```
- Module CJupiter -
 1 [
    Model of our own CJupiter protocol.
 5 EXTENDS StateSpace, JupiterSerial
 6 <del>|</del>
    VARIABLES
                   css[r]: the n-ary ordered state space at replica r \in Replica
          css
    vars \triangleq \langle int Vars, ctx Vars, serial Vars, css \rangle
10
     TypeOK \stackrel{\triangle}{=}
12
                TypeOKInt
13
                TypeOKCtx
14
                TypeOKSerial
15
                Comm(Cop)! TypeOK
                \forall r \in Replica : IsSS(css[r])
17
18
    Init \stackrel{\triangle}{=}
19
          \wedge InitInt
20
          \wedge InitCtx
21
          \land \ InitSerial
22
          \land Comm(Cop)!Init
23
          \land css = [r \in Replica \mapsto EmptySS]
25 l
    xForm: Iteratively transform cop with a path through the css at replica r \in Replica, following
    the first edges.
    xForm(cop, r) \triangleq
          Let rcss \stackrel{\triangle}{=} css[r]
31
                u \triangleq Locate(cop, rcss)
32
                v \stackrel{\triangle}{=} u \cup \{cop.oid\}
33
                RECURSIVE xFormHelper(\_, \_, \_, \_)
                 xFormHelper(uh, vh, coph, xcss) \stackrel{\triangle}{=} xcss: eXtra css created during transformation
35
                      If uh = ds[r] then [xcss \mapsto xcss, \overline{xcop} \mapsto coph]
36
                       ELSE LET fedge \stackrel{\triangle}{=} \text{CHOOSE } e \in rcss.edge :
37
                                                      \wedge e.from = uh
38
                                                      \land \forall uhe \in rcss.edge \setminus \{e\}:
39
                                                            (uhe.from = uh) \Rightarrow tb(e.cop.oid, uhe.cop.oid, serial[r])
40
                                       uprime \triangleq fedge.to
41
                                      fcop \triangleq fedge.cop
42
                                       coph2fcop \triangleq COT(coph, fcop)
43
                                      fcop2coph \triangleq COT(fcop, coph)
44
                                        vprime \stackrel{\triangle}{=} vh \cup \{fcop.oid\}
45
                                       xFormHelper(uprime, vprime, coph2fcop,
46
                                            xcss \oplus [node \mapsto \{vprime\},\
                                                      edge \mapsto \{[from \mapsto vh, \ to \mapsto vprime, \ cop \mapsto fcop2coph], \}
48
                                                                   [from \mapsto uprime, to \mapsto vprime, cop \mapsto coph2fcop]\}])
49
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IN xFormHelper(u, v, cop, [node \mapsto \{v\}, edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto cop]\}])
 50
     Perform cop at replica r \in Replica.
     Perform(cop, r) \triangleq
 54
          LET xform \triangleq xForm(cop, r) xform: [xcss, xcop]
 55
                \land css' = [css \ \text{EXCEPT} \ ![r] = @ \oplus xform.xcss]
 56
                 \land state' = [state \ EXCEPT \ ![r] = Apply(xform.xcop.op, @)]
 57
 58
     Client c \in Client issues an operation op.
     DoOp(c, op) \triangleq
 62
              \wedge LET cop \stackrel{\triangle}{=} [op \mapsto op, oid \mapsto [c \mapsto c, seq \mapsto cseq'[c]], ctx \mapsto ds[c]]
 63
                       \land Perform(cop, c)
 64
                       \land Comm(Cop)! CSend(cop)
 65
     DoIns(c) \triangleq
 67
          \exists ins \in \{op \in Ins : op.pos \in 1 .. (Len(state[c]) + 1) \land op.ch \in chins \land op.pr = Priority[c]\}:
 68
              \wedge DoOp(c, ins)
 69
              \wedge chins' = chins \setminus \{ins.ch\}
 70
      DoDel(c) \triangleq
 72
          \exists del \in \{op \in Del : op.pos \in 1 .. Len(state[c])\}:
 73
              \wedge DoOp(c, del)
 74
              \land UNCHANGED chins
 75
     Do(c) \triangleq
 77
             \wedge DoCtx(c)
 78
             \wedge DoSerial(c)
 79
             \land \lor DoIns(c)
 80
 81
                \vee DoDel(c)
     Client c \in Client receives a message from the Server.
     Rev(c) \triangleq
 85
            \wedge Comm(Cop)! CRev(c)
 86
            \land Perform(Head(cincoming[c]), c)
 87
            \land RevSerial(c)
 88
            \wedge RevCtx(c)
 89
            ∧ UNCHANGED chins
 90
 91
     The Server receives a message.
     SRev \triangleq
 95
           \land Comm(Cop)!SRev
 96
           \wedge \text{ LET } cop \stackrel{\triangle}{=} Head(sincoming)
 97
                    \land Perform(cop, Server)
 98
                    \land Comm(Cop)!SSendSame(cop.oid.c, cop) broadcast the original operation
 99
           \land SRevSerial
100
           \wedge SRevCtx
101
           ∧ UNCHANGED chins
102
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103 ⊢
104 Next \triangleq
           \vee \exists c \in Client : Do(c) \vee Rev(c)
105
           \vee SRev
106
     Fairness \stackrel{\Delta}{=} There is no requirement that the clients ever generate operations.
108
          WF_{vars}(SRev \vee \exists c \in Client : Rev(c))
109
     Spec \triangleq Init \wedge \Box [Next]_{vars} \wedge Fairness (We care more about safety.)
111
112 ⊦
     Compactness \stackrel{\triangle}{=} The compactness of CJupiter: the CSSes at all replicas are the same.
113
          Comm(Cop)!EmptyChannel \Rightarrow Cardinality(Range(css)) = 1
114
116 THEOREM Spec \Rightarrow Compactness
117 └
      \* Modification History
      \* Last modified Mon Dec 31 11:02:07 CST 2018 by hengxin
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<sup>\*</sup> Created Sat Sep 01 11:08:00 CST 2018 by hengxin