

Las Positas College
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Course Outline for MATH 2

CALCULUS II

Effective: Fall 2016

I. CATALOG DESCRIPTION:

MATH 2 — CALCULUS II — 5.00 units

Continuation of single-variable differential and integral calculus. Topics covered include: inverse and hyperbolic functions; techniques of integration; polar and parametric equations; infinite sequences, series, power series and Taylor series; applications of integration. Primarily for mathematics, physical science and engineering majors.

5.00 Units Lecture

Prerequisite

MATH 1 - Calculus I
with a minimum grade of C

Grading Methods:

Letter Grade

Discipline:

	<u>MIN</u>
Lecture Hours:	90.00
Total Hours:	90.00

II. NUMBER OF TIMES COURSE MAY BE TAKEN FOR CREDIT: 1

III. PREREQUISITE AND/OR ADVISORY SKILLS:

Before entering the course a student should be able to:

A. MATH1

IV. MEASURABLE OBJECTIVES:

Upon completion of this course, the student should be able to:

- A. Graph, differentiate, and integrate inverse functions and transcendental functions such as trigonometric, exponential and logarithmic functions;
- B. Evaluate limits by applying L'Hospital's rule and techniques appropriate to limits of indeterminate forms;
- C. Evaluate definite and indefinite integrals by a variety of integration techniques;
- D. Apply numerical methods to approximate definite integrals;
- E. Evaluate improper integrals;
- F. Use integration to solve applications such as work, arc length and the surface area of a solid of revolution;
- G. Solve separable first order differential equations;
- H. Solve exponential growth and decay problems;
- I. Graph, differentiate and integrate functions in polar and parametric form;
- J. Determine convergence or divergence of an infinite sequence;
- K. Determine convergence or divergence of an infinite series, alternating or non-alternating, by applying tests for convergence;
- L. Estimate the sum of a convergent series;
- M. Determine convergence or divergence of a power series, and find the radius and interval of convergence;
- N. Find the radius and interval of convergence;
- O. Apply theorems for differentiation and integration of a power series;
- P. Find Taylor and Maclaurin series for a given function;
- Q. Use the binomial series to find a power series of a function;

V. CONTENT:

- A. Transcendental functions
 1. Exponential functions
 - a. Differentiation
 - b. Integration
 2. Logarithmic functions
 - a. Differentiation
 - b. Logarithmic differentiation
 - c. Integration
- B. Inverse trigonometric functions
 1. Domain and range

- 2. Graphs
- 3. Differentiation
- 4. Antiderivatives and integration formulas
- C. Hyperbolic functions
 - 1. Definitions and graphs
 - 2. Identities
 - 3. Differentiation
 - 4. Antiderivatives and integration formulas
 - 5. Inverse hyperbolic functions
 - 6. Differentiation
 - 7. Antiderivatives and integration formulas
- D. Indeterminate forms
 - 1. Types of indeterminate forms
 - 2. L'Hospital's rule
 - 3. Techniques for evaluating limits of indeterminate forms
- E. Techniques of integration
 - 1. Substitution
 - 2. Inverse trigonometric function integration formulas
 - 3. Integration by parts
 - 4. Products of trigonometric functions
 - 5. Trigonometric substitution
 - 6. Partial fraction decomposition
 - 7. Table of Integrals
- F. Numerical methods of integration
 - 1. Midpoint rule
 - 2. Trapezoidal rule
 - 3. Simpson's rule
 - 4. Error analysis
- G. Improper integrals
- H. Applications of integration
 - 1. Arc length
 - 2. Surface area of a solid of revolution
 - 3. Moments and center of mass
 - 4. Work
- I. Separable first order differential equations
- J. Exponential growth and decay
- K. Parametric curves and equations;
 - 1. Curve sketching and direction of motion
 - 2. Elimination of a parameter
 - 3. Calculus with parametric curves
 - a. Slope of a tangent line
 - b. Area
 - c. Arc length
- L. Polar curves and equations;
 - 1. Polar coordinates
 - 2. Curve sketching
 - 3. Calculus with polar curves
 - a. Slope of tangent line
 - b. Area
 - c. Arc length
- M. Infinite sequences
 - 1. Definition
 - 2. Geometric sequence
 - 3. Convergence
 - 4. Divergence
- N. Infinite series
 - 1. Geometric series
 - 2. Telescoping series
 - 3. p-series
 - 4. Alternating series
 - 5. Tests for convergence or divergence
 - a. nth term divergence test
 - b. Integral test
 - c. p-series test
 - d. Comparison tests
 - e. Alternating series test
 - f. Ratio and root tests
 - 6. Sum of a convergent series
- O. Power series
 - 1. Definition
 - 2. Power series representation of a function
 - 3. Tests for convergence
 - 4. Radius and interval of convergence
 - 5. Applications
 - 6. Binomial series
- P. Taylor and Maclaurin series
 - 1. Definition
 - 2. Finding the Taylor or Maclaurin series representation of a function
 - 3. Taylor's inequality

VI. METHODS OF INSTRUCTION:

- A. **Discussion** -
- B. **Lecture** -
- C. Web- or CD-Rom-based tutorials
- D. Student presentations
- E. Collaborative learning

VII. TYPICAL ASSIGNMENTS:

- A. Homework

1. Homework should be assigned from the text and should include a sufficient number and variety of problems to develop both skill and conceptual understanding. Problems should range in level of difficulty from introductory level to challenging. A typical assignment should take an average student 1 to 2 hours for each hour in class.
- B. Collaborative learning
 1. Collaborative learning, done in small groups of 2-4 students, can be used to introduce new concepts, build skills, or teach problem solving. Students may be asked to present their results on the board.
 2. Example collaborative learning assignment: Have each group solve a curve-sketching problem and then present their work to the rest of the class, explaining the process they used and their results.

VIII. EVALUATION:

A. **Methods**

1. Exams/Tests
2. Quizzes
3. Home Work
4. Other:
 - a. Collaborative Group Activities

B. **Frequency**

1. Exams/Tests
 - a. Recommend minimum of four exams
 - b. Comprehensive final examination
2. Quizzes
 - a. Announced or unannounced, in-class or take home at the discretion of the instructor
3. Homework
 - a. Assigned for each section covered
4. Collaborative Group Activities
 - a. At the discretion of the instructor

IX. TYPICAL TEXTS:

1. Briggs, W., Cochran, L., & Gillett, B. (2015). *Calculus* (2nd ed.). Boston, MA: Pearson.
2. Larson, R., & Edwards, B. (2014). *Calculus* (10th ed.). Boston, MA: Cengage Learning.
3. Rogawski, J., & Adams, C. (2015). *Calculus* (3rd ed.). New York, NY: W.H Freeman.

X. OTHER MATERIALS REQUIRED OF STUDENTS:

- A. Graphing calculator may be required