# Defining a latent model in R or C: The rgeneric and cgeneric model

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# Introduction

This is a class of generic models allows the user to define latent model component in R or C, for cases where the requested model is not yet implemented in INLA. The model component implemented in R will run slower, whereas the model component implemented in C will run just slightly slower, compared to a similar model implemented in INLA,

We will first describe the more accessible R interface, then at the end, the C interface as it is buildt on the same ideas.

# Defining a latent model in R

A rgeneric model is defined in a function rmodel (to be defined later), and the usage is quite simple. First we need to define a inla-rgeneric object

```
model = inla.rgeneric.define(rmodel, ...)
```

with additional variables/functions/etc in ... that we might use in rmodel. This can be the size, prior parameters, covariates, external functions and so on. This object can then be used to define a normal model component in INLA using f(),

```
y ~ ... + f(idx, model=model, ...)
```

where idx can take values  $1, 2, \ldots, n$  where n is the size of model. All additional features for f() will still be valid.

# Example: The AR1 model

The function rmodel needs to follow some rules to provide the required features. We explain this while demonstrating how to implement the AR1-model. This model already exists, see inla.doc("ar1"). With the parmeterisation we use, the AR1-model is defined as

$$x_1 \sim \mathcal{N}(0,\tau)$$
 and  $x_t \mid x_1,\ldots,x_{t-1} \sim \mathcal{N}(\rho x_{t-1},\tau_I), \quad t=2,\ldots,n.$ 

where  $\tau_I = \tau/(1-\rho^2)$ . The scale-parameter is the marginal precision  $\tau$ , not the commonly used innovation precision  $\tau_I$ . The joint density of x is Gaussian

$$\pi(x|\rho,\tau) = \left(\frac{1}{\sqrt{2\pi}}\right)^n \tau_I^{n/2} (1-\rho^2)^{1/2} \exp\left(-\frac{\tau_I}{2} x^T R x\right)$$

where the precision-matrix is

$$Q = \tau_I R = \tau_I \begin{bmatrix} 1 & -\rho & & & & \\ -\rho & 1 + \rho^2 & -\rho & & & \\ & -\rho & 1 + \rho^2 & -\rho & & \\ & & \ddots & \ddots & \ddots & \\ & & & -\rho & 1 + \rho^2 & -\rho \\ & & & & -\rho & 1 \end{bmatrix}$$

There are two (hyper-)parameters for this model: the marginal precision  $\tau$  and the lag-one correlation  $\rho$ . We will reparameterise these as

$$\tau = \exp(\theta_1),$$
 and  $\rho = 2\frac{\exp(\theta_2)}{1 + \exp(\theta_2)} - 1.$ 

It is required that the parameters  $\theta = (\theta_1, \theta_2)$  have support on  $\Re^2$  and the priors for  $\tau$  and  $\rho$  are given as the corresponding priors for  $\theta_1$  and  $\theta_2$ .

A good re-parameterisation is required for INLA to work well. A good parmeterisation makes, ideally, the Fisher information matrix of  $\theta$  constant with respect to to  $\theta$ . It is sufficient to check this in a frequentistic setting with data directly from the AR(1) model, in this case. INLA will provide the posterior marginals for  $\theta$ , but inla.tmarginal() can be used to convert it to the appropriate marginals for  $\rho$  and  $\tau$ .

We assign Gamma prior  $\Gamma(.; a, b)$  (with mean a/b and variance  $a/b^2$ ) for  $\tau$  and a Gaussian prior  $\mathcal{N}(\mu, \kappa)$  for  $\theta_2$ , so the joint prior for  $\theta$  becomes

$$\pi(\theta) = \Gamma(\exp(\theta_1); a, b) \exp(\theta_1) \times \mathcal{N}(\theta_2; \mu, \kappa).$$

The extra term,  $\exp(\theta_1)$  is the Jacobian for the change of variable from  $\tau$  to  $\theta_1$ . We will in this example use a = b = 1,  $\mu = 0$  and  $\kappa = 1$ .

In order to define the AR1-model, we need to make R-functions that returns

- the graph,
- the precision matrix  $Q(\theta)$ ,
- the zero mean,
- the initial values of  $\theta$ ,
- the log-normalising constant, and
- the log-prior

We need to incorporate these functions into rmodel, in the following way

```
initial = function() { <to be completed> }
  quit = function() { <to be completed> }

# sometimes this is useful, as argument 'graph' and 'quit'
# will pass theta=numeric(0) (or NULL in R-3.6...) as
# the values of theta are NOT
# required for defining the graph. however, this statement
# will ensure that theta is always defined.
if (!length(theta)) theta = initial()

val = do.call(match.arg(cmd), args = list())
return (val)
}
```

The input parameters are

- cmd What to return
- theta The values of the  $\theta$ -parameters

Other parameters in the model definition, like n and possibly the parameters of the prior, goes into the ... part of inla.rgeneric.define(), like

```
model = inla.rgeneric.define(inla.rgeneric.ar1.model, n = 100)
```

and is assigned in the environment of inla.rgeneric.ar1.model. Using variable n inside this function will then return 100. This environment can also be accessed as envir as defined in the function skeleton. Sometimes this is useful, to hold static varibles or to cache intermediate calculations.

Our next task, is to *fill in the blanks* and define the functions required. To help us, we will add a function that return a list of the **real** parameters in the model from  $\theta$ ,

Since theta exist already within inla.rgeneric.ar1.model we do not need to pass it as an argument.

We also assume that variable n is defined as an argument in inla.rgeneric.define().

### Function graph()

This is normally an easy function to add, as it is essentially the matrix Q. One can construct cases where this is not so<sup>1</sup>, and for this reason it exists as a separate function. The only thing that matter is if the elements are zero or non-zero. Also, it should return a sparse matrix as we do not want to pass  $n^2$  elements when  $\mathcal{O}(n)$  are sufficient. Also, only the upper triangular matrix (diagonal included) are actually used, since the graph must be symmetric.

```
graph = function() {
    return (Q())
}
```

#### function Q()

This is normally the most tricky function, as we need to return the precision matrix (as a sparse matrix) for the given values of  $\theta$ . Only the upper triangular matrix (diagonal included) are read.

<sup>&</sup>lt;sup>1</sup>Depending on  $\theta$  an element  $Q_{ij}$  might be exactly zero

A dense matrix version is as follows, and is easier to read

```
Q = function() {
    p = interpret.theta()
    Q = p$prec/(1 - p$rho^2) *
        toeplitz(c(1 + p$rho^2, -p$rho, rep(0, n - 2L)))
    Q[1, 1] = Q[n, n] = p$prec/(1 - p$rho^2)
    return (inla.as.sparse(Q))
}
```

The function inla.as.sparse() convert a matrix or sparse matrix, into the appropriate sparse matrix format used internally in INLA. This version of Q() creates a dense matrix and then make it sparse, and is not the way to do it. The better way, is to define the (upper triangular) sparse matrix directly using sparseMatrix.

```
Q = function() {
    p = interpret.theta()
    i = c(1L, n, 2L:(n - 1L), 1L:(n - 1L))
    j = c(1L, n, 2L:(n - 1L), 2L:n)
    x = p$prec/(1 - p$rho^2) *
        c(1L, 1L, rep(1 + p$rho^2, n - 2L),
            rep(-p$rho, n - 1L))
    return (sparseMatrix(i = i, j = j, x = x, giveCsparse = FALSE))
}
```

This is both faster and requires less memory, but it gets somewhat unreadable and hard to debug. The dense matrix version above, is at least easier to debug against for reasonable values of n.

### Function mu()

This function must return the mean which might depend on  $\theta$ . The convention, is that if numeric(0) is returned, then the mean is identical to zero (and then there is no need to check for this later)

```
mu = function() {
    return(numeric(0))
}
```

#### Function log.norm.const()

This function must return the log of the normalising constant. For the AR1-model the normalising constant is

$$\left(\frac{1}{\sqrt{2\pi}}\right)^n \tau_I^{n/2} (1 - \rho^2)^{1/2}$$

where

$$\tau_I = \tau/(1-\rho^2).$$

The function can then be implemented as

Since the normalizing constant is known, we can ask INLA to evaluate

$$-\frac{n}{2}\log(2\pi) + \frac{1}{2}\log(|Q(\theta)|)$$

and  $\log |Q(\theta)|$  can be computed from the sparse Cholesky factorisation of  $Q(\theta)$ . In this case we can return numeric(0) (which is a code for "compute it yourself, please!")

```
log.norm.const = function() {
  return (numeric(0))
}
```

Unless the log-normalizing constant is known analytically (and the precision matrix depends on  $\theta$ ) it is both better, and easier, just to return numeric(0).

# Function log.prior()

This function must return the (log-)prior of the prior density for  $\theta$ . For the AR1-model, we have for simplicity chosen this prior

```
\pi(\theta) = \Gamma(\exp(\theta_1); a, b) \exp(\theta_1) \times \mathcal{N}(\theta_2; \mu, \kappa)
```

so we can implement this as with our choices  $a=b=1,\,\mu=0$  and  $\kappa=1$  as

The parameters in the joint prior can also be defined in the inla.rgeneric.define() call, by adding arguments a=1, b=1 and so on.

**Note** that log.prior() must return the log prior for  $\theta$ , and not the prior for the more natural parameters defined in interpret.theta().

### Function initial()

This function returns the initial values for  $\theta$ , like

```
initial = function() {
   return (rep(1, 2))
}
```

or numeric(0) is there are no  $\theta$ 's. For a precision parameters it is generally advisable to chose a high precision as the initial value, as this helps the optimizer. INLA generally use initial value 4 for log precisions.

# Function quit()

This function is called when all the computations are done and before exit-ing the C-program. If there is some cleanup to do, you can do this here. In our example, there is nothing do to.

```
quit = function() {
   return (invisible())
}
```

#### Example of usage

Here is an example of use. The function inla.rgeneric.ar1.model() contains the functions given above, and can be used directly like this.

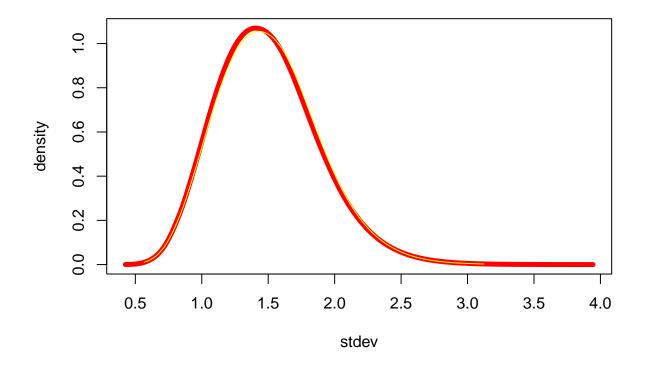
```
n = 100
rho=0.9
x = arima.sim(n, model = list(ar = rho)) * sqrt(1-rho^2)
```

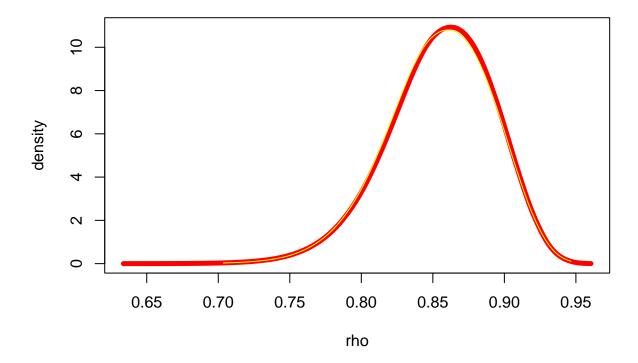
```
y = x + rnorm(n, sd = 0.1)
model = inla.rgeneric.define(inla.rgeneric.ar1.model, n=n)
formula = y ~ -1 + f(idx, model=model)
r = inla(formula, data = data.frame(y, idx = 1:n))
```

We can also compare with the buildt-in version, if we make sure to use the same priors

```
fformula = y ~ -1 +
    f(idx, model = "ar1",
        hyper = list(prec = list(prior = "loggamma", param = c(1,1)),
        rho = list(prior = "normal", param = c(0,1))))
rr = inla(fformula, data = data.frame(y, idx = 1:n))
```

and plot the hyperparameters in the same scale





The running time will of'course be quite different

# Example: The iid-model

The following function defines the iid-model, see inla.doc("iid"), which we give without further comments. To run this model in R, you may run demo(rgeneric).

inla.rgeneric.iid.model

```
## function (cmd = c("graph", "Q", "mu", "initial", "log.norm.const",
       "log.prior", "quit"), theta = NULL)
##
## {
##
       envir <- parent.env(environment())</pre>
##
       interpret.theta <- function() {</pre>
##
            return(list(prec = exp(theta[1L])))
##
##
       graph <- function() {</pre>
            G \leftarrow Diagonal(n, x = rep(1, n))
##
##
            return(G)
##
##
       Q <- function() {
```

```
##
            prec <- interpret.theta()$prec</pre>
##
            Q <- Diagonal(n, x = rep(prec, n))
##
            return(Q)
##
       }
##
        mu <- function() {</pre>
            return(numeric(0))
##
##
        log.norm.const <- function() {</pre>
##
##
            prec <- interpret.theta()$prec</pre>
            val <- sum(dnorm(rep(0, n), sd = 1/sqrt(prec), log = TRUE))</pre>
##
##
            return(val)
        }
##
##
        log.prior <- function() {</pre>
            prec <- interpret.theta()$prec</pre>
##
##
            val <- dgamma(prec, shape = 1, rate = 1, log = TRUE) +</pre>
##
                 theta[1L]
##
            return(val)
##
        }
##
        initial <- function() {</pre>
##
            ntheta <- 1
##
            return(rep(1, ntheta))
##
##
        quit <- function() {</pre>
            return(invisible())
##
##
        }
##
        if (!length(theta)) {
##
            theta <- initial()</pre>
##
        val <- do.call(match.arg(cmd), args = list())</pre>
##
        return(val)
##
## }
## <bytecode: 0x55823576da50>
## <environment: namespace:INLA>
```

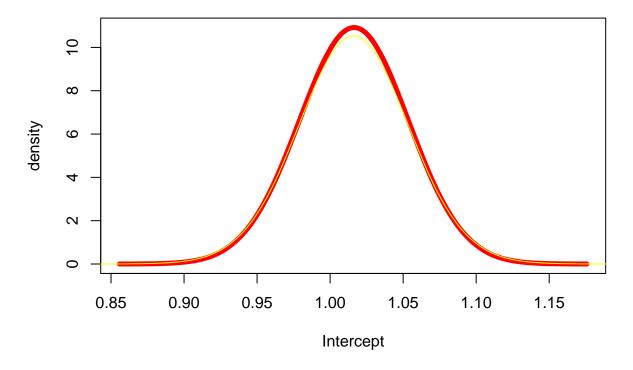
# Example: A model for the mean structure

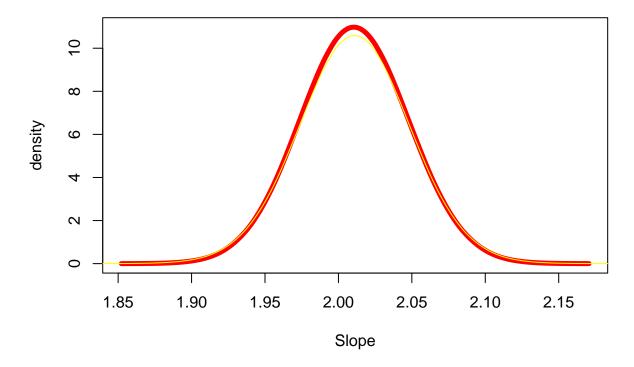
Up to now, we have assumed zero mean. In this example, we will illustrate how to add a non-zero mean model, focusing on the mean model only. We can of course have a mean model and a non-trivial precision matrix together.

```
prec.high = exp(15)
   interpret.theta = function() {
        return(list(a = theta[1L], b = theta[2L]))
   graph = function() {
       G = Diagonal(n = length(x), x=1)
       return(G)
   }
   Q = function() {
        Q = prec.high * graph()
       return(Q)
   }
   mu = function() {
       par = interpret.theta()
       return(par$a + par$b * x)
   }
   log.norm.const = function() {
        return(numeric(0))
   log.prior = function() {
       par = interpret.theta()
        val = (dnorm(par$a, mean=0, sd=1, log=TRUE) +
               dnorm(par$b, mean=0, sd=1, log=TRUE))
       return(val)
   }
   initial = function() {
       return(rep(0, 2))
   }
   quit = function() {
       return(invisible())
   val = do.call(match.arg(cmd), args = list())
   return(val)
and we can run this as
a = 1
```

```
a = 1
b = 2
n = 50
x = rnorm(n)
eta = a + b*x
s = 0.25
y = eta + rnorm(n, sd=s)
```

and we can compare the results with the native model





The tiny in-accuacy is due to treatment of a and b as hyperparameters in the rgeneric model. ###We can improve the estimates using inla.hyperpar() as usual, ###{r} ###r = inla.hyperpar(r) ### ###Replotting the results shows improvement: ###{r} ###plot(inla.smarginal(r\$marginals.hyperpar[['Theta1 for idx']]), ### type="l", lwd=5, col="red", xlab="Intercept", ylab="density") ###lines(inla.smarginal(r\$marginals.hyperpar[['Theta2 for idx']]), ### type="l", lwd=5, col="red", xlab="Slope", ylab="density") ###lines(inla.smarginal(rr\$m col="yellow") ###

# Some comments on optimization

The regeneric-interface is not ment to be a replacement for implementing a model component in C, but rather a tool to experiment with new models and adding case spesific model components. Needless to say, it will be a somewhat slower than a model that is implemented in C. For smaller problems the overhead is relative larger than for larger problems, since more less time is used to factorize matrices etc, compared to constructing the matrices.

To discuss some easy steps that can be taken, we can consider this simple Gaussian model with zero mean and precision matrix

$$Q = \tau R$$
.

We observe a sample from this matrix with known Gaussian noise.

The regeneric implementation of this, could be as follows.

```
rgeneric.test = function(
    cmd = c("graph", "Q", "mu", "initial", "log.norm.const", "log.prior", "quit"),
    theta = NULL)
{
```

```
envir = parent.env(environment())
    graph = function() {
        return(matrix(1, n, n))
    Q = function() {
        R \leftarrow matrix(sin(1:n^2), n, n)
        R <- R %*% t(R)
        diag(R) \leftarrow diag(R)+1
        Q \leftarrow \exp(\text{theta}[1]) * R
        return(Q)
    }
    mu = function() return (numeric(0))
    log.norm.const = function() {
        return (numeric(0))
    }
    log.prior = function() {
        return (dgamma(exp(theta[1]), shape = 1, rate = 1, log=TRUE) + theta[1])
    initial = function() {
        return(4)
    if (!length(theta)) theta = initial()
    val = do.call(match.arg(cmd), args = list())
    return (val)
}
```

We can now simulate some data and compare the results with the buildt-in implementation

```
n = 200
s = .1
Q <- rgeneric.test("Q", theta = 0)
library(mvtnorm)
S <- solve(as.matrix(Q))</pre>
S \leftarrow (S + t(S))/2
x <- drop(rmvnorm(1, sigma = S))
y \leftarrow x + rnorm(n, sd = s)
cont.family = list(hyper = list(prec = list(initial=log(1/s^2), fixed=TRUE)))
r1 = inla(y ~ -1 + f(idx, model="generic", Cmatrix = Q,
                      hyper = list(prec = list(prior = "loggamma", param = c(1, 1)))),
          data = data.frame(y = y, idx = 1:n), control.family = cont.family)
ld <- 0.5 * log(det(as.matrix(Q)))</pre>
r1$mlik <- r1$mlik + ld ## see the documentation for why
model2 = inla.rgeneric.define(rgeneric.test, n=n, optimize = FALSE)
r2 = inla(y \sim -1 + f(idx, model=model2),
```

```
data = data.frame(y = y, idx = 1:n), control.family = cont.family)
```

We can compare the results, with

```
r2$mlik - r1$mlik
```

```
## [,1]
## log marginal-likelihood (integration) -3.401460e-06
## log marginal-likelihood (Gaussian) -3.028282e-07
```

there are a couple of things that can be done in order to improve the speed of the regeneric model. The first is to *cache* intermediate calculations and to make sure the same calculations are not done over and over again.

For this, we use the regeneric function's environment. We can cache the matrix R and also precompute large parts of the normalizing constant.

```
rgeneric.test.opt.1 = function(
    cmd = c("graph", "Q", "mu", "initial", "log.norm.const", "log.prior", "quit"),
    theta = NULL)
    envir = parent.env(environment())
    if (!exists("cache.done", envir = envir)) {
        R \leftarrow matrix(sin(1:n^2), n, n)
        R \leftarrow R \% \% t(R)
        diag(R) \leftarrow diag(R)+1
        R.logdet <- log(det(R))</pre>
        R <- inla.as.sparse(R)</pre>
        idx <- which(R@i <= R@j)</pre>
        R@i <- R@i[idx]
        R@j <- R@j[idx]
        R@x <- R@x[idx]</pre>
        assign("R", R, envir = envir)
        norm.const <--n/2 * log(2*pi) + 0.5 * R.logdet
        assign("norm.const", norm.const, envir = envir)
        assign("cache.done", TRUE, envir = envir)
    }
    graph = function() {
        return (R)
    }
    Q = function() {
        return(exp(theta[1]) * R)
    }
    mu = function() return (numeric(0))
    log.norm.const = function() {
        return (norm.const + n/2 * theta[1])
    log.prior = function() {
        return (dgamma(exp(theta[1]), shape = 1, rate = 1, log=TRUE) + theta[1])
    }
```

```
initial = function() {
    return(4)
}

if (!length(theta)) theta = initial()
val = do.call(match.arg(cmd), args = list())

return (val)
}
```

We can also go one step further, to add option optimize=TRUE when calling inla.rgeneric.define, which inform the interpreter that we pass only the matrix values of Q, not the indices! This impose a constraint on the ordering, which must be the that is defined after converting the matrix to inla.as.sparse and returning only the upper triangular part. This is a row-based ordering, like

```
A=matrix(1:9,3,3)

A

## [,1] [,2] [,3]

## [1,] 1 4 7

## [2,] 2 5 8

## [3,] 3 6 9

inla.as.sparse(A)@x
```

```
## [1] 1 2 3 4 5 6 7 8 9
```

The updated model will then be

```
rgeneric.test.opt.2 = function(
    cmd = c("graph", "Q", "mu", "initial", "log.norm.const", "log.prior", "quit"),
    theta = NULL)
{
    envir = parent.env(environment())
    if (!exists("cache.done", envir = envir)) {
        R \leftarrow matrix(sin(1:n^2), n, n)
        R \leftarrow R \% * \% t(R)
        diag(R) \leftarrow diag(R)+1
        R.logdet <- log(det(R))</pre>
        R <- inla.as.sparse(R)</pre>
        idx <- which(R@i <= R@j)
        R@i <- R@i[idx]
        R@j <- R@j[idx]</pre>
        R@x <- R@x[idx]</pre>
        assign("R", R, envir = envir)
        norm.const <--n/2 * log(2*pi) + 0.5 * R.logdet
        assign("norm.const", norm.const, envir = envir)
        assign("cache.done", TRUE, envir = envir)
    }
    graph = function() {
        return (R)
    Q = function() {
```

```
## since R was created with 'inla.sparse.matrix' above, the indices are sorted in a
        ## spesific order. This ordering is REQUIRED for R@x to be interpreted correctly.
        return(exp(theta[1]) * R@x)
   }
   mu = function() return (numeric(0))
   log.norm.const = function() {
        return (norm.const + n/2 * theta[1])
   log.prior = function() {
        return (dgamma(exp(theta[1]), shape = 1, rate = 1, log=TRUE) + theta[1])
   }
   initial = function() {
        return(4)
   if (!length(theta)) theta = initial()
   val = do.call(match.arg(cmd), args = list())
   return (val)
}
We can now run the two optimized variants
model3 = inla.rgeneric.define(rgeneric.test.opt.1, n=n, optimize = FALSE)
r3 = inla(y \sim -1 + f(idx, model=model3),
          data = data.frame(y = y, idx = 1:n), control.family = cont.family)
model4 = inla.rgeneric.define(rgeneric.test.opt.2, n=n, optimize = TRUE)
r4 = inla(y \sim -1 + f(idx, model=model4),
          data = data.frame(y = y, idx = 1:n), control.family = cont.family)
We can now compare the time and results for all models
print(r2$mlik - r1$mlik)
                                                   [,1]
## log marginal-likelihood (integration) -3.401460e-06
                                         -3.028282e-07
## log marginal-likelihood (Gaussian)
print(r3$mlik - r1$mlik)
                                                  [,1]
## log marginal-likelihood (integration) 2.486816e-06
## log marginal-likelihood (Gaussian)
                                          4.559917e-07
print(r4$mlik - r1$mlik)
                                                  [,1]
## log marginal-likelihood (integration) 2.486816e-06
## log marginal-likelihood (Gaussian)
                                          4.559917e-07
print(rbind(native = r1$cpu[2],
            rgeneric.plain = r2$cpu[2],
```

```
rgeneric.cache = r3$cpu[2],
rgeneric.optimze = r4$cpu[2]))
```

```
## Running
## native 0.4463739
## rgeneric.plain 2.2405379
## rgeneric.cache 1.7328994
## rgeneric.optimze 1.6230755
```

Another general approach to optimizing R-code, is to write critical parts in C or C++. This can also be done here, by calling C-code within the regeneric model.

# The Cgeneric interface

The new interface in C (as of Dec 2021) allows one to do similar as described above using C code. The advantage is mainly speed but that benefite could be dramatic, as the R interpreter is avoided and the calls to the generic functions are no longer wrapped in an OpenMP critical region which is required due to the serial nature of libR.

The main idea is to provide a C implementation with similar features as for the R interface, and to pass the name of the function and its binary in a form of a shared/dynamic library. The GNU library ltdl is used for cross-platform compatabilty, see https://www.gnu.org/software/libtool/manual/html\_node/Using-libltdl.html.

# Example of usage

In short, the usage is as follows. First compile and build a shared object

```
gcc -Wall -fpic -g -O -c -o cgeneric-demo.o cgeneric-demo.c gcc -shared -o cgeneric-demo.so cgeneric-demo.o
```

then use this file to define the cgeneric model,

where n is the size of the model. Unfortunately, this needs to be known before the model is loaded.

The usage is similar to rgeneric, as

```
rc <- inla(
   y ~ -1 + f(idx, model = cmodel),
   data = data.frame(y, idx = 1:n),
   control.family = list(hyper = list(prec = list(initial = 12, fixed = TRUE))))</pre>
```

The following example implements the same model using the builtin model, rgeneric and cgeneric.

```
n <- 100
y <- rnorm(n)

r <- inla(
    y ~ -1 + f(idx, model = "iid", hyper = list(prec = list(param = c(1, 1)))),
    data = data.frame(y, idx = 1:n),
    control.family = list(hyper = list(prec = list(initial = 12, fixed = TRUE))))

rmodel <- inla.rgeneric.define(inla.rgeneric.iid.model, n = n)

rr <- inla(
    y ~ -1 + f(idx, model = rmodel),</pre>
```

```
data = data.frame(y, idx = 1:n),
    control.family = list(hyper = list(prec = list(initial = 12, fixed = TRUE))))
cmodel <- inla.cgeneric.define(model = "inla_cgeneric_iid_model",</pre>
                               shlib = "cgeneric-demo.so", n = n)
rc <- inla(</pre>
    y \sim -1 + f(idx, model = cmodel),
    data = data.frame(y, idx = 1:n),
    control.family = list(hyper = list(prec = list(initial = 12, fixed = TRUE))))
print(cbind(r$mlik, rr$mlik-r$mlik, rc$mlik-r$mlik))
print(cbind(r$cpu[2], rr$cpu[2], rc$cpu[2]))
The behaviour of the cgeneric model can be verified using inla.cgeneric.q(), like
gcc -Wall -fpic -g3 -0 -c -o cgeneric-demo.o cgeneric-demo.c
gcc -shared -o cgeneric-demo.so cgeneric-demo.o
> n <- 5
> cmodel <- inla.cgeneric.define(model = "inla_cgeneric_ar1_model",</pre>
                                 shlib = "cgeneric-demo.so", n = n)
> inla.cgeneric.q(cmodel)
$theta
[1] 1 1
$graph
5 x 5 sparse Matrix of class "dgCMatrix"
[1,] 1 1 . . .
[2,] 1 1 1 . .
[3,] . 1 1 1 .
[4,] . . 1 1 1
[5,] . . . 1 1
5 x 5 sparse Matrix of class "dgCMatrix"
[1,] 3.45640494 -1.59726402 .
[2,] -1.59726402 4.19452805 -1.59726402 .
[3,] . -1.59726402 4.19452805 -1.59726402 .
                . -1.59726402 4.19452805 -1.59726402
[4,]
[5,]
                                        -1.59726402 3.45640494
$m11
numeric(0)
$log.prior
[1] -3.13722036
$log.norm.const
[1] -1.61423464
```

# Header file and example file

The header-file cgeneric.h is included in the package in the include directory, and in the cgeneric directory, the header-file and the example file given above is included.

The header file cgeneric.h needs to be included in any implementation as it defines the data types and definitions needed, like

```
typedef enum {
    INLA_CGENERIC_VOID = 0,
    INLA_CGENERIC_Q,
    INLA_CGENERIC_GRAPH,
    INLA_CGENERIC_MU,
    INLA_CGENERIC_INITIAL,
    INLA_CGENERIC_LOG_NORM_CONST,
    INLA_CGENERIC_LOG_PRIOR,
    INLA_CGENERIC_COM_TOWN
} inla_cgeneric_cmd_tp;
```

to define the various actions.

# Example iid

It is easier to see how this is one by a simple iid-model example

```
#include <assert.h>
#if !defined(__FreeBSD__)
#include <malloc.h>
#endif
#include <math.h>
#include <stdlib.h>
#include <strings.h>
#include "cgeneric.h"
#define Calloc(n_, type_) (type_ *)calloc((n_), sizeof(type_))
#define SQR(x) ((x)*(x))
double *inla_cgeneric_iid_model(inla_cgeneric_cmd_tp cmd, double *theta, inla_cgeneric_data_tp * data)
    // this reimplement `inla.rgeneric.iid.model` using cgeneric
    double *ret = NULL, prec = (theta ? exp(theta[0]) : NAN), lprec = (theta ? theta[0] : NAN);
    assert(!strcasecmp(data->ints[0]->name, "n"));
                                                             // this will always be the case
    int N = data \rightarrow ints[0] \rightarrow ints[0];
                                                     // this will always be the case
    assert(N > 0);
    switch (cmd) {
    case INLA_CGENERIC_VOID:
        assert(!(cmd == INLA_CGENERIC_VOID));
        break;
    }
    case INLA_CGENERIC_GRAPH:
```

```
// return a vector of indices with format
   // c(N, M, ii, jj)
   // where ii<=jj, ii is non-decreasing and jj is non-decreasing for the same ii
   // so like the loop
    // for i=0, ...
    // for j=i, ...
              Gij =
   // and M is the total length while N is the dimension
   int M = N;
   ret = Calloc(2 + 2 * N, double);
   ret[0] = N;
                                   /* dimension */
   ret[1] = M;
                                   /* number of (i <= j) */
    for (int i = 0; i < M; i++) {</pre>
       ret[2 + i] = i;
                                      /* i */
       ret[2 + N + i] = i;
                                      /* j */
   break;
}
case INLA_CGENERIC_Q:
   // return c(-1, M, Qij) in the same order as defined in INLA_CGENERIC_GRAPH
   int M = N;
   ret = Calloc(2 + N, double);
   ret[0] = -1;
                                   /* REQUIRED! */
   ret[1] = M;
                               /* number of (i <= j) */
   for (int i = 0; i < M; i++) {</pre>
       ret[2 + i] = prec;
   break;
}
case INLA_CGENERIC_MU:
   // return (N, mu)
   // if N==0 then mu is not needed as its taken to be mu[]==0
   ret = Calloc(1, double);
   ret[0] = 0;
   break;
}
case INLA_CGENERIC_INITIAL:
{
   // return c(M, initials)
    // where M is the number of hyperparameters
   ret = Calloc(2, double);
   ret[0] = 1;
   ret[1] = 4.0;
   break;
}
```

```
case INLA_CGENERIC_LOG_NORM_CONST:
        // return c(NORM CONST) or a NULL-pointer if INLA should compute it by itself
        ret = Calloc(1, double);
        ret[0] = N * (-0.9189385332 + 0.5 * lprec);
        break;
    }
    case INLA_CGENERIC_LOG_PRIOR:
        // return c(LOG_PRIOR)
        ret = Calloc(1, double);
        ret[0] = -prec + lprec;
                                              // prec ~ gamma(1,1)
        break;
    }
    case INLA_CGENERIC_QUIT:
    default:
        break;
    return (ret);
}
```

The return values must be allocated dynamically, and is free'ed in the main program after use.

### Example ar1

The reimplementation of the AR1 model as in inla.rgeneric.ar1.model is as follows.

```
#include <assert.h>
#if !defined(__FreeBSD__)
#include <malloc.h>
#endif
#include <math.h>
#include <stdlib.h>
#include <strings.h>
#include "cgeneric.h"
#define Calloc(n_, type_) (type_ *)calloc((n_), sizeof(type_))
#define SQR(x) ((x)*(x))
double *inla_cgeneric_ar1_model(inla_cgeneric_cmd_tp cmd, double *theta, inla_cgeneric_data_tp * data)
    // this reimplement `inla.rgeneric.ar1.model` using cgeneric
    double *ret = NULL, prec, lprec, rho, rho_intern;
    if (theta) {
        lprec = theta[0];
        prec = exp(lprec);
        rho_intern = theta[1];
        rho = 2.0 * \exp(\text{rho\_intern}) / (1.0 + \exp(\text{rho\_intern})) - 1.0;
```

```
} else {
   prec = lprec = rho = rho_intern = NAN;
assert(N > 0);
switch (cmd) {
case INLA_CGENERIC_VOID:
   assert(!(cmd == INLA_CGENERIC_VOID));
   break;
}
case INLA_CGENERIC_GRAPH:
   // return a vector of indices with format
   // c(N, M, ii, jj)
   // where ii<=jj, ii is non-decreasing and jj is non-decreasing for the same ii
   // so like the loop
   // for i=0, ...
   // for j=i, ...
   //
            G_ij =
   // and M is the length of ii
   int M = N + N - 1, offset, i, k;
   ret = Calloc(2 + 2 * m, double);
   offset = 2;
   ret[0] = N;
                               /* dimension */
   ret[1] = M;
                               /* number of (i <= j) */
   for (k = i = 0; i < N; i++) {
                                      /* i */
       ret[offset + k] = i;
       ret[offset + M + k++] = i; /* j */
       if (i < N - 1) {
          ret[offset + k] = i;
                                      /* i */
          ret[offset + M + k++] = i + 1; /* j */
       }
   }
   break;
}
case INLA_CGENERIC_Q:
{
   // optimized format
   // return c(-1, M, Qij) in the same order as defined in INLA_CGENERIC_GRAPH
   // where M is the length of Qij
   double param = prec / (1.0 - SQR(rho));
   int M = N + N - 1;
   int offset, i, k;
   ret = Calloc(2 + M, double);
```

```
offset = 2;
   ret[0] = -1;
                                       /* REQUIRED */
   ret[1] = M;
    for (i = k = 0; i < N; i++) {
        ret[offset + k++] = param * (i == 0 || i == N - 1 ? 1.0 : (1.0 + SQR(rho)));
        if (i < N - 1) {
           ret[offset + k++] = -param * rho;
    }
   break;
}
case INLA_CGENERIC_MU:
   // return (N, mu)
   // if N==0 then mu is not needed as its taken to be mu[]==0
   ret = Calloc(1, double);
   ret[0] = 0;
   break;
}
case INLA_CGENERIC_INITIAL:
    // return c(M, initials)
   // where M is the number of hyperparameters
   ret = Calloc(3, double);
   ret[0] = 2;
   ret[1] = 1.0;
   ret[2] = 1.0;
   break;
}
case INLA_CGENERIC_LOG_NORM_CONST:
   // return c(NORM_CONST) or a NULL-pointer if INLA should compute it by itself
   double prec_innovation = prec / (1.0 - SQR(rho));
   ret = Calloc(1, double);
   ret[0] = N * (-0.5 * log(2.0 * M_PI) + 0.5 * log(prec_innovation)) + 0.5 * log(1.0 - SQR(rho));
}
case INLA_CGENERIC_LOG_PRIOR:
   // return c(LOG_PRIOR)
   ret = Calloc(1, double);
   ret[0] = -prec + lprec - 0.5 * log(2.0 * M_PI) - 0.5 * SQR(rho_intern);
   break;
}
```

```
case INLA_CGENERIC_QUIT:
    default:
        break;
}
return (ret);
}
```

### Passing arguments to inla.cgeneric.define

The R interface is easier when it comes to passing arguments throughout the system, as any non-standard arguments to inla.rgeneric.define is stored in environment of the function and is then available when the function is evaluated in libR.

For the C interface, this has to be done manually, and pointer to a data structure that contains all arguments to inla.cgeneric.define is passed to the C function. The data structure is as follows

```
typedef struct {
   int n_ints;
   inla_cgeneric_vec_tp **ints;

int n_doubles;
   inla_cgeneric_vec_tp **doubles;

int n_chars;
   inla_cgeneric_vec_tp **chars;

int n_mats;
   inla_cgeneric_mat_tp **mats;

int n_smats;
   inla_cgeneric_smat_tp **smats;
} inla_cgeneric_data_tp;
```

where integers, doubles (or numerics), characters (or strings), dense matrices and sparse matrices are stored in named lists. The n\_ints gives the number of integers or integer vectors, and similar with n\_doubles, n\_chars, n\_mats and n\_smats. The predefined named arguments in inla.cmatrix.define are stored first, then additional named arguments are stored. This implies that the argument n is always the first one in the integer list, like used in the examples above

```
assert(!strcasecmp(data->ints[0]->name, "n")); // this will always be the case
int N = data->ints[0]->ints[0]; // this will always be the case
```

The integers, doubles and characters, are stored in

```
typedef struct
{
    char *name;
    int len;
    int *ints;
    double *doubles;
    char *chars;
}
inla_cgeneric_vec_tp;
```

so possible vectors with length len or a string with len characters.

Dense matrices are stored row wise (as natural in C), which is NOT how it is stored in R.

```
matrix storage is stored row by row.
        In R the (default) storage is column by column, like
        > matrix(1:6,2,3)
        [,1] [,2] [,3]
        [1,]
                1
                          6
        [2,]
                2
                     4
       hence
       > c(matrix(1:6,2,3))
        [1] 1 2 3 4 5 6
       while in cgeneric, the matrix elements 'x', is stored as
       x[] = \{ 1, 3, 5, 2, 4, 6 \}
typedef struct {
    char *name;
    int nrow;
    int ncol;
   double *x;
} inla_cgeneric_mat_tp;
```

and sparse matrices are stored as triplets (i,j,x),

```
/*
* sparse matrix format, stored used O-based indices.
 * If the matrix is not a 'dgTMatrix', it is converted using
* 'inla.as.sparse()'
 * the matrix is stored in the order it appears, like
       > A <- inla.as.sparse(matrix(c(1,2,3,0,0,6),2,3))
       2 x 3 sparse Matrix of class "dgTMatrix"
       [1,] 1 3 .
       [2,] 2 . 6
       > cbind(i=A@i, j=A@j, x=A@x)
             i j x
       [1,] 0 0 1
       [2,] 1 0 2
       [3,] 0 1 3
       [4,] 1 2 6
       If you want to have this matrix stored this column by column,
       then swap @i and @j, and rearrange @x, before passing them into
       'inla.cgeneric.define'.
       For example, if we want to pass only the upper half of a
       symmetric sparse matrix, stored by column, then we can do
       A <- inla.as.sparse(A)
       ii <- A@i
```

```
A@i <- A@j
        A@j <- ii
        idx <- which(A@i <= A@j)
        A@i <- A@i[idx]
        A@j <- A@j[idx]
        A@x \leftarrow A@x[idx]
        before passing it on into 'inla.cgeneric.define'
 */
typedef struct {
    char *name;
    int nrow;
    int ncol;
                                         /* number of triplets (i,j,x) */
    int n;
    int *i;
    int *j;
    double *x;
} inla_cgeneric_smat_tp;
```

R-objects not of the above types cannot be handled, but one can always, for example, store them in a file and pass the filename.

Adding the option debug=TRUE to inla.cgeneric.define will turn on debug-output and the contents of inla\_cgeneric\_data\_tp \* data is displayed. Only use this option for small size problems as the output can be excessive.

#### Thread safe

The implementation of the cgeneric model must be thread safe. If you use internal cache in the cgeneric, you need copy one per thread.

### Reimplementing model generic0

Here is an example of reimplementing generic0 using cgeneric. The C-code is in cgeneric-demo.c, and the following R-code compare the builtin and cgeneric implementation

```
library(mvtnorm)
n <- 10
A <- matrix(rnorm(n^2), n, n)
Q \leftarrow A \% * \% t(A)
S \leftarrow solve(Q)
S <- S / exp(mean(log(diag(S))))
Q <- solve(S)
Cmatrix <- inla.as.sparse(Q)</pre>
s < -0.1
y \leftarrow c(rmvnorm(1, sigma = S)) + rnorm(n, sd = s)
r <- inla(
    y ~ -1 + f(idx, model = "generic0", Cmatrix = Cmatrix,
               hyper = list(prec = list(prior = "loggamma",
                                           param = c(1, 1),
                                           initial = 4,
                                           fixed = FALSE))),
    num.threads = "1:1",
```

```
data = data.frame(y, idx = 1:n),
    control.family = list(hyper =
        list(prec = list(initial = log(1/s^2), fixed = TRUE))))
## pass in the Cmatrix so its a good fit for
## the cgeneric-implementation, so we store 'Cmatrix'
## column-wise, and upper half only (diagonal included)
ii <- Cmatrix@i
Cmatrix@i <- Cmatrix@j
Cmatrix@j <- ii
idx <- which(Cmatrix@i <= Cmatrix@j)</pre>
Cmatrix@i <- Cmatrix@i[idx]</pre>
Cmatrix@j <- Cmatrix@j[idx]</pre>
Cmatrix@x <- Cmatrix@x[idx]</pre>
cmodel <- inla.cgeneric.define(model = "inla_cgeneric_generic0_model",</pre>
                               shlib = "cgeneric-demo.so",
                               n = n, Cmatrix = Cmatrix, debug = FALSE)
rc <- inla(</pre>
    y \sim -1 + f(idx, model = cmodel),
    num.threads = "1:1",
    data = data.frame(y, idx = 1:n),
    control.family = list(hyper = list(
                     prec = list(initial = log(1/s^2), fixed = TRUE))),
    verbose = TRUE)
print(r$mode$theta - rc$mode$theta)
print(r$mode$x - rc$mode$x)
print(r$mlik - rc$mlik)
which produces output like
> print(r$mode$theta - rc$mode$theta)
Log precision for idx
     -8.710710942e-06
> print(r$mode$x - rc$mode$x)
 [1] -6.988149615e-08 9.218204538e-08 1.151077143e-07 -3.683823807e-08
 [5] -8.793919748e-08 -9.518123112e-08 2.305469839e-08 -2.043514372e-08
[9] -7.478532010e-08 1.064667019e-07 -6.988848433e-08 9.219126358e-08
[13] 1.151192251e-07 -3.684192190e-08 -8.794799145e-08 -9.519074928e-08
[17] 2.305700385e-08 -2.043718722e-08 -7.479279862e-08 1.064773486e-07
> print(r$mlik - rc$mlik)
                                                   [,1]
log marginal-likelihood (integration) 2.070899825e-07
log marginal-likelihood (Gaussian) 1.150937410e-05
```