The Matérn-model

Parametrisation

This model is the Gaussian field with Matérn correlation function on a regular nrow x ncol -lattice. On an infinite lattice, the correlation function is

$$Corr(d) = \frac{1}{2^{\nu-1}\Gamma(\nu)} (\kappa d)^{\nu} K_{\nu}(\kappa d), \qquad \alpha = \nu + d/2,$$

where K_{ν} is the modified Bessel function and $\Gamma(\cdot)$ is the Gamma-function. The range is defined to be

$$r = \sqrt{8\nu}/\kappa$$

which about the distance where the covariance function becomes about 0.1.

The boundary conditions are so that the values are taken to be 0 outside the lattice. No further boundary options are available at this time.

Hyperparameters

The hyperparameters are the precision parameter τ and the range r,

$$\theta = (\tau, r)$$

The latent field has marginal variance $1/\tau$ and range (as defined above) r. Note that ν is fixed parameter and the model is available only for $\nu = 1, 2, 3$ ($\nu = 0$ is not yet ready). The hyperparameters are represented internally as

$$(\log \tau, \log r)$$

the prior are assigned to these quantities.

Specification

The matern2d model is specified inside the f() function as:

Hyperparameter spesification and default values

 $\operatorname{\mathbf{doc}}$ Matern covariance function on a regular grid

hyper

theta1

hyperid 35001
name log precision
short.name prec
initial 4
fixed FALSE
prior loggamma
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)

```
theta2
         hyperid 35002
         name log range
         short.name range
         initial 2
         fixed FALSE
         prior loggamma
         param 1 0.01
         to.theta function(x) log(x)
         from.theta function(x) exp(x)
constr FALSE
nrow.ncol TRUE
augmented FALSE
aug.factor 1
aug.constr
n.div.by
n.required FALSE
set.default.values TRUE
pdf matern2d
Example
nrow=20
ncol=30
n = nrow*ncol
s.noise = 1
zi.mat = matrix(NA,nrow=nrow,ncol=ncol)
i=1:nrow
for(j in 1:ncol)
    zi.mat[i,j] = 3*exp(-(i-j)^2/4)
## iid noise
noise.mat=matrix(rnorm(nrow*ncol, sd=s.noise),nrow,ncol)
## make simulated data with no spatial component
y.mat = zi.mat + noise.mat
## convert matrices to the internal representation in INLA
y = inla.matrix2vector(y.mat)
node = 1:n
formula= y ~ 1+ f(node, model="matern2d", nu=1, nrow=nrow, ncol=ncol,
        hyper = list(range = list(param =c(1, 1),
                                  prior = "loggamma",
```

Notes

All indexes in the R-INLA library are one-dimensional so an appropriate mapping is required to get it into the ordering defined internally in inla; see ?inla.matrix2vector, ?inla.vector2matrix, ?inla.node2lattice and ?inla.lattice2node.

This model has much similarity with rw2d; please read the documentation for rw2d.