Note: This unit contains many significant multiplication and division concepts. You may wish to spread these sessions across a Semester, or repeat to use it as a base on which to add your own ideas, according to your student's needs.

Topic: Multiplicat	tion and Division Level:	4					
KEY CONCEPTS: (p	olease insert your relevant curric	ulum outcomes here)					
*Recall multiplica	tion facts up to 10 x 10 and relate	ed division facts.					
*Investigate numb	per sequences involving multiples	of 3, 4, 6, 7, 8, and 9.					
*Develop efficient	t mental and written strategies for	or multiplication and for division w	here there is no remainder.				
	Equipment/Resources: Arrays, printed games (links provided below), printed  Vocabulary: 'rows of', array, double, product, multiple, factor, divisible,						
	ask sheets (link below), Mfacts121		strategy language- 'double, double', col	•			
'	dividual whiteboards and markers	taran da antara da a	strategy language abusic, abusic, col	initiatativity tarif are	Julia lacts		
SESSION &	TOOLS / WARM UP	WHOLE GROUP LEARNING	INDEPENDENT LEARNING	REFLECTION/	ASSESSMENT		
LEARNING				SUMMARY	and FEEDBACK		
INTENTION							
(L.I.)							
Session 1	Whole class- each student will	Teacher explains: 'We will be	<u>Pre-Assessment Task</u>	Teacher	Collect		
L.I: We are	be given one minute to write	finding out what we already	&	summarises-	pre-assessment		
reflecting on	down the multiples of 6 (skip	know about multiplication and	Teacher Talk & Marking Guide for	'today we were	task and sort		
what we know	count by 6s) (or could be	what we don't know <b>yet,</b> with	<u>Assessment</u>	thinking about	into groups		
about	multiples of 7- teacher	this task. Let's do that now.'	Teacher explains- students are to	what we know	according to		
multiplication	chooses based on class		answer the questions and explain	about	level of		
and what we	needs). How far can each		their thinking.	multiplication.	understanding.		
don't know <b>yet.</b>	student get in <b>one minute</b> ?			In the next few	Notice trends to		
	Students write in their		Teacher to rove and question the	sessions, we will	inform teaching		
	books/whiteboards.		students on their thinking- record any	be working on	practice for this		
	After the one minute		observations on the student work.	strategies for	unit.		
	concludes, the class calls out		Try to question the students in order	learning our	Teacher Talk &		
	the list of multiples and		to get more information.	multiplication	Marking Guide		
	students correct their own		Students may be reluctant to record	facts (times	<u>for Assessment</u>		
	work. Teacher briefly draws		their thinking- it's very useful to rove	tables)'			
	attention to patterns/		and get better insights.				
	strategies. Asks students to look at their own work- what						
	was tricky for you? What strategies can help you when						
	counting by 6s/7s? <b>Then,</b>						

	repeat- can students go				
	further and improve on their				
	personal best? Provide one				
	more minute for students to				
	count as far as they can by 6s.				
	Becoming proficient at				
	anything takes effort and				
	practise.				
	Teacher Talk Video: 'Skip				
	Counting and Multiples'				
Session 2	Whole class- each student will	Write 4 x 7 on the board and	Students have individual	What new idea	
L.I: We are	be given one minute to write	ask-	whiteboards/workbooks so everybody	did you learn	
solving 4 X _	down the multiples of 6 (skip	'How would <i>you read</i> this	has the chance to participate:	today?	
equations and	count by 6s) (or could be	number sentence/equation?'			
exploring our	multiples of 7- teacher	Record variations- '4 times 7',	Write <b>4 X 7 = ?</b> on the board. Ask		
strategies.	chooses based on class	'4 groups of 7', '4 multiplied	students: how would <i>you</i> solve this		
	needs). How far can each	by 7'	equation? Ask all students to record		
	student get in one minute?		their answers and workings. Writing		
	Students write in their	Introduce the idea that X also	not only the answer, but using		
	books/whiteboards.	means 'rows of'. Add '4 rows	diagrams or showing workings out, to		
	After the one minute	of 7' to the list.	demonstrate how they would explain		
	concludes, the class calls out		their answer.		
	the list of multiples and	On individual whiteboards/in	Teacher note: we are looking for		
	students correct their own	workbooks, ask students to	strategies such as skip counting by 7s		
	work. Teacher briefly draws	draw 4 x 6 as an array (4 rows	or 4s, repeated addition, drawing a		
	attention to patterns/	of 6).	diagram (drawing arrays or groups of),		
	<b>strategies.</b> Asks students to		making connections (e.g.I knew 3 x 7 is		
	look at their own work- what	<u>Teacher note-</u> many children	21, so I added an extra 7).		
	was tricky for you? What	will draw <b>6 rows of 4</b> . This is not			
	strategies can help you when	the array they were asked to	Did any student think of doubling		
	counting by 6s/7s? <b>Then,</b>	draw. Discuss with class. Does it	twice? View '4 x Strategy' Video,		
	repeat- can students go	matter? If you needed to set	saying 'Here is another example of a		
	further and improve on their	out 4 rows of 6 chairs for a	good way to solve <b>4 X</b> anything'.		
	personal best? Provide one	concert, would it be the same if	Teacher note: we wish to have		
	more minute for students to	you set our 6 rows of 4 chairs	students discussing and sharing their		
	count as far as they can by 6s.	instead? You will get the same	strategies, learning from each other		
	Becoming proficient at	answer/product, but <u>6 rows of 4</u>	and exploring efficient ideas. The aim		
	anything takes effort and	is the turn around fact for $\frac{4}{}$	is to move students on from skip		
	practise.	<u>rows of 6</u> . You can literally turn	counting, to more sophisticated and		

	Teacher Talk Video: 'Skip	the array around 90°, to show	effective strategies.		
	Counting and Multiples'	the two arrays.	<i>"</i>		
		Teacher Talk Video: 'Using	Play '4 x Game'		
		Arrays & meaning of the X sign'			
			*Extend- play an adjusted version of		
			the '4 x _ Game', increasing the		
			number range, so that high attainers		
			are to multiply 4 x 2-digit numbers		
			(refer to instructions on game)		
Session 3	Count aloud as a class, by 4s,	Students have individual	Begin Rotations: (complete over two	What are your	
L.I: We are	6s or 7s. Note patterns or	whiteboards/workbooks so	sessions)	strategies for	
practising	strategies. Reiterate that	everybody has the chance to		doubling	
solving 4 X _	these are the multiples of	participate:	1. Students to log onto mfacts121.com	numbers?	
equations using	4/6/7.		and view the '4 x Strategy' Video.		
efficient		Write <b>4 X 5 = ?</b> on the board.	They then complete 'Online Practise'	E.g. how would	
strategies.		Ask students: how would you	for the level they are working on.	you solve double	
		solve this equation? Ask all		Double 12?	
		students to record their	2. Worksheet: Worksheet- doubling	Double 26?	
		answers and workings. Writing	numbers 10-50		
		not only the answer, but using	And /or:	Look for efficient	
		diagrams or showing workings	Worksheet- doubling numbers from	strategies such	
		out, to demonstrate how they	<u>50-99</u>	as double the	
		would explain their answer.		tens, then the	
		Teacher note: we wish to have	3. Students use the Mfacts121 Playing	ones, then add	
		students discussing and sharing	Cards: students choose the level they	back together for	
		their strategies, learning from	are working on and play card games	the total.	
		each other and exploring	(answers on back of each card).		
		efficient ideas. The aim is to	Teachers: please print these <b>playing</b>		
		move students on from skip	card sets for your classroom, on		
		counting, to more sophisticated	coloured card. Photocopy		
		and effective strategies.	back-to-back, so answers are on the		
			back of each card. They can all be		
		View '4 x _ Strategy' Video	found here: <u>Printable Resources</u> , for		
		again, if you believe this would	example <u>Red Apprentice</u> Playing Cards.		
		be beneficial.			
		*See <u>'Teacher Talk'</u> for ideas			
		and tips on teaching the Fours			
		Facts. You will also find ideas			
		about student prerequisite			

		skills required for learning this strategy.			
Session 4	Count aloud as a class, by 4s,	Provide instructions for the	Rotations- continued- complete the	What are your	
L.I: We are	6s or 7s. Note patterns or	rotational activities, to be	rotations from last session:	strategies for	
practising	strategies. Reiterate that	completed this session.		doubling	
solving 4 X _	these are the multiples of		1. Students to log onto mfacts121.com	numbers?	
equations using	4/6/7.		and view the '4 x Strategy' Video.		
efficient			They then complete 'Online Practise'	E.g. how would	
strategies.			for the level they are working on.	you solve double	
				Double 12?	
			2. Worksheet: Worksheet- doubling	Double 26?	
			numbers 10-50		
			And /or:	Look for efficient	
			Worksheet- doubling numbers from	strategies such	
			<u>50-99</u>	as double the	
				tens, then the	
			3. Students use the Mfacts121 Playing	ones, then add	
			Cards: students choose the level they	back together for	
			are working on and play card games	the total.	
			(answers on back of each card).		
			Teachers: please print these <b>playing</b>		
			card sets for your classroom, on		
			coloured card. Photocopy		
			back-to-back, so answers are on the		
			back of each card. They can all be		
			found here: <u>Printable Resources</u> , for		
			example <u>Red Apprentice</u> Playing Cards.		
Session 5	Play 'Multiples Game'	Write <b>5 X 8=?</b> on the board.	In pairs, students play '5 x Game'	Growth Mindset	Assessment-
L.I: We are	(Teacher chooses which	Ask students: how would <i>you</i>		Reflection:	Teacher logs
solving <b>5 X</b>	multiple they would like to	solve this equation? Allow think	*Extend- play an adjusted version of	How have you	onto
equations and	focus on- perhaps 6 or 7).	time and share ideas. E.g.	the '5 x _ Game', increasing the	grown your	mfacts121.com
exploring our		students may say: turn it	number range, so that high attainers	maths brain?	and clicks
strategies.		around and make it 8 x 5 and	are multiplying 5 x 2-digit numbers	How do you	<b>'Results'</b> button
		count by 5s up to 40, or count	(refer to instructions on game).	improve at your	on top of page,
		by 8s, or 'I just know it' (ask for		multiplication	to view, at a
		an explanation!)	*See <u>'Teacher Talk'</u> for ideas and tips	facts?	glance, which
			on teaching the Fives Facts. You will		level of facts
		Begin recording strategies for	also find ideas about student		each child is up
		multiplication on a class chart-	prerequisite skills required for	Optional extra:	to.

		'Multiplication Facts – Our Strategy List' You can skip count 1 2 X _ you can double it 1 4 X _ you can double it twice  (It's a good idea to start with the class building up their own list, rather than giving them the pre-determined list of strategies. The Mfacts121 Strategy List can be brought in later and linked to what students have developed themselves.  View - '5 x _ Strategy' Video	learning this strategy.	Growing Your Maths Brain, reflection sheet Keep the worksheet safe and add to it later as students continue to work on the multiplication.	Click this Levels and Strategies Teacher Checklist to see the progression of levels.
Session 6 L.I: We are	(Repeat Session 1 Tools/Warm Up)	Depending on the stage your class is at, either:	In pairs, students play Play 4 x  Game', 5 x Game' or 6 x Game'.	What are your favourite	
investigating	Whole class- each student will	revise the fours facts and the	Students can self-reflect and decide	strategies for	
efficient strategies for	be given one minute to write down the multiples of 6 (skip	<i>fives facts</i> , by posing questions such as:	which strategy/facts they believe they need to work on, choosing the	your multiplication	
the	count by 6s) (or could be	How would you solve:	appropriate game in pairs.	facts so far?	
multiplication	multiples of 7- teacher	4 x 8	appropriate game in pairs.	Why?	
facts.	chooses based on class	4 x 23 (you could use 'double,	*Extend- for high attainers, play an	,	
	needs). How far can each	double' with large numbers too)	adjusted version of the '6 x _ Game',		
	student get in one minute?	5 x 8	increasing the number range, so that		
	Students write in their	5 x 50 (you could use 'think 10 X	high attainers are multiplying <u>6 x</u>		
	books/whiteboards.	50, then halve it' for example)	<b>2-digit numbers.</b> They may need pencil		
	After the one minute	Students have their	and paper to calculate these products		
	concludes, the class calls out	workbooks/whiteboards to try	and can be encouraged to use <b>a range</b>		
	the list of multiples and	these equations, to ensure	of efficient strategies, including		
	students correct their own	maximum involvement.	'distributive property- separate the		
	work. Teacher briefly draws		question into easier parts' such as for		
	attention to patterns/	or	6 X 23, think 6 X 20 and 6 X 3 and add.		
	strategies. Asks students to look at their own work- what	Introduce the 6 V strategy	(refer to instructions on game for		
	Took at their own work- what	Introduce the 6 X_ strategy,	'extend' version).		

	and the Committee of th	the control of the second			1
	was tricky for you? What	through the video,			
	strategies can help you when	View <u>'6 x Strategy' Video'</u>			
	counting by 6s/7s? <b>Then,</b>				
	repeat- can students go				
	further and improve on their				
	personal best? Provide one				
	more minute for students to				
	count as far as they can by 6s.				
	Becoming proficient at				
	anything takes effort and				
	practise.				
	Teacher Talk Video: 'Skip				
	Counting and Multiples				
Session 7	Mfacts121 Practise Cards-	View the <u>'Turn Around Facts</u>	Rotational Activities: (done over two	What helps you	
L.I: We are	These cards should be	Strategy' Video	sessions)	learn your	
investigating	photocopied <i>back-to-back</i> so	(Commutativity)		multiplication	
strategies for	that you have questions on		1) <u>Self-Directed Tasks:</u> students	facts?	
the	the front and questions with		log on to their <u>mfacts121.com</u>		
multiplication	answers on the back.	Continue recording on a <b>class</b>	account and choose which		
facts.		chart-	colour <i>Self-Directed task</i> they		
	Best to do it on <i>coloured card</i>	'Multiplication Facts – Our	will complete. They will need a		
	and keep sets in the	Strategy List'	desktop / laptop or tablet,		
	classroom for regular use.		their workbook and		
			headphones (preferably) to		
	Students can choose	Suggestion- this may be a good	complete these tasks.		
	whichever colour level they	point to introduce the	2) <b>Game- '</b> 4 X <u>Game</u> ' or ' <u>6 X</u>		
	are working on, or wish to	Mfacts121 Strategy List.	Game' from last sessions		
	revise, and use that Practise	E.g. you could: display in	3) Worksheet- 4 x and 6 x facts		
	Card.	classroom/stick in student's			
	Students will be given <b>two</b>	books/students self-reflect and tick off each strategy, once they	*Early finishers: choose a Practise Card (from Tools/Warm Up) to keep		
	minutes to see how many	understand it.	working on.		
	'	unucistanu it.	working on.		
	they can answer. They must				
	write each question and the				
	answer in their book.				
	When time is up, students				
	turn their Practise Card over				
	tarii tileli i idetise cara over				

		I	*Fault Calabana abasas a Duartin	T .	
	minutes to see how many		*Early finishers: choose a Practise Card (from Tools/Warm Up) to keep		
	they can answer. They must		working on.		
	write each question and the				
	answer in their book.				
	When time is up, students				
	turn their Practise Card over				
l	and self correct (answers will				
	be on the back of their card).				
	Next, teacher picks out a				
	multiplication question from				
	any card, to discuss- E.g. 4 x 6				
	ask: what is your strategy? or				
	'How did you know the				
	answer?' Discuss ideas.				
	Now repeat the practise				
	cards. <u>Provide <b>two minutes</b></u>				
	again. Can the students				
	improve on their score?				
	Aim is to continue to improve				
	on personal best,				
	<u>Teacher Talk Video: 'Practise</u>				
	Cards'.				
Session 9	Whole class- each student will	Teacher explains: 'we have	Pre-Assessment Task		Correct the Post
L.I: We are reflecting on	be given one minute to write down the multiples of 6 (skip	learnt about multiplying. You	& Teacher Talk & Marking Guide for		Assessment and identify new
what we have	count by 6s) (or could be	are going to reflect on what you	Assessment		learnings and
learnt about	multiples of 7- teacher	have learnt, by having another	Students are given back their <b>original</b>		growth for each
multiplication.	chooses based on class	look at the <b>task</b> you did in the	assessment task and now they add to		student.
	needs). How far can each	beginning.'	/change their answers based on their		
	student get in <b>one minute</b> ?		new learnings (using a different colour		Give the task
	Students write in their		pen/pencil).		back to
	books/whiteboards.		, perion,		students, so they

After the one minute	Teacher to rove and question the	can view their
concludes, the class calls out	students on their thinking- record any	own growth and
the list of multiples and	observations on the student work.	achievements.
students correct their own	Question the students, to obtain more	
work. Teacher briefly draws	information.	
attention to patterns/		
strategies. Asks students to		
look at their own work- what		
was tricky for you? What		
strategies can help you when		
counting by 6s/7s? <b>Then,</b>		
repeat- can students go		
further and improve on their		
personal best? Provide one		
more minute for students to		
count as far as they can by 6s.		
Becoming proficient at		
anything takes effort and		
practise.		
<u>Teacher Talk Video: 'Skip</u>		
Counting and Multiples'		
 lext are sessions which build on the previous multiplication	on concents	•

- Next, are sessions which build on the previous multiplication concepts.
- Division is introduced and strategies for multiplication with larger numbers are explored.
- You may wish to do these sessions in the second Semester.
- Remember to regularly revisit multiplication concepts, strategies and facts, during 'Tools time/Warm Ups' throughout the whole year, as it's such a vital part of Senior Primary Maths and requires regular attention.

puit or or	part of School Filmary Matris and requires regular determinant						
Session 10	Play 'Multiples Game'	View 'Making Connections	Fill in the Making Connections Chart-	What are your	Assessment-		
L.I: We are	(Teacher chooses which	Strategy' Video.	individually or in pairs.	favourite	Teacher logs		
investigating	multiple they would like to			strategies for	onto		
strategies for	focus on, perhaps 6 or 7).	*See <u>'Teacher Talk'</u> for ideas		multiplication	mfacts121.com		
the		and tips on teaching the		facts?	and clicks		
multiplication		Making Connections strategy.		What facts	'Results' button		
facts.				and/or strategies	on top of page,		
				do you not	to view, at a		
				understand YET?	glance, which		
					level of facts		
					each child is up		
					to.		

					Click this Levels and Strategies Teacher Checklist to see the progression of levels.
Session 11 L.I: We are using our knowledge of multiplication to help with division.	Once multiplication facts are consolidated, division facts can be introduced, by relating to multiplication.  'Fact families'. Write a multiplication fact on the board e.g.  3 x 5 = 15  Ask students to draw the array; 3 rows of 5. Use the array to explore these facts-  *3 rows of 5 is 15 (3 x 5 = 15)  *5 rows of 3 is 15 (5 x 3 = 15) (turn the array 90 degrees to illustrate this).  The array also helps with division. Let's think about:  *15 ÷ 3 = ? Encourage students to 'think multiplication' to solve division facts- i.e. think: 3 whats are 15? Or 3 X ? = 15 3 fives are 15.	View the video relating division and multiplication.  Connecting Multiplication and Division video.	Worksheets: Fact Families- Connecting Multiplication and Division  Fact Families- Connecting Multiplication and Division 2  *Extend: Challenge: Fact Families- Connecting Multiplication and Division Challenge!	Have you ever 'thought multiplication' to help with division?	

	Highlight or ring each row of five. 3 fives are 15 (or 3 rows of 5 is 15)  Now turn the array 90 degrees around so it's showing 5 rows of 3.				
	*15 ÷ 5 = ?  Encourage students to 'think multiplication' to solve division- i.e. think: 5 whats are 15?  Or 5 X ? = 15  5 threes are 15.  Next, highlight or ring each row of three. 5 threes are 15				
	(or 5 rows of 3 is 15)  Students then write the 4 facts, in the fact family:  3 x 5 = 15  5 x 3 = 15  15 ÷ 3 = 5  15 ÷ 5 = 3				
Session 12 L.I: We are using our knowledge of multiplication to help with division.	'Fact families' - Write a multiplication fact equation on the board e.g. 6 x 4 = 24  Students to draw the array, (6 rows of 4), then write the 4 facts in the fact family 6 x 4 = 24 4 x 6 = 24 24 ÷ 6 = 4	If you wish, review all or parts of the Connecting  Multiplication and Division video.	Students complete another 'Making Connections' chart to show how knowing one multiplication fact, can help us with many more facts, including division.  *Early finishers/ Extend: Play online division games. Teacher to search for free online division games.	What does 'inverse' operation mean? Find definition.	

Session 13	24 ÷ 4 = 6  Now call on students to explain each fact, using the array as a model -  E.g. 6 x 4 = 24, we can see six rows of 4, equals 24 on the array  4 x 6 = 24, if we rotate the array, we can also see that 4 rows of 6, equals 24  24 ÷ 6 = 4, if we divide 24 into 6 equal groups, it's 4 in each 24 ÷ 4 = 6, if we divide 24 into 4 equal groups, it's 6 in each  Count aloud as a class, by 6s		What you need: playing cards spread	What does	
We are multiplying with larger numbers.	or 7s. Note patterns or strategies. Reiterate that these are the multiples of 6 or 7.	Write the equation:  4 X 18 =  All students to have workbooks/whiteboards to ensure engagement with this question. Ask: how could you solve this?  Allow time to think- ask students to show any working. Teacher notes: you may see attempts at repeated addition, lists of counting by 4s, perhaps 'double, double'. Or the formal algorithm. Ask students who use the formal algorithm if they have another mental strategy too. We are aiming to develop number sense, as well as the formal algorithm.  Share suggestions. Focus in on	around student's tables (picture cards removed).  Students make their own 2 digit by 1 digit multiplication equations, by choosing 3 playing cards and making the numbers.  They record their equation and solve, using any strategy they feel is efficient for them.  Draw attention to any efficient mental strategies being used- such as distributive property.	distributive property mean to you?	

Session 14 Mfacts121 Practise Cards-	anyone who uses the distributive property (separating the question into parts- e.g. 4 x 10 and 4 x 8) View Distributive Property Video Teacher explains: 'We are going	Students work on Grid Method	What do you	
These cards should be photocopied back-to-back so that you have questions on the front and questions with answers on the back.  Best to do it on coloured card and keep sets in the classroom for regular use.  Students can choose whichever colour level they are working on, or wish to revise, and use that Practise Card.  Students will be given two minutes to see how many they can answer. They must write each question and the answer in their book.  When time is up, students turn their Practise Card over and self correct (answers will be on the back of their card).  Next, teacher picks out a multiplication question from	to learn a great strategy for larger multiplication questions.' View this demonstration video link: Grid Method  Teacher demonstrates grid method (2 x 1 digit). Teacher note: this is really a version of 'distributive property-separating the question into easier parts'. Place value is important to draw attention to as well.  If you would like to view the distributive property video again: Distributive Property  Video	worksheets.  Grid Method Worksheet- 2 x 1 digit numbers  *Extend: high attainers may be challenged to use the same approach with 2 x 2 digit numbers:  Grid Method Worksheet- 2 x 2 digit	think of using the grid method as a mental strategy? What are the positives and negatives of it?	

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	any card, to discuss- E.g. 4 x 6				
	ask: what is your strategy? or				
	'How did you know the				
	answer?' Discuss ideas.				
	Now repeat the practise				
	cards. Provide two minutes				
	again. Can the students				
	improve on their score?				
	Aim is to continue to improve				
	on personal best,				
	Teacher Talk Video: 'Practise				
	Cards'.				
Session 14 and	Play 'Multiples Game'	At this point, formal written	What you need: playing cards spread	How confident	
beyond-	(Teacher chooses which	algorithms can be introduced. It	around student's tables (picture cards	do you feel with	
	multiple they would like to	is our belief that introducing	removed).	multiplication	
We are	focus on, perhaps 6 or 7).	them too early, stifles the		and division?	
multiplying and		development of flexible mental	Students make their own 2 digit by 1		
dividing with		strategies, which are so	digit multiplication/division equations,		
larger numbers.		important.	by choosing 3 playing cards and		
			making the numbers.		
		In the following sessions, model			
		the use of the formal written	They record their equation and solve		
		algorithms for multiplication	(twice), using two strategies- one		
		and division. Still being aware	mental and also the formal written		
		that students should be able to	algorithm.		
		explain each step in the			
		process.	Draw attention to any efficient mental		
			strategies being used.		

Other Strategy Videos suggested for this level: (use across the year, in 'Tools/Warm Up time'- add to your bank of strategies, etc.)

• Tens Facts: 10 x \_ = Think 'make it 10 times bigger with a zero'