# **Box-Cox Gaussian**

## Parametrisation

The Gaussian distribution is

$$f(y) = \frac{\sqrt{s\tau}}{\sqrt{2\pi}} y^{\lambda - 1} \exp\left(-\frac{1}{2}s \left(f_{\lambda}(y) - \mu\right)^{2}\right)$$

for continuously responses y > 0 where

 $\mu$ : is the mean

 $\tau$ : is the precision

s: is a fixed scaling, s > 0.

and the Box-Cox transformation is

$$f_{\lambda}(y) = \frac{y^{\lambda} - 1}{\lambda} - \frac{\mu^{\lambda} - 1}{\lambda}$$

#### **Link-function**

The mean and variance of y are given as

$$\mu$$
 and  $\sigma^2 = \frac{1}{s\tau}$ 

and the mean is linked to the linear predictor by

$$\mu = \eta$$

## Hyperparameters

The precision is  $\tau$  and

$$\theta_1 = \log \tau$$

and the prior is defined on  $\theta_1$ .

The Box-Cox transformation-parameter  $\lambda$  is  $\theta_2 = \lambda$  and the prior is defined on  $\theta_2$ .

## **Specification**

- family="bcgaussian"
- Required arguments: y and s (argument scale)

The scalings have default value 1.

### Hyperparameter spesification and default values

## Example

n=100

a = 1

b = 1

z = rnorm(n)

eta = a + b\*z

tau = 100

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scale = exp(rnorm(n))
prec = scale*tau
y = rnorm(n, mean = eta, sd = 1/sqrt(prec))
data = list(y=y, z=z)
formula = y ~ 1+z
result = inla(formula, family = "gaussian", data = data,
        control.family = list(hyper = list(
                                    prec = list(
                                            prior = "loggamma",
                                            param = c(1.0, 0.01),
                                             initial = 2))),
              scale=scale, keep=TRUE)
summary(result)
## with an offset in the variance
var0 = 1.0 ## fixed offset
var1 = 2.0
v = var0 + var1
s = sqrt(v)
x = rnorm(n)
y = 1 + x + rnorm(n, sd = s)
rr = inla(y ~ x,
         data = data.frame(y, x),
         control.family = list(
             hyper = list(precoffset = list(initial = log(1/var0)))),
         verbose = TRUE)
summary(rr)
plot(rr$internal.marginals.hyperpar[[1]], type = "l", lwd=3)
abline(v = log(1.0/var1), lwd=3, col = "blue")
```

Notes