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1  ┌────────────────────────── MODULE XJupiterImplCJupiter ───────────────────────────┐
  In this module, we show that XJupiter implements CJupiter. To this end, we first extends
  XJupiter by replacing its Cop with that used in CJupiter.
7  EXTENDS XJupiterExtended

9  VARIABLES
10   cincomingCJ, cincoming for CJupiter which contains original operations
11                  instead of transformed ones in XJupiter
12   op2ss,        a function from an operation (represented by its Oid)
13                  to the part of 2D state space produced while the operation is transformed
14   c2ssX          c2ssX[c]: redundant (eXtra) 2D state space maintained for client c ∈ Client

16  varsImpl  $\triangleq$   $\langle \text{vars}, \text{cincomingCJ}, \text{op2ss}, \text{c2ssX} \rangle$ 

18  TypeOKImpl  $\triangleq$ 
19    $\wedge \text{TypeOK}$ 
20    $\wedge \text{cincomingCJ} \in [\text{Client} \rightarrow \text{Seq}(\text{Cop})]$ 
21    $\wedge \forall \text{oid} \in \text{DOMAIN } \text{op2ss} : \text{oid} \in \text{Oid} \wedge \text{IsSS}(\text{op2ss}[\text{oid}])$ 
22    $\wedge \forall c \in \text{Client} : \text{IsSS}(\text{c2ssX}[c])$ 

  The Init predicate.
27  InitImpl  $\triangleq$ 
28    $\wedge \text{Init}$ 
29    $\wedge \text{cincomingCJ} = [c \in \text{Client} \mapsto \langle \rangle]$ 
30    $\wedge \text{op2ss} = \langle \rangle$ 
31    $\wedge \text{c2ssX} = [c \in \text{Client} \mapsto [\text{node} \mapsto \{\{\}\}, \text{edge} \mapsto \{\}]]$ 

  Client c ∈ Client generates an operation and performs it locally.
36  DoImpl(c)  $\triangleq$ 
37    $\wedge \text{Do}(c)$ 
38    $\wedge \text{UNCHANGED } \langle \text{cincomingCJ}, \text{op2ss}, \text{c2ssX} \rangle$ 

40  ss1  $\oplus$  ss2  $\triangleq$ 
41   [ss1 EXCEPT  $!\text{node} = @ \cup \text{ss2.node}$ ,
42     $!\text{edge} = @ \cup \text{ss2.edge}$ ]

  Client c ∈ Client receives a message and processes it.
46  RevImpl(c)  $\triangleq$ 
47    $\wedge \text{Rev}(c)$ 
48    $\wedge \text{cincomingCJ}[c] \neq \langle \rangle$  there are (original) operations to handle with
49    $\wedge \text{cincomingCJ}' = [\text{cincomingCJ} \text{ EXCEPT } ![c] = \text{Tail}(@)]$  also consume a message
50    $\wedge \text{LET } \text{cop} \triangleq \text{Head}(\text{cincoming}[c])$ 
51    $\text{IN } \text{c2ssX}' = [\text{c2ssX} \text{ EXCEPT } ![c] = @ \oplus \text{op2ss}[\text{cop.oid}]]$ 
52    $\wedge \text{UNCHANGED } \langle \text{op2ss} \rangle$ 

  Also broadcast the original operation to clients (using the cincomingCJ channels)

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57  $SRevImpl \triangleq$ 
58    $\wedge SRev$ 
59    $\wedge LET \ cop \triangleq [Head(sincoming) \text{ EXCEPT } !.sctx = soids]$ 
60      $c \triangleq cop.oid.c$ 
61      $ss \triangleq xForm(cop, s2ss[c], scur[c], Remote)$ 
62   IN    $\wedge cincomingCJ' = [cl \in Client \mapsto$ 
63         IF  $cl = c$ 
64           THEN  $cincomingCJ[cl]$ 
65           ELSE  $Append(cincomingCJ[cl], cop)]$ 
66      $\wedge op2ss' = op2ss @@ (cop.oid :> [node \mapsto Range(ss.node), edge \mapsto Range(ss.edge)])$ 
67    $\wedge UNCHANGED \langle c2ssX \rangle$ 

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The next-state relation.

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72  $NextImpl \triangleq$ 
73    $\vee \exists c \in Client : DoImpl(c) \vee RevImpl(c)$ 
74    $\vee SRevImpl$ 

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The specification.

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79  $SpecImpl \triangleq InitImpl \wedge \Box [NextImpl]_{varsImpl} \wedge WF_{varsImpl}(SRevImpl \vee \exists c \in Client : RevImpl(c))$ 

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Ignore the lr field in edges of 2D state space.

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84  $IgnoreDir(ss) \triangleq$ 
85    $[ss \text{ EXCEPT } !.edge =$ 
86      $\{[field \in (DOMAIN \ e \setminus \{“lr”\}) \mapsto e.field] : e \in @\}]$ 
87      $\{[from \mapsto e.from, to \mapsto e.to, cop \mapsto e.cop] : e \in @\}]$ 
89  $CJ \triangleq$  INSTANCE  $CJupiter$ 
90   WITH  $cincoming \leftarrow cincomingCJ,$ 
91      $css \leftarrow [r \in Replica \mapsto$ 
92       IF  $r = Server$ 
93         THEN  $IgnoreDir(SetReduce(\oplus, Range(s2ss), [node \mapsto \{\{\}, edge \mapsto \{\}\}))$ 
94         ELSE  $IgnoreDir(c2ss[r] \oplus c2ssX[r])],$ 
95      $cur \leftarrow [r \in Replica \mapsto$ 
96       IF  $r = Server$ 
97          $It \text{ SHOULD be that } Cardinality(Range(scur)) = 1$ 
98         THEN CHOOSE  $n \in Range(scur) : TRUE$ 
99         ELSE  $ccur[r]]$ 

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101 THEOREM  $SpecImpl \Rightarrow CJ!Spec$ 
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\ * Modification History
\ * Last modified Thu Nov 01 13:51:35 CST 2018 by hengxin
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