LogNormal

Parametrisation

The LogNormal has density

$$f(y) = \frac{1}{y\sqrt{2\pi}}\sqrt{\tau}\exp\left(-\frac{1}{2}\tau(\log y - \mu)^2\right), \quad y > 0$$

where

 $\tau > 0$ is the precision parameter,

 μ is the mean parameter.

Link-function

The parameter μ is linked to the linear predictor as:

$$\eta = \mu$$

Hyperparameters

The τ parameter is represented as

$$\theta = \log \tau$$

and the prior is defined on θ .

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Specification

- family="lognormal" for regression models and family="lognormalsurv" for survival models.
- Required arguments: y. Given in a format by using inla.surv() function for "lognormal.surv"

Hyperparameter spesification and default values

lognormal

```
\operatorname{\mathbf{doc}} The log-Normal likelihood
hyper
    theta
        hyperid 77101
        name log precision
        short.name prec
        output.name Precision for the lognormal observations
        output.name.intern Log precision for the lognormal observations
        initial 0
        fixed FALSE
        prior loggamma
        param 1 5e-05
        to.theta function(x) log(x)
        from.theta function(x) exp(x)
survival FALSE
discrete FALSE
link default identity
```

lognormalsurv

```
doc The log-Normal likelihood (survival)
    theta1
       hyperid 78001
       name log precision
       short.name prec
       output.name Precision for the lognormalsurv observations
       output.name.intern Log precision for the lognormalsurv observations
       initial 0
        fixed FALSE
       prior loggamma
       param 1 5e-05
       to.theta function(x) log(x)
       from.theta function(x) exp(x)
    theta2
       hyperid 78002
       name beta1
       short.name beta1
       output.name beta1 for logNormal-Cure
       output.name.intern beta1 for logNormal-Cure
       initial -7
       fixed FALSE
       prior normal
       param -4 100
       to.theta function(x) x
       from.theta function(x) x
    theta3
       hyperid 78003
       name beta2
       short.name beta2
       output.name beta2 for logNormal-Cure
       output.name.intern beta2 for logNormal-Cure
       initial 0
       fixed FALSE
       prior normal
       param 0 100
        to.theta function(x) x
       from.theta function(x) x
    theta4
       hyperid 78004
       name beta3
       short.name beta3
        output.name beta3 for logNormal-Cure
```

```
output.name.intern beta3 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta5
   hyperid 78005
   name beta4
   short.name beta4
   output.name beta4 for logNormal-Cure
   output.name.intern beta4 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta6
   hyperid 78006
   name beta5
   short.name beta5
   output.name beta5 for logNormal-Cure
   output.name.intern beta5 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta7
   hyperid 78007
   name beta6
   short.name beta6
   output.name beta6 for logNormal-Cure
   output.name.intern beta6 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta8
   hyperid 78008
```

```
name beta7
   short.name beta7
   output.name beta7 for logNormal-Cure
   output.name.intern beta7 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta9
   hyperid 78009
   name beta8
   short.name beta8
   output.name beta8 for logNormal-Cure
   output.name.intern beta8 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta10
   hyperid 78010
   name beta9
   short.name beta9
   output.name beta9 for logNormal-Cure
   output.name.intern beta9 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
   from.theta function(x) x
theta11
   hyperid 78011
   name beta10
   short.name beta10
   output.name beta10 for logNormal-Cure
   output.name.intern beta10 for logNormal-Cure
   initial 0
   fixed FALSE
   prior normal
   param 0 100
   to.theta function(x) x
```

```
from.theta function(x) x
survival TRUE
discrete FALSE
link default identity
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```

Example

In the following example we estimate the parameters in a simulated case

```
n = 300
x = c(scale(runif(n)))
eta = 1+2.2*x
y = exp(rnorm(n, mean = eta, sd = 1))
data = list(y=y, event=rep(1, n), x=x)
formula = inla.surv(y, event) ~ 1 + x
r=inla(formula, family ="lognormalsurv", data=data)
summary(r)

data = data.frame(y, x)
formula = y ~ 1 + x
r=inla(formula, family ="lognormal", data=data)
summary(r)
```

Notes

• lognormalsurv can be used for right censored, left censored, interval censored data. A general framework to represent time is given by inla.surv. If the observed times y are large/huge, then this can cause numerical overflow, and if you encounter this problem, try to scale the observatios, like time = time / max(time).