The modal-Gamma-distribution

Parametrisation

The modal-Gamma-distribution has the following density

$$\pi(y) = \frac{b^a}{\Gamma(a)} y^{a-1} \exp(-by), \qquad a > 1, \quad b > 0, \quad y > 0.$$

where the mode m = (a-1)/b is the target of the regression model instead of the mean or quantile. Note the constraint a > 1.

With precision

$$\tau = (s\phi)/m^2$$

for fixed scaling s and precision parameter ϕ , this complete the spesification. The mapping back to the (a,b)-parameterisation is then $\phi'=s\phi,\ \delta=\left(\sqrt{\phi'(\phi'+4)}+\phi'\right)/2$, then

$$a = 1 + \delta$$
 and $b = \delta/m$

Link-function

The linear predictor η is linked to the mode m using a default log-link

$$m = \exp(\eta)$$

Hyperparameter

The hyperparameter is the precision parameter ϕ , which is represented as

$$\phi = \exp(\theta)$$

and the prior is defined on θ .

Specification

- family="mgamma" for regression models and family="mgamma.surv" for survival models.
- Required arguments: for mgamma.surv, y (to be given in a format by using inla.surv()), and for mgamma, y and s (default value 1).

The scalings s is **not** used for family="mgamma.surv".

Hyperparameter spesification and default values

doc The modal Gamma likelihood

hyper

theta

hyperid 58002

name precision parameter

short.name prec

output.name Precision-parameter for the modal Gamma observations

output.name.intern Intern precision-parameter for the modal Gamma observations initial 4.60517018598809

```
fixed FALSE
         prior loggamma
         param 1 0.01
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
survival FALSE
discrete FALSE
link default log
pdf mgamma
doc The modal Gamma likelihood (survival)
hyper
    theta1
         hyperid 58121
         name precision parameter
         short.name prec
         output.name Precision-parameter for the modal Gamma surv observations
         output.name.intern Intern precision-parameter for the modal Gamma surv observations
         initial 0
         fixed FALSE
         prior loggamma
         param 1 0.01
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
    theta2
         hyperid 58122
         name beta1
         short.name beta1
         output.name beta1 for modal Gamma-Cure
         output.name.intern beta1 for modal Gamma-Cure
         initial -7
         fixed FALSE
         prior normal
         param -4 100
         to.theta function(x) x
         from.theta function(x) x
    theta3
         hyperid 58123
         name beta2
         short.name beta2
         output.name beta2 for modal Gamma-Cure
         output.name.intern beta2 for modal Gamma-Cure
```

```
initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta4
    hyperid 58124
    name beta3
    short.name beta3
    output.name beta3 for modal Gamma-Cure
    output.name.intern beta3 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta5
    hyperid 58125
    name beta4
    short.name beta4
    output.name beta4 for Ga mma-Cure
    output.name.intern beta4 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta6
    hyperid 58126
    name beta5
    short.name beta5
    output.name beta5 for modal Gamma-Cure
    output.name.intern beta5 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta7
    hyperid 58127
```

```
name beta6
    short.name beta6
    output.name beta6 for modal Gamma-Cure
    output.name.intern beta6 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta8
    hyperid 58128
    name beta7
    short.name beta7
    output.name beta7 for modal Gamma-Cure
    output.name.intern beta7 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta9
    hyperid 58129
    name beta8
    short.name beta8
    output.name beta8 for modal Gamma-Cure
    output.name.intern beta8 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
    to.theta function(x) x
    from.theta function(x) x
theta10
    hyperid 58130
    name beta9
    short.name beta9
    output.name beta9 for modal Gamma-Cure
    output.name.intern beta9 for modal Gamma-Cure
    initial 0
    fixed FALSE
    prior normal
    param 0 100
```

```
to.theta function(x) x
         from.theta function(x) x
    theta11
         hyperid 58131
         name beta10
         short.name beta10
         output.name beta10 for modal Gamma-Cure
         output.name.intern beta10 for modal Gamma-Cure
         initial 0
         fixed FALSE
         prior normal
         param 0 100
         to.theta function(x) x
         from.theta function(x) x
survival TRUE
discrete FALSE
link default log neglog
pdf agamma
```

Example

In the following example we estimate the parameters in a simulated example.

```
n <- 10<sup>4</sup>
phi <- 2.2
x \leftarrow rnorm(n)
m \leftarrow exp(1.1 + 1.2 * x)
delta <- (sqrt(phi * (phi + 4.0)) + phi) / 2.0
y <- rgamma(n, shape = 1 + delta, rate = delta / m)
r \leftarrow inla(y ~1 + x,
           data = data.frame(y, x),
           family = "mgamma",
           control.compute = list(cpo = T),
           verbose = TRUE)
Y <- inla.surv(y, 1)
rr <- inla(Y ~ 1 + x,
           data = list(Y = Y, x = x),
           family = "mgammasurv",
           control.compute = list(cpo = T),
           verbose = TRUE)
```

Notes

None.