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- MODULE HopProtocol -
EXTENDS Integers, Naturals, TLC, Sequences, FiniteSets
VARIABLES
  l1 Chain,
  l2 Chain,
  chains,
  pending {\it Transfers},
  commitThreshold,
  bonded Withdrawals,
  roots
SumSeq(S) \triangleq
  Let seq \triangleq S
          Sum[i \in 1 ... Len(seq)] \stackrel{\triangle}{=} IF i = 1 THEN seq[i] ELSE seq[i] + Sum[i-1]
       IF seq = \langle \rangle THEN 0 ELSE Sum[Len(seq)]
RECURSIVE SeqFromSet(_)
SeqFromSet(S) \triangleq
  If S = \{\} then \langle \rangle
   ELSE LET x \stackrel{\triangle}{=} \text{CHOOSE } x \in S : \text{TRUE}
           IN \langle x \rangle \circ SeqFromSet(S \setminus \{x\})
Range(s) \triangleq \{s[x] : x \in DOMAIN \ s\}
Hash(v) \stackrel{\triangle}{=} CHOOSE \ n \in 1..5 : TRUE
Assume (Hash(\langle 1 \rangle) = Hash(\langle 1 \rangle))
ASSUME (Hash((\{1, 2, 3\})) = Hash((\{2, 1, 3, 1\})))
Init \triangleq
   \wedge l1 Chain = 1
  \wedge l2Chain = 2 \dots 3
   \land\ chains = 1\ldots 3
   \land pendingTransfers = [c \in l2Chain \mapsto \langle \rangle]
   \land commitThreshold = 1
   \land roots = [c \in chains \mapsto \langle \rangle]
   \land bondedWithdrawals = [c \in chains \mapsto \{\}]
SendTransfer(c) \triangleq
  \wedge c \neq 1
  \land Len(pendingTransfers[c]) < 5
   \land pending Transfers' = [pending Transfers \ EXCEPT \ ![c] = pending Transfers[c] \circ \langle [
       target \mapsto chains, \ amount \mapsto 1, \ id \mapsto Hash(1 \dots 2)
  \land Print(\langle "send", Len(pendingTransfers[c]) \rangle, TRUE)
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\(\triangle \) UNCHANGED \(\langle 11 Chain, \) 12 Chain, \(\chains, \) roots, \(\chains, \) roots, \(\chains, \) threshold, \(\begin{aligned} \begin{aligned} \langle 11 Chain, \) 12 Chain, \(\chains, \) roots, \(\chains, \chains, \) roots, \(\chains, \chains, \) roots, \(\chains, \chains, \chains, \chains, \chains, \) roots, \(\chains, \chains, \chain
CommitTransfers(c) \stackrel{\triangle}{=}
      \land c \neq 1
      \land Len(roots[c]) < 20
      \land SumSeq([x \in DOMAIN \ pendingTransfers[c] \mapsto pendingTransfers[c][x].amount]) > commitThreshold
      \wedge Print(\langle \text{"commit"} \rangle, \text{TRUE})
      \land pendingTransfers' = [pendingTransfers \ EXCEPT \ ![c] = \langle \rangle]
      \land roots' = [k \in chains \mapsto roots[k] \circ \langle Hash(pendingTransfers[c]) \rangle]
      \land UNCHANGED \langle l1 Chain, l2 Chain, chains, commitThreshold, bondedWithdrawals <math>\rangle
BondWithdrawal(dest) \stackrel{\Delta}{=}
      \land \exists source \in l2Chain :
          \land Len(pendingTransfers[source]) > 0
          \land \exists x \in \text{DOMAIN } pendingTransfers[source] :
                \land pendingTransfers[source][x].id \notin bondedWithdrawals[dest]
                \land bondedWithdrawals' = [bondedWithdrawals Except ![dest] = bondedWithdrawals[dest] \cup {pending
                \land Print(\langle "bondWithdrawal", bondedWithdrawals' \rangle, TRUE)
          \land UNCHANGED \langle l1 Chain, l2 Chain, chains, commitThreshold, pendingTransfers, roots <math>\rangle
Next \stackrel{\triangle}{=}
      \land \exists c \in chains:
               \land \lor SendTransfer(c)
                     \vee CommitTransfers(c)
                      \vee BondWithdrawal(c)
AllHaveTransferRoots \triangleq \land \forall c \in chains:
                                                                            \wedge Len(roots[c]) > 0
                                                                                 \land \forall k \in chains : Range(roots[c]) \cap Range(roots[k]) \neq \{\}
AllHaveBondedWithdrawals \stackrel{\triangle}{=} \land \forall c \in chains:
                                                                                          \land Len(SeqFromSet(bondedWithdrawals[c])) > 0
EventuallyAllHaveTransferRoots \triangleq \Diamond \Box AllHaveTransferRoots
Eventually All Have Bonded With drawals \triangleq \Diamond \Box All Have Bonded With drawals
vars \triangleq \langle l1 Chain, l2 Chain, chains, pending Transfers, commit Threshold, roots, bonded Withdrawals \rangle
Spec \stackrel{\triangle}{=} Init \wedge \Box [Next]_{vars} \wedge WF_{vars}(Next)
Live \triangleq EventuallyAllHaveTransferRoots \land EventuallyAllHaveBondedWithdrawals
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