

```

1  |----- MODULE StateSpace -----|
   | The graph representation of  $n$ -ary ordered state space and 2D state space used in CJupiter and XJupiter, respectively. |
6  | EXTENDS JupiterCtx, GraphsUtil |
7  |-----|
8   $IsSS(G) \triangleq$  A state space is a digraph with labeled edges.
9     $\wedge IsGraph(G)$  It is a digraph (represented by a record).
10    $\wedge G.node \subseteq (SUBSET\ Oid)$  Each node represents a document state, i.e., a set of Oid.
11    $\wedge G.edge \subseteq [from : G.node, to : G.node, cop : Cop]$  Each edge is labeled with a Cop operation.

13  $EmptySS \triangleq EmptyGraph$ 
14 |-----|
15  $Locate(cop, ss) \triangleq$  Locate the (unique) node in state space  $ss$  that matches the context of  $cop$ .
16   CHOOSE  $n \in ss.node : n = cop.ctx$ 

18 RECURSIVE  $ExtractCopSeq(-, -, -, -)$  Extract Cop sequences starting with  $u$  in  $ss$  at replica  $r$ .
19  $ExtractCopSeq(NextEdge(-, -, -), r, u, ss) \triangleq$ 
20   IF  $u = ds[r]$  THEN  $\langle \rangle$ 
21   ELSE LET  $e \triangleq NextEdge(r, u, ss)$ 
22     IN  $\langle e.cop \rangle \circ ExtractCopSeq(NextEdge, r, e.to, ss)$ 

24  $xFormCopCopsSS(cop, cops) \triangleq$  Transform  $cop$  against  $cops$  (a sequence of Cop) on state space.
25   LET RECURSIVE  $xFormCopCopsSSHelper(-, -, -)$  Return the extra state space.
26      $xFormCopCopsSSHelper(coph, copsh, xss) \triangleq$   $xss$ : the eXtra state space
27     LET  $u \triangleq coph.ctx$ 
28      $v \triangleq u \cup \{coph.oid\}$ 
29      $uvSS \triangleq [node \mapsto \{u, v\}, edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto coph]\}]$ 
30     IN IF  $copsh = \langle \rangle$  THEN  $[xcop \mapsto coph, xss \mapsto xss \oplus uvSS, lss \mapsto uvSS]$ 
31     ELSE LET  $copprimeh \triangleq Head(copsh)$ 
32        $uprime \triangleq u \cup \{copprimeh.oid\}$ 
33        $vprime \triangleq u \cup \{coph.oid, copprimeh.oid\}$ 
34        $coph2copprimeh \triangleq COT(coph, copprimeh)$ 
35        $copprimeh2coph \triangleq COT(copprimeh, coph)$ 
36       IN  $xFormCopCopsSSHelper(coph2copprimeh, Tail(copsh),$ 
37          $xss \oplus [node \mapsto \{u, v\},$ 
38          $edge \mapsto \{[from \mapsto u, to \mapsto v, cop \mapsto coph],$ 
39          $[from \mapsto u, to \mapsto uprime, cop \mapsto copprimeh],$ 
40          $[from \mapsto v, to \mapsto vprime, cop \mapsto copprimeh2coph]\})$ 
41     IN  $xFormCopCopsSSHelper(cop, cops, EmptySS)$ 

43  $xFormSS(cop, copprime) \triangleq$  Transform  $cop$  against  $copprime$  on state space.
44   LET  $u \triangleq cop.ctx$  Return the extra state space.
45    $v \triangleq u \cup \{cop.oid\}$ 
46    $uprime \triangleq u \cup \{copprime.oid\}$ 
47    $vprime \triangleq u \cup \{cop.oid, copprime.oid\}$ 
48    $cop2copprime \triangleq COT(cop, copprime)$ 

```

```

49       $\text{copprime2cop} \triangleq \text{COT}(\text{copprime}, \text{cop})$ 
50      IN   $[\text{node} \mapsto \{u, v, \text{uprime}, \text{vprime}\},$ 
51           $\text{edge} \mapsto \{[\text{from} \mapsto u, \text{to} \mapsto v, \text{cop} \mapsto \text{cop}],$ 
52                   $[\text{from} \mapsto u, \text{to} \mapsto \text{uprime}, \text{cop} \mapsto \text{copprime}],$ 
53                   $[\text{from} \mapsto v, \text{to} \mapsto \text{vprime}, \text{cop} \mapsto \text{copprime2cop}],$ 
54                   $[\text{from} \mapsto \text{uprime}, \text{to} \mapsto \text{vprime}, \text{cop} \mapsto \text{cop2copprime}]]\}$ 
55  ]

```

```

\ * Modification History
\ * Last modified Tue Jan 08 14:33:51 CST 2019 by hengxin
\ * Created Wed Dec 19 18:15:25 CST 2018 by hengxin

```