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MODULE AbsJupiter -
 1 1
     Abstract Jupiter, inspired by the COT algorithm proposed by Sun and Sun. See their paper
    published on TPDS'2009.
    EXTENDS JupiterSerial
 7 |
    VARIABLES
         cseq,
                    cseq[c]: local sequence number at client c \in client
 9
         ds,
                    ds[r]: document state at replica r \in Replica
10
                    copss[r]: the state space (i.e., a set) of Cops maintained at replia r \in Replica
11
         copss
    vars \stackrel{\triangle}{=} \langle intVars, serialVars, cseq, ds, copss \rangle
13
14
     TypeOK \triangleq
15
               TypeOKInt
          Λ
16
17
               TypeOKSerial
               Comm(Cop)! TypeOK
18
               cseq \in [Client \rightarrow Nat]
19
               ds \in [Replica \rightarrow SUBSET \ Oid]
          \land
20
               copss \in [Replica \rightarrow SUBSET \ Cop]
21
22
    Init \triangleq
23
          \land InitInt
24
          \land InitSerial
25
          \land Comm(Cop)!Init
26
          \land cseq = [c \in Client \mapsto 0]
27
          \land ds = [r \in Replica \mapsto \{\}]
28
          \land copss = [r \in Replica \mapsto \{\}]
29
30
    RECURSIVE xForm(\_, \_)
31
    xForm(cop, r) \triangleq
32
         Let ctxDiff \triangleq ds[r] \setminus cop.ctx theorem : cop.ctx \subseteq ds[r]
33
               RECURSIVE xFormHelper(\_, \_, \_)
34
                xFormHelper(coph, ctxDiffh, copssr) \stackrel{\Delta}{=}
                                                                       'h' stands for "helper"
35
                     IF ctxDiffh = \{\}
36
                      THEN \langle coph, copssr \cup \{coph\} \rangle
37
                      ELSE LET foph \stackrel{\triangle}{=} CHOOSE \ op \in ctxDiffh: the first op (specifically, oid) in serial
38
                                                   \forall opprime \in ctxDiffh :
39
                                                      opprime \neq op \Rightarrow tb(op, opprime, serial[r])
40
                                    fcophDict \triangleq \{op \in copssr : op.oid = foph \land op.ctx = coph.ctx\}
41
                                    fcoph \stackrel{\triangle}{=} CHOOSE \ op \in fcophDict : TRUE \ THEOREM : Cardinality(fophDict) = 1
42
                                    cophx \triangleq COT(coph, fcoph)
43
                                     fcophx \triangleq COT(fcoph, coph)
44
                                   xFormHelper(cophx, ctxDiffh \setminus \{foph\}, copssr \cup \{cophx, fcophx\})
45
                xFormHelper(cop, ctxDiff, copss[r])
46
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Perform(cop, r) \triangleq
48
          LET xform \stackrel{\triangle}{=} xForm(cop, r) \quad \langle xcop, xcopss \rangle
49
                 xcop \triangleq xform[1]
xcopssr \triangleq xform[2]
50
51
                  \land state' = [state \ EXCEPT \ ![r] = Apply(xcop.op, @)]
52
                  \wedge ds' = [ds \text{ EXCEPT } ! [r] = @ \cup \{cop.oid\}]
53
                  \land copss' = [copss \ EXCEPT \ ![r] = xcopssr]
54
     Client c \in Client issues an operation op.
     DoOp(c, op) \stackrel{\Delta}{=} op: the raw operation generated by the client c \in Client
59
              \land cseq' = [cseq \ EXCEPT \ ![c] = @ + 1]
60
              \wedge LET cop \stackrel{\triangle}{=} [op \mapsto op, oid \mapsto [c \mapsto c, seq \mapsto cseq'[c]], ctx \mapsto ds[c]]
61
                       \wedge Perform(cop, c)
62
                        \land Comm(Cop)! CSend(cop)
63
     DoIns(c) \triangleq
65
          \exists \ ins \in \{op \in Ins : op.pos \in 1 .. (Len(state[c]) + 1) \land op.ch \in chins \land op.pr = Priority[c]\} :
66
              \wedge DoOp(c, ins)
67
              \wedge chins' = chins \setminus \{ins.ch\} We assume that all inserted elements are unique.
68
     DoDel(c) \triangleq
70
          \exists del \in \{op \in Del : op.pos \in 1 .. Len(state[c])\}:
71
72
              \wedge DoOp(c, del)
              \land UNCHANGED chins
73
     Do(c) \triangleq
75
            \wedge DoSerial(c)
76
            \land \lor DoIns(c)
77
                \vee DoDel(c)
78
79
     Rev(c) \triangleq
80
            \land Comm(Cop)! CRev(c)
81
            \land Perform(Head(cincoming[c]), c)
82
            \land RevSerial(c)
83
            \land UNCHANGED \langle chins, cseq \rangle
84
85
     SRev \triangleq
86
           \land \; Comm(\mathit{Cop}) ! \mathit{SRev}
87
           \wedge LET cop \stackrel{\triangle}{=} Head(sincoming)
88
                      \land Perform(cop, Server)
89
                      \land Comm(Cop)!SSendSame(cop.oid.c, cop)
90
           \land SRevSerial
           \land UNCHANGED \langle chins, cseq \rangle
92
93 |
    Next \triangleq
94
           \vee \exists c \in Client : Do(c) \vee Rev(c)
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98 Fairness \triangleq
99 WF_{vars}(SRev \lor \exists c \in Client : Rev(c))

101 Spec \triangleq Init \land \Box[Next]_{vars} \land Fairness

102 \land Fairness

\land Fairness
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