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- MODULE StateSpace
 1
     The graph representation of n-ary ordered state spaces and 2D state spaces used in CJupiter and
    XJupiter, respectively.
    EXTENDS JupiterCtx, GraphsUtil
 7 |
    A state space is a directed graph with labeled edges. Each node is characterized by its context, a
    set of operations. Each edge is labeled with an operation.
    IsSS(G) \triangleq
13
            \wedge IsGraph(G)
14
           \land G.node \subseteq (SUBSET\ Oid)
15
           \land G.edge \subseteq [from : G.node, to : G.node, cop : Cop]
16
    EmptySS \triangleq EmptyGraph
18
    Locate the node in a state space that matches the context ctx of cop.
    Locate(cop, ss) \stackrel{\Delta}{=} CHOOSE \ n \in ss.node : n = cop.ctx
    Do transformation on state space. Return the extra state space.
    xFormSS(cop, copprime) \stackrel{\Delta}{=}
26
         Let u \stackrel{\triangle}{=} cop.ctx
27
               \begin{array}{l} u & \stackrel{\frown}{=} u \cup \{cop.oid\} \\ uprime & \stackrel{\frown}{=} u \cup \{copprime.oid\} \end{array}
28
29
                vprime \stackrel{\triangle}{=} u \cup \{cop.oid, copprime.oid\}
30
                cop2copprime \stackrel{\triangle}{=} COT(cop, copprime)
31
                 copprime2cop \triangleq COT(copprime, cop)
32
                 [node \mapsto \{u, v, uprime, vprime\},\]
33
                  edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto cop],
34
                               [from \mapsto u, to \mapsto uprime, cop \mapsto copprime],
35
                               [from \mapsto v, to \mapsto vprime, cop \mapsto copprime2cop],
36
37
                               [from \mapsto uprime, to \mapsto vprime, cop \mapsto cop2copprime]\}]
    Transform cop against cops (a sequence of cops) on state space. Return the extra state space.
    xFormCopCopsSS(cop, cops) \stackrel{\Delta}{=}
42
         LET RECURSIVE xFormCopCopsSSHelper(_, _, _)
43
                 xFormCopCopsSSHelper(coph, copsh, xss) \stackrel{\Delta}{=}
                                                                                 xss: the eXtra state space
44
                      Let u \triangleq coph.ctx
45
                            v \triangleq u \cup \{coph.oid\}
                       uvSS \stackrel{\triangle}{=} [node \mapsto \{u, v\}, edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto coph]\}]
47
                       IN IF copsh = \langle \rangle Then [lss \mapsto uvSS, xss \mapsto xss \oplus uvSS]
48
                               ELSE LET copprimeh \stackrel{\triangle}{=} Head(copsh)
49
                                                 uprime \triangleq u \cup \{copprimeh.oid\}
50
                                                 vprime \stackrel{\Delta}{=} u \cup \{coph.oid, copprimeh.oid\}
51
                                              coph2copprimeh \triangleq COT(coph, copprimeh)
52
                                               copprimeh2coph \stackrel{\Delta}{=} COT(copprimeh, coph)
53
                                              xFormCopCopsSSHelper(coph2copprimeh, Tail(copsh),
54
                                                   xss \oplus [node \mapsto \{u, v\},
55
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 $edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto coph],$