```
- MODULE StateSpace
1 1
    The graph representation of n-ary ordered state space and 2D state space used in CJupiter and
    XJupiter, respectively.
   EXTENDS JupiterCtx, GraphsUtil
 7 |
    IsSS(G) \stackrel{\Delta}{=} A state space is a digraph with labeled edges.
           \wedge IsGraph(G) It is a digraph (represented by a record).
9
           \land G.node \subseteq (SUBSET\ Oid) Each node represents a document state, i.e., a set of Oid.
10
           \land G.edqe \subseteq [from: G.node, to: G.node, cop: Cop] Each edge is labeled with a Cop operation.
11
    EmptySS \stackrel{\triangle}{=} EmptyGraph
13
14
    Locate(cop, ss) \stackrel{\Delta}{=} Locate the (unique) node in state space ss that matches the context ctx of cop.
15
         CHOOSE n \in ss.node : n = cop.ctx
16
    xFormSS(cop, copprime) \triangleq
                                           Transform cop against copprime on state space.
18
         Let u \triangleq cop.ctx
                                           Return the extra state space.
19
               v \stackrel{\triangle}{=} u \cup \{cop.oid\}
20
               uprime \stackrel{\triangle}{=} u \cup \{copprime.oid\}
21
               vprime \stackrel{\triangle}{=} u \cup \{cop.oid, copprime.oid\}
22
               cop2copprime \stackrel{\triangle}{=} COT(cop, copprime)
23
                copprime2cop \triangleq COT(copprime, cop)
24
                [node \mapsto \{u, v, uprime, vprime\},\]
25
                 edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto cop],
26
                             [from \mapsto u, to \mapsto uprime, cop \mapsto copprime],
27
                             [from \mapsto v, to \mapsto vprime, cop \mapsto copprime2cop],
28
                             [from \mapsto uprime, to \mapsto vprime, cop \mapsto cop2copprime]\}]
29
    xFormCopCopsSS(cop, cops) \triangleq
                                                    Transform cop against cops (a sequence of Cop) on state space.
31
         LET RECURSIVE xFormCopCopsSSHelper(\_, \_, \_) Return the extra state space.
32
                xFormCopCopsSSHelper(coph, copsh, xss) \stackrel{\Delta}{=} xss: the eXtra state space
33
                     Let u \triangleq coph.ctx
34
                           v \triangleq u \cup \{coph.oid\}
35
                      uvSS \stackrel{\Delta}{=} [node \mapsto \{u, v\}, edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto coph]\}]
36
                           If copsh = \langle \rangle then [lss \mapsto uvSS, xss \mapsto xss \oplus uvSS]
37
                             ELSE LET copprimeh \stackrel{\Delta}{=} Head(copsh)
38
                                               uprime \triangleq u \cup \{copprimeh.oid\}
39
                                               vprime \stackrel{\triangle}{=} u \cup \{coph.oid, copprimeh.oid\}
40
                                            coph2copprimeh \triangleq COT(coph, copprimeh)
                                             copprimeh2coph \triangleq COT(copprimeh, coph)
42
                                            xFormCopCopsSSHelper(coph2copprimeh, Tail(copsh),
43
                                                xss \oplus [node \mapsto \{u, v\},
44
                                                         edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto coph],
45
                                                                     [from \mapsto u, to \mapsto uprime, cop \mapsto copprimeh],
46
                                                                     [from \mapsto v, to \mapsto vprime, cop \mapsto copprimeh2coph]\}])
47
                xFormCopCopsSSHelper(cop, cops, EmptySS)
48
```