Occupancy likelihood

Parametrisation

This is a specialized likelihood to for occupancy models.

Details

An observation is an vector $y = (y_1, \ldots, y_m)$ of binary observations, each depending on spesific covariates, with additional zero-inflation. If there fewer than m observations, like $m' < m$, then "observations not observed" must be set to `NA`. The likelihood for one observation(-vector) is

$$f(y) = \phi \prod_{i=1}^{m} p_i^{y_i} (1 - p_i)^{1-y_i} + (1 - \phi) 1_{[y_i = 0, \forall i]}$$

with the convension that if y_i=`NA`, the contribution from y_i is ignored. Further,

$$\text{logit}(p_i) = x_i^T \beta$$

and $x_i = (x_{i1}, \ldots, x_{ik})$ are the $k > 0$ covariate associated to y_i, and $\beta = (\beta_1, \ldots, \beta_k)$ are the regression coefficients. The linear predictor from the formula η, goes into ϕ, as

$$\text{logit}(\phi) = \eta$$

Link-function

The link-function for the p_i-model is given by argument `link.simple` in the `control.family`-argument. The link-function for the ϕ-model is given as normal. Both defaults to the logit-link.

Hyperparameters

The regression coefficients β are treated as hyperparameters, and k is maximum 10. An intercept must be defined manually by adding a constant covariate vector.

Specification

- `family="occupancy"`
- Required arguments: A matrix Y with the observations and a matrix X with the covariates.

The matrix Y is $n \times m$, where m is then the *maximum* number of observations over all locations. If there fewer than m observations in one location, then `NA` must be added to reach m.

The matrix X stored the covariates. Since there are k covariate for each observation, then the dimension of X is $n \times mk$. For the ith observation(-vector), then the ith row of X is $(x_{i1}, x_{i2}, \ldots, x_{im})$, where x_{ij} is the covariate vector for jth observation at location i. In a single observation is `NA`, the corresponding covariate(-vectors) is not used (but it still needs to be given).

Here is a simple example with $n = 5$ locations, maximum $m = 3$ observations, and $k = 2$ covariates.

```
> Y
     [,1] [,2] [,3]
[1,]    1    1   NA
[2,]    0    1    0
[3,]    0    0    0
[4,]    0    1    0
[5,]   NA    0    0
> round(dig=3,X)
     [,1]   [,2] [,3]   [,4] [,5]   [,6]
[1,]    1 -0.129    1 -0.248   NA     NA
[2,]    1 -0.030    1  0.151    1  0.100
[3,]    1 -0.148    1 -0.061    1  0.023
[4,]    1 -0.055    1  0.081    1 -0.112
[5,]   NA     NA    1  0.164    1  0.027
```

For $Y[1,1]$ the covariates are $(1, -0.129)$, for $Y[1,2]$ the covariates are $(1, -0.248)$, for $Y[1,3]$ is `NA` hence not used, for $Y[2,1]$ the covariates are $(1, -0.030)$, etc. We pass both Y and X in the `inla.mdata()` in the formula, as

```
inla.mdata(Y,X) ~ ...
```

Hyperparameter spesification and default values

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hyper

theta1

hyperid `56601`
name `beta1`
short.name `beta1`
output.name `beta1 for occupancy observations`
output.name.intern `beta1 for occupancy observations`
initial `-2`
fixed `FALSE`
prior `normal`
param `-2 10`
to.theta `function(x) x`
from.theta `function(x) x`

theta2

hyperid `56602`
name `beta2`
short.name `beta2`
output.name `beta2 for occupancy observations`
output.name.intern `beta2 for occupancy observations`
initial `0`
fixed `FALSE`
prior `normal`
param `0 10`
to.theta `function(x) x`

from.theta `function(x) x`

theta3

hyperid `56603`
name `beta3`
short.name `beta3`
output.name `beta3 for occupancy observations`
output.name.intern `beta3 for occupancy observations`
initial `0`
fixed `FALSE`
prior `normal`
param `0 10`
to.theta `function(x) x`
from.theta `function(x) x`

theta4

hyperid `56604`
name `beta4`
short.name `beta4`
output.name `beta4 for occupancy observations`
output.name.intern `beta4 for occupancy observations`
initial `0`
fixed `FALSE`
prior `normal`
param `0 10`
to.theta `function(x) x`
from.theta `function(x) x`

theta5

hyperid `56605`
name `beta5`
short.name `beta5`
output.name `beta5 for occupancy observations`
output.name.intern `beta5 for occupancy observations`
initial `0`
fixed `FALSE`
prior `normal`
param `0 10`
to.theta `function(x) x`
from.theta `function(x) x`

theta6

hyperid `56606`
name `beta6`
short.name `beta6`
output.name `beta6 for occupancy observations`
output.name.intern `beta6 for occupancy observations`
initial `0`
fixed `FALSE`
prior `normal`
param `0 10`
to.theta `function(x) x`
from.theta `function(x) x`

theta7

hyperid 56607
name beta7
short.name beta7
output.name beta7 for occupancy observations
output.name.intern beta7 for occupancy observations
initial 0
fixed FALSE
prior normal
param 0 10
to.theta function(x) x
from.theta function(x) x

theta8

hyperid 56608
name beta8
short.name beta8
output.name beta8 for occupancy observations
output.name.intern beta8 for occupancy observations
initial 0
fixed FALSE
prior normal
param 0 10
to.theta function(x) x
from.theta function(x) x

theta9

hyperid 56609
name beta9
short.name beta9
output.name beta9 for occupancy observations
output.name.intern beta9 for occupancy observations
initial 0
fixed FALSE
prior normal
param 0 10
to.theta function(x) x
from.theta function(x) x

theta10

hyperid 56610
name beta10
short.name beta10
output.name beta10 for occupancy observations
output.name.intern beta10 for occupancy observations
initial 0
fixed FALSE
prior normal
param 0 10
to.theta function(x) x
from.theta function(x) x

survival FALSE

discrete `TRUE`

link `default logit loga cauchit probit cloglog ccloglog loglog log`

link.simple `default logit cauchit probit cloglog ccloglog`

pdf `occupancy`

Example

```
n <- 1000
m <- 3
nc <- 2
beta <- c(-1, rnorm(nc-1, sd = 0.2))
Y <- matrix(NA, n, m)
X <- matrix(NA, n, m*nc)
z <- rnorm(n, mean = 0, sd = 0.3)
eta <- 3 + z
p.obs <- 1/(1 + exp(-eta))
for (i in 1:n) {
    is.zero <- rbinom(1, size = 1, prob = 1 - p.obs[i])
    nyy <- sample(2:m, 1)
    for(j in 1:m) {
        off <- (j-1) * nc
        if (j <= nyy) {
            X[i, off + 1:nc] <- c(1, rnorm(nc-1, sd = 0.1))
            eeta <- sum(X[i, off + 1:nc] * beta)
            p <- 1/(1 + exp(-eeta))
            if (is.zero) {
                Y[i, j] <- 0
            } else {
                Y[i, j] <- rbinom(1, size = 1, prob = p)
            }
        } else {
            X[i, off + 1:nc] <- rep(NA, nc)
            Y[i, j] <- NA
        }
    }
}

r <- inla(inla.mdata(Y, X) ~ 1 + z,
          family = "occupancy",
          data = list(Y = Y, X = X, z = z),
          control.fixed = list(prec.intercept = 1),
          control.inla = list(cmin = 0.0))
summary(r)
cbind(beta, r$summary.hyperpar[, "mean"])
```