# From Function1#compose to Kleisli

Different Ways of Function Composition

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## Abstract

Fine-grained composability of functions is one of the core advantages of FP.

In this talk I demonstrate different ways of composing functions.

I only deal with *scala.Function1*, because due to currying we can regard any function (except *Function0*) as a *Function1*.

I start with the methods on Function1: *compose* and *andThen*. Then I show how to fold a List of functions.

Then I turn to and demonstrate function composition with Monoids.

I implement *map* and *flatMap* for *Function1* what allows me to compose functions in for-comprehensions. I also make it a Monad in order to treat functions as Monads, i.e. to use them in any monadic context.

Next I implement my own mycats. Kleisli similar to cats. data. Kleisli and show its usage with flatMap, flatMapF, and Then and compose. I then show the Reader Monad, a Kleisli simplified with Id.

## Agenda

- 1. Preliminaries
  - Kind Projector
  - Partial Unification
  - Curried Functions
- 2. Function1#compose and Function1#andThen
- 3. Composing Functions with Monoid
- 4. Function1 as Functor and Monad
- 5. Kleisli Composition done manually
- 6. case class Kleisli
- 7. Reader Monad
- 8. Resources

## 1. Preliminaries

- **1.1** Kind Projector
- **1.2 Partial Unification**
- 1.3 Currying

## 1.1 Kind Projector - Compiler Plugin

Enable *kind-projector* in *build.sbt*:

```
addCompilerPlugin("org.spire-math" %% "kind-projector" % "0.9.7")
```

See: demo.Demo1aKindProjector

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```
trait Functor[F[_]] {
  def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

It is parameterized with a generic type constructor F[\_] which "has one hole", i.e. F[\_] needs another type parameter when reified.

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```
implicit val listFunctor: Functor[List] = new Functor[List] {
  override def map[A, B](fa: List[A])(f: A => B): List[B] = fa map f
}
implicit val optionFunctor: Functor[Option] = new Functor[Option] {
  override def map[A, B](fa: Option[A])(f: A => B): Option[B] = fa map f
}
```

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implicit val listFunctor: Functor[List] = new Functor[List] {
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}
implicit val optionFunctor: Functor[Option] = new Functor[Option] {
  override def map[A, B](fa: Option[A])(f: A => B): Option[B] = fa map f
}
```

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But we can fix one of the type parameters and leave the other one open.

```
// Code compiles without kind-projector.
// It uses a type alias within a structural type.
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
   new Functor[({type f[x] = Either[L, x]})#f] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

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}
```

This is a type lambda (analogous to a partially applied function on the value level).

The type alias must be defined inside def eitherFunctor[L] because the type parameter L is used in the type alias. This is done inside a structural type where f is returned through a type projection.

```
Functor[({type f[x] = Either[L, x]})#f]
```

This code is ugly but can be improved if *kind-projector* is enabled.

```
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
  new Functor[({type f[x] = Either[L, x]})#f] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
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    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

#### With *kind-projector*.

```
implicit def eitherFunctor[L]: Functor[Lambda[x => Either[L, x]]] =
  new Functor[Lambda[x => Either[L, x]]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

```
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
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}
```

#### With *kind-projector*:

```
implicit def eitherFunctor[L]: Functor[Lambda[x => Either[L, x]]] =
  new Functor[Lambda[x => Either[L, x]]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

```
implicit def eitherFunctor[L]: Functor[\(\lambda[x => Either[L, x]]\)] =
  new Functor[\(\lambda[x => Either[L, x]]\)] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

```
implicit def eitherFunctor[L]: Functor[({type f[x] = Either[L, x]})#f] =
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```

#### With kind-projector:

```
implicit def eitherFunctor[L]: Functor[Lambda[x => Either[L, x]]] =
   new Functor[Lambda[x => Either[L, x]]] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}

implicit def eitherFunctor[L]: Functor[\(\lambla[x => Either[L, x]])] =
   new Functor[\(\lambla[x => Either[L, x]])] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}

implicit def eitherFunctor[L]: Functor[Either[L, ?]] =
   new Functor[Either[L, ?]] {
     override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] = fa map f
}
```

## 1.2 Compiler Flag \*-Ypartial-unification

Enable partial unification in *build.sbt*:

```
scalacOptions += "-Ypartial-unification"
```

See: demo.Demo1bPartialUnification

```
def foo[F[ ], A](fa: F[A]): String = fa.toString
foo { x: Int => x * 2 }
[error] no type parameters for method foo: (fa: F[A])String exist
        so that it can be applied to arguments (Int => Int)
[error] --- because ---
[error] argument expression's type is not compatible with formal parameter type;
[error] found : Int => Int
[error] required: ?F[?A]
         foo { x: Int => x * 2 }
[error]
[error]
[error] type mismatch;
[error] found : Int => Int
[error] required: F[A]
         foo((x: Int) \Rightarrow x * 2)
[error]
```

This code doesn't compile without -Ypartial-unification. Why?

This code doesn't compile without -Ypartial-unification. Why?

def foo requires a type constructor F[\_] with "one hole". It's kind is: \* --> \*.

foo is invoked with a function Int => Int. Int => Int is syntactic sugar for Function1[Int, Int]. Function1 like Either has two holes. It's kind is: \* --> \* --> \*.

#### The Solution:

-Ypartial-unification solves the problem by partially fixing (unifying) the type parameters <u>from left to right</u> until it fits to the number of holes required by the definition of *foo*.

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Imagine this flag turns *Function1[A, B]* into *Function1Int[B]*. With this fix on the fly *Function1Int* has kind \*--> \* which is the kind required by F[\_]. What the compiler transforms the invocation to would look something like this:

```
def foo[F[_], A](fa: F[A]): String = fa.toString
foo[Function1Int, Int] { x: Int => x * 2 }
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```
def foo[F[_], A](fa: F[A]): String = fa.toString
foo[Function1Int, Int] { x: Int => x * 2 }
```

Note that the partial unification fixes the types always in a <u>left-to-right order</u> which is a good fit for most cases where we have <u>right-biased types</u> like *Either*, *Tuple2* or *Function1*. (It is not a good fit for the very rare cases when you use a left-biased type like Scalactic's *Or* data type (a left-biased *Either*).)

## When to use *kind-projector* and *-Ypartial-unification*?

Enable plugin and the flag when using a Functor, Applicative or a Monad instance for higher-kinded types which take more than one type parameter. *Either, Tuple2* and *Function1* are the best known representatives of this kind of types.

When programming on the type level regard both as your friends and keep them enabled.

## When to use *kind-projector* and *-Ypartial-unification*?

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Very good explanations of partial unification by Miles Sabin and Daniel Spiewak can be found at these links:

https://github.com/scala/scala/pull/5102 https://gist.github.com/djspiewak/7a81a395c461fd3a09a6941d4cd040f2

## 1.3 Curried functions

See: demo.Demo1cCurriedFunctions

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```
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
// sumCurried: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/9914305
```

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The type arrow ( $\Rightarrow$ ) is syntactic sugar for *Function1*.  $A \Rightarrow B$  is equivalent to *Function1[A, B]*.

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```
val sumCurried2: Function1[Int, Function1[Int, Function1[Int, Int]]] = sumCurried
// sumCurried2: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/991430
```

... if you curry it.

```
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
// sumCurried: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/9914305
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```
val sumCurried2: Function1[Int, Function1[Int, Function1[Int, Int]]] = sumCurried
// sumCurried2: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/991430
```

If uncurried again, we get the original function back.

```
val sumUncurried: (Int, Int, Int) => Int = Function.uncurried(sumCurried)
// sumUncurried: (Int, Int, Int) => Int = scala.Function$$$Lambda$6605/301079867@1
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int => sum3Ints.curried
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int => sum3Ints.curried
val applied1st: Int => Int => Int = sumCurried(1)
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _ 
val sumCurried: Int => Int => Int = sum3Ints.curried

val applied1st: Int => Int => Int = sumCurried(1)

val applied2nd: Int => Int = applied1st(2)
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _
val sumCurried: Int => Int => Int = sum3Ints.curried

val applied1st: Int => Int = sumCurried(1)

val applied2nd: Int => Int = applied1st(2)

val applied3rd: Int = applied2nd(3)
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ +
val sumCurried: Int => Int => Int = sum3Ints.curried

val applied1st: Int => Int = sumCurried(1)

val applied2nd: Int => Int = applied1st(2)

val applied3rd: Int = applied2nd(3)

val appliedAllAtOnce: Int = sumCurried(1)(2)(3)
```

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They are better <u>composable</u> than their uncurried counterparts.

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```
def filter2[A](la: List[A])(p: A => Boolean) = ??? // curried

scala> filter2(List(0,1,2))(_ < 2)
res5: List[Int] = List(0,1)</pre>
```

# 2. Function1#compose and Function1#apply

See: demo.Demo2ComposingFunctions

#### Trait Function1

```
trait Function1[-T1, +R] {

    def apply(a: T1): R
    def compose[A](g: A => T1): A => R = { x => apply(g(x)) }
    def andThen[A](g: R => A): T1 => A = { x => g(apply(x)) }
    override def toString = "<function1>"
}
```

#### Trait Function1

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    def andThen[A](g: R => A): T1 => A = { x => g(apply(x)) }
    override def toString = "<function1>"
}
```

```
scala> val f: Int => Int = _ + 10
f: Int => Int = $$Lambda$4204/320646851@733dc5b7

scala> val g: Int => Int = _ * 2
g: Int => Int = $$Lambda$4205/1093482910@3a179009

scala> (f compose g apply 1) == f(g(1))
res6: Boolean = true

scala> (f andThen g apply 1) == g(f(1))
res7: Boolean = true
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

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val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

```
// Function1#compose
val fComposed0: String => String = d2s compose div10By compose plus2 compose s2i
val res0 = fComposed0("3") // 2.0 !!!
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

```
// Function1#compose
val fComposed0: String => String = d2s compose div10By compose plus2 compose s2i
val res0 = fComposed0("3") // 2.0 !!!
```

```
// Function1#andThen
val fComposed1: String => String = s2i andThen plus2 andThen div10By andThen d2s
val res1 = fComposed1("3") // 2.0 !!!
```

#### Function composition in Haskell

```
s2i :: String -> Int
s2i = read

plus2 :: Int -> Int
plus2 = (+2)

div10By :: Int -> Double
div10By x = (10.0 / fromIntegral x)

d2s :: Double -> String
d2s d = (show d) ++ " !!!"
```

#### Function composition in Haskell

```
s2i :: String -> Int
s2i = read

plus2 :: Int -> Int
plus2 = (+2)

div10By :: Int -> Double
div10By x = (10.0 / fromIntegral x)

d2s :: Double -> String
d2s d = (show d) ++ " !!!"
```

```
-- (.) is the function composition operator

fComposed :: String -> String

fComposed = d2s . div10By . plus2 . s2i

result = fComposed "3"

-- "2.0 !!!"
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)
val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)
// 222
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)

// 222

val lfFoldedLeft = lf.foldLeft(identity[Int] _) {(acc, f) => acc andThen f}
val resLfFoldedLeft = lfFoldedLeft(1)
// 112
```

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)
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val lfFoldedLeft = lf.foldLeft(identity[Int] _) {(acc, f) => acc andThen f}
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// 112
```

The *identity* function is the no-op of function composition.

```
val lf: List[Int => Int] = List(_*2, _+10, _+100)

val lfFoldedRight = lf.foldRight(identity[Int] _) {(f, acc) => acc andThen f}
val resLfFoldedRight = lfFoldedRight(1)
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val lfFoldedLeft = lf.foldLeft(identity[Int] _) {(acc, f) => acc andThen f}
val resLfFoldedLeft = lfFoldedLeft(1)
// 112
```

The *identity* function is the no-op of function composition.

Folding functions is not a commutative operation! Hence *foldRight* and *foldLeft* return different results.

## 3. Composing Functions with Monoid

 $See: {\it demo.Demo3ComposingWithMonoid}$ 

#### Trait Monoid

```
trait Monoid[A] {
    def empty: A
    def combine(x: A, y: A): A

    def combineAll(as: List[A]): A = // combines all functions in a List of funct
        as.foldLeft(empty)(combine)
}
```

#### Trait Monoid

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trait Monoid[A] {
   def empty: A
   def combine(x: A, y: A): A

   def combineAll(as: List[A]): A = // combines all functions in a List of funct
        as.foldLeft(empty)(combine)
}
```

When composing functions with Monoid the functions must have the same input and output type. You cannot compose functions of type  $A \Rightarrow B$ , only functions of type  $A \Rightarrow A$ .

#### Default Monoid Instance for *Function1*

```
// This one is the default Function1-Monoid in Cats
implicit def function1Monoid[A: Monoid]: Monoid[A => A] = new Monoid[A => A] {
    override def empty: A => A =
        _ => Monoid[A].empty
    override def combine(f: A => A, g: A => A): A => A =
        a => Monoid[A].combine(f(a), g(a))
}
```

#### Default Monoid Instance for *Function1*

```
// This one is the default Function1-Monoid in Cats
implicit def function1Monoid[A: Monoid]: Monoid[A => A] = new Monoid[A => A] {
    override def empty: A => A =
        _ => Monoid[A].empty
    override def combine(f: A => A, g: A => A): A => A =
        a => Monoid[A].combine(f(a), g(a))
}
```

- This instance defines a Monoid for Functions of type  $A \Rightarrow A$ .
- It requires *A* to be a Monoid too.
- *empty* defines a function which ignores it's input and returns *Monoid[A].empty*.
- *combine* takes two functions f and g, invokes f(a) and g(a) on it's input and returns the combined result.

### Composition with Monoid

```
val f: Int => Int = _ + 1
val g: Int => Int = _ * 2
val h: Int => Int = _ + 100
```

#### Composition with Monoid

```
val f: Int => Int = _ + 1
val g: Int => Int = _ * 2
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```

#### Composition with Monoid

```
val f: Int => Int = _ + 1
val g: Int => Int = _ * 2
val h: Int => Int = _ + 100
```

Another Monoid instance yields a different result.

#### Instance for *function1ComposeMonoid*

```
implicit def function1ComposeMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f compose g
}
```

#### Instance for *function1ComposeMonoid*

```
implicit def function1ComposeMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f compose g
}
```

• This instance composes the Functions *Function1#compose*.

## Instance for *function1ComposeMonoid*

```
implicit def function1ComposeMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f compose g
}
```

• This instance composes the Functions *Function1#compose*.

## Instance for *function1AndThenMonoid*

```
implicit def function1AndThenMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f andThen g
}
```

## Instance for *function1AndThenMonoid*

```
implicit def function1AndThenMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f andThen g
}
```

• This instance composes the Functions *Function1#andThen*.

## Instance for *function1AndThenMonoid*

```
implicit def function1AndThenMonoid[A]: Monoid[A => A] = new Monoid[A => A] {
  override def empty: A => A = identity
  override def combine(f: A => A, g: A => A): A => A = f andThen g
}
```

• This instance composes the Functions *Function1#andThen*.

# 4. *Function1* as Functor and Monad

See: demo.Demo4FunctorAndMonad

## **Functor**

A Functor is any Context F[\_] that provides a function *map* ... and abides by the Functor laws (which I don't present here).

```
trait Functor[F[_]] {
   def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

#### Functor instance

A Functor instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Functor* companion object):

```
implicit def function1Functor[P]: Functor[Function1[P, ?]] =
  new Functor[Function1[P, ?]] {
    override def map[A, B](f: Function1[P, A])(g: A => B): Function1[P, B] =
        f andThen g
}
```

#### Functor instance

A Functor instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Functor* companion object):

```
implicit def function1Functor[P]: Functor[Function1[P, ?]] =
  new Functor[Function1[P, ?]] {
    override def map[A, B](f: Function1[P, A])(g: A => B): Function1[P, B] =
        f andThen g
}
```

A Functor instance for *Either* (just for comparison):

```
implicit def eitherFunctor[L]: Functor[Either[L, ?]] =
  new Functor[Either[L, ?]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] =
        fa map f
}
```

#### Functor instance

A Functor instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Functor* companion object):

```
implicit def function1Functor[P]: Functor[Function1[P, ?]] =
  new Functor[Function1[P, ?]] {
    override def map[A, B](f: Function1[P, A])(g: A => B): Function1[P, B] =
        f andThen g
}
```

A Functor instance for *Either* (just for comparison):

```
implicit def eitherFunctor[L]: Functor[Either[L, ?]] =
  new Functor[Either[L, ?]] {
    override def map[A, B](fa: Either[L, A])(f: A => B): Either[L, B] =
        fa map f
}
```

Using the *Function1* Functor:

```
val h = Functor[Function1].map(f)(g)
```

defined as <u>implicit conversion</u> ...

defined as implicit conversion ...

in a specific way for *Functor[Function1]*:

```
implicit class FunctorSyntaxFunction1[P, A](fa: Function1[P, A]) {
  def map[B](f: A => B): Function1[P, B] = Functor[Function1[P, ?]].map(fa)(f)
}
```

defined as implicit conversion ...

in a specific way for *Functor*[Function1]:

```
implicit class FunctorSyntaxFunction1[P, A](fa: Function1[P, A]) {
  def map[B](f: A => B): Function1[P, B] = Functor[Function1[P, ?]].map(fa)(f)
}
```

or in a generic way for any *Functor[F[\_]]*:

```
implicit class FunctorSyntax[F[_]: Functor, A](fa: F[A]) {
  def map[B](f: A => B): F[B] = Functor[F].map(fa)(f)
}
```

defined as implicit conversion ...

in a specific way for *Functor[Function1]*:

```
implicit class FunctorSyntaxFunction1[P, A](fa: Function1[P, A]) {
  def map[B](f: A => B): Function1[P, B] = Functor[Function1[P, ?]].map(fa)(f)
}
```

or in a generic way for any *Functor[F[\_]]*:

```
implicit class FunctorSyntax[F[_]: Functor, A](fa: F[A]) {
  def map[B](f: A => B): F[B] = Functor[F].map(fa)(f)
}
```

This allows for convenient invocation of *map* as if *map* were a method of *Function1*:

```
val h = f map g
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

#### composed with *map*:

```
val fMapped = s2i map plus2 map div10By map d2s // requires -Ypartial-unification
val res1 = fMapped("3") // 2.0 !!!
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString
```

#### composed with *map*:

```
val fMapped = s2i map plus2 map div10By map d2s // requires -Ypartial-unification
val res1 = fMapped("3") // 2.0 !!!
```

Function1 can also be seen as a Monad ...

#### Monad

A Monad is any Context F[\_] that provides the functions *pure* and *flatMap* ... and abides by the Monad laws (which I don't present here).

```
trait Monad[F[_]] extends Functor[F] {
  def pure[A](a: A): F[A]
  def flatMap[A, B](fa: F[A])(f: A => F[B]): F[B]
}
```

## Monad instance

A Monad instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Monad* companion object):

```
implicit def function1Monad[P]: Monad[P => ?] = new Monad[P => ?] {
  override def pure[A](r: A): P => A = _ => r
  override def flatMap[A, B](f: P => A)(g: A => P => B)
    : P => B = p => g(f(p))(p)
}
```

### Monad instance

A Monad instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Monad* companion object):

```
implicit def function1Monad[P]: Monad[P => ?] = new Monad[P => ?] {
  override def pure[A](r: A): P => A = _ => r
  override def flatMap[A, B](f: P => A)(g: A => P => B)
    : P => B = p => g(f(p))(p)
}
```

Alternative instance definition:

```
implicit def function1Monad[P]: Monad[Function1[P, ?]] = new Monad[Function1[P, ?]
  override def pure[A](r: A): Function1[P, A] = _ => r
  override def flatMap[A, B](f: Function1[P, A])(g: A => Function1[P, B])
    : Function1[P, B] = p => g(f(p))(p)
}
```

### Monad instance

A Monad instance for *Functions* (found automatically by the compiler if defined in implicit scope, i.e inside the *Monad* companion object):

```
implicit def function1Monad[P]: Monad[P => ?] = new Monad[P => ?] {
  override def pure[A](r: A): P => A = _ => r
  override def flatMap[A, B](f: P => A)(g: A => P => B)
    : P => B = p => g(f(p))(p)
}
```

Alternative instance definition:

```
implicit def function1Monad[P]: Monad[Function1[P, ?]] = new Monad[Function1[P, ?]
  override def pure[A](r: A): Function1[P, A] = _ => r
  override def flatMap[A, B](f: Function1[P, A])(g: A => Function1[P, B])
  : Function1[P, B] = p => g(f(p))(p)
}
```

A Monad instance for *Either* (just for comparison):

```
implicit def eitherMonad[L]: Monad[Either[L, ?]] = new Monad[Either[L, ?]] {
   override def pure[A](r: A): Either[L, A] = Right(r)
   override def flatMap[A, B](fa: Either[L, A])(f: A => Either[L, B])
   : Either[L, B] = fa flatMap f
}
```

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defined as <u>implicit conversion</u> ...

defined as implicit conversion ...

in a specific way for *Monad[Function1]*:

```
implicit class MonadSyntaxFunction1[P, A](f: Function1[P, A]) {
  def flatMap[B](g: A => P => B): P => B = Monad[Function1[P, ?]].flatMap(f)(g)
}
```

defined as implicit conversion ...

in a specific way for *Monad[Function1]*:

```
implicit class MonadSyntaxFunction1[P, A](f: Function1[P, A]) {
  def flatMap[B](g: A => P => B): P => B = Monad[Function1[P, ?]].flatMap(f)(g)
}
```

or in a generic way for any *Monad[F[\_]]*:

```
implicit class MonadSyntax[F[_]: Monad, A](fa: F[A]) {
  def flatMap[B](f: A => F[B]): F[B] = Monad[F].flatMap(fa)(f)
}
```

defined as implicit conversion ...

in a specific way for *Monad[Function1]*:

```
implicit class MonadSyntaxFunction1[P, A](f: Function1[P, A]) {
  def flatMap[B](g: A => P => B): P => B = Monad[Function1[P, ?]].flatMap(f)(g)
}
```

or in a generic way for any *Monad[F[\_]]*:

```
implicit class MonadSyntax[F[_]: Monad, A](fa: F[A]) {
  def flatMap[B](f: A => F[B]): F[B] = Monad[F].flatMap(fa)(f)
}
```

This allows for convenient invocation of *flatMap* as if *flatMap* were a method of *Function1*:

```
val h = f flatMap g
```

instead of:

```
val h = Monad[Function1].flatMap(f)(g)
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```

```
val countLines: String => Int = text => text.split("\n").length
val countWords: String => Int = text => text.split("\\W+").length
val countChars: String => Int = text => text.length
```

```
val countLines: String => Int = text => text.split("\n").length
val countWords: String => Int = text => text.split("\\W+").length
val countChars: String => Int = text => text.length
```

#### FlatMapping over *Function1*:

```
val countLines: String => Int = text => text.split("\n").length
val countWords: String => Int = text => text.split("\\W+").length
val countChars: String => Int = text => text.length
```

#### FlatMapping over *Function1*:

#### with a for-comprehension:

#### Another Reader Monad example - a bit more realistic ...

```
val users: Map[Int, String] = Map(
          1 -> "dade", 2 -> "kate", 3 -> "margo")
val passwords: Map[String, String] = Map(
          "dade" -> "zerocool", "kate" -> "acidburn", "margo" -> "secret")
case class Db(usernames: Map[Int, String], passwords: Map[String, String])
val db = Db(users, passwords)
type DbReader[A] = Db => A // ^= Function1[Db, A]
def findUsername(userId: Int): DbReader[Option[String]] =
  db => db.usernames.get(userId)
def checkPassword(username: String, password: String): DbReader[Boolean] =
  db => db.passwords.get(username).contains(password)
def checkLogin(userId: Int, password: String): DbReader[Boolean] = // ^= Function1
  for {
    optUsername <- findUsername(userId)</pre>
    passwordOk <- optUsername
      .map(name => checkPassword(name, password))
      .qetOrElse(( :Db) => false)
  } vield password0k
val login10k = checkLogin(1, "zerocool")(db) // true
val login40k = checkLogin(4, "davinci")(db) // false
```

Example taken from "Scala with Cats" (see chapter Resource for link)

# 5. Kleisli composition done manually

See: demo.Demo5KleisliDoneManually

```
// Functions: A => F[B], where F is Option in this case
val s2iOpt: String => Option[Int] = s => Option(s.toInt)
val plus2Opt: Int => Option[Int] = i => Option(i + 2)
val div10ByOpt: Int => Option[Double] = i => Option(10.0 / i)
val d2sOpt: Double => Option[String] = d => Option(d.toString)
```

These functions take an A and return a B inside of a context  $F[]: A \Rightarrow F[B]$  In our case F[] is *Option*, but could be *List*, *Future* etc.

```
// Functions: A => F[B], where F is Option in this case
val s2iOpt: String => Option[Int] = s => Option(s.toInt)
val plus2Opt: Int => Option[Int] = i => Option(i + 2)
val div10ByOpt: Int => Option[Double] = i => Option(10.0 / i)
val d2sOpt: Double => Option[String] = d => Option(d.toString)
```

These functions take an A and return a B inside of a context  $F[]: A \Rightarrow F[B]$  In our case F[] is *Option*, but could be *List*, *Future* etc.

We want to compose these functions to a single function which is the fed with some input string.

```
// Functions: A => F[B], where F is Option in this case
val s2iOpt: String => Option[Int] = s => Option(s.toInt)
val plus2Opt: Int => Option[Int] = i => Option(i + 2)
val div10ByOpt: Int => Option[Double] = i => Option(10.0 / i)
val d2sOpt: Double => Option[String] = d => Option(d.toString)
```

These functions take an A and return a B inside of a context  $F[]: A \Rightarrow F[B]$  In our case F[] is *Option*, but could be *List*, *Future* etc.

We want to compose these functions to a single function which is the fed with some input string.

Let's try map.

```
val fMapped: String => Option[Option[Option[Option[String]]]] = str =>
    s2iOpt(str) map { i1 =>
    plus2Opt(i1) map { i2 =>
        div10ByOpt(i2) map {
        d => d2sOpt(d)
    }
}}
```

We get nested *Options*. So lets try *flatMap* on the *Option* context.

#### FlatMapping on the *Option* context

#### FlatMapping on the *Option* context

with *flatMap* (this works):

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with *flatMap* (this works):

```
val flatMappedOnOpt1: String => Option[String] = input =>
    s2iOpt(input) flatMap { i1 =>
        plus2Opt(i1) flatMap { i2 =>
            div10ByOpt(i2) flatMap { d =>
                  d2sOpt(d)
        }}}
val res1: Option[String] = flatMappedOnOpt1("3") // Some(2.0)
```

with a for-comprehension (this looks nicer):

```
val flatMappedOnOpt2: String => Option[String] = input => for {
   i1 <- s2iOpt(input)
   i2 <- plus2Opt(i1)
   d <- div10ByOpt(i2)
   s <- d2sOpt(d)
} yield s
val res2: Option[String] = flatMappedOnOpt2("3") // Some(2.0)</pre>
```

#### FlatMapping on the *Option* context

with *flatMap* (this works):

```
val flatMappedOnOpt1: String => Option[String] = input =>
    s2iOpt(input) flatMap { i1 =>
        plus2Opt(i1) flatMap { i2 =>
            div10ByOpt(i2) flatMap { d =>
                  d2sOpt(d)
        }}}
val res1: Option[String] = flatMappedOnOpt1("3") // Some(2.0)
```

with a for-comprehension (this looks nicer):

```
val flatMappedOnOpt2: String => Option[String] = input => for {
   i1 <- s2iOpt(input)
   i2 <- plus2Opt(i1)
   d <- div10ByOpt(i2)
   s <- d2sOpt(d)
} yield s
val res2: Option[String] = flatMappedOnOpt2("3") // Some(2.0)</pre>
```

<u>But:</u> We still have to bind the variables *i1*, *i2*, *d* and *s* to names. We would like to build a function pipeline with some kind of *andThenF*.

s2iOpt andThenF plus2Opt andThenF div10ByOpt andThenF d2sOpt

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

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Let's define *kleisli*:

```
def kleisli[F[_]: Monad, A, B, C](f: A => F[B], g: B => F[C]): A => F[C] =
    a => Monad[F].flatMap(f(a))(g)
```

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

Let's define *kleisli*:

```
def kleisli[F[_]: Monad, A, B, C](f: A => F[B], g: B => F[C]): A => F[C] =
    a => Monad[F].flatMap(f(a))(g)
```

#### Using *kleisli*:

```
val kleisliComposed1: String => Option[String] =
   kleisli(kleisli(s2iOpt, plus2Opt), div10ByOpt), d2sOpt)
val resKleisli = kleisliComposed1("3")
```

Kleisli composition takes two functions  $A \Rightarrow F[B]$  and  $B \Rightarrow F[C]$  and yields a new function  $A \Rightarrow F[C]$  where the context F[] is required to be a Monad.

Let's define *kleisli*:

```
def kleisli[F[_]: Monad, A, B, C](f: A => F[B], g: B => F[C]): A => F[C] =
    a => Monad[F].flatMap(f(a))(g)
```

#### Using *kleisli*:

```
val kleisliComposed1: String => Option[String] =
   kleisli(kleisli(s2iOpt, plus2Opt), div10ByOpt), d2sOpt)
val resKleisli = kleisliComposed1("3")
```

This works, but is still not exactly what we want. *kleisli* should be a method of *Function1*.

with an implicit conversion:

with an implicit conversion:

#### Using it:

```
val kleisliComposed2: String => Option[String] =
   s2iOpt kleisli plus2Opt kleisli div10ByOpt kleisli d2sOpt
kleisliComposed2("3") foreach println
```

with an implicit conversion:

#### Using it:

```
val kleisliComposed2: String => Option[String] =
   s2iOpt kleisli plus2Opt kleisli div10ByOpt kleisli d2sOpt
kleisliComposed2("3") foreach println
```

(s2iOpt andThenF plus2Opt andThenF div10ByOpt andThenF d2sOpt) foreach println

with an implicit conversion:

#### Using it:

```
val kleisliComposed2: String => Option[String] =
    s2iOpt kleisli plus2Opt kleisli div10ByOpt kleisli d2sOpt
kleisliComposed2("3") foreach println

(s2iOpt andThenF plus2Opt andThenF div10ByOpt andThenF d2sOpt) foreach println

(s2iOpt >=> plus2Opt >=> div10ByOpt >=> d2sOpt) foreach println
```

# 6. case class Kleisli

See: demo.Demo6KleisliCaseClass

### case class Kleisli

Cats does not provide a *kleisli* method on *Function1*. Cats provides a *case class Kleisli* with the functionality shown above and more.

#### case class Kleisli

Cats does not provide a *kleisli* method on *Function1*. Cats provides a *case class Kleisli* with the functionality shown above and more.

I tinkered my own impl in *mycats.Kleisli* which works much like the Cats impl: see next slide.

#### case class Kleisli

```
case class Kleisli[F[ ], A, B](run: A => F[B]) {
 def apply(a: A): F[B] = run(a)
 def map[C](f: B => C)(implicit F: Functor[F]): Kleisli[F, A, C] =
    Kleisli { a => F.map(run(a))(f) }
 def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C]
    Kleisli { a => M.flatMap(run(a))(b => f(b).run(a)) }
  def flatMapF[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    Kleisli { a => M.flatMap(run(a))(f) }
  def andThen[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    flatMapF(f)
 def andThen[C](that: Kleisli[F, B, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    this and Then that.run
  def compose[Z](f: Z => F[A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
    Kleisli(f) and Then this.run
  def compose[Z](that: Kleisli[F, Z, A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
    that andThen this
```

The case class methods delegate to the wrapped *run* function and return the resulting *run* function rewrapped in a *Kleisli* instance.

#### *Kleisli* companion object with Monad instance

```
object Kleisli { self =>

def pure[F[_], A, B](b: B)(implicit F: Monad[F]): Kleisli[F, A, B] =
    Kleisli { _ => F.pure(b) }

object ops {
    implicit def kleisliMonad[F[_] : Monad, A]: Monad[Kleisli[F, A, ?]] =
        new Monad[Kleisli[F, A, ?]] {
        override def pure[B](b: B): Kleisli[F, A, B] = self.pure(b)
        override def flatMap[B, C](kl: Kleisli[F, A, B])(f: B => Kleisli[F, A, C])
        : Kleisli[F, A, C] = kl flatMap f
    }
}
```

## Kleisli#flatMap

```
def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    M.flatMap(run(a))(b => f(b).run(a))
}
```

flatMap composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow Kleisli[F, A, C]$  yielding a new Kleisli[F, A, C] wrapping a new function  $F(A) \Rightarrow F(C)$ .

## Kleisli#flatMap

```
def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    M.flatMap(run(a))(b => f(b).run(a))
}
```

flatMap composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow Kleisli[F, A, C]$  yielding a new Kleisli[F, A, C] wrapping a new function F(C).

```
val kleisli1: String => Option[String] = input =>
   Kleisli(s2iOpt).run(input) flatMap { i1 =>
        Kleisli(plus2Opt).run(i1) flatMap { i2 =>
        Kleisli(div10ByOpt).run(i2) flatMap { d =>
        Kleisli(d2sOpt).run(d)
        }   }
   kleisli1("3") foreach println
```

## Kleisli#flatMap

```
def flatMap[C](f: B => Kleisli[F, A, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
    M.flatMap(run(a))(b => f(b).run(a))
}
```

flatMap composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow Kleisli[F, A, C]$  yielding a new Kleisli[F, A, C] wrapping a new function  $F(A) \Rightarrow F(C)$ .

```
val kleisli2: String => Option[String] = input => for {
   i1 <- Kleisli(s2iOpt).run(input)
   i2 <- Kleisli(plus2Opt).run(i1)
   d <- Kleisli(div10ByOpt).run(i2)
   s <- Kleisli(d2sOpt).run(d)
} yield s
kleisli2("3") foreach println</pre>
```

## Kleisli#flatMapF

As we saw *Kleisli#flatMap* is not very convenient. We have to bind values to variables and thread them through the for-comprehension. *flatMapF* is simpler.

## Kleisli#flatMapF

As we saw *Kleisli#flatMap* is not very convenient. We have to bind values to variables and thread them through the for-comprehension. *flatMapF* is simpler.

```
def flatMapF[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
  Kleisli { a => M.flatMap(run(a))(f) }
```

flatMapF composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow F[C]$  yielding a new Kleisli[F, A, C] wrapping a new function run:  $A \Rightarrow F[C]$ .

## Kleisli#flatMapF

As we saw *Kleisli#flatMap* is not very convenient. We have to bind values to variables and thread them through the for-comprehension. *flatMapF* is simpler.

```
def flatMapF[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
  Kleisli { a => M.flatMap(run(a))(f) }
```

flatMapF composes this.run:  $A \Rightarrow F[B]$  with the function  $f: B \Rightarrow F[C]$  yielding a new Kleisli[F, A, C] wrapping a new function run:  $A \Rightarrow F[C]$ .

```
val kleisli4: Kleisli[Option, String, String] =
   Kleisli(s2iOpt) flatMapF plus2Opt flatMapF div10ByOpt flatMapF d2sOpt
kleisli4.run("3") foreach println
```

The behaviour of *flatMap* is exactly what we expect from *andThen*.

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```
def andThen[C](f: B => F[C])(implicit M: Monad[F]): Kleisli[F, A, C] =
   flatMapF(f)
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The first version of andThen is an alias for flatMapF.

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(Kleisli(s2iOpt) andThen plus2Opt andThen div1OByOpt andThen d2sOpt) foreach println
```

```
def andThen[C](that: Kleisli[F, B, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
   this andThen that.run
```

This overloaded version of *andThen* doesn't take a function  $f: B \Rightarrow F[C]$ . Instead it takes a *Kleisli*[F, B, C] wrapping such a function. This version allows us to concatenate several Kleislis to a pipeline.

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def andThen[C](that: Kleisli[F, B, C])(implicit M: Monad[F]): Kleisli[F, A, C] =
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```
(Kleisli(s2iOpt) andThen Kleisli(plus2Opt) andThen Kleisli(div1OByOpt) andThen Kleisli(d2sOpt)) foreach println
```

## Kleisli#compose

As with *andThen* there are two versions of *compose*. They work like *andThen* with the arguments flipped.

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def compose[Z](f: Z => F[A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
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def compose[Z](that: Kleisli[F, Z, A])(implicit M: Monad[F]): Kleisli[F, Z, B] =
   that andThen this
```

```
(Kleisli(d2sOpt) compose div10ByOpt compose
   plus2Opt compose s2iOpt) foreach println

(Kleisli(d2sOpt) compose Kleisli(div10ByOpt) compose
   Kleisli(plus2Opt) compose Kleisli(s2iOpt)) foreach println
```

# 7. Reader Monad

See: demo.Demo7Reader

## Reader again

We already saw, that the Function1 Monad is the Reader Monad.

But *Kleisli* can also be used as *Reader*, if *F*[\_] is fixed to the *Id* context.

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We already saw, that the Function1 Monad is the Reader Monad.

But *Kleisli* can also be used as *Reader*, if *F*[\_] is fixed to the *Id* context.

```
type Id[A] = A

type ReaderT[F[_], A, B] = Kleisli[F, A, B]
val ReaderT = Kleisli

type Reader[A, B] = Kleisli[Id, A, B]

object Reader {
  def apply[A, B](f: A => B): Reader[A, B] = ReaderT[Id, A, B](f)
}
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString + " !!!"
```

```
val s2i: String => Int = _.toInt
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```

```
val reader1: String => String = input => for {
  i1 <- Reader(s2i).run(input)
  i2 <- Reader(plus2).run(i1)
  d <- Reader(div10By).run(i2)
  s <- Reader(d2s).run(d)
} yield s

println(reader1("3"))</pre>
```

```
val s2i: String => Int = _.toInt
val plus2: Int => Int = _ + 2
val div10By: Int => Double = 10.0 / _
val d2s: Double => String = _.toString + " !!!"
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```
val reader1: String => String = input => for {
  i1 <- Reader(s2i).run(input)
  i2 <- Reader(plus2).run(i1)
  d <- Reader(div10By).run(i2)
  s <- Reader(d2s).run(d)
} yield s

println(reader1("3"))</pre>
```

Again *flatMap* is not the best choice as we have to declare all these intermediate identifiers in the for-comprehension.

```
val reader2 =
  Reader(s2i) andThen Reader(plus2) andThen Reader(div10By) andThen Reader(d2s)
println(reader2("3"))
```

```
val reader2 =
  Reader(s2i) andThen Reader(plus2) andThen Reader(div10By) andThen Reader(d2s)
println(reader2("3"))
```

```
val reader3 =
  Reader(s2i) andThen plus2 andThen div10By andThen d2s
println(reader3("3"))
```

```
val reader2 =
  Reader(s2i) andThen Reader(plus2) andThen Reader(div10By) andThen Reader(d2s)
println(reader2("3"))
```

```
val reader3 =
  Reader(s2i) andThen plus2 andThen div10By andThen d2s
println(reader3("3"))
```

All methods of *Kleisli* are available for Reader, because *Kleisli* is *Reader*.

#### The Reader example from before runs with minor changes.

```
val users: Map[Int, String] = Map(
              1 -> "dade", 2 -> "kate", 3 -> "margo" )
val passwords: Map[String, String] = Map(
              "dade" -> "zerocool", "kate" -> "acidburn", "margo" -> "secret" )
case class Db(usernames: Map[Int, String], passwords: Map[String, String])
val db = Db(users, passwords)
type DbReader[A] = Reader[Db, A] // ^= Kleisli[Id, Db, Boolean]
def findUsername(userId: Int): DbReader[Option[String]] =
  Reader { db => db.usernames.get(userId) }
def checkPassword(username: String, password: String): DbReader[Boolean] =
  Reader { db => db.passwords.get(username).contains(password) }
def checkLogin(userId: Int, password: String): DbReader[Boolean] =
  for {
    optUsername <- findUsername(userId)</pre>
    passwordOk <- optUsername
      .map(name => checkPassword(name, password))
      .getOrElse(Kleisli.pure[Id, Db, Boolean](false))
  } vield password0k
val loginOk1 = checkLogin(1, "zerocool").run(db) // true
val login0k2 = checkLogin(4, "davinci").run(db) // false
```

Example taken from "Scala with Cats" (see chapter Resource for link)

# 8. Resources

#### Scala Resources (1/2)

- Code and Slides of this Talk: https://github.com/hermannhueck/use-applicative-where-applicable
- Cats documentation:

https://typelevel.org/cats/typeclasses/applicative.html https://typelevel.org/cats/typeclasses/traverse.html https://typelevel.org/cats/datatypes/validated.html

• Herding Cats, Day 2 and 3:

http://eed3si9n.com/herding-cats/Functor.html http://eed3si9n.com/herding-cats/Semigroupal.html http://eed3si9n.com/herding-cats/Apply.html http://eed3si9n.com/herding-cats/Applicative.html

 "Scala with Cats", Chapters 6 and 7
 Book by Noel Welsh and Dave Gurnell https://underscore.io/books/scala-with-cats/

#### Scala Resources (2/2)

• Live Coding Tutorial on Functor and Applicative by Michael Pilquist FSiS Part 1 - Type Constructors, Functors, and Kind Projector

https://www.youtube.com/watch?v=Dsd4pc99FSY

FSiS Part 2 - Applicative type class

https://www.youtube.com/watch?v=tD\_EyIKqqCk

#### Haskell Resources

- Learn You a Haskell for Great Good!, Chapter 11 Online book by Miran Lipovaca http://learnyouahaskell.com/functors-applicative-functors-and-monoids
- Applicative Programming with Effects
   Conor McBride and Ross Paterson in Journal of Functional Programming
   18:1 (2008), pages 1-13
   http://www.staff.city.ac.uk/~ross/papers/Applicative.pdf
- The Essence of the Iterator Pattern Jeremy Gibbons and Bruno C. d. S. Oliveira, Oxford University Computing Laboratory

https://www.cs.ox.ac.uk/jeremy.gibbons/publications/iterator.pdf

#### Thanks for Listening

ABQ

https://github.com/hermannhueck/use-applicative-where-applicable