

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## Model Features

We compute a simplified version of [Huggett \(1996\)](#)

Households:

- Live for many ( $a_D$ ) periods
- Earnings are random
- Age of retirement is fixed ( $a_R$ ).

Government:

- Pays transfers to retired households (annuitized income in the data)

Simplifying assumptions:

- Partial equilibrium
- No random mortality
- No intergenerational links
- No labor-leisure choice.

# Model Primitives

## Demographics

Households live for exactly  $a_D$  periods.

Total mass of households is  $N = 1$ .

## Preferences

$$\mathbb{E} \sum_{a=1}^{a_D} \beta^a u(c_a) \quad (1)$$

## Endowments

Working agents are endowed with labor efficiency  $\eta_a e_a$

$\eta_a$ : age-efficiency profile

$e_a$ : labor efficiency (wage) shock

- governed by a Markov chain:  $\Pr(e' = \varepsilon_k | e = \varepsilon_j) = P_e(k, j)$ .
- new agents draw labor endowments from a fixed distribution.
- number of states:  $N_e$ .

## Markets

Labor: wage  $w$

Capital rental:  $r$

Goods: numeraire.

## Government

Taxes labor income:  $T = \tau_w w L$ .

Pays retirement transfers:  $\varpi(a) = \varpi$  if  $a > a_R$ .

## Household Problem

Exogenous state variables are age  $a$  and labor endowment  $e$ :  $s = (a, e)$ .

Endogenous state variable: wealth  $k$ .

Borrowing constraint:  $k \geq 0$ .

## Sequence problem

$$\max E \sum_{a=1}^{a_D} \beta^a u(c_a)$$

subject to

$$k_{a+1} = y_a - c_a \geq 0$$

$$y_a = R k_a + w(1 - \tau_w) \eta_a e_a + \varpi(a) \quad (2)$$

## Household Dynamic Program

$$V(k, s) = \max u(y(k, s) - k') + \beta \mathbb{E} V(k', s') \quad (3)$$

with

$$y(k, s) = Rk + w(1 - \tau_w) \eta_a e + \varpi(s) \quad (4)$$

subject to  $k' \geq 0$ .

Euler equation:

$$u'(c) \geq \beta R \mathbb{E} u'(c') \quad (5)$$

with equality if  $k' > 0$ .

## Household Solution

*Solution* is a consumption function  $c(k, a, e)$  which satisfies

$$u'(c[k, a, e]) \geq \beta R \sum_{e'} P_e(e, e') u'(c[y - c(k, a, e), a + 1, e'])$$

In the last period, consume all income:

$$c(k, a_D, e) = y(k, a_D, e) \quad (6)$$

## Parameter Choices

We simply take parameters from Huggett's paper.

Exercise: implement the calibration.

Calibrated parameters:  $\beta, \delta, A$ .

Calibration targets:  $K/Y, w = 1, R$ .

## Preferences

$$u(c) = c^{1-\sigma}/(1-\sigma)$$

$$\sigma = 2.$$

Choose  $\beta$  to match  $K/Y = 2.9/\lambda$ .

## Demographics

Households live from age 20 to 79.

Work from 20 to 64 (45 years).

Retire for 15 years.

## Prices

- $w = 1$
- $R = 1.04$

## Government

$\tau_w = 0.4$  (Trostel 1993).

Set transfers to 40% of average earnings.

- This can be done before computing equilibrium.

## Labor Endowments

Can be set before equilibrium is computed.

Empirical studies estimate AR(1) processes for [log earnings] minus [mean log earnings,  $\eta_a$ ] by age.

New agents draw endowments from exogenous distribution:

$$\ln(e_1) \sim N(0, \sigma_1^2).$$

Over time, endowments are drawn from an AR(1):

$$\ln(e_a) = \eta_a + \gamma \ln(e_{a-1}) + \varepsilon_a.$$

$$\ln(\varepsilon_a) \sim N(0, \sigma_\varepsilon^2).$$

We follow [Huggett \(1996\)](#):

- $\sigma_1^2 = 0.38, \sigma_\varepsilon^2 = 0.045, \gamma = 0.96$ .

- Approximate the AR(1) on a grid of 18 states equally spaced over  $\pm 4\sigma_1$ .
- Add an additional state at  $+6\sigma_1$  to capture skewness of earnings distribution.
- Use Tauchen (1986) (we have code for that)

## Age-efficiency profile

From PSID data (Huggett, 1996)

## References

- HUGGETT, M. (1996): "Wealth distribution in life-cycle economies," *Journal of Monetary Economics*, 38, 469–494.
- TAUCHEN, G. (1986): "Finite state markov-chain approximations to univariate and vector autoregressions," *Economics letters*, 20, 177–181.