Zero-inflated models: Beta-Binomial

Parameterisation

There is support for a further zero-inflated model of type 2 (see zero-inflated.pdf), the zero-inflated beta-binomial. It is only defined for type 2.

Type 2

The likelihood is defined as

$$Prob(y \mid \ldots) = p \times 1_{[y=0]} + (1-p) \times Beta-binomial(y)$$

where:

$$p = 1 - \left(\frac{\exp(x)}{1 + \exp(x)}\right)^{\alpha}$$

Link-function

As for the Binomial (see Zero-inflated.pdf).

Hyperparameters

The Beta-binomial distribution has two arguments ($\beta_1 \& \beta_2$) which we assume are a (specific) function of an underlying hyperparameter (δ) & x. There is a further hyperparameter, α , governing zero-inflation where:

The parameter controlling the degree of overdispersion, δ , is represented as

$$\theta_1 = \log(\delta)$$

and the prior is defined on θ_1 .

The zero-inflation parameter α , is represented as

$$\theta_2 = \log(\alpha)$$

and the prior and initial value is is given for θ_2 .

Specification

- family="zeroinflatedbetabinomial2"
- Required arguments: As for the zero-inflated-nbinomial likelihood.

Hyperparameter spesification and default values

doc Zero inflated Beta-Binomial, type 2

hyper

theta1

hyperid 94001 name log alpha short.name a

```
output.name zero-probability parameter for zero-inflated betabinomial_2
         output.name.intern intern zero-probability parameter for zero-inflated betabinomial_
         initial 0.693147180559945
         fixed FALSE
         prior gaussian
         param 0.693147180559945 1
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
    theta2
         hyperid 94002
         name beta
         short.name b
         output.name overdispersion parameter for zero-inflated betabinomial_2
         output.name.intern intern overdispersion parameter for zero-inflated betabinomial_2
         initial 0
         fixed FALSE
         prior gaussian
         param 0 1
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
survival FALSE
discrete FALSE
link default logit loga cauchit probit cloglog ccloglog loglog robit sn
pdf zeroinflated
Example
In the following we estimate the parameters in a simulated example.
Example-zero-inflated-beta-binomial2.R
nx = 1000
                          # number of x's to consider
                          # size of each binomial trial
n.trial = 20
x = rnorm(nx)
                          # generating x
delta = 10
                              #hyperparameter 1
p = \exp(1+x)/(1+\exp(1+x))
                             #hyperparameter 2
alpha = 2
                               #ZI parameter
                               #prob presence
q = p^alpha
beta_1=delta*p
                                   #beta-bin parameter 1
beta_2=delta*(1-p)
                                   #beta-bin parameter 2
rb = rbeta(nx, beta_1, beta_2, ncp = 0)
y = rep(0,nx)
                                     #generating data
```