# From Function1#compose to Kleisli

Different Ways of Function Composition

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## Abstract (1/2)

Fine-grained composability of functions is one of the core advantages of FP.

Treating "Functions as Data" means that we can ...

- store a function in a val
- pass it as args to other (higher order) functions (HOFs)
- return a function from other functions
- process/manipulate a function like data
- organize functions in data structures like List, Option etc.
- wrap a function in a case class

In this talk I demonstrate different ways of function composition.

I only deal with *scala.Function1*, because due to tupling and currying we can regard any function (except *Function0*) as a *Function1*. Curried functions are easier to compose.

## Abstract (2/2)

I start with the methods on *scala.Function1*: *compose* and *andThen*. Then I show how to fold a List of functions.

Then I turn to function composition with Monoids.

Functions are Functors, i.e they can be mapped over.
Functions are Monads, i.e they can be flatMapped over.
With *map* and *flatMap* we can write for-comprehensions over functions.
Being Monads, we can use functions in any monadic context.

The most powerful way of function composition is Kleisli and the Reader Monad.

## Agenda

- 1. Preliminaries
  - Kind Projector
  - Partial Unification
- 2. Functions as Data
- 3. Tupling and Currying Functions
- 4. Function1#compose and Function1#andThen
- 5. Monoidal Function Composition
- 6. Function1 as Functor
- 7. Function1 as Monad
- 8. Kleisli Composition done manually
- 9. case class Kleisli
- 10. Reader Monad
- 11. Resources

## 1. Preliminaries

- **1.1** Kind Projector
- 1.2 Partial Unification

### 1.1 Kind Projector - Compiler Plugin

Enable *kind-projector* in *build.sbt*:

```
addCompilerPlugin("org.spire-math" %% "kind-projector" % "0.9.7")
```

Kind projector on Github:

https://github.com/non/kind-projector

See: demo.Demo01aKindProjector

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```
trait Functor[F[_]] {
  def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

It is parameterized with a generic type constructor F[\_] which "has one hole", i.e. F[\_] needs another type parameter when reified.

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```
implicit val listFunctor: Functor[List] = new Functor[List] {
  override def map[A, B](fa: List[A])(f: A => B): List[B] = fa map f
}
implicit val optionFunctor: Functor[Option] = new Functor[Option] {
  override def map[A, B](fa: Option[A])(f: A => B): Option[B] = fa map f
}
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}
implicit val optionFunctor: Functor[Option] = new Functor[Option] {
  override def map[A, B](fa: Option[A])(f: A => B): Option[B] = fa map f
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But we can fix one of the type parameters and leave the other one open.

```
// Code compiles without kind-projector.
// It uses a type alias within a structural type.
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
   new Functor[({type f[x] = Either[L, x]})#f] {
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}
```

This is a type lambda (analogous to a partially applied function on the value level).

The type alias must be defined inside def eitherFunctor[L] because the type parameter L is used in the type alias. This is done inside a structural type where f is returned through a type projection.

```
Functor[({type f[x] = Either[L, x]})#f]
```

This code is ugly but can be improved if *kind-projector* is enabled.

```
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
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}
```

#### With *kind-projector*.

```
implicit def eitherFunctor[L]: Functor[Lambda[x => Either[L, x]]] =
  new Functor[Lambda[x => Either[L, x]]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

```
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
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}
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}
```

```
implicit def eitherFunctor[L]: Functor[\(\lambda[x => Either[L, x]]\)] =
  new Functor[\(\lambda[x => Either[L, x]]\)] {
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implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
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```

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implicit def eitherFunctor[L]: Functor[Lambda[x => Either[L, x]]] =
   new Functor[Lambda[x => Either[L, x]]] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}

implicit def eitherFunctor[L]: Functor[\(\lambla[x => Either[L, x]])] =
   new Functor[\(\lambla[x => Either[L, x]])] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}

implicit def eitherFunctor[L]: Functor[Either[L, ?]] =
   new Functor[Either[L, ?]] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

### 1.2 Compiler Flag -Ypartial-unification

Enable partial unification in *build.sbt*:

```
scalacOptions += "-Ypartial-unification"
```

See: demo.Demo01bPartialUnification

This code doesn't compile without -Ypartial-unification. Why?

```
def foo[F[ ], A](fa: F[A]): String = fa.toString
foo { x: Int => x * 2 }
[error] no type parameters for method foo: (fa: F[A])String exist
        so that it can be applied to arguments (Int => Int)
[error] --- because ---
[error] argument expression's type is not compatible with formal parameter type:
[error] found : Int => Int
[error] required: ?F[?A]
       foo { x: Int => x * 2 }
[error]
[error]
[error] type mismatch:
[error] found : Int => Int
[error] required: F[A]
        foo((x: Int) \Rightarrow x * 2)
[error]
```

This code doesn't compile without -*Ypartial-unification*. Why?

def foo requires a type constructor F[\_] with "one hole". It's kind is: \* --> \*.

foo is invoked with a function Int => Int. Int => Int is syntactic sugar for Function1[Int, Int]. Function1 like Either has two holes. It's kind is: \* --> \* --> \*.

#### The Solution:

-Ypartial-unification solves the problem by partially fixing (unifying) the type parameters <u>from left to right</u> until it fits to the number of holes required by the definition of *foo*.

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Imagine this flag turns *Function1[A, B]* into *Function1Int[B]*. With this fix on the fly *Function1Int* has kind \*--> \* which is the kind required by F[\_]. What the compiler transforms the invocation to would look something like this:

```
def foo[F[_], A](fa: F[A]): String = fa.toString
foo[Function1Int, Int] { x: Int => x * 2 }
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```
def foo[F[_], A](fa: F[A]): String = fa.toString
foo[Function1Int, Int] { x: Int => x * 2 }
```

Note that the partial unification fixes the types always in a <u>left-to-right order</u> which is a good fit for most cases where we have <u>right-biased types</u> like *Either*, *Tuple2* or *Function1*. (It is not a good fit for the very rare cases when you use a left-biased type like Scalactic's *Or* data type (a left-biased *Either*).)

## When to use *kind-projector* and *-Ypartial-unification*?

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Enable plugin and the flag when using a Functor, Applicative or a Monad instance for higher-kinded types which take more than one type parameter. *Either*, *Tuple2* and *Function1* are the best known representatives of this kind of types.

When programming on the type level regard both as your friends and keep them enabled.

## When to use *kind-projector* and *-Ypartial-unification*?

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When programming on the type level regard both as your friends and keep them enabled.

Very good explanations of partial unification by Miles Sabin and Daniel Spiewak can be found at these links:

https://github.com/scala/scala/pull/5102 https://gist.github.com/djspiewak/7a81a395c461fd3a09a6941d4cd040f2

## 2. Functions as Data

allows us to ...

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• store a function in a val

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val str2Int: String => Int = str => str.toInt
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• pass it as arg to other (higher order) functions (HOFs)

```
val mapped = List("1", "2", "3").map(str2Int)
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val mapped = List("1", "2", "3").map(str2Int)
```

• return a function from other functions

```
val plus100: Int => Int = { i =>
  val j = manipulate(i)
  j + 100
}
```

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store a function in a val

```
val str2Int: String => Int = str => str.toInt
```

• pass it as arg to other (higher order) functions (HOFs)

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val mapped = List("1", "2", "3").map(str2Int)
```

• return a function from other functions

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val plus100: Int => Int = { i =>
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   j + 100
}
```

• process/manipulate a function like data

```
str2Int map plus100 // Functor instance for Function1 must be defined
```

allows us to ...

# Treating Functions as Data (2/2)

allows us to ...

• organize functions (like data) in data structures like List, Option etc.

```
val functions: List[Int => Int] = List(_ + 1, _ + 2, _ + 3)
val f[Int => Int] = functions.foldRight(...)(...)
```

# Treating Functions as Data (2/2)

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```
val functions: List[Int => Int] = List(_ + 1, _ + 2, _ + 3)
val f[Int => Int] = functions.foldRight(...)(...)
```

• wrap a function in a case class *MyWrapper* 

We can define methods on *MyWrapper* which manipulate the wrapped function and return the manipulation result again wrapped in a new instance of *case class MyWrapper*.

```
case class MyWrapper[A, B](run: A => B) {
  def map[C](f: B => C): MyWrapper[A, C] = ???
  def flatMap[C](f: B => MyWrapper[A, C]): MyWrapper[A, C] = ???
  // other methods ...
}
```

# 3. Tupling and Currying Functions

See: demo.Demo03aTupledFunctions demo.Demo03bCurriedFunctions

... if you tuple up it's parameters.

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```
val sumTupled: ((Int, Int, Int)) => Int = sum3Ints.tupled
// sumTupled: ((Int, Int, Int)) => Int = scala.Function3$$Lambda$1018/1492801385@4
val sumTupled2: Function1[(Int, Int, Int), Int] = sum3Ints.tupled
// sumTupled2: ((Int, Int, Int)) => Int = scala.Function3$$Lambda$1018/1492801385@
val resTupled = sumTupled((1,2,3)) // 6
val resTupled2 = sumTupled2((1,2,3)) // 6
```

... if you tuple up it's parameters.

```
val sumTupled: ((Int, Int, Int)) => Int = sum3Ints.tupled
// sumTupled: ((Int, Int, Int)) => Int = scala.Function3$$Lambda$1018/1492801385@4
val sumTupled2: Function1[(Int, Int, Int), Int] = sum3Ints.tupled
// sumTupled2: ((Int, Int, Int)) => Int = scala.Function3$$Lambda$1018/1492801385@
val resTupled = sumTupled((1,2,3)) // 6
val resTupled2 = sumTupled2((1,2,3)) // 6
```

If untupled again, we get the original function back.

```
val sumUnTupled: (Int, Int, Int) => Int = Function.untupled(sumTupled)
// sumUnTupled: (Int, Int, Int) => Int = scala.Function$$$Lambda$3583/1573807728@7
val resUnTupled = sumUnTupled(1,2,3) // 6
```

... if you curry it.

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```
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
// sumCurried: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/9914305
```

... if you curry it.

```
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
// sumCurried: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/9914305
```

The type arrow ( => ) is right associative. Hence we can omit the parentheses.

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The type arrow ( $\Rightarrow$ ) is syntactic sugar for *Function1*.  $A \Rightarrow B$  is equivalent to *Function1[A, B]*.

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The type arrow ( $\Rightarrow$ ) is syntactic sugar for *Function1*.  $A \Rightarrow B$  is equivalent to *Function1[A, B]*.

```
val sumCurried2: Function1[Int, Function1[Int, Function1[Int, Int]]] = sumCurried
// sumCurried2: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/991430
```

... if you curry it.

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val sumCurried: Int => Int => Int => Int = sum3Ints.curried
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The type arrow ( $\Rightarrow$ ) is syntactic sugar for *Function1*.  $A \Rightarrow B$  is equivalent to *Function1[A, B]*.

```
val sumCurried2: Function1[Int, Function1[Int, Function1[Int, Int]]] = sumCurried
// sumCurried2: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/991430
```

If uncurried again, we get the original function back.

```
val sumUncurried: (Int, Int, Int) => Int = Function.uncurried(sumCurried)
// sumUncurried: (Int, Int, Int) => Int = scala.Function$$$Lambda$6605/301079867@1
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int => sum3Ints.curried
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int => sum3Ints.curried

val applied1st: Int => Int => Int = sumCurried(1)
// applied1st: Int => (Int => Int) = scala.Function3$$Lambda$4348/1531035406@5a231
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int = sum3Ints.curried

val applied1st: Int => Int => Int = sumCurried(1)
// applied1st: Int => (Int => Int) = scala.Function3$$Lambda$4348/1531035406@5a231
val applied2nd: Int => Int = applied1st(2)
// applied2nd: Int => Int = scala.Function3$$Lambda$4349/402963549@117e96fb
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ +
val sumCurried: Int => Int => Int = sumSInts.curried

val applied1st: Int => Int => Int = sumCurried(1)
// applied1st: Int => (Int => Int) = scala.Function3$$Lambda$4348/1531035406@5a231

val applied2nd: Int => Int = applied1st(2)
// applied2nd: Int => Int = scala.Function3$$Lambda$4349/402963549@117e96fb

val applied3rd: Int = applied2nd(3)
// applied3rd: Int = 6
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int => Int = sumCurried(1)
// applied1st: Int => Int => Int = sumCurried(1)
// applied2st: Int => (Int => Int) = scala.Function3$$Lambda$4348/1531035406@5a231
val applied2nd: Int => Int = applied1st(2)
// applied2nd: Int => Int = scala.Function3$$Lambda$4349/402963549@117e96fb

val applied3rd: Int = applied2nd(3)
// applied3rd: Int = 6

val appliedAllAtOnce: Int = sumCurried(1)(2)(3)
// appliedAllAtOnce: Int = 6
```

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They are <u>easier to compose</u> than their uncurried counterparts.

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```
def filter2[A](la: List[A])(p: A => Boolean) = ??? // curried

scala> filter2(List(0,1,2))(_ < 2)
res5: List[Int] = List(0,1)</pre>
```

# 4. Function1#compose and Function1#andThen

See: demo.Demo04ComposingFunctions

#### Trait Function1

```
trait Function1[-T1, +R] {
    def apply(a: T1): R
    def compose[A](g: A => T1): A => R = { x => apply(g(x)) }
    def andThen[A](g: R => A): T1 => A = { x => g(apply(x)) }
    override def toString = "<function1>"
}
```

#### Trait Function1

```
trait Function1[-T1, +R] {

    def apply(a: T1): R
    def compose[A](g: A => T1): A => R = { x => apply(g(x)) }
    def andThen[A](g: R => A): T1 => A = { x => g(apply(x)) }
    override def toString = "<function1>"
}
```

```
scala> val f: Int => Int = _ + 10
f: Int => Int = $$Lambda$4204/320646851@733dc5b7

scala> val g: Int => Int = _ * 2
g: Int => Int = $$Lambda$4205/1093482910@3a179009

scala> (f compose g apply 1) == f(g(1))
res6: Boolean = true

scala> (f andThen g apply 1) == g(f(1))
res7: Boolean = true
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

```
val s2i: String => Int = _.toInt
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val d2s: Double => String = _.toString
```

```
// Function1#compose
val fComposed1: String => String = d2s compose div10By compose plus2 compose s2i
val res1 = fComposed1("3") // 2.0 !!!
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

```
// Function1#compose
val fComposed1: String => String = d2s compose div10By compose plus2 compose s2i
val res1 = fComposed1("3") // 2.0 !!!
```

```
// Function1#andThen
val fComposed2: String => String = s2i andThen plus2 andThen div10By andThen d2s
val res2 = fComposed2("3") // 2.0 !!!
```

# Folding a List of Functions

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```
val lf: List[Int => Int] = List(_*2, _+10, _+100)
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)
// 222
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)

// 222

val lfFoldedLeft = lf.foldLeft(identity[Int] _) {(acc, f) => acc andThen f}
val resLfFoldedLeft = lfFoldedLeft(1)
// 112
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)
// 222

val lfFoldedLeft = lf.foldLeft(identity[Int] _) {(acc, f) => acc andThen f}
val resLfFoldedLeft = lfFoldedLeft(1)
// 112
```

The *identity* function is the no-op of function composition.

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)
// 222

val lfFoldedLeft = lf.foldLeft(identity[Int] _) {(acc, f) => acc andThen f}
val resLfFoldedLeft = lfFoldedLeft(1)
// 112
```

The *identity* function is the no-op of function composition.

Folding functions is not a commutative operation! Hence *foldRight* and *foldLeft* return different results.

# 5. Monoidal Function Composition

See: demo.Demo05ComposingWithMonoid

#### Trait Monoid

```
trait Monoid[A] {
    def empty: A
    def combine(x: A, y: A): A

    def combineAll(as: List[A]): A = // combines all functions in a List of funct
        as.foldLeft(empty)(combine)
}
```

#### Default Monoid Instance for *Function1*

```
// This one is the default Function1-Monoid in Cats.
// It requires the result type B to be a Monoid too.
//
implicit def function1Monoid[A, B: Monoid]: Monoid[A => B] = new Monoid[A => B] {
    override def empty: A => B =
        _ => Monoid[B].empty
    override def combine(f: A => B, g: A => B): A => B =
        a => Monoid[B].combine(f(a), g(a))
}
```

#### Default Monoid Instance for *Function1*

```
// This one is the default Function1-Monoid in Cats.
// It requires the result type B to be a Monoid too.
//
implicit def function1Monoid[A, B: Monoid]: Monoid[A => B] = new Monoid[A => B] {
    override def empty: A => B =
        _ => Monoid[B].empty
    override def combine(f: A => B, g: A => B): A => B =
        a => Monoid[B].combine(f(a), g(a))
}
```

- This instance defines a Monoid for Functions of type  $A \Rightarrow B$ .
- It requires type *B* to be a Monoid too.
- *empty* defines a function which ignores it's input and returns *Monoid[B].empty*.
- *combine* takes two functions f and g, invokes f(a) and g(a) on it's input and returns the combined result.

# Composition with Monoid

```
val f: Int => Int = _ + 1
val g: Int => Int = _ * 2
val h: Int => Int = _ + 100
```

# Composition with Monoid

```
val f: Int => Int = _ + 1
val g: Int => Int = _ * 2
val h: Int => Int = _ + 100
```

# Composition with Monoid

```
val f: Int => Int = _ + 1
val g: Int => Int = _ * 2
val h: Int => Int = _ + 100
```

Other Monoid instances for *Function1* yield different results.

# Instance for *function1ComposeMonoid*

```
implicit def function1ComposeMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f compose g
}
```

# Instance for *function1ComposeMonoid*

```
implicit def function1ComposeMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f compose g
}
```

- This instance composes the Functions with *Function1#compose*.
- It works only for functions of type  $A \Rightarrow A$ . (Input and output type are the same type.)

# Instance for *function1ComposeMonoid*

```
implicit def function1ComposeMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f compose g
}
```

- This instance composes the Functions with *Function1#compose*.
- It works only for functions of type  $A \Rightarrow A$ . (Input and output type are the same type.)

#### Instance for *function1AndThenMonoid*

```
implicit def function1AndThenMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f andThen g
}
```

#### Instance for *function1AndThenMonoid*

```
implicit def function1AndThenMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f andThen g
}
```

- This instance composes the Functions with *Function1#andThen*.
- It works only for functions of type  $A \Rightarrow A$ . (Input and output type are the same type.)

#### Instance for *function1AndThenMonoid*

```
implicit def function1AndThenMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f andThen g
}
```

- This instance composes the Functions with *Function1#andThen*.
- It works only for functions of type  $A \Rightarrow A$ . (Input and output type are the same type.)

# 6. Function1 as Functor

See: demo.Demo06Functor

#### **Functor**

A Functor is any Context F[] that provides a function  $map \dots$  and abides by the Functor laws (not presented here).

```
trait Functor[F[_]] {
   def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

#### Functor instance

A Functor instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Functor* companion object):

```
implicit def function1Functor[P]: Functor[Function1[P, ?]] =
  new Functor[Function1[P, ?]] {
    override def map[A, B](f: Function1[P, A])(g: A => B): Function1[P, B] =
        f andThen g
}
```

#### Functor instance

A Functor instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Functor* companion object):

```
implicit def function1Functor[P]: Functor[Function1[P, ?]] =
  new Functor[Function1[P, ?]] {
    override def map[A, B](f: Function1[P, A])(g: A => B): Function1[P, B] =
        f andThen g
}
```

A Functor instance for *Either* (just for comparison):

```
implicit def eitherFunctor[L]: Functor[Either[L, ?]] =
  new Functor[Either[L, ?]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] =
        fa map f
}
```

#### Functor instance

A Functor instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Functor* companion object):

```
implicit def function1Functor[P]: Functor[Function1[P, ?]] =
  new Functor[Function1[P, ?]] {
    override def map[A, B](f: Function1[P, A])(g: A => B): Function1[P, B] =
        f andThen g
}
```

A Functor instance for *Either* (just for comparison):

```
implicit def eitherFunctor[L]: Functor[Either[L, ?]] =
  new Functor[Either[L, ?]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] =
    fa map f
}
```

Using the *Function1* Functor:

```
val f: Int => Int = _ + 3
val g: Int => Int = _ * 2
val h = Functor[Function1[Int, ?]].map(f)(g)
val res = h(2) // 10
```

defined as <u>implicit conversion</u> ...

defined as implicit conversion ...

in a specific way for *Functor[Function1]*:

```
implicit class FunctorSyntaxFunction1[P, A](fa: Function1[P, A]) {
  def map[B](f: A => B): Function1[P, B] = Functor[Function1[P, ?]].map(fa)(f)
}
```

defined as implicit conversion ...

in a specific way for *Functor*[Function1]:

```
implicit class FunctorSyntaxFunction1[P, A](fa: Function1[P, A]) {
  def map[B](f: A => B): Function1[P, B] = Functor[Function1[P, ?]].map(fa)(f)
}
```

or in a generic way for any *Functor[F[\_]]*:

```
implicit class FunctorSyntax[F[_]: Functor, A](fa: F[A]) {
  def map[B](f: A => B): F[B] = Functor[F].map(fa)(f)
}
```

defined as <u>implicit conversion</u> ...

in a specific way for *Functor*[Function1]:

```
implicit class FunctorSyntaxFunction1[P, A](fa: Function1[P, A]) {
  def map[B](f: A => B): Function1[P, B] = Functor[Function1[P, ?]].map(fa)(f)
}
```

or in a generic way for any *Functor[F[\_]]*:

```
implicit class FunctorSyntax[F[_]: Functor, A](fa: F[A]) {
  def map[B](f: A => B): F[B] = Functor[F].map(fa)(f)
}
```

This allows for convenient invocation of *map* as if *map* were a method of *Function1*:

```
val f: Int => Int = _ + 3
val g: Int => Int = _ * 2
val h = f map g
val res = h(2) // 10
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

#### composed with *map*:

```
val fMapped = s2i map plus2 map div10By map d2s // requires -Ypartial-unification
val res1 = fMapped("3") // 2.0 !!!
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

#### composed with *map*:

```
val fMapped = s2i map plus2 map div10By map d2s // requires -Ypartial-unification
val res1 = fMapped("3") // 2.0 !!!
```

Function1 can also be seen as a Monad ...

# 7. Function1 as Monad

See: demo.Demo07Monad

#### Monad

A Monad is any Context F[\_] that provides the functions *pure* and *flatMap* ... and abides by the Monad laws (not presented here).

```
trait Monad[F[_]] extends Functor[F] {
  def pure[A](a: A): F[A]
  def flatMap[A, B](fa: F[A])(f: A => F[B]): F[B]
}
```

#### Monad instance

A Monad instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Monad* companion object):

```
implicit def function1Monad[P]: Monad[P => ?] = new Monad[P => ?] {
  override def pure[A](r: A): P => A = _ => r
  override def flatMap[A, B](f: P => A)(g: A => P => B)
    : P => B = p => g(f(p))(p)
}
```

#### Monad instance

A Monad instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Monad* companion object):

```
implicit def function1Monad[P]: Monad[P => ?] = new Monad[P => ?] {
  override def pure[A](r: A): P => A = _ => r
  override def flatMap[A, B](f: P => A)(g: A => P => B)
    : P => B = p => g(f(p))(p)
}
```

Alternative instance definition:

```
implicit def function1Monad[P]: Monad[Function1[P, ?]] = new Monad[Function1[P, ?]
  override def pure[A](r: A): Function1[P, A] = _ => r
  override def flatMap[A, B](f: Function1[P, A])(g: A => Function1[P, B])
    : Function1[P, B] = p => g(f(p))(p)
}
```

#### Monad instance

A Monad instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Monad* companion object):

```
implicit def function1Monad[P]: Monad[P => ?] = new Monad[P => ?] {
  override def pure[A](r: A): P => A = _ => r
  override def flatMap[A, B](f: P => A)(g: A => P => B)
    : P => B = p => g(f(p))(p)
}
```

Alternative instance definition:

```
implicit def function1Monad[P]: Monad[Function1[P, ?]] = new Monad[Function1[P, ?]
  override def pure[A](r: A): Function1[P, A] = _ => r
  override def flatMap[A, B](f: Function1[P, A])(g: A => Function1[P, B])
  : Function1[P, B] = p => g(f(p))(p)
}
```

A Monad instance for *Either* (just for comparison):

```
implicit def eitherMonad[L]: Monad[Either[L, ?]] = new Monad[Either[L, ?]] {
   override def pure[A](r: A): Either[L, A] = Right(r)
   override def flatMap[A, B](fa: Either[L, A])(f: A => Either[L, B])
   : Either[L, B] = fa flatMap f
}
```

# Monad syntax

defined as <u>implicit conversion</u> ...

# Monad syntax

defined as implicit conversion ...

in a specific way for *Monad[Function1]*:

```
implicit class MonadSyntaxFunction1[P, A](f: Function1[P, A]) {
  def flatMap[B](g: A => P => B): P => B = Monad[Function1[P, ?]].flatMap(f)(g)
}
```

# Monad syntax

defined as implicit conversion ...

in a specific way for *Monad[Function1]*:

```
implicit class MonadSyntaxFunction1[P, A](f: Function1[P, A]) {
  def flatMap[B](g: A => P => B): P => B = Monad[Function1[P, ?]].flatMap(f)(g)
}
```

or in a generic way for any *Monad[F[\_]]*:

```
implicit class MonadSyntax[F[_]: Monad, A](fa: F[A]) {
  def flatMap[B](f: A => F[B]): F[B] = Monad[F].flatMap(fa)(f)
}
```

## Monad syntax

defined as <u>implicit conversion</u> ...

in a specific way for *Monad[Function1]*:

```
implicit class MonadSyntaxFunction1[P, A](f: Function1[P, A]) {
  def flatMap[B](g: A => P => B): P => B = Monad[Function1[P, ?]].flatMap(f)(g)
}
```

or in a generic way for any *Monad[F[\_]]*:

```
implicit class MonadSyntax[F[_]: Monad, A](fa: F[A]) {
  def flatMap[B](f: A => F[B]): F[B] = Monad[F].flatMap(fa)(f)
}
```

This allows for convenient invocation of *flatMap* as if *flatMap* were a method of *Function1*:

```
val h = f flatMap g
```

instead of:

```
val h = Monad[Function1[Int, ?]].flatMap(f)(g)
111 / 172
```

```
val countLines: String => Int = text => text.split("\n").length
val countWords: String => Int = text => text.split("\\W+").length
val countChars: String => Int = text => text.length
```

```
val countLines: String => Int = text => text.split("\n").length
val countWords: String => Int = text => text.split("\\W+").length
val countChars: String => Int = text => text.length
```

#### FlatMapping over *Function1*:

```
val countLines: String => Int = text => text.split("\n").length
val countWords: String => Int = text => text.split("\\W+").length
val countChars: String => Int = text => text.length
```

#### FlatMapping over *Function1*:

#### alternatively with a for-comprehension:

#### Another Reader Monad example - a bit more realistic ...

```
val users: Map[Int, String] = Map(
          1 -> "dade", 2 -> "kate", 3 -> "margo")
val passwords: Map[String, String] = Map(
          "dade" -> "zerocool", "kate" -> "acidburn", "margo" -> "secret")
case class Db(usernames: Map[Int, String], passwords: Map[String, String])
val db = Db(users, passwords)
type DbReader[A] = Db => A // ^= Function1[Db, A]
def findUsername(userId: Int): DbReader[Option[String]] =
  db => db.usernames.get(userId)
def checkPassword(username: String, password: String): DbReader[Boolean] =
  db => db.passwords.get(username).contains(password)
def checkLogin(userId: Int, password: String): DbReader[Boolean] = // ^= Function1
  for {
    optUsername <- findUsername(userId)</pre>
    passwordOk <- optUsername
      .map(name => checkPassword(name, password))
      .qetOrElse(( :Db) => false)
  } vield password0k
val login0k1 = checkLogin(1, "zerocool")(db) // true
val login0k2 = checkLogin(4, "davinci")(db) // false
```

Example taken from "Scala with Cats" (see chapter Resources for link)

# 8. Kleisli composition done manually

See: demo.Demo08KleisliDoneManually

```
// Functions: A => F[B], where F is Option in this case
val s2iOpt: String => Option[Int] = s => Option(s.toInt)
val plus2Opt: Int => Option[Int] = i => Option(i + 2)
val div10ByOpt: Int => Option[Double] = i => Option(10.0 / i)
val d2sOpt: Double => Option[String] = d => Option(d.toString + " !!!")
```

These functions take an A and return a B inside of a context  $F[_]: A \Rightarrow F[B]$  In our case  $F[_]$  is Option, but could be List, Future etc.

```
// Functions: A => F[B], where F is Option in this case
val s2iOpt: String => Option[Int] = s => Option(s.toInt)
val plus2Opt: Int => Option[Int] = i => Option(i + 2)
val div10ByOpt: Int => Option[Double] = i => Option(10.0 / i)
val d2sOpt: Double => Option[String] = d => Option(d.toString + " !!!")
```

These functions take an A and return a B inside of a context  $F[_]: A \Rightarrow F[B]$  In our case  $F[_]$  is Option, but could be List, Future etc.

We want to compose these functions to a single function which is then fed with some input string.

```
// Functions: A => F[B], where F is Option in this case
val s2iOpt: String => Option[Int] = s => Option(s.toInt)
val plus2Opt: Int => Option[Int] = i => Option(i + 2)
val div10ByOpt: Int => Option[Double] = i => Option(10.0 / i)
val d2sOpt: Double => Option[String] = d => Option(d.toString + " !!!")
```

These functions take an A and return a B inside of a context  $F[_]: A \Rightarrow F[B]$  In our case  $F[_]$  is Option, but could be List, Future etc.

We want to compose these functions to a single function which is then fed with some input string.

Let's try map.

```
val fMapped: String => Option[Option[Option[Option[String]]]] = str =>
    s2iOpt(str) map { i1 =>
    plus2Opt(i1) map { i2 =>
        div10ByOpt(i2) map {
        d => d2sOpt(d)
    }
}}
```

We get nested *Options*. So lets try *flatMap* on the *Option* context.

with *flatMap* (this works):

```
val flatMappedOnOpt1: String => Option[String] = input =>
    s2iOpt(input) flatMap { i1 =>
        plus2Opt(i1) flatMap { i2 =>
            div10ByOpt(i2) flatMap { d =>
                  d2sOpt(d)
        }}}
val res1: Option[String] = flatMappedOnOpt1("3") // Some(2.0)
```

with *flatMap* (this works):

or with a for-comprehension (this looks nicer):

```
val flatMappedOnOpt2: String => Option[String] = input => for {
   i1 <- s2iOpt(input)
   i2 <- plus2Opt(i1)
   d <- div10ByOpt(i2)
   s <- d2sOpt(d)
} yield s
val res2: Option[String] = flatMappedOnOpt2("3") // Some(2.0)</pre>
```

with *flatMap* (this works):

or with a for-comprehension (this looks nicer):

```
val flatMappedOnOpt2: String => Option[String] = input => for {
   i1 <- s2iOpt(input)
   i2 <- plus2Opt(i1)
   d <- div10ByOpt(i2)
   s <- d2sOpt(d)
} yield s
val res2: Option[String] = flatMappedOnOpt2("3") // Some(2.0)</pre>
```

<u>But:</u> We still have to bind the variables *i1*, *i2*, *d* and *s* to names. We would like to build a function pipeline with some kind of *andThenF*.

s2iOpt andThenF plus2Opt andThenF div10ByOpt andThenF d2sOpt

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

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Let's define kleisli:

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

Let's define *kleisli*:

```
def kleisli[F[_]: Monad, A, B, C](f: A => F[B], g: B => F[C]): A => F[C] =
    a => Monad[F].flatMap(f(a))(g)
```

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

Let's define *kleisli*:

```
def kleisli[F[_]: Monad, A, B, C](f: A => F[B], g: B => F[C]): A => F[C] =
    a => Monad[F].flatMap(f(a))(g)
```

#### Using *kleisli*:

```
val kleisliComposed1: String => Option[String] =
   kleisli(kleisli(s2iOpt, plus2Opt), div10ByOpt), d2sOpt)
val resKleisli1 = kleisliComposed1("3") // 2.0 !!!
```

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

Let's define *kleisli*:

```
def kleisli[F[_]: Monad, A, B, C](f: A => F[B], g: B => F[C]): A => F[C] =
    a => Monad[F].flatMap(f(a))(g)
```

Using *kleisli*:

```
val kleisliComposed1: String => Option[String] =
   kleisli(kleisli(s2iOpt, plus2Opt), div10ByOpt), d2sOpt)
val resKleisli1 = kleisliComposed1("3") // 2.0 !!!
```

This works, but is still not exactly what we want. *kleisli* should behave like a method of *Function1*.

with an implicit conversion:

with an implicit conversion:

#### Using it:

```
val kleisliComposed2: String => Option[String] =
   s2iOpt kleisli plus2Opt kleisli div10ByOpt kleisli d2sOpt
kleisliComposed2("3") foreach println // 2.0 !!!
```

with an implicit conversion:

#### Using it:

```
val kleisliComposed2: String => Option[String] =
   s2iOpt kleisli plus2Opt kleisli div10ByOpt kleisli d2sOpt
kleisliComposed2("3") foreach println // 2.0 !!!
```

(s2iOpt andThenF plus2Opt andThenF div10ByOpt andThenF d2sOpt) foreach println

with an implicit conversion:

#### Using it:

# 9. case class Kleisli

See: demo.Demo09KleisliCaseClass

## case class Kleisli

That was my artefact. Cats does not provide a *kleisli* method on *Function1*. Cats instead provides a *case class Kleisli* with the functionality shown above and more.

#### case class Kleisli

That was my artefact. Cats does not provide a *kleisli* method on *Function1*. Cats instead provides a *case class Kleisli* with the functionality shown above and more.

I tinkered my own impl in *mycats.Kleisli* which works much like the Cats impl: see next slide.

#### case class Kleisli

```
case class Kleisli[F[ ], A, B](run: A => F[B]) {
 def apply(a: A): F[B] = run(a)
 def map[C](f: B => C)(implicit F: Functor[F]): Kleisli[F, A, C] =
    Kleisli { a => F.map(run(a))(f) }
 def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C]
    Kleisli { a => M.flatMap(run(a))(b => f(b).run(a)) }
  def flatMapF[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    Kleisli { a => M.flatMap(run(a))(f) }
  def andThen[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    flatMapF(f)
 def andThen[C](that: Kleisli[F, B, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    this and Then that.run
  def compose[Z](f: Z => F[A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
    Kleisli(f) and Then this.run
  def compose[Z](that: Kleisli[F, Z, A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
    that andThen this
```

The case class methods delegate to the wrapped *run* function and return the resulting *run* function rewrapped in a *Kleisli* instance.

#### *Kleisli* companion object with Monad instance

```
object Kleisli { self =>

def pure[F[_], A, B](b: B)(implicit F: Monad[F]): Kleisli[F, A, B] =
    Kleisli { _ => F.pure(b) }

object ops {

implicit def kleisliMonad[F[_] : Monad, A]: Monad[Kleisli[F, A, ?]] =
    new Monad[Kleisli[F, A, ?]] {

    override def pure[B](b: B): Kleisli[F, A, B] = self.pure(b)

    override def flatMap[B, C](kl: Kleisli[F, A, B])(f: B => Kleisli[F, A, C])
        : Kleisli[F, A, C] = kl flatMap f
    }
}
```

## Kleisli#flatMap

```
def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    M.flatMap(run(a))(b => f(b).run(a))
}
```

flatMap composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow Kleisli[F, A, C]$  yielding a new Kleisli[F, A, C] wrapping a new function  $F(A) \Rightarrow F(C)$ .

# Kleisli#flatMap

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def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    M.flatMap(run(a))(b => f(b).run(a))
}
```

flatMap composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow Kleisli[F, A, C]$  yielding a new Kleisli[F, A, C] wrapping a new function F(C).

```
val kleisli1: String => Option[String] = input =>
   Kleisli(s2iOpt).run(input) flatMap { i1 =>
        Kleisli(plus2Opt).run(i1) flatMap { i2 =>
        Kleisli(div10ByOpt).run(i2) flatMap { d =>
        Kleisli(d2sOpt).run(d)
        }   }
   kleisli1("3") foreach println
```

# Kleisli#flatMap

```
def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    M.flatMap(run(a))(b => f(b).run(a))
}
```

flatMap composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow Kleisli[F, A, C]$  yielding a new Kleisli[F, A, C] wrapping a new function  $F(A) \Rightarrow F(C)$ .

```
val kleisli2: String => Option[String] = input => for {
   i1 <- Kleisli(s2iOpt).run(input)
   i2 <- Kleisli(plus2Opt).run(i1)
   d <- Kleisli(div10ByOpt).run(i2)
   s <- Kleisli(d2sOpt).run(d)
} yield s
kleisli2("3") foreach println</pre>
```

## Kleisli#flatMapF

As we saw *Kleisli#flatMap* is not very convenient. We have to bind values to variables and thread them through the for-comprehension. *flatMapF* is easier to use.

### Kleisli#flatMapF

As we saw *Kleisli#flatMap* is not very convenient. We have to bind values to variables and thread them through the for-comprehension. *flatMapF* is easier to use.

```
def flatMapF[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
  Kleisli { a => M.flatMap(run(a))(f) }
```

flatMapF composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow F[C]$  yielding a new Kleisli[F, A, C] wrapping a new function run:  $A \Rightarrow F[C]$ .

### Kleisli#flatMapF

As we saw *Kleisli#flatMap* is not very convenient. We have to bind values to variables and thread them through the for-comprehension. *flatMapF* is easier to use.

```
def flatMapF[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
  Kleisli { a => M.flatMap(run(a))(f) }
```

flatMapF composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow F[C]$  yielding a new Kleisli[F, A, C] wrapping a new function run:  $A \Rightarrow F[C]$ .

```
val kleisli4: Kleisli[Option, String, String] =
   Kleisli(s2iOpt) flatMapF plus2Opt flatMapF div10ByOpt flatMapF d2sOpt
kleisli4.run("3") foreach println
```

The behaviour of *flatMap* is exactly what we expect from *andThen*.

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```
def andThen[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
   flatMapF(f)
```

The behaviour of *flatMap* is exactly what we expect from *andThen*.

```
def andThen[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
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```

The first version of andThen is an alias for flatMapF.

The behaviour of *flatMap* is exactly what we expect from *andThen*.

```
def andThen[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
   flatMapF(f)
```

The first version of andThen is an alias for flatMapF.

```
(Kleisli(s2iOpt) andThen plus2Opt andThen div1OByOpt andThen d2sOpt) foreach println
```

```
def andThen[C](that: Kleisli[F, B, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
   this andThen that.run
```

This overloaded version of *andThen* doesn't take a function  $f: B \Rightarrow F[C]$ . Instead it takes a *Kleisli*[F, B, C] wrapping such a function. This version allows us to concatenate several Kleislis to a pipeline.

```
def andThen[C](that: Kleisli[F, B, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
   this andThen that.run
```

This overloaded version of *andThen* doesn't take a function  $f: B \Rightarrow F[C]$ . Instead it takes a *Kleisli*[F, B, C] wrapping such a function. This version allows us to concatenate several Kleislis to a pipeline.

```
(Kleisli(s2iOpt) andThen Kleisli(plus2Opt) andThen
Kleisli(div10ByOpt) andThen Kleisli(d2sOpt)) foreach println
```

### Kleisli#compose

As with *andThen* there are two versions of *compose*. They work like *andThen* with the arguments flipped.

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def compose[Z](f: Z => F[A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
   Kleisli(f) andThen this.run

def compose[Z](that: Kleisli[F, Z, A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
   that andThen this
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### Kleisli#compose

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```
def compose[Z](f: Z => F[A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
   Kleisli(f) andThen this.run

def compose[Z](that: Kleisli[F, Z, A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
   that andThen this
```

```
(Kleisli(d2sOpt) compose div10ByOpt compose
   plus2Opt compose s2iOpt) foreach println

(Kleisli(d2sOpt) compose Kleisli(div10ByOpt) compose
   Kleisli(plus2Opt) compose Kleisli(s2iOpt)) foreach println
```

# 10. Reader Monad

See: demo.Demo10Reader

# Reader again

We already saw, that the Function1 Monad is the Reader Monad.

But *Kleisli* can also be used as *Reader*, if *F*[\_] is fixed to the *Id* context.

### Reader again

We already saw, that the Function1 Monad is the Reader Monad.

But *Kleisli* can also be used as *Reader*, if *F*[\_] is fixed to the *Id* context.

```
type Id[A] = A

type ReaderT[F[_], A, B] = Kleisli[F, A, B]
val ReaderT = Kleisli

type Reader[A, B] = Kleisli[Id, A, B]

object Reader {
  def apply[A, B](f: A => B): Reader[A, B] = ReaderT[Id, A, B](f)
}
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString + " !!!"
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString + " !!!"
```

```
val reader1: String => String = input => for {
  i1 <- Reader(s2i).run(input)
  i2 <- Reader(plus2).run(i1)
  d <- Reader(div10By).run(i2)
  s <- Reader(d2s).run(d)
} yield s

println(reader1("3")) // 2.0 !!!</pre>
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString + " !!!"
```

```
val reader1: String => String = input => for {
  i1 <- Reader(s2i).run(input)
  i2 <- Reader(plus2).run(i1)
  d <- Reader(div10By).run(i2)
  s <- Reader(d2s).run(d)
} yield s

println(reader1("3")) // 2.0 !!!</pre>
```

Again *flatMap* is not the best choice as we have to declare all these intermediate identifiers in the for-comprehension.

```
val reader2 =
  Reader(s2i) andThen Reader(plus2) andThen Reader(div10By) andThen Reader(d2s)
println(reader2("3"))  // 2.0 !!!
```

```
val reader2 =
  Reader(s2i) andThen Reader(plus2) andThen Reader(div10By) andThen Reader(d2s)
println(reader2("3"))  // 2.0 !!!
```

```
val reader3 =
  Reader(s2i) andThen plus2 andThen div10By andThen d2s
println(reader3("3"))  // 2.0 !!!
```

```
val reader2 =
  Reader(s2i) andThen Reader(plus2) andThen Reader(div10By) andThen Reader(d2s)
println(reader2("3"))  // 2.0 !!!
```

```
val reader3 =
  Reader(s2i) andThen plus2 andThen div10By andThen d2s
println(reader3("3"))  // 2.0 !!!
```

All methods of *Kleisli* are available for Reader, because *Kleisli* **is** *Reader* with *Id*.

#### The Reader example from before runs with minor changes.

```
val users: Map[Int, String] = Map(
              1 -> "dade", 2 -> "kate", 3 -> "margo" )
val passwords: Map[String, String] = Map(
              "dade" -> "zerocool", "kate" -> "acidburn", "margo" -> "secret" )
case class Db(usernames: Map[Int, String], passwords: Map[String, String])
val db = Db(users, passwords)
type DbReader[A] = Reader[Db, A] // ^= Kleisli[Id, Db, Boolean]
def findUsername(userId: Int): DbReader[Option[String]] =
  Reader { db => db.usernames.get(userId) }
def checkPassword(username: String, password: String): DbReader[Boolean] =
  Reader { db => db.passwords.get(username).contains(password) }
def checkLogin(userId: Int, password: String): DbReader[Boolean] =
  for {
    optUsername <- findUsername(userId)</pre>
    passwordOk <- optUsername
      .map(name => checkPassword(name, password))
      .getOrElse(Kleisli.pure[Id, Db, Boolean](false))
  } vield password0k
val loginOk1 = checkLogin(1, "zerocool").run(db) // true
val login0k2 = checkLogin(4, "davinci").run(db) // false
```

Example taken from "Scala with Cats" (see chapter Resources for link)

# 11. Resources

# Resources (1/2)

- Code and Slides of this Talk: https://github.com/hermannhueck/composing-functions
- "Scala with Cats"
   Book by Noel Welsh and Dave Gurnell
   https://underscore.io/books/scala-with-cats/
- "Functional Programming in Scala"
   Book by Paul Chiusano and Dave Gurnell
   https://www.manning.com/books/functional-programming-in-scala
- Cats documentation for *Kleisli*: https://typelevel.org/cats/datatypes/kleisli.html

# Resources (2/2)

- Miles Sabin's pull request for partial unification: https://github.com/scala/scala/pull/5102
- "Explaining Miles's Magic: Gist of Daniel Spiewak on partial unification https://gist.github.com/djspiewak/7a81a395c461fd3a09a6941d4cd040f2
- "Kind Projector Compiler Plugin: https://github.com/non/kind-projector

# Thanks for Listening

ABQ

https://github.com/hermannhueck/composing-functions