

# Human capital mediates natural selection in contemporary humans

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## Abstract

Natural selection has been documented in contemporary humans, but little is known about the mechanisms behind it. We test for natural selection through the association between 33 polygenic scores and fertility, across two generations, using data from UK Biobank (N = 409,629 British subjects with European ancestry). Consistently over time, polygenic scores that predict lower earnings, education and health also predict lower fertility. Selection effects are concentrated among lower SES groups, younger parents, people with more lifetime sexual partners, and people not living with a partner. The direction of natural selection is reversed among older parents, or after controlling for age at first live birth. These patterns are in line with economic theories of fertility, in which earnings-increasing human capital may either increase or decrease fertility via income and substitution effects in the labour market. Studying natural selection can help us understand the genetic architecture of health outcomes: we find evidence in modern day Great Britain for multiple natural selection pressures that vary between subgroups in the direction and strength of their effects, that are strongly related to the socio-economic system, and that may contribute to health inequalities across income groups.

## I Introduction

Living organisms evolve through natural selection, in which allele frequencies change in the population through differential reproduction rates. Studying the mechanisms behind natural selection can help us better understand how individual differences in complex traits and disease risk arise (Benton et al. 2021). Recent work confirms that natural selection is taking place in modern human populations, using genome-wide analysis (Barban et al. 2016; Beauchamp 2016; Conley et al. 2016; Kong et al. 2017; Sanjak et al. 2018; Fieder and Huber 2022). In particular, genetic variants associated with higher educational attainment are being selected against, although effect sizes appear small.

As yet we know little about the social mechanisms behind natural selection. A potential explanation comes from the economic theory of fertility (Becker 1960). In this theory, higher potential earnings have two opposite effects on fertility:

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a fertility-increasing *income effect* (higher income makes children more affordable), and a fertility-lowering *substitution effect* (time spent on childrearing has a higher cost in foregone earnings). Thus, an individual’s *human capital* – skills and personality traits which are valuable in labour markets – can increase or decrease his or her fertility. This can lead to selection on inherited variants which are linked to human capital. Furthermore, the economic theory predicts systematic variation in the relative strength of the income and substitution effects across different social groups.

This study uses data from UK Biobank (Bycroft et al. 2018) to learn more about contemporary natural selection. We test for natural selection on 33 different polygenic scores by estimating their correlation with fertility. We extend the analysis over two generations, using data on respondents’ number of siblings as well as their number of children. This is interesting because consistent natural selection over multiple generations could lead to substantive effects in the long run. Next, we examine correlations with fertility in different subgroups. Across the board, selection effects are stronger in groups with lower income and less education, among younger parents, people not living with a partner, and people with more lifetime sexual partners. Outside these groups, effects are weaker and often statistically insignificant. In some subgroups, the direction of selection is even reversed.

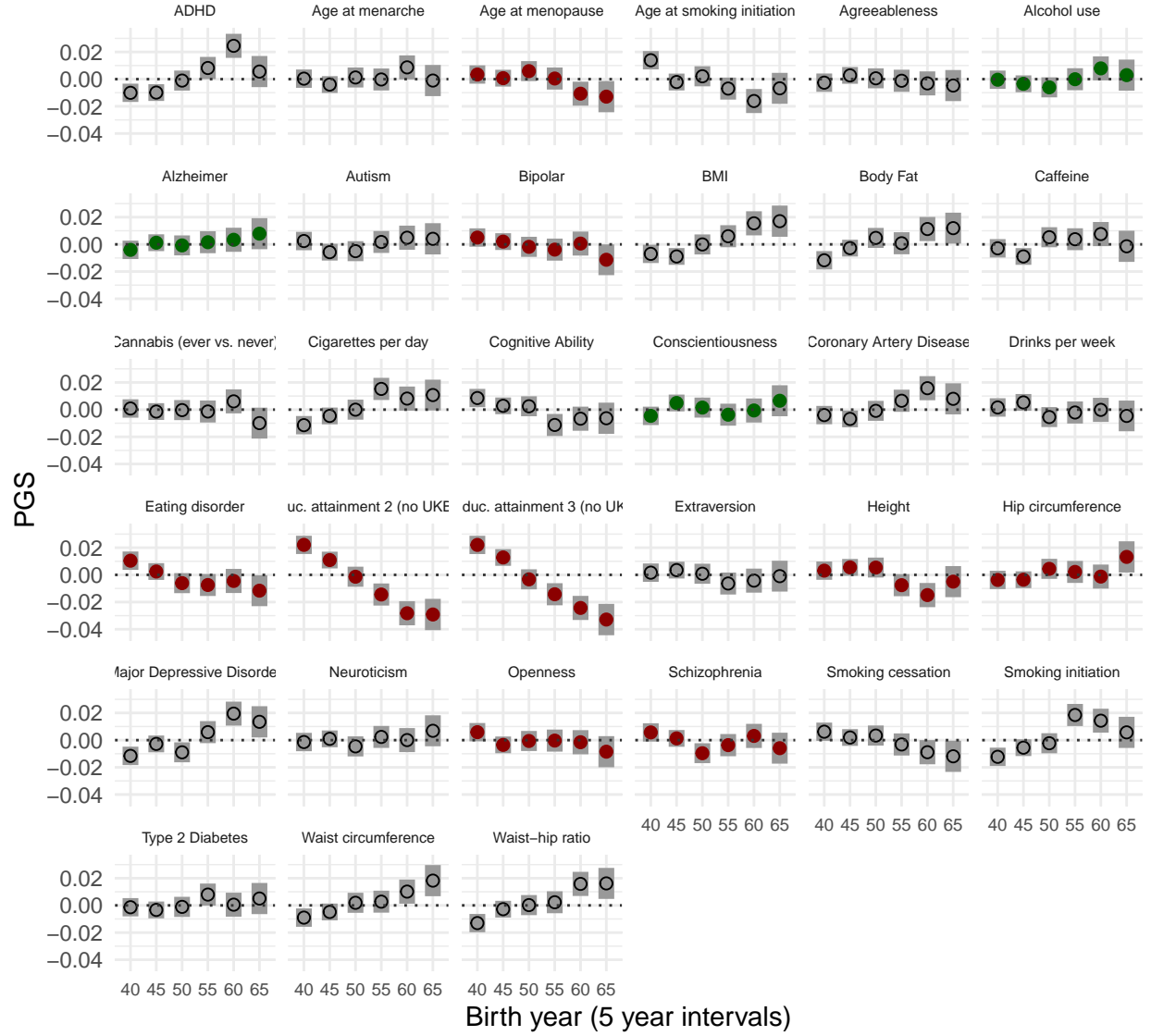
We then show that a simple model of human capital, education and fertility choices can give rise to these empirical results. To test the theory, we show that polygenic scores’ correlation with fertility is associated with their correlation with education and earnings. Furthermore, a mediation analysis shows that part of the correlation with fertility is indeed *via* education. Thus, contemporary natural selection on polygenic scores can be explained by scores’ correlation with earnings-increasing human capital.

Lastly, we discuss the effects of natural selection. While measured effects on mean genetic scores are small, natural selection may substantially increase the correlation between genetic scores and income, increasing genetic differences between different social groups, and thus making the “genetic lottery” (Harden 2021) more unfair.

## 2 Results

We created polygenic scores for 33 traits in 409,629 individuals of European descent, corrected for ancestry using 100 genetic principal components (see Materials and Methods). Figure 1 plots mean polygenic scores in the sample by 5-year birth intervals. Several scores show consistent increases or declines over this 30-year period, of the order of 5% of a standard deviation. These changes could reflect natural selection within the UK population, but also emigration, or ascertainment bias within the sample (Fry et al. 2017).

To test more directly for natural selection, we regress respondents’ relative lifetime reproductive success (RLRS) on their polygenic scores (PGS):

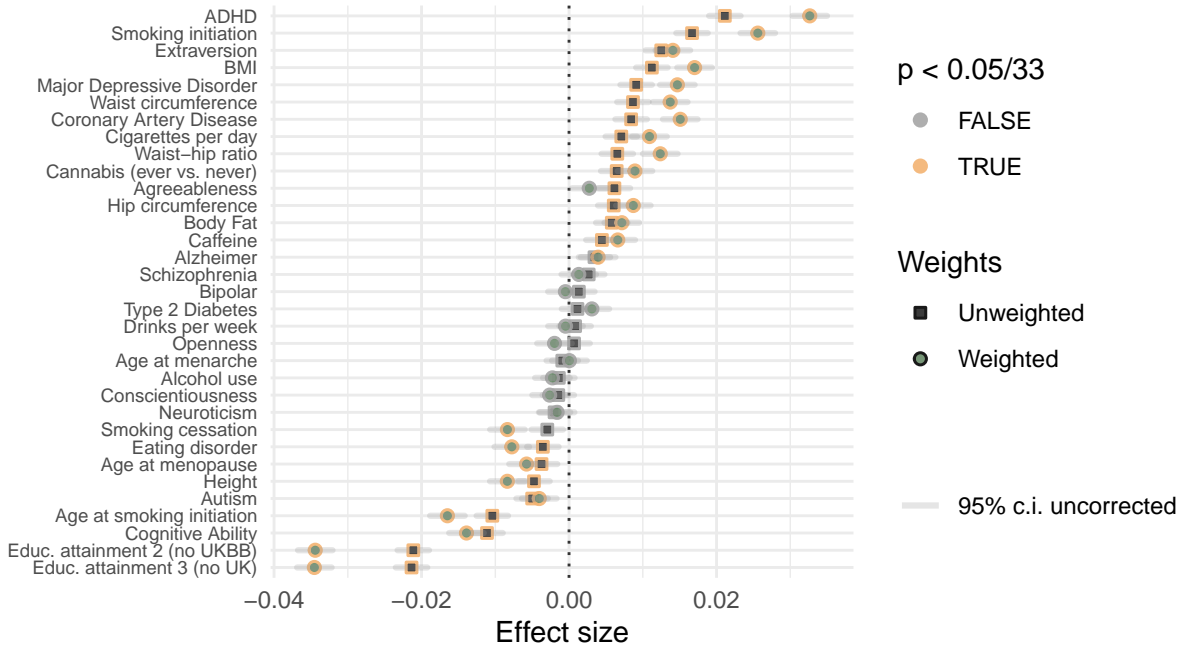


**Figure 1:** Mean polygenic scores (PGS) by birth year in UK Biobank. Circles are means for 5-year intervals. Lines are 95% confidence intervals. Solid circles show a significant linear increase (green) or decrease (red) over time ( $p < 0.05/33$ ).

$$RLRS_i = \alpha + \beta PGS_i + \varepsilon_i \quad (1)$$

RLRS is defined as respondents' number of children, divided by the mean number of children of people born in the same year. The "selection effect",  $\beta$ , reflects the strength of natural selection within the sample. In fact, since polygenic scores are normalized,  $\beta$  is the expected polygenic score among children of the sample (Beauchamp 2016).<sup>1</sup> Note that equation (1) does not control for many environmental and genetic factors that could affect fertility, and as a result,  $\beta$  is not an estimate of the causal effect of a polygenic score on fertility. However, natural selection is a correlational phenomenon: polygenic scores which correlate with high fertility are being selected for, whatever the underlying causal relationship.

Figure 2 plots selection effects among the entire sample.<sup>2</sup> To correct for ascertainment bias, we weight participants using the model of Alten et al. (2021). Weighting makes a large difference to estimates, increasing effect sizes by a mean factor of 1.48.<sup>3</sup>



**Figure 2:** Selection effects: weighted and unweighted regressions. Each point represents a single bivariate regression of number of children on a polygenic score. P value threshold is 0.05, Bonferroni-corrected for multiple comparisons. Confidence intervals are uncorrected.

<sup>1</sup>The selection effect  $\beta$  equals  $Cov(RLRS, PGS)/Var(PGS)$ . Since PGS are normalized to variance 1 and mean 0, this reduces to  $Cov(RLRS, PGS) = E(RLRS \times PGS) - E(RLRS)E(PGS) = E(RLRS \times PGS)$ . This is the polygenic score weighted by relative lifetime reproductive success, which is the average polygenic score in the next generation (Robertson 1966).

<sup>2</sup>We also check for stabilizing and disruptive selection by estimating (1) with a quadratic term. Stabilizing selection selects for intermediate values, while disruptive selection selects for extreme values. In particular, we find disruptive selection for educational attainment polygenic scores: at higher values of these scores, the negative effect on fertility is smaller (Appendix Figure 10).

<sup>3</sup>We use these weights throughout. All results are robust if we run unweighted regressions. Appendix Table 2 shows results using alternative weighting schemes.

We now show the empirical puzzles which motivate our economic model. Each concerns differences in the strength of natural selection across different subgroups in the sample. Splitting the sample by demographic and social variables, we re-estimate (1) within each subgroup. We use socio-economic variables including income and education, and family structure variables including age at first live birth, presence of a partner, and lifetime number of sexual partners.

Figure 3 plots selection effects for each polygenic score, grouping respondents by age of completing full-time education, and by household income. Effects are larger and more significant for the lowest income category, and for the lowest education category. These results are robust to controlling for respondents' age (Appendix section 7.4).

Turning to family structure, we split respondents by lifetime number of sexual partners, at the median value of 3 (Figure 4a). Selection effects are larger and more significant among those with more than 3 lifetime partners. Next we split respondents by whether they were living with a spouse or partner at the time of interview. Effects are larger among those not living with a spouse or partner (Figure 4b).<sup>4</sup>

Lastly, we split female respondents by age at first live birth (AFLB).<sup>5</sup> There is evidence for genetic effects on AFLB (Barban et al. 2016), and there is a close link between this variable and number of children born. Figure 5 shows effect sizes estimated separately for each tercile of AFLB. Effects are strikingly different across terciles. Educational attainment, ADHD and MDD are selected for amongst the youngest third of mothers, but selected against among the oldest two-thirds. Similarly, several polygenic scores for body measurements are selected against only among older mothers. The correlation between effect sizes for the youngest and oldest terciles is  $-0.83$ . To investigate this further, we estimate equation (1) among females, *controlling* for AFLB. In 18 out of 33 cases, effects change sign when controls are added. The correlation between effect sizes controlling for AFLB, and raw effect sizes, is  $-0.58$ . Thus, selection effects seem to come through two opposing channels: a correlation with AFLB, and an opposite-signed correlation with number of children after AFLB is controlled for.

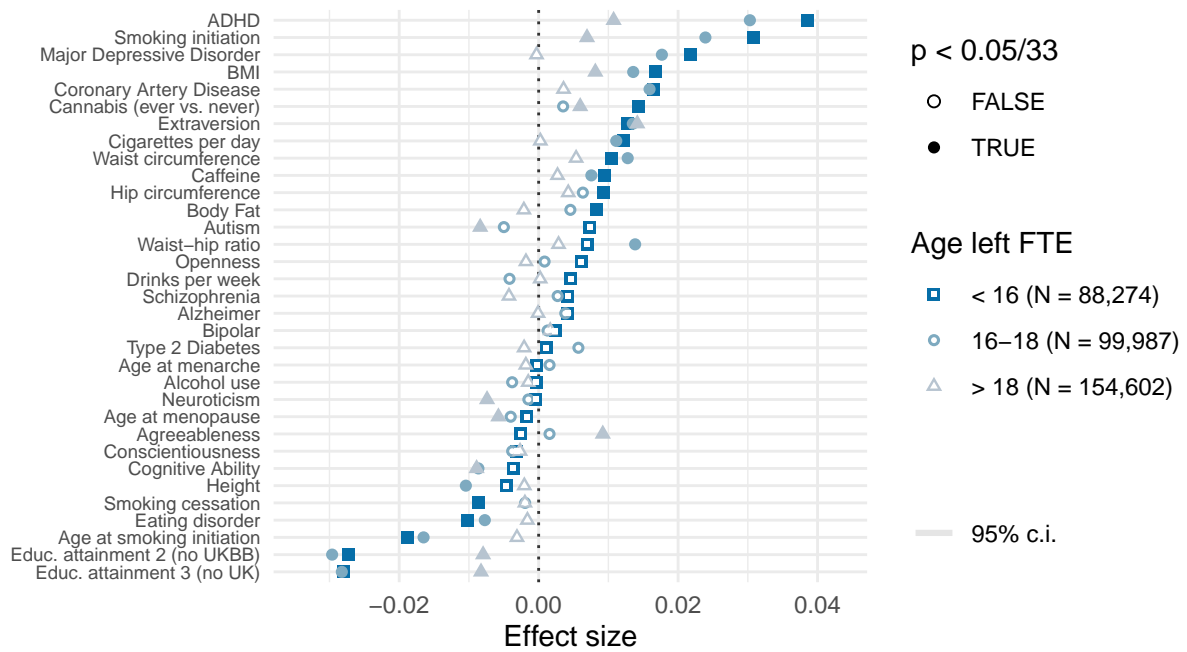
We emphasize that our categories are not necessarily exogenous to polygenic scores. For example – both in the data (Appendix Figure 17) and in our model – age at first live birth is a choice variable, which is endogenous to an individual's human capital and related polygenic scores. Nevertheless, observed differences in equation (1) across subgroups constrain the set of possible theories; a good theory of contemporary natural selection needs to explain how these results arise. As we show below, a model based on the economic theory of fertility can do just that.

We also examine selection effects among respondents' parents, using information on respondents' number of siblings to calculate parents' RLRs. Effect sizes of polygenic scores are highly correlated across the two generations (Appendix Figure 12). Median-splitting respondents by year of birth, we find little evidence of change in effect sizes among the

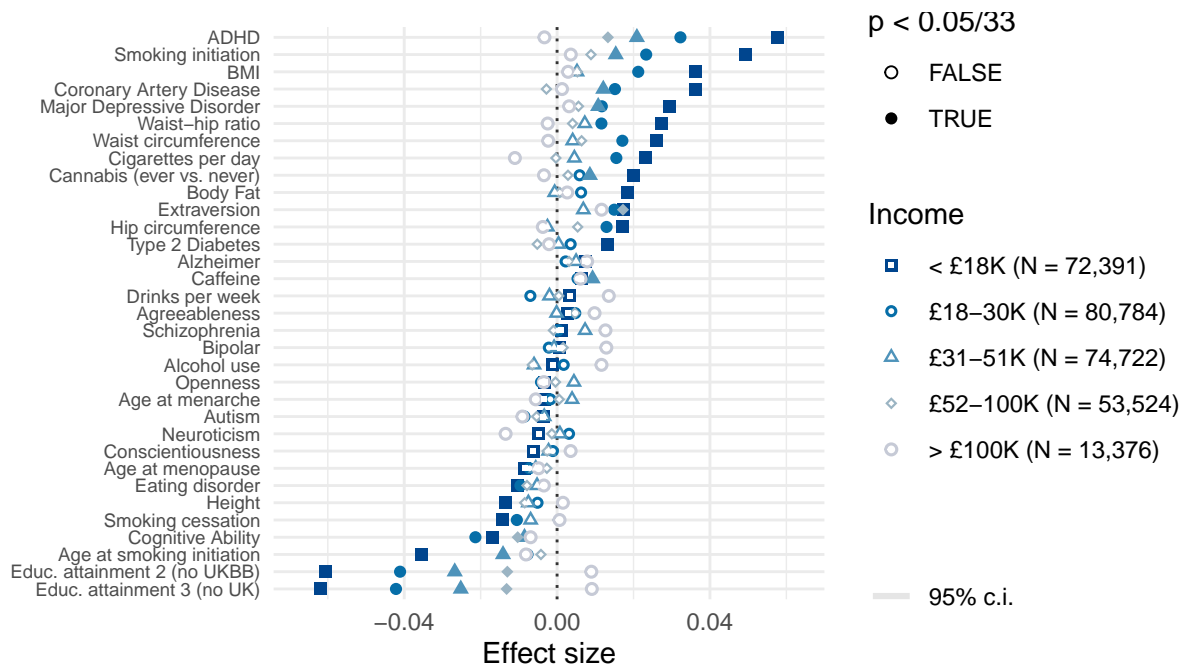
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<sup>4</sup>The same pattern holds if we analyse men and women separately (Appendix Figure 11). We also directly compared selection effects between men and women (Appendix Figure 9).

<sup>5</sup>AFLB is unavailable for men.

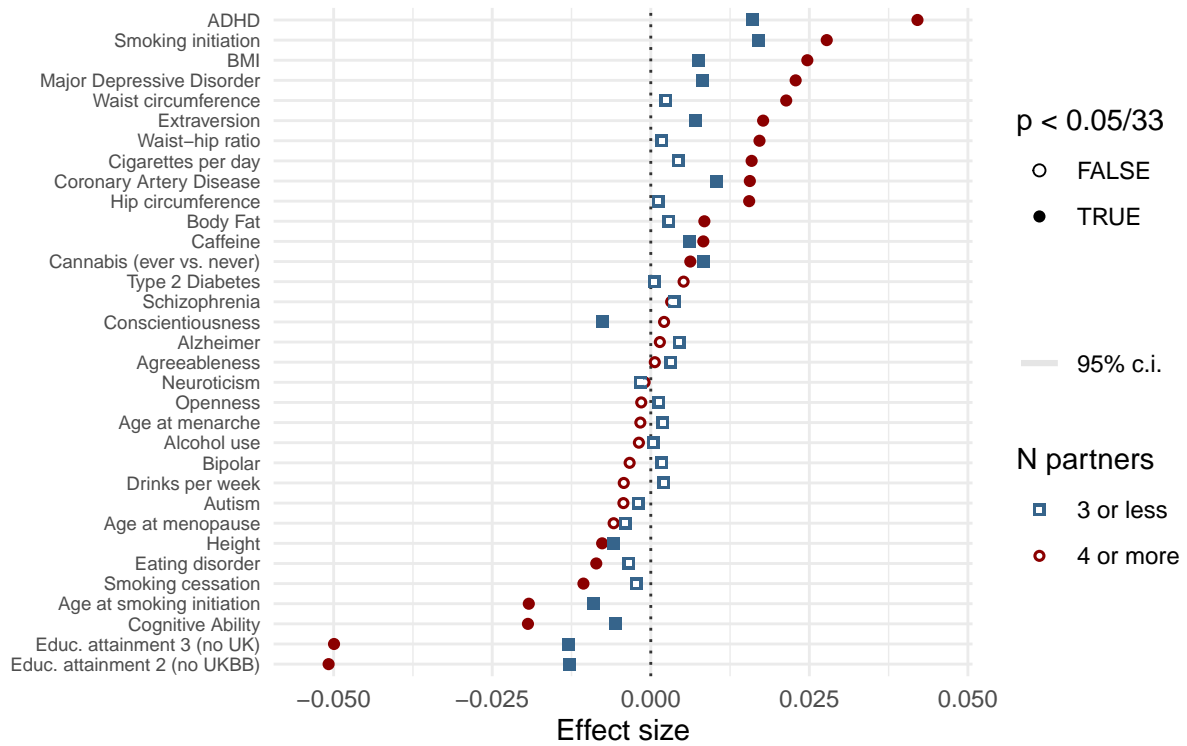


(a) Age left full-time education

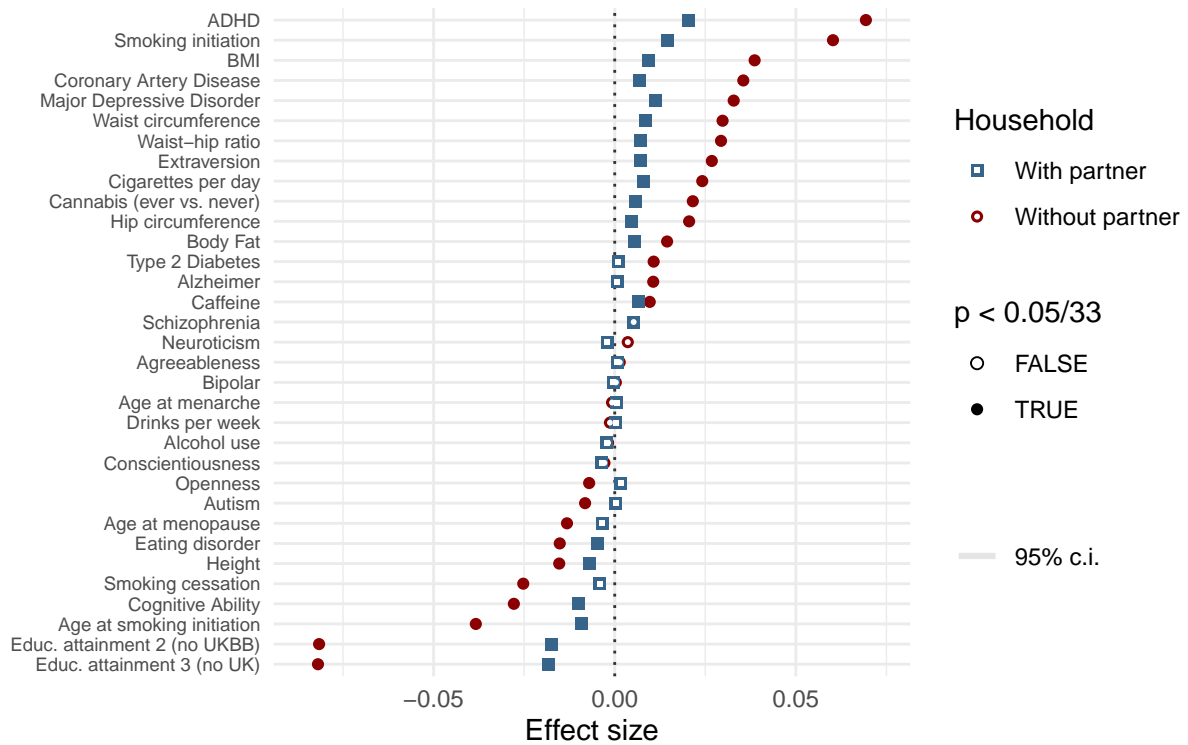


(b) Household income

**Figure 3:** Selection effects by education and income.

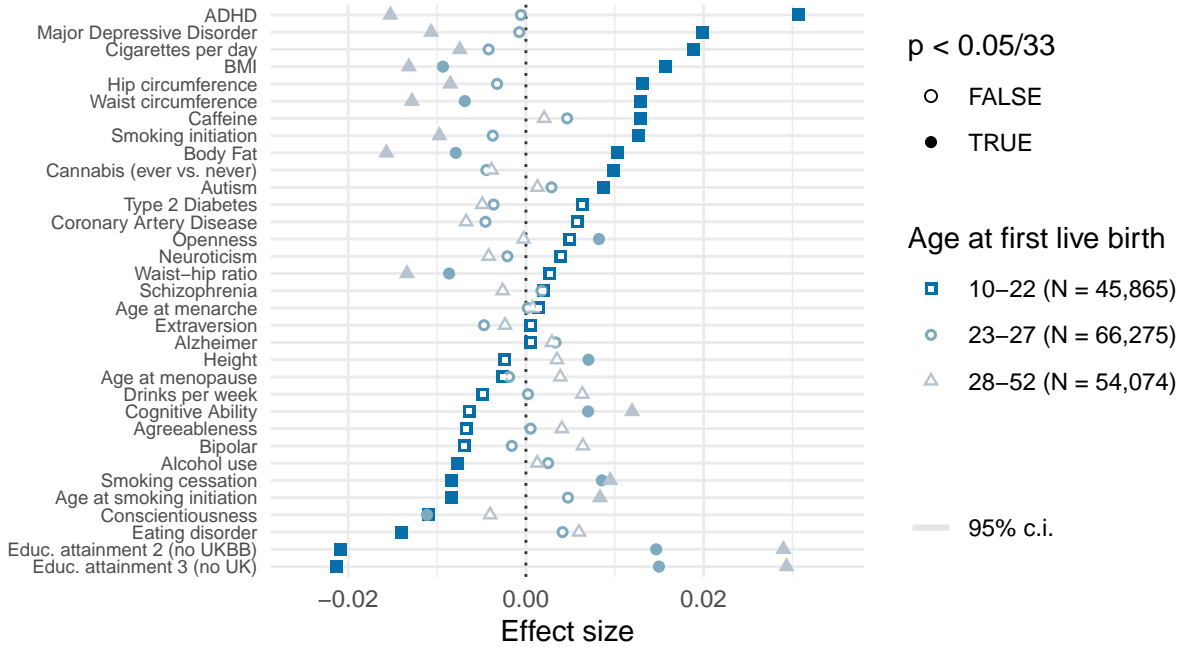


(a) Lifetime number of sexual partners



(b) Presence of a partner

**Figure 4:** Selection effects by number of sexual partners and presence of a partner.



**Figure 5:** Selection effects by age at first live birth terciles (women only).

parents' generation. There is some evidence that selection effect sizes are increasing in the respondents' generation, with 9 polygenic scores showing a significant increase. We also check whether selection effects vary by socio-economic status and AFLB in the parents' generation. We have no information about parents' income, so we use the 1971 Townsend deprivation score of respondents' birthplace as a proxy (Townsend 1987). Results show the same pattern as for respondents. Effect sizes are larger and more often significant in the most deprived areas (Appendix Figure 13). Effects are larger among younger parents, and change sign when controlling for AFLB, among both mothers and fathers (Appendix Figures 15, 16). Lastly, we check for a "quantity-quality tradeoff" between parents' number of children and number of grandchildren. We do not find any: in fact, the correlation between respondents' and parents' RLRS is positive ( $\rho = 0.1, p < 2 \times 10^{-16}$ ).

### 3 Human capital and natural selection

These results show that selection effects are weaker, absent, or even reversed among some subgroups of the population. A possible explanation for this comes from the economic theory of fertility (Becker 1960; Willis 1973; Becker and Tomes 1976). According to this theory, increases in a person's wage affect their fertility via two opposing channels. There is an *income effect* by which children become more affordable, like any other good. There is also a *substitution effect*: since childrearing has a cost in time, the opportunity cost of childrearing increases if one's market wage is higher. The income effect leads higher earners to have more children. The substitution effect leads them to have fewer.



Suppose that certain genetic variants correlate with *human capital*: skills or other characteristics that affect an individual's earnings in the labour market (Mincer 1958; Becker 1964). These variants may then be associated with opposing effects on fertility. The income effect will lead to natural selection in favour of earnings-increasing variants (or variants that are merely associated with higher earnings). The substitution effect will do the reverse.

To show this, we write down a simple model of fertility choices.  $h$  is an individual's level of human capital. For now, we simply identify this with his or her wage  $W$ . Raising a child takes time  $b$ . People maximize utility  $U$  from the number of children  $N$  and from income  $Y \equiv (1 - bN)W$ :

$$U = u(Y) + aN.$$

Here  $a$  captures the strength of preference for children.  $u(\cdot)$  captures the taste for income, and is increasing and concave. We treat  $N$  as continuous, in line with the literature: this can be thought of as the expected number of children among people with a given  $a$ ,  $b$  and  $W$ . The marginal benefit of an extra child is  $\frac{dU}{dN} = -bWu'(Y) + a$ . The effect of an increase in human capital on this marginal benefit is

$$\frac{d^2U}{dNd h} = \underbrace{-bu'(Y)}_{\text{Substitution effect}} \underbrace{-bYu''(Y)}_{\text{Income effect}}.$$

The *substitution effect* is negative and reflects that when wages increase, time devoted to childcare costs more in foregone income. The positive *income effect* depends on the curvature of the utility function, and reflects that when income is higher, the marginal loss of income from children is less painful.

To examine education and fertility timing, we extend the model to two periods. For convenience we ignore time discounting, and assume that credit markets are imperfect so that agents cannot borrow. Write

$$U(N_1, N_2) = u(Y_1) + u(Y_2) + aN_1 + aN_2 \quad (2)$$

Instead of identifying human capital with wages, we now allow individuals to choose a level of education  $s \in [0, 1]$ , which has a time cost in period 1. Education is complementary to human capital  $h > 0$ , and increases period 2 wages, which take the simple functional form  $w(s, h) = sh$ . We normalize period 1 wages to 1, and let  $u(\cdot)$  take the constant relative risk aversion form  $u(y) = \frac{y^{1-\sigma}-1}{1-\sigma}$ .  $\sigma > 0$  measures the curvature of the utility function, i.e. the decline in marginal utility of income as income increases. We examine total fertility  $N^* = N_1^* + N_2^*$  and the *fertility-human capital relationship*,  $\frac{dN^*}{dh}$ . For  $\sigma < 1$  in a neighbourhood of  $\sigma = 1$ , Table 1 shows five theoretical predictions, along with our

corresponding empirical results for the correlation between polygenic scores and RLRS.<sup>6</sup> The key insight of the model is that for middling levels of  $\sigma$ , the substitution effect dominates at low income levels, but is balanced by the income effect as income increases.

**Table 1:** Predictions from the theoretical model and corresponding empirical results.

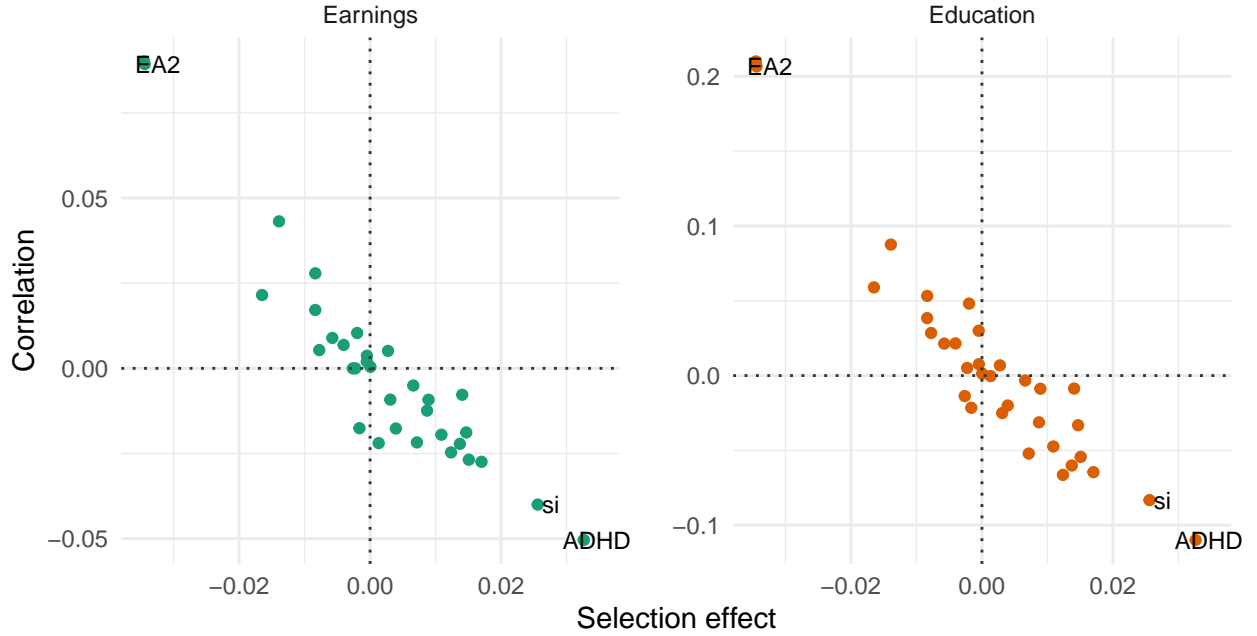
	<b>Theory: the fertility-human capital relationship is...</b>	<b>Empirical results</b>
1.	Negative: $\frac{dN^*}{dh} < 0$ .	Figures 1 and 2.
2.	Weaker (closer to zero) at higher wages and/or levels of human capital.	Figure 3a. Selection effects are also weaker at higher polygenic scores for educational attainment (Appendix Figure 10).
3.	More negative when the time burden of children $b$ is larger.	Stronger effects for single parents (Figure 4).
4.	Weaker at higher levels of education $s$ .	Figure 3b.
5.	Weaker among those who start fertility in period 2 ( $N_1^* = 0$ ) than among those who start fertility in period 1 ( $N_1^* > 0$ ).	Effects weaker among those starting fertility later (Figure 5).

Thus, a simple economic model can explain many of our results. Other empirical work in economics also supports our mechanism. Caucutt, Guner, and Knowles (2002) and Monstad, Proper, and Salvanes (2008) show that education and skills affect age at first birth and fertility. Income decreases fertility at low income levels, but increases it at higher income levels (Cohen, Dehejia, and Romanov 2013). US fertility decreases faster with education among single mothers than married mothers (Baudin, De La Croix, and Gobbi 2015), in line with our prediction 3 and as predicted by Becker (1981). A related literature shows negative correlations between IQ and fertility (e.g. Lynn and Van Court 2004; Reeve, Heeney, and Menie 2018).

## 4 Testing the theory

We test this explanation in two ways. First, the economic theory predicts that genetic variants will be selected for (or against) in proportion to their correlation with human capital. Figure 6 plots selection effects on each polygenic score against that score's correlation with two measures of human capital: earnings in a respondent's first job, and educational attainment. The relationships are strongly negative. Thus, human capital appears to be relevant to natural selection. The negative relationship suggests that substitution effects dominate income effects, which fits the known

<sup>6</sup>Predictions 1-3 also hold in the one-period model with constant relative risk aversion. Our empirical results are actually stronger than prediction 5, in that correlations with fertility are *reversed* at higher AFLB. This prediction can be accommodated in the model if children have a money cost as well as a time cost (Appendix Figure 24).

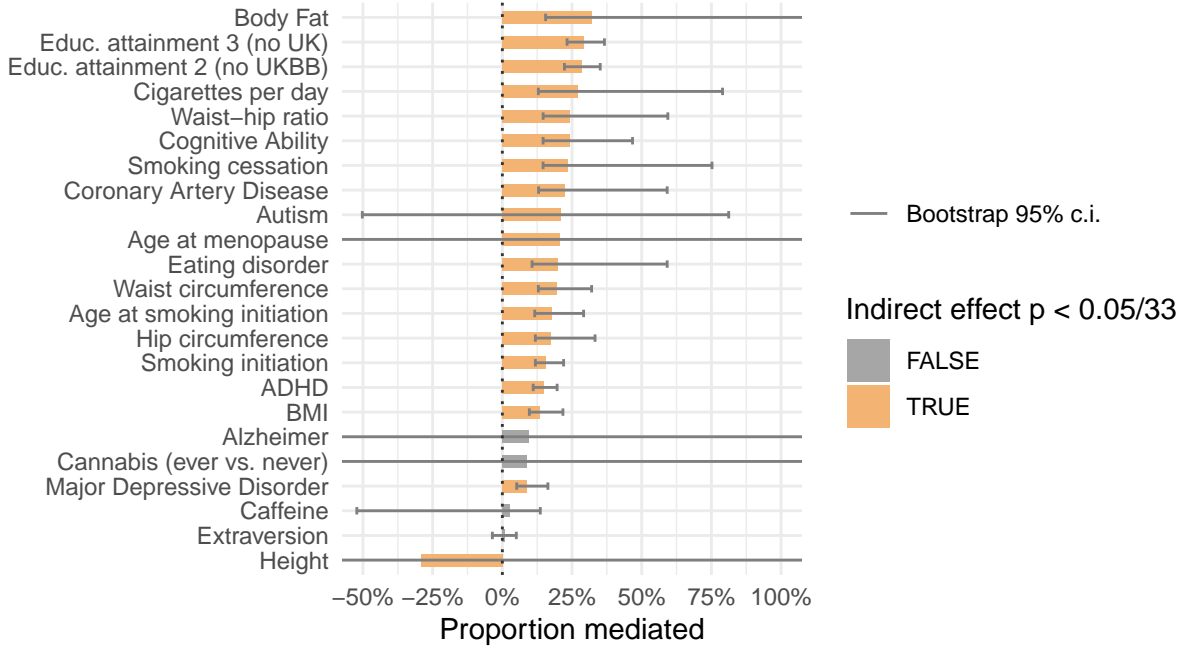


**Figure 6:** Selection effects by correlations with earnings and educational attainment. Each point represents one polygenic score.

negative association between income and fertility (Becker 1960; Jones and Tertilt 2006). The correlations reverse when we control for age at first live birth, suggesting that within AFLB categories, the income effect dominates.

Second, for the 23 scores where the bivariate correlation in (1) is significant at  $p < 0.05/33$ , we run a mediation analysis to directly test whether the correlation between each polygenic score and fertility is mediated by educational attainment (Appendix Table 4). Figure 7 shows estimated proportions explained along with bootstrap 95% confidence intervals (uncorrected; 100 bootstraps). For 18 scores, the indirect effect of the score on fertility *via* educational attainment takes the same sign as the overall effect, and is significantly different from zero ( $p < 0.05/33$ ). Among these scores, the median proportion of the total effect explained by the indirect effect is 20.8%. The educational attainment variable is a relatively crude measure of human capital: more accurate measures would likely explain more of the total effect.

We consider three alternative theories that might explain our results. First, welfare benefits which incentivize child-bearing might be taken up more among low-income individuals. However, the majority of effect sizes appear unchanged over a large span of twentieth-century history (Appendix Table 3), during which government spending on child-related benefits varied considerably (Social Security Committee 1999). In general, there is only weak evidence that welfare benefits affect fertility (Gauthier 2007). Future work could test this theory more explicitly. A second alternative theory is that polygenic scores correlate with the motivation to have children, i.e. parameter  $a$  in the model (cf. Jones, Schoonbroodt, and Tertilt 2008). This theory would not explain why selection effects are smaller at higher incomes and education levels. Indeed, in the model, the effect of  $a$  on fertility becomes stronger at higher levels of human



**Figure 7:** Proportion of selection effect mediated by educational attainment, polygenic scores with significant selection effects

capital. A third alternative is that traits under selection are linked to externalizing behaviour and risk-seeking. This might be partially captured by our parameter  $\sigma$ , which can be interpreted as a measure of risk aversion over income. However, a more direct channel is risky sexual behaviour (Mills et al. 2021). The data here provide some support for this: scores which might plausibly be linked to externalizing behaviour, like ADHD and younger age at smoking initiation, are selected for. This theory is less good, though, at explaining variation in selection across the full range of scores, including physical measures such as waist-hip ratio and BMI. We test the theory directly by re-estimating equation (1) controlling for a measure of risk attitude (UK Biobank field 2040). The median ratio of effect sizes between regressions with and without controls is 0.98; all scores which are significant at  $p < 0.05/33$  in uncontrolled regressions remain so when controlling for risk attitude. This non-result could simply reflect the imprecision of the risk attitude measure, which is a single yes/no question. But this measure *does* predict the overall number of children, highly significantly ( $p < 2 \times 10^{-16}$  in 33 out of 33 regressions). Given that, and the statistical power we get from our sample size, we believe that the non-result is real: while risk attitude does predict fertility in the sample, it is not an important channel for natural selection.

## 5 Discussion

Previous work has documented natural selection in modern populations on variants underlying polygenic traits (Beauchamp 2016; Kong et al. 2017; Sanjak et al. 2018). We show that correlations between polygenic scores and

fertility are highly concentrated among specific subgroups of the population, including people with lower income, lower education, younger first parenthood, and more lifetime sexual partners. Among mothers aged 22+, selection effects are reversed. Furthermore, the size of selection effects on a polygenic score correlates with that score's association with labour market earnings. Strikingly, some of these results were predicted by Fisher (1930), pp. 253-254.

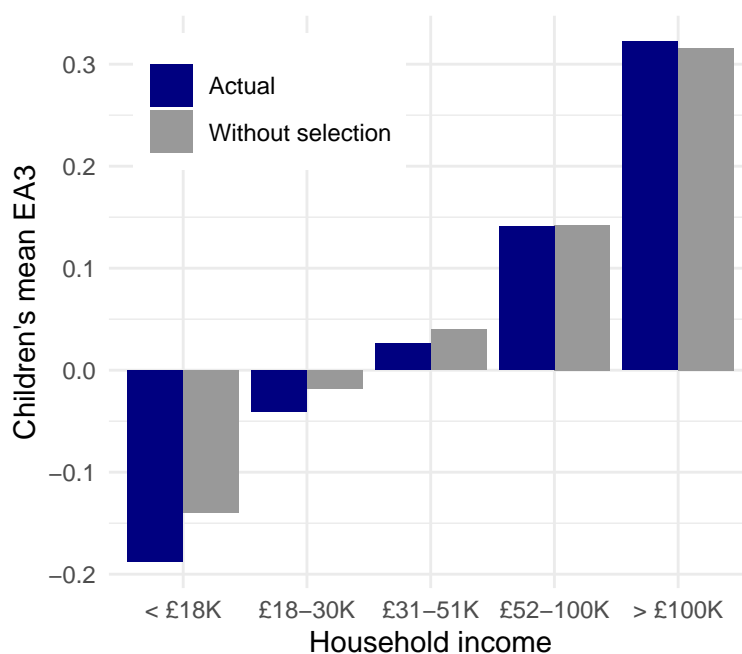
The economic theory of fertility provides a parsimonious explanation for these findings. Because of the substitution effect of earnings on fertility, scores are selected for when they correlate with low human capital, and this effect is stronger at lower levels of income and education.

Polygenic scores which correlate with high (low) earnings and more (less) education are being selected against (selected for). In addition, many of the phenotypes under positive selection are linked to disease risk. Many people would probably prefer to have high educational attainment, a low risk of ADHD and major depressive disorder, and a low risk of coronary artery disease, but natural selection is pushing against genes associated with these traits. Potentially, this could increase the health burden on modern populations, but that depends on effect sizes. Our results suggest that naïve estimates can be affected by sample ascertainment bias. There may be remaining sources of ascertainment bias after our weighting; if so, we expect that, like the sources of ascertainment we have controlled for, they probably bias our results towards zero. This problem may be less serious in surveys which aim to be representative (as the UK Biobank does not). However, there is still scope for bias, since not all respondents consent to the collection of genetic data. For instance, completion rates for genotype data in the US Health and Retirement Study were around 80-85% (HRS 2020). Researchers should be aware of the risks of ascertainment when studying modern natural selection.

We also do not know how estimated effect sizes of natural selection will change as more accurate measures of genetic variation are produced, or whether genetic variants underlying other phenotypes will show a similar pattern to those studied here. In addition, effects of polygenic scores may be inflated in population-based samples, because of indirect genetic effects, gene-environment correlations, and/or assortative mating (Lee et al. 2018; Selzam et al. 2019; Kong et al. 2018; Howe et al. 2021), although we do not expect that this should impact their association with number of offspring, or the resulting changes in allele frequencies. Lastly, although effects on our measured polygenic scores are small, even after weighting, disadvantages which are individually small may cumulate and/or interact to create larger effects. Overall, it is probably too early to tell whether modern natural selection has a substantively important effect on population means.

Because selection effects are concentrated in lower-income groups, they may also increase inequality with respect to polygenic scores. For example, Figure 8 graphs mean polygenic scores for educational attainment (EA3) among children from households of different income groups. The blue bars show the actual means, i.e. parents' mean polygenic score weighted by number of children. The grey bars show the hypothetical means if all households had equal numbers of

211 children. Natural selection against genes associated with educational attainment, which lowers the mean, is stronger  
 212 at the bottom of the income distribution, and this increases the differences between groups. Overall, natural selection  
 213 increases the correlation of polygenic scores with income for 28 out of 33 polygenic scores, with a median percentage  
 214 increase of 16.43% (Appendix Table 5). If inequalities in polygenic scores are important for understanding social  
 215 structure and mobility (Belsky et al. 2018; Rimfeld et al. 2018; Harden 2021), then these increases are substantive.  
 216 Similarly, since many polygenic scores are predictive of disease risk, they could potentially increase health inequalities.  
 217 In general, the evolutionary history of anatomically modern humans is related to disease risk (Benton et al. 2021);  
 218 understanding the role of contemporary natural selection may aid in mapping the genetic architecture of current health  
 219 disparities.



**Figure 8:** Mean polygenic score for educational attainment (EA3) of children by household income group. Blue is actual. Grey is hypothetical in the absence of selection effects.

220 Existing evidence on human natural selection has led some to “biocosmic pessimism” (Sarraf, Feltham, et al. 2019).  
 221 Others are more sanguine, and argue that natural selection’s effects are outweighed by environmental improvements,  
 222 such as those underlying the Flynn effect (Flynn 1987). The evidence here may add some nuance to this debate. Patterns  
 223 of natural selection have been relatively consistent across the past two generations, but they are not the outcome of a  
 224 single, society-wide phenomenon. Instead they result from opposing forces, operating in different parts of society and  
 225 pulling in different directions.

226 Any model of fertility is implicitly a model of natural selection, but so far, the economic and human genetics literatures  
 227 have developed in parallel. Integrating the two could deepen our understanding of natural selection in modern societies.

Economics possesses a range of theoretical models on the effects of skills, education and income (see Hotz, Klerman, and Willis 1997; Lundberg and Pollak 2007). One perennial problem is how to test these theories in a world where education, labour and marriage markets all interact. Genetic data, such as polygenic scores, could help to pin down the direction of causality, for example via Mendelian randomization (Davey Smith and Ebrahim 2003). Conversely, economic theories and empirical results can shine a light on the mechanisms behind natural selection, and thereby on the nature of individual differences in complex traits and disease risk.

## 6 Materials and methods

We use participant data from UK Biobank (Bycroft et al. 2018), which has received ethical approval from the National Health Service North West Centre for Research Ethics Committee (reference: 11/NW/0382). We limit the sample to white British participants of European descent, as defined by genetic estimated ancestry and self-identified ethnic group, giving a sample size of 409,629. For regressions on number of children we use participants over 50 (males)/45 (females), since most fertility is completed by this age. This gives a sample size of 348,595.

Polygenic scores were chosen so as to cover a reasonably broad range of traits, and based on the availability of a large and powerful GWAS which did not include UK Biobank. Scores were computed by summing the alleles across ~1.3 million genetic variants weighted by their effect sizes as estimated in 33 genome-wide association studies (GWASs) that excluded UK Biobank. To control for population stratification, we corrected the polygenic scores for 100 principal components (PCs).

To compute polygenic scores and PCs, the same procedures were followed as described in Abdellaoui et al. (2019).

Earnings in first job are estimated from mean earnings in the 2007 Annual Survey of Hours and Earnings, using the SOC 2000 job code (Biobank field 22617).

Weighting data was kindly provided by Alten et al. (2021).

Code for this paper is available at <https://github.com/hughjonesd/why-natural-selection>.

### 6.1 Acknowledgements

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## 7 Appendix

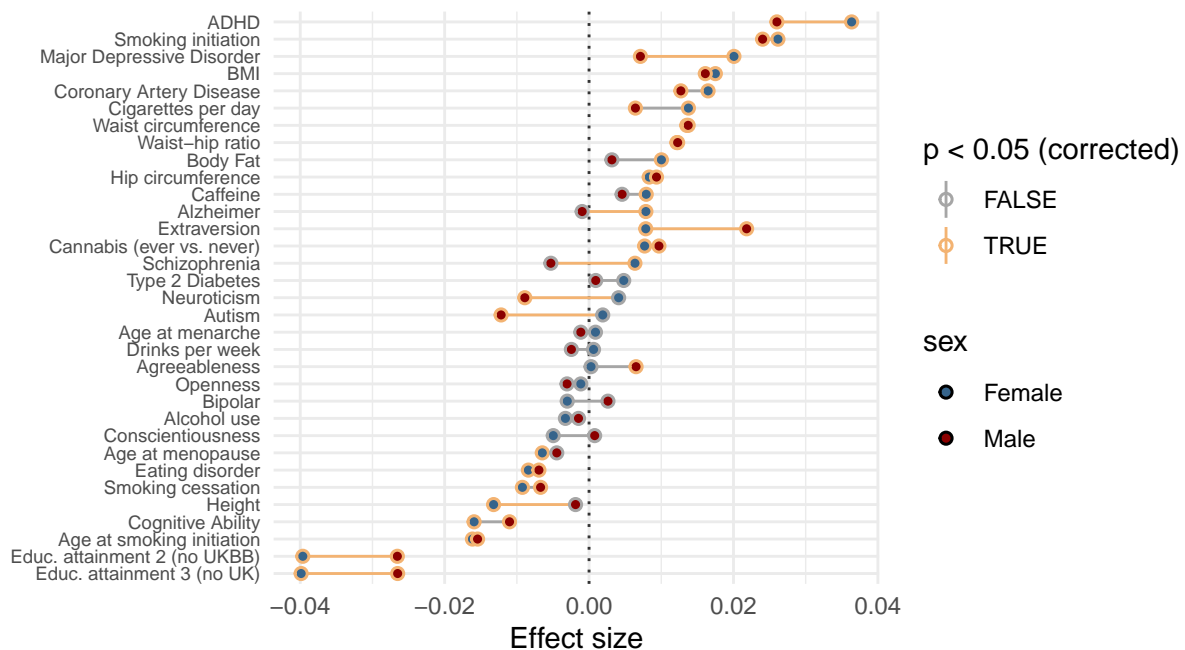
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## 7.1 Selection effects by sex

Figure 9 plots selection effects by sex. Differences are particularly large for educational attainment, height and MDD. Several polygenic scores for mental illness and personality traits are more selected for (or less against) among women, including major depressive disorder (MDD), schizophrenia and neuroticism, while extraversion is more selected for among men. Scores for waist circumference and waist-hip ratio are less selected for among women. One possible reason for these sex differences is that polygenic scores may affect fertility via success in marriage markets, and men and women may value different characteristics in these.



**Figure 9:** Selection effects by sex. Highlighted lines are significant differences at  $p < 0.05/33$ . Highlighted points are significantly different from 0 at  $p < 0.05/66$ .

## 7.2 Alternative weighting schemes

We report results for 3 alternative weighting schemes: weighting by age/qualification; geographical (weighting by Middle Super Output Area); and for women only, age, qualification and age at first live birth. Population data for weighting is taken from the 2011 UK Census and the 2006 General Household Survey (GHS). Weighting for Age/Qualification and Age/Qualification/AFLB weights was done using marginal totals from a linear model, using the `calibrate()` function in the R “survey” package (Lumley 2020). Geographical weighting was done with iterative post-stratification using the `rake()` function, on Census Middle Layer Super Output Areas, sex and presence/absence of a partner.

Table 2 gives effect sizes as a proportion of the unweighted effect size, for all polygenic scores which are consistently signed and which are significantly different from zero in unweighted regressions.

**Table 2:** Weighted effect sizes as a proportion of unweighted effect sizes.

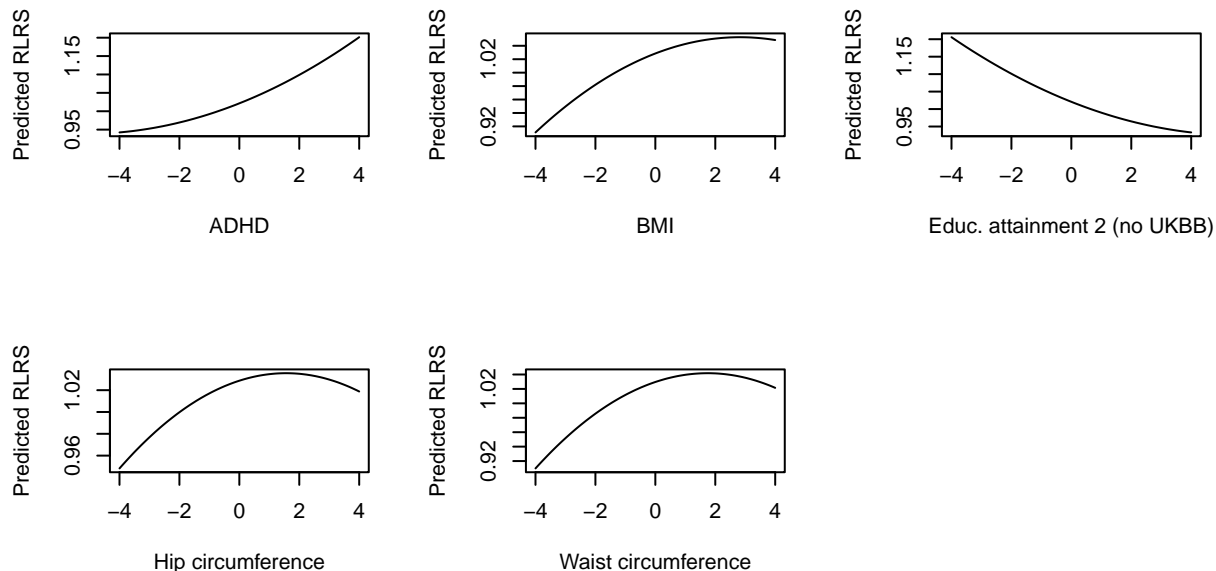
PGS	Weighting			
	Main	Geographical	Age/Qualification	Age/Qual/AFLB
Eating disorder	2.19	1.62	1.69	0.76
Waist-hip ratio	1.89	1.54	1.19	0.96
Coronary Artery Disease	1.79	0.97	1.17	1.09
Height	1.76	1.85	1.31	0.98
Educ. attainment 2 (no UKBB)	1.63	1.51	1.25	1.14
Educ. attainment 3 (no UK)	1.62	1.57	1.24	1.17
Major Depressive Disorder	1.61	1.44	1.24	1.01
Age at smoking initiation	1.59	1.38	1.13	0.97
Waist circumference	1.58	1.52	1.09	1.19
ADHD	1.54	1.14	1.15	1.03
Age at menopause	1.54	1.63	1.17	0.85
Cigarettes per day	1.54	1.73	0.97	0.98
Smoking initiation	1.53	1.30	1.07	0.87
BMI	1.52	1.68	1.01	1.20
Caffeine	1.48	0.86	1.14	1.44
Hip circumference	1.44	1.51	0.98	1.44
Cannabis (ever vs. never)	1.38	1.41	1.02	0.83
Cognitive Ability	1.25	1.21	1.09	1.59
Body Fat	1.23	1.36	1.13	1.16
Extraversion	1.13	0.91	1.08	2.47
Autism	0.81	1.51	0.57	−0.70
Agreeableness	0.45	0.99	0.63	13.30
<i>Mean</i>	1.48	1.39	1.11	1.62
<i>Median</i>	1.54	1.47	1.13	1.06

Only consistently-signed and significant (when unweighted) estimates are shown.  
Age/Qual/AFLB as a proportion of unweighted regressions including females only.

### 7.3 Stabilizing and disruptive selection

Stabilizing selection reduces variance in the trait under selection, while disruptive selection increases variance. To check for these, we rerun equation (1), adding a quadratic term in  $PGS_i$ . Scores for hip circumference show significant stabilizing selection ( $p < 0.05/33$ , negative coefficient on quadratic term). The EA2 score for educational attainment shows significant disruptive selection ( $p < 0.05/33$ , positive coefficient), which reduces the strength of selection against educational attainment at very high levels of the PGS. (The quadratic on the EA3 score has a similar coefficient but is not significant at  $p < 0.05/33$ .) Figure 10 plots predicted number of children against polygenic score from these regressions.

We also checked for stabilizing selection in the parents' generation, using weights multiplied by the inverse of number of siblings. Scores for EA2 and EA3 show significant disruptive selection ( $p < 0.05/33$ , positive coefficient on quadratic). Other scores including hip circumference were not significant.



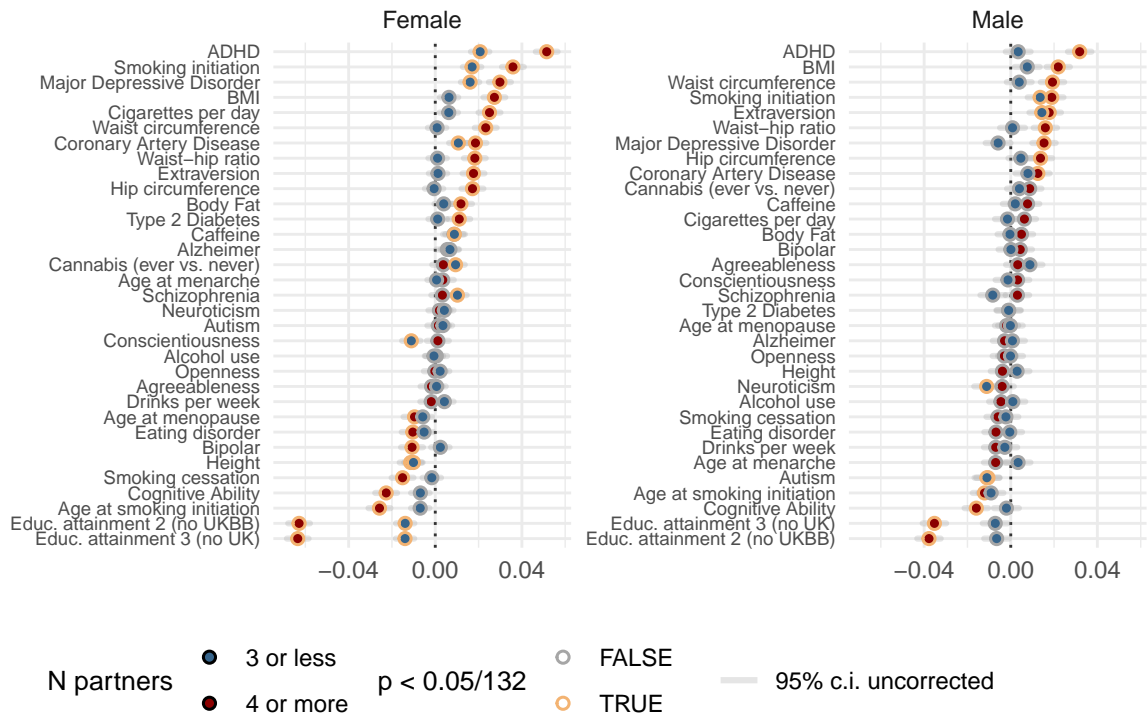
**Figure 10:** Stabilizing/disruptive selection: predicted number of children by polygenic score.

## 7.4 Controlling for age

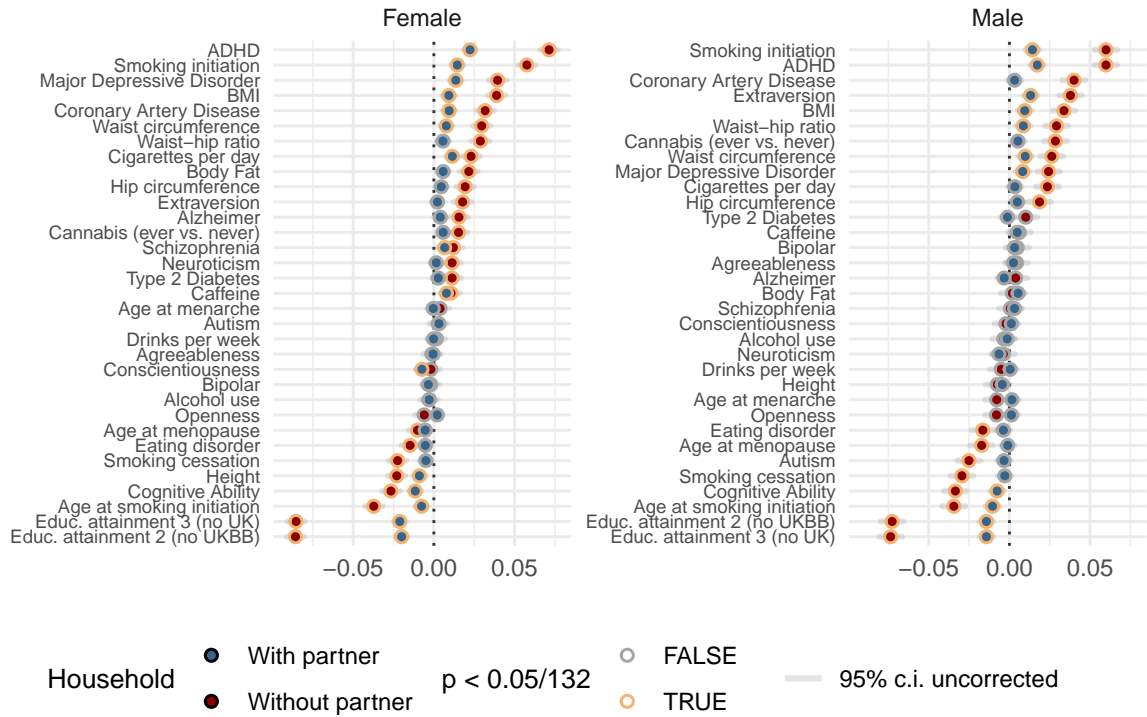
Results in Figure 3 could be explained by age, if older respondents have lower income and are less educated, and also show more natural selection on polygenic scores. However, when we rerun the regressions, interacting the polygenic score with income category and also with a quadratic in age, the interaction with income remains significant at  $p < 0.05/33$  for 17 out of 33 regressions. Similarly if we interact the PGS with age of leaving full time education and a quadratic in age, the interaction with age leaving full time education remains significant at  $p < 0.05/33$  for 12 out of 33 regressions.

## 307 *7.5 Number of partners and presence of partner by sex*

308 Figure 11 splits up Figure 4 by sex. The pattern of results is the same in both sexes: selection effects are stronger among  
309 those with more lifetime sexual partners, and among those not currently living with a partner.



(a) Lifetime number of sexual partners



(b) Presence of a partner

**Figure 11:** Selection effects by number of sexual partners and presence of a partner, for men and women separately.

## 7.6 Parents' generation

### 7.6.1 Selection effects and change over time

The UK Biobank data contains information on respondents' number of siblings (including them), i.e. their parents' number of children. Since respondents' polygenic scores are equal in expectation to the mean scores of their parents, we can use this to look at selection effects in the parents' generation. We estimate equation (1) using parents' RLRS as the dependent variable.<sup>7</sup> The parents' generation has an additional source of ascertainment bias: sampling parents of respondents overweights parents who have many children. For instance, parents of three children will have, on average, three times more children represented in UK Biobank than parents of one child. Parents of no children will by definition not be represented. To compensate, we multiply our weights by the inverse of *number of siblings*.

Figure 12 shows regressions of parents' RLRS on polygenic scores. For a clean comparison with the respondents' generation, we rerun regressions on respondents' RLRS excluding those with no children, and show results in the figure. Selection effects are highly correlated across the two generations, and most share the same sign. Absolute effect size estimates are larger for the parents' generation. We treat this result cautiously, because effect sizes in both generations may depend on polygenic scores' correlation with childlessness, and we cannot estimate this for the parents' generation.

To learn more about this, we compare effect sizes excluding and including childless people in the *current* generation. The correlation between the two sets of effect sizes is 0.95. So, patterns across different scores are broadly similar whether the childless are counted or not. However, absolute effect sizes are smaller when the childless are excluded, for 27 out of 33 scores; the median percentage change is -40.95%.

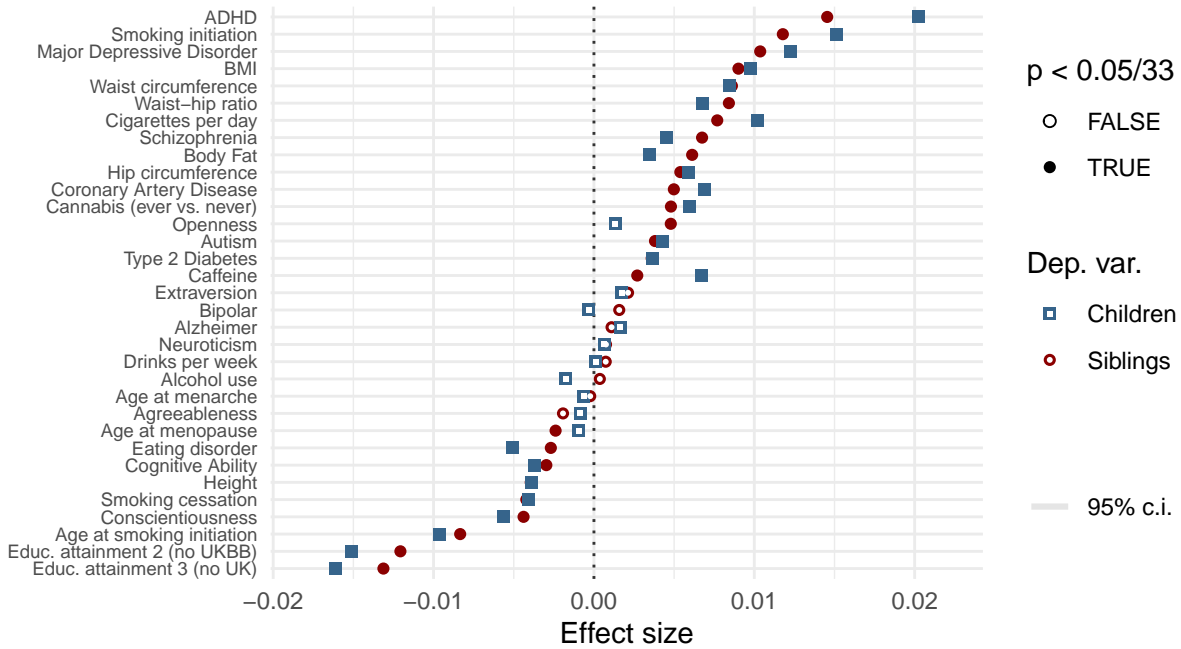
The fact that childless people have such a strong effect on estimates makes it hard to compare total effect sizes across generations. In particular, since the parents' generation has a different distribution of numbers of children, childless people may have had more or less effect in that generation. Another issue is that we are estimating parents' polygenic scores by the scores of their children. This introduces noise into our independent variable, which might lead to errors-in-variables and bias coefficients towards zero.

As an alternative approach, we run regressions interacting polygenic scores with birth year, median split at 1950 ("early born" versus "late born"). We use both respondents' RLRS and parents' RLRS as a dependent variable. We use our standard weights, and further adjust for selection in the parents' generation (see above).

Table 3 summarizes the results. We report the number of scores showing significant changes over time (i.e. a significant

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<sup>7</sup>We don't have data on parents' year of birth for most respondents. To create parents' RLRS, we divide respondents' number of siblings by the average number of siblings of all respondents born in the same year, weighting the average by respondents' inverse of number of siblings to compensate for ascertainment bias.



**Figure 12:** Selection effects, respondents' parents vs. respondents. Parental generation weights multiplied by 1/number of siblings. Respondents' regression excludes childless respondents.

interaction between polygenic score and the “late born” dummy): either a significant change in sign, a significant increase in size, or a significant decrease in size. There is little evidence for changes in selection effects within the parents' generation, with just one score showing a significant decrease in size. In the respondents' generation, effect sizes were significantly larger in absolute size among the later-born for eight polygenic scores: ADHD, age at menopause, cognitive ability, Coronary Artery Disease, EA2, EA3, extraversion and Major Depressive Disorder. These changes are inconsistent with the intergenerational change, where estimated effect sizes were larger among the earlier, parents' generation.

Overall, there is some evidence for an increase in the strength of selection in recent history. The clearest result is that the pattern of relative effect sizes across scores is broadly consistent over time.

**Table 3:** Numbers of polygenic scores showing changes in selection effects between early and late born. Parental generation weights multiplied by 1/number of siblings.

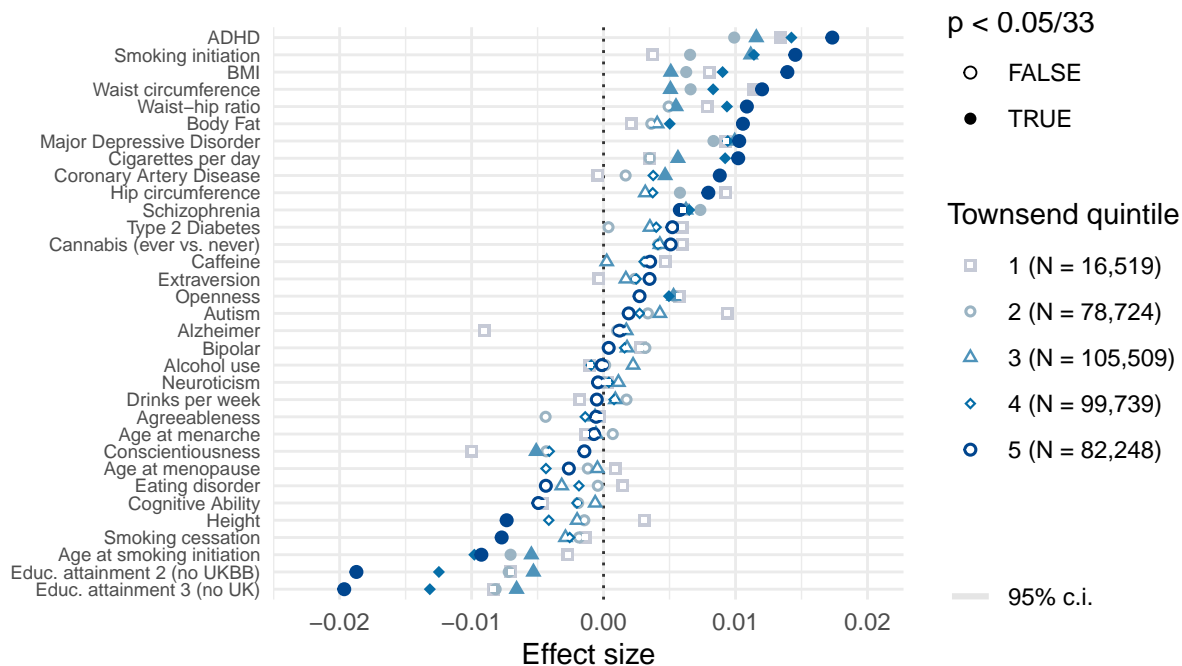
Change	Parents' RLRS	Respondents' RLRS
Insignificant	32	25
Size decreasing	1	
Size increasing		8

Significance is measured at  $p < 0.05/66$ .



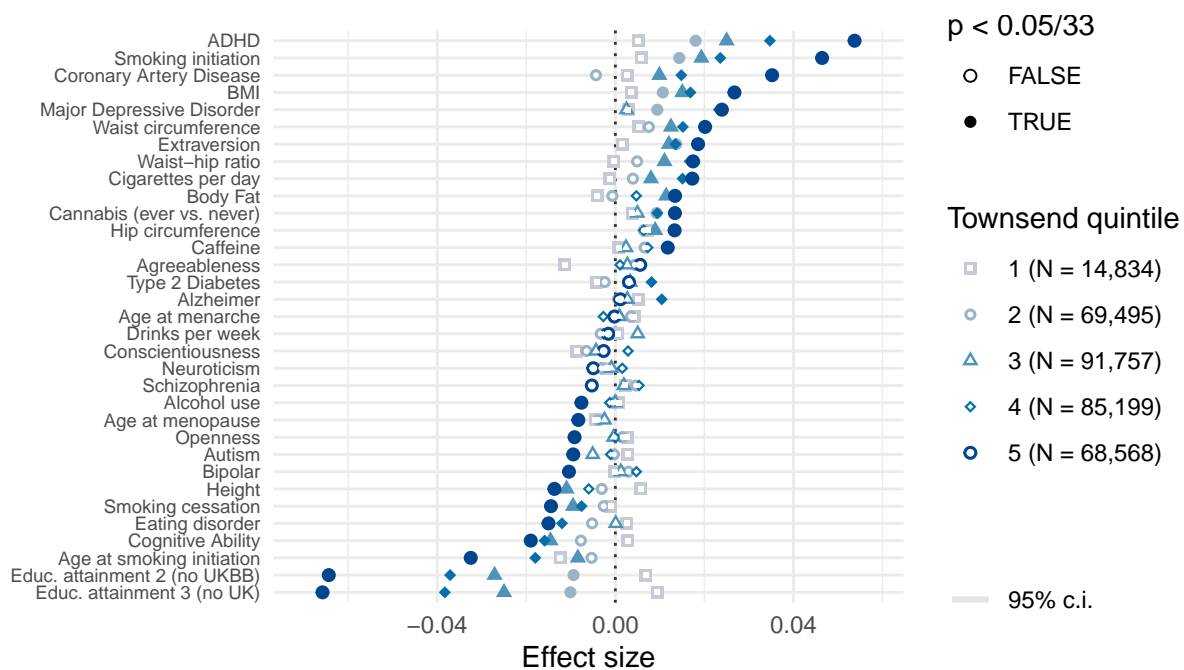
## 347 7.6.2 Area deprivation

348 Figure 13 plots effects on parents' RLRS by Townsend deprivation quintile of birth area.



**Figure 13:** Selection effects (parents' RLRS) by Townsend deprivation quintile of birth area. Higher = more deprived. Weights multiplied by 1/number of siblings.

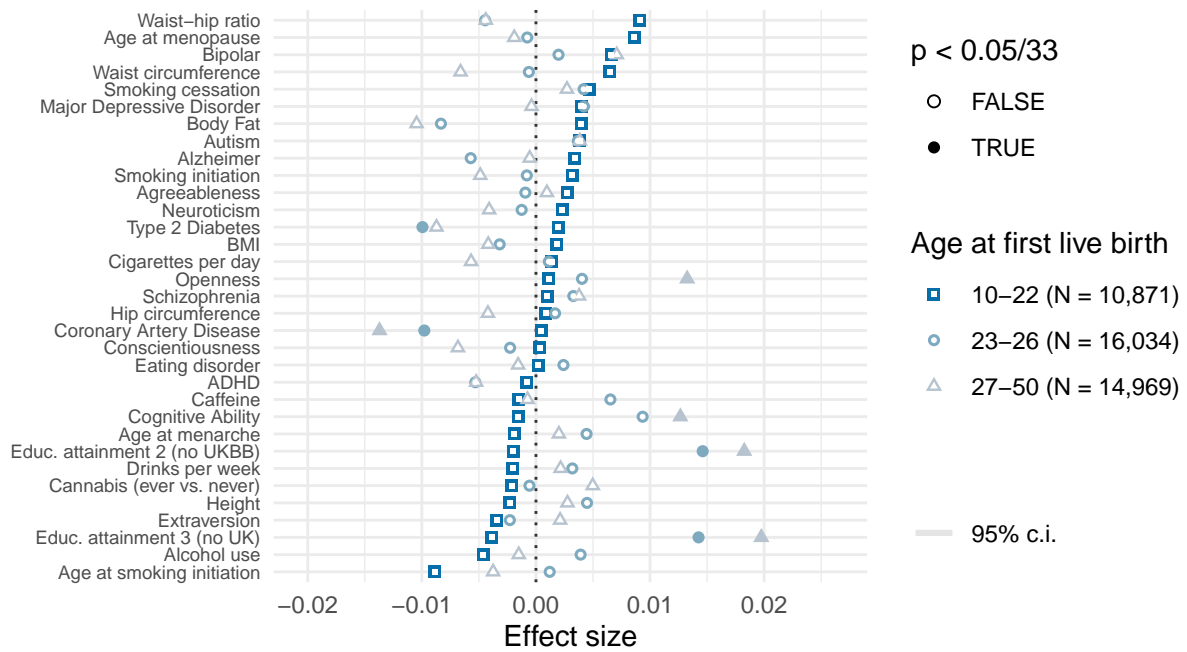
349 For comparison, Figure 14 plots effects on respondents' RLRS by Townsend deprivation quintile of birth area.



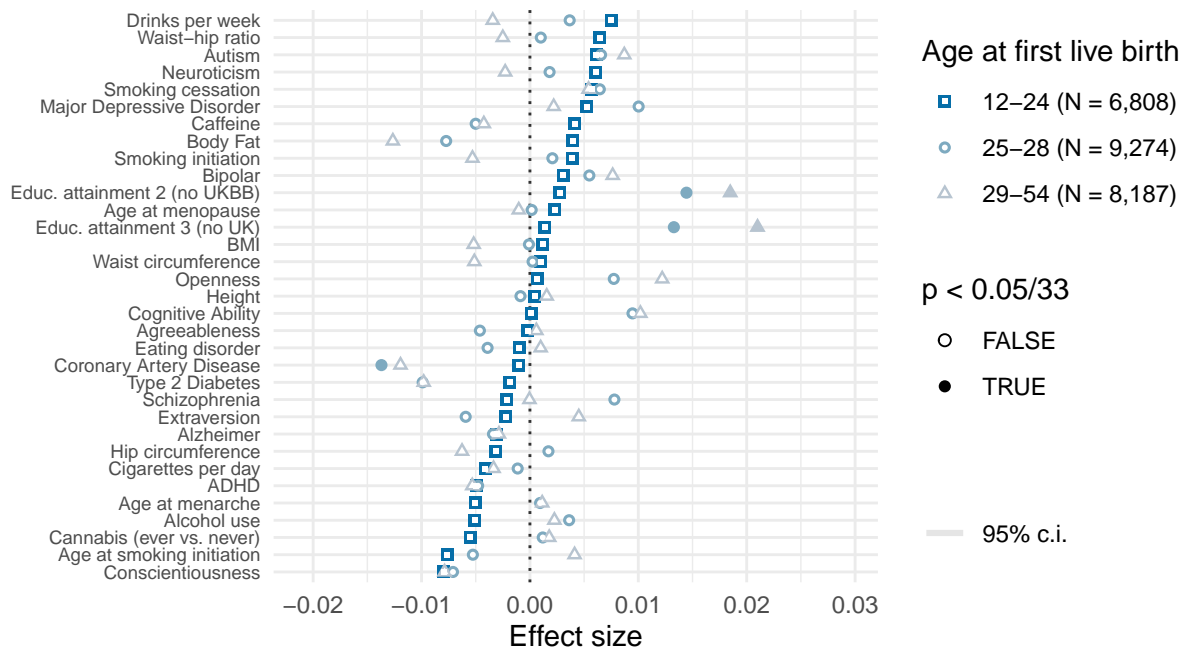
**Figure 14:** Selection effects in the respondents' generation by Townsend deprivation quintile of birth area. Higher = more deprived.

### 7.6.3 Age at first live birth

Among the parents' generation, we can control for age at first live birth using the subsets of respondents who reported their mother's or father's age, and who had no elder siblings. We run regressions on parents' RLRS on these subsets. Figure 15 shows selection effects by terciles of age at first live birth, for mothers and fathers. As in the respondents' generation, effect sizes are smaller, or even oppositely signed, for older parents. Importantly, this holds for both sexes. Figure 16 shows the regressions controlling for either parent's age at their birth. Effect sizes are very similar, whether controlling for father's or mother's age. As in the respondents' generation, effect sizes are negatively correlated with the effect sizes from bivariate regressions without the age at birth control (father's age at birth:  $\rho -0.43$ ; mother's age at birth:  $\rho -0.59$ ).

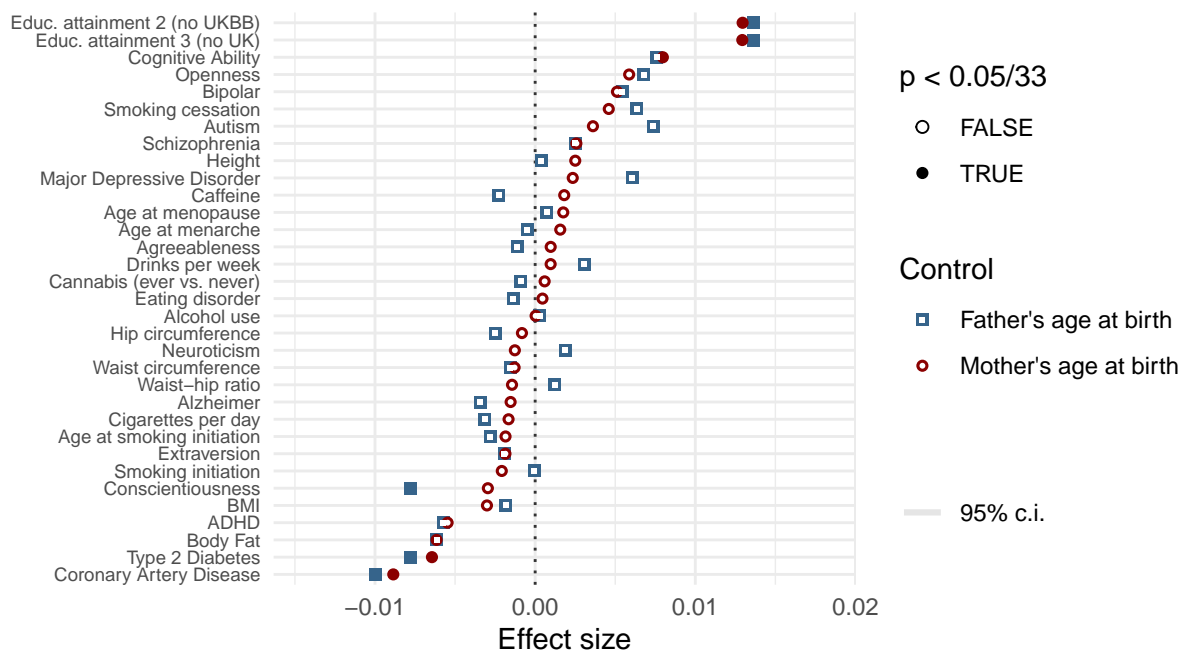


(a) Mothers



(b) Fathers

**Figure 15:** Selection effects (parents' RLRs) by age at first live birth terciles. Weights multiplied by 1/number of siblings.



**Figure 16:** Selection effects (parents' generation) among eldest siblings, controlling for parents' age at birth. Weights multiplied by 1/number of siblings.

## 7.7 Effects of polygenic scores on age at first live birth

Our results suggest that polygenic scores may directly correlate with age at first live birth. Figure 17 plots estimated effect sizes from bivariate regressions for respondents. Figure 18 does the same for their parents, using only eldest siblings.<sup>8</sup> Effect sizes are reasonably large. They are also highly correlated across generations. Effect sizes of polygenic scores on father's age at own birth, and on own age at first live birth, have a correlation of 0.99; for mother's age and own age it is 0.99.

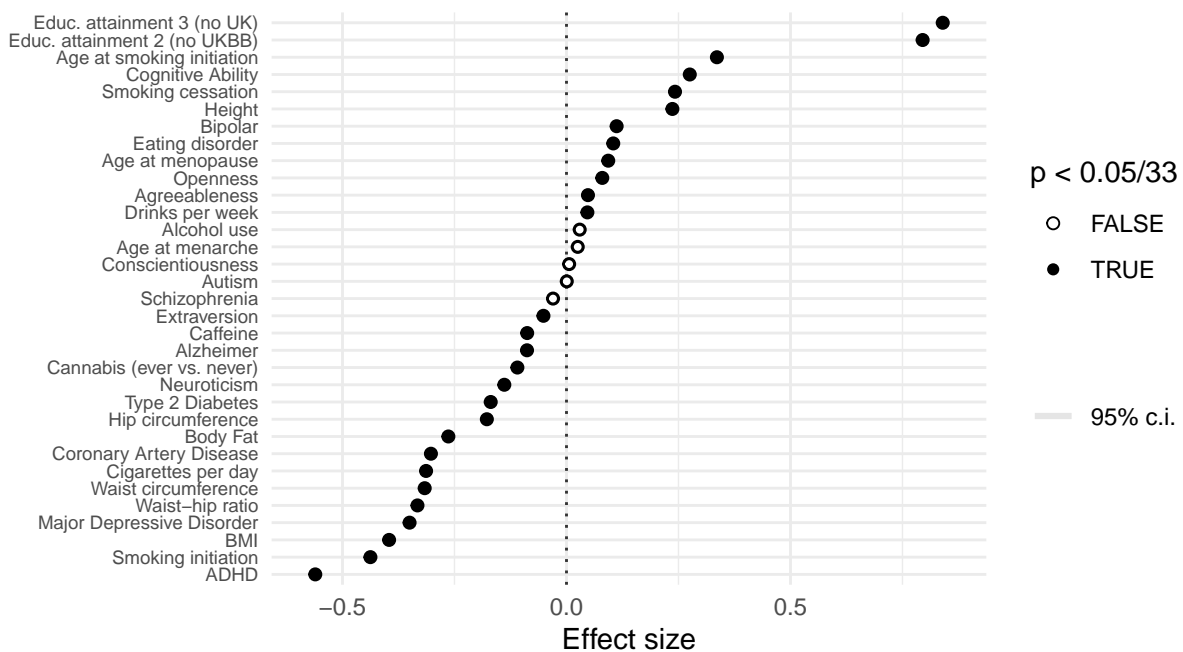
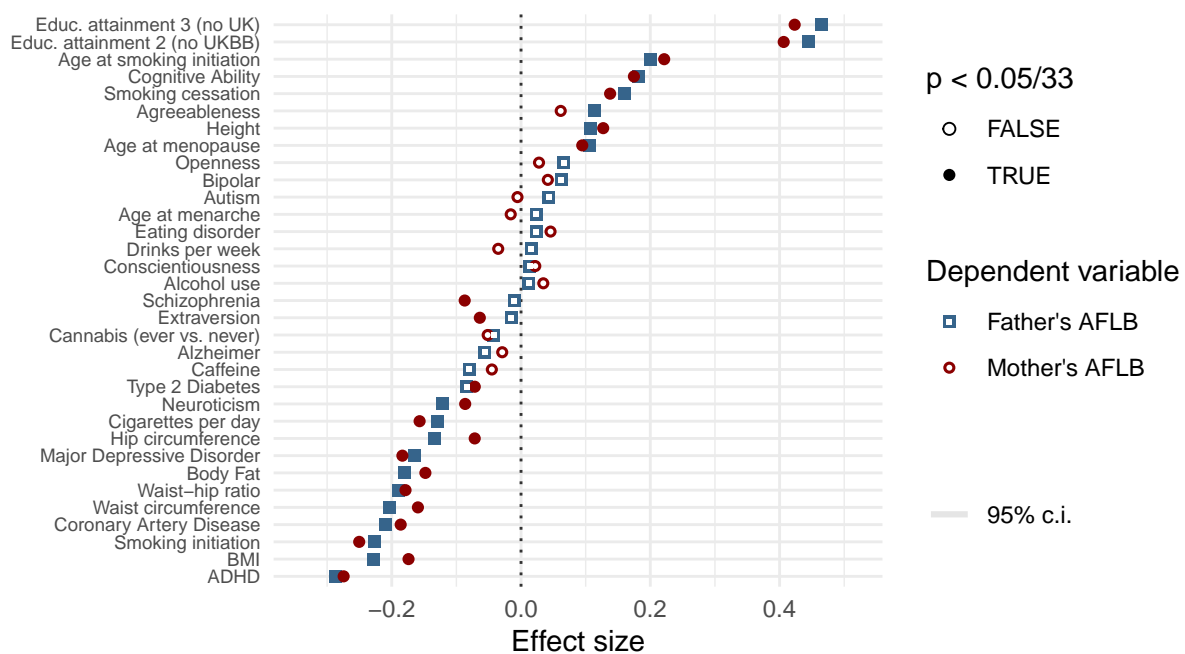


Figure 17: Effects of polygenic scores on age at first live birth.

<sup>8</sup>Parental AFLB can only be calculated for this group.



**Figure 18:** Effects of polygenic scores on parents' age at respondent's birth, eldest siblings. Weights multiplied by 1/number of siblings.

## 7.8 Mediation analysis

We run a standard mediation analysis in the framework of Baron and Kenny (1986). For each polygenic score where the bivariate correlation with RLRS is significant at  $p < 0.05/33$ , we estimate

$$RLRS_i = \alpha + \beta PGS_i + \gamma EA_i + X_i\mu + \varepsilon_i \quad (3)$$

$$EA_i = \delta + \zeta PGS_i + X_i\mu + \eta_i \quad (4)$$

where  $RLRS_i$  is relative lifetime reproductive success,  $PGS_i$  is the polygenic score,  $EA_i$  is educational attainment (age of leaving fulltime education), and  $X_i$  is a vector of controls. The total effect of  $PGS$  on number of children is  $\beta + \gamma\zeta$ . The “indirect effect” mediated by  $EA$  is  $\gamma\zeta$ . The standard error of the indirect effect can be calculated as

$$\sqrt{\hat{\gamma}^2 \hat{\sigma}_\zeta^2 + \hat{\zeta}^2 \hat{\sigma}_\gamma^2}$$

where  $\hat{\sigma}_\zeta$  is the standard error of  $\hat{\zeta}$ , etc.

We are not concerned about endogeneity of polygenic scores, since our theory requires only that these correlate with human capital. However, endogeneity of educational attainment is a concern, i.e., educational attainment might correlate with unobserved characteristics that affect one’s fertility (and which are not related to human capital). To partially address this, we include controls for age, sex, fluid IQ, height and risk attitude in  $X$ . Note that controlling for fluid IQ is conservative, in the sense that IQ might also measure human capital; nevertheless, we control for it because fluid IQ might affect fertility decisions via other channels than human capital.

Table 4 shows results. For 18 out of 23 scores, the indirect effect on fertility via human capital is significantly different from 0 at  $p = 0.05/33$  and has the same sign as the total effect. We also calculate the proportion of the total effect that is mediated via the indirect effect, along with uncorrected 95% confidence intervals (100 bootstraps).



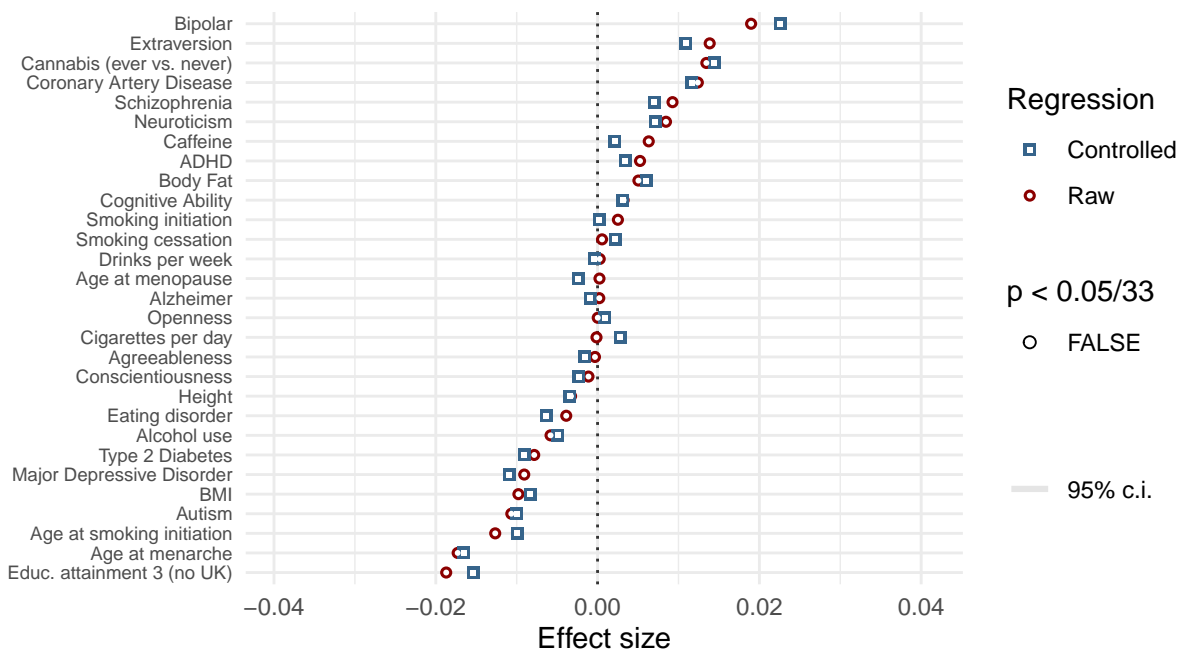
**Table 4:** *Mediation analysis*

<b>PGS</b>	<b>Total effect</b>	<b>Indirect effect</b>	<b>Proportion (%)</b>	<b>Proportion 95% c.i. (%)</b>
ADHD	0.0232	0.0035 *	15.0	[11.1, 19.7]
Smoking initiation	0.0205	0.0032 *	15.6	[11.9, 22.0]
BMI	0.0163	0.0022 *	13.4	[9.7, 21.7]
Waist circumference	0.0140	0.0027 *	19.6	[12.9, 32.0]
Major Depressive Disorder	0.0137	0.0012 *	8.7	[5.2, 16.3]
Hip circumference	0.0127	0.0022 *	17.3	[11.9, 33.3]
Extraversion	0.0110	0.0001	0.8	[−3.6, 5.0]
Waist-hip ratio	0.0089	0.0022 *	24.4	[14.6, 59.4]
Coronary Artery Disease	0.0088	0.0020 *	22.3	[13.0, 59.1]
Cigarettes per day	0.0079	0.0021 *	27.2	[12.9, 79.0]
Body Fat	0.0058	0.0019 *	32.1	[15.5, 225.0]
Caffeine	0.0054	0.0001	2.5	[−52.2, 13.6]
Cannabis (ever vs. never)	0.0042	0.0004	8.8	[−101.0, 146.0]
Alzheimer	0.0038	0.0004	9.4	[−164.6, 109.4]
Autism	−0.0040	−0.0008 *	20.9	[−50.2, 81.2]
Age at menopause	−0.0044	−0.0009 *	20.7	[−91.5, 569.4]
Height	−0.0047	0.0014 *	−29.1	[−626.0, 459.7]
Eating disorder	−0.0076	−0.0015 *	19.9	[10.7, 59.1]
Smoking cessation	−0.0076	−0.0018 *	23.5	[14.6, 75.2]
Cognitive Ability	−0.0102	−0.0025 *	24.1	[14.6, 46.7]
Age at smoking initiation	−0.0138	−0.0024 *	17.6	[11.6, 29.2]
Educ. attainment 3 (no UK)	−0.0257	−0.0075 *	29.2	[23.2, 36.6]
Educ. attainment 2 (no UKBB)	−0.0260	−0.0074 *	28.4	[22.3, 35.1]

\*  $p < 0.05/33$ .

## 7.9 Within-siblings regressions

Results in the main text support our theory that natural selection on polygenic scores is driven by their *correlation* with human capital. Here, we test whether polygenic scores *cause* fertility by running within-siblings regressions (Figure 19). With a reduced sample size, all within-sibling effects are insignificant after Bonferroni correction. However, effect sizes are positively correlated with effect sizes from the pooled model, and about 50% smaller (regressing within-sibling on pooled effect sizes,  $b = 0.292$ ). This attenuation is in line with the  $\sim 50\%$  decrease in heritability in within-sibling GWASs on age at first birth and educational attainment (Howe et al. 2021). We see these results as providing tentative evidence that polygenic scores cause fertility, with effects being partly driven by correlations with environmental variation in human capital. We also reran within-siblings regressions adding a control for education. Most effect sizes barely change, suggesting that our measure of education does not in general mediate differences in fertility among siblings.



**Figure 19:** Selection effects controlling for sibling-group fixed effects, with and without a control for education (left education before 16, 16-18, or after 18). Each set of 29 results is from a single regression of RLRS on 29 polygenic scores. Standard errors clustered by sibling group.

We run a single regression on 29 polygenic scores within 17161 sibling groups ( $N = 31169$ ). Thus, we control both for environmental confounds (since scores are randomly allocated within sib-groups by meiosis), and for genetic confounds captured by our polygenic scores. We remove four scores which correlate highly with other scores (educational attainment 2, hip circumference, waist circumference and waist-hip ratio). Figure 19 shows the results.

## 7.10 Effects on inequality

Table 5 shows correlations between children’s polygenic scores and household income (UKB data field 738). Column “With selection” uses respondents’ scores, multiplying weights by number of children. Column “Without selection” uses our standard weights, i.e. it estimates the counterfactual correlation if all respondents had the same number of children.

**Table 5:** *Correlations of polygenic scores with income group.*

PGS	Cor. with selection	Cor. without selection	Ratio
Educ. attainment 3 (no UK)	0.163	0.141	1.15
Educ. attainment 2 (no UKBB)	0.155	0.135	1.15
Cognitive Ability	0.058	0.053	1.08
Age at smoking initiation	0.049	0.039	1.26
Smoking cessation	0.047	0.042	1.13
Height	0.043	0.039	1.09
Eating disorder	0.020	0.018	1.10
Agreeableness	0.018	0.017	1.02
Openness	0.016	0.014	1.19
Extraversion	0.014	0.016	0.92
Age at menopause	0.014	0.012	1.18
Bipolar	0.014	0.012	1.17
Drinks per week	0.009	0.009	1.08
Alcohol use	0.005	0.006	0.83
Age at menarche	0.004	0.002	1.82
Conscientiousness	0.003	0.001	3.63
Autism	−0.009	−0.009	1.00
Caffeine	−0.011	−0.011	1.00
Alzheimer	−0.012	−0.011	1.06
Cannabis (ever vs. never)	−0.015	−0.008	1.72
Schizophrenia	−0.027	−0.029	0.94
Type 2 Diabetes	−0.030	−0.025	1.24
Neuroticism	−0.031	−0.031	1.02
Hip circumference	−0.033	−0.027	1.24
Body Fat	−0.050	−0.043	1.15
Cigarettes per day	−0.052	−0.043	1.22
Coronary Artery Disease	−0.053	−0.039	1.33
Waist circumference	−0.057	−0.048	1.18
Waist-hip ratio	−0.060	−0.051	1.17
Major Depressive Disorder	−0.063	−0.054	1.16
BMI	−0.065	−0.052	1.24
Smoking initiation	−0.074	−0.059	1.25
ADHD	−0.095	−0.077	1.24

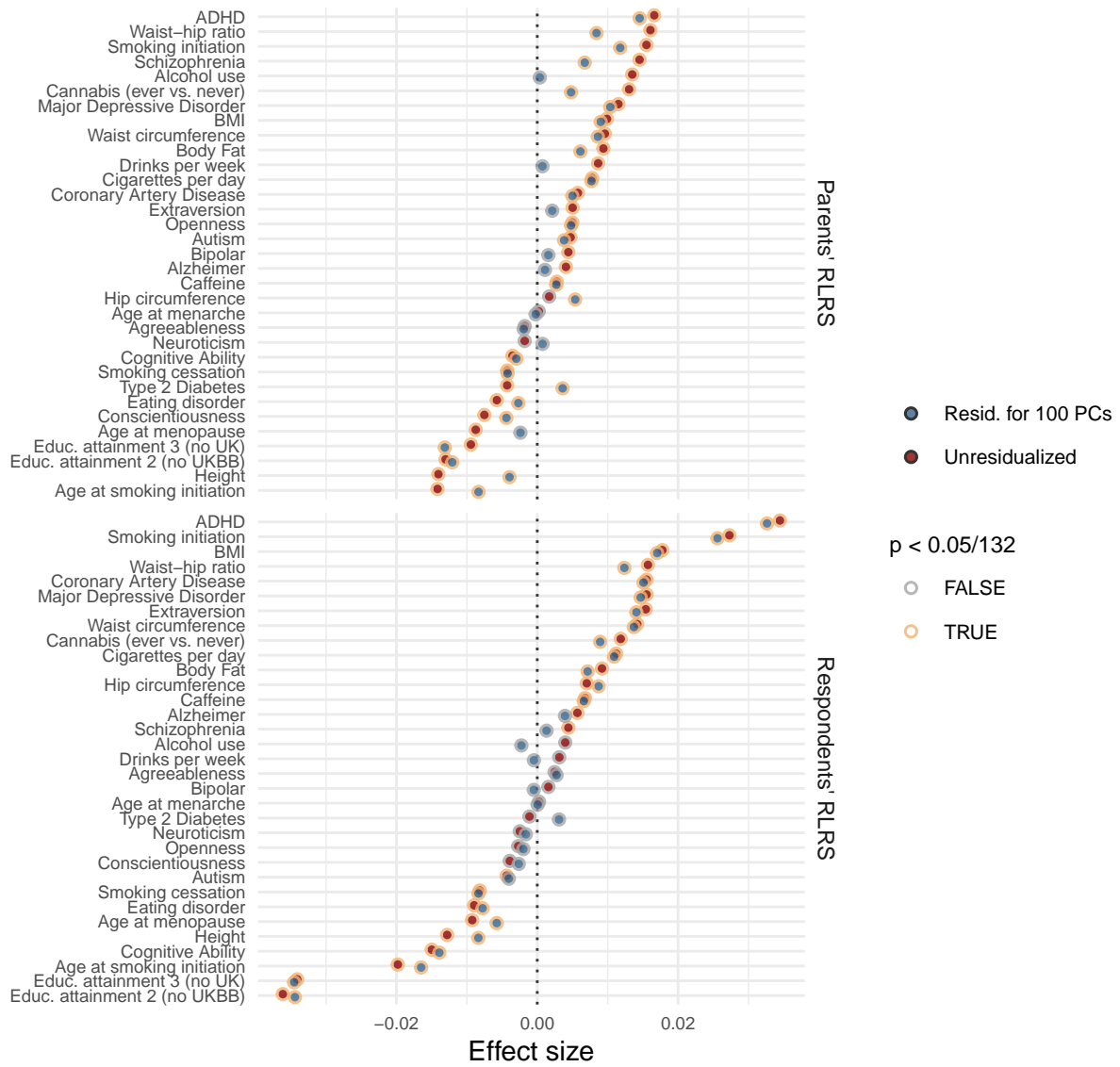
## 7.11 Further results

### 7.11.1 Selection effects on raw polygenic scores

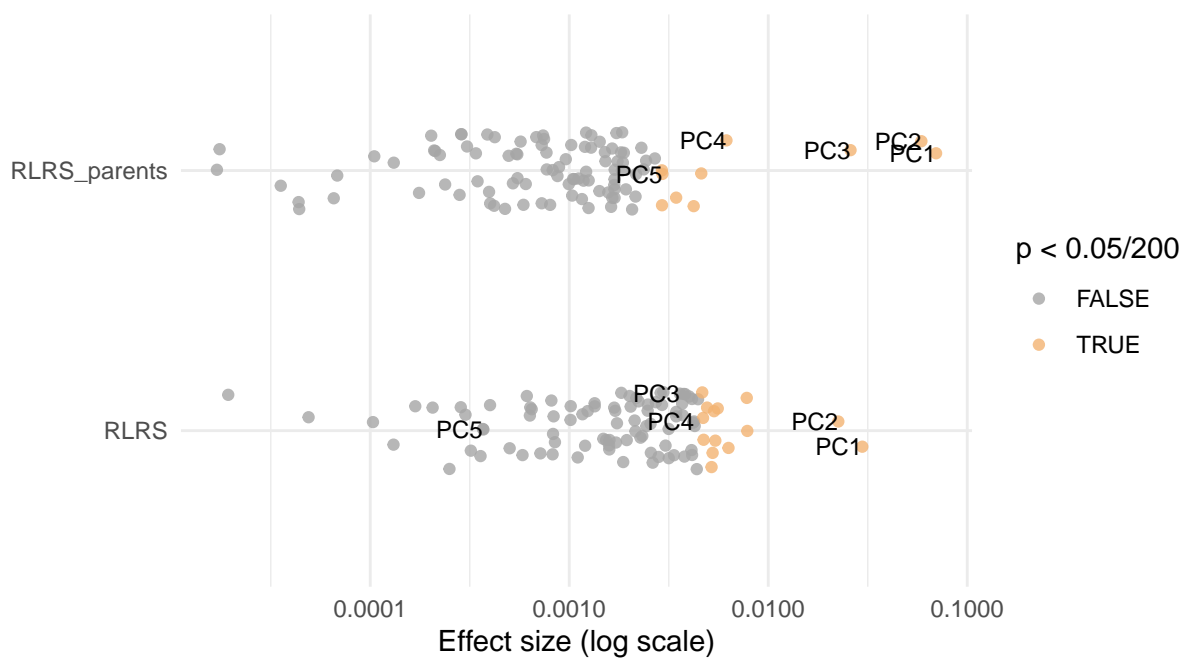
Figure 20 compares selection effects on polygenic scores residualized for the top 100 principal components of the genetic data, to selection effects on raw, unresidualized polygenic scores. In siblings regressions, effect sizes are larger for raw scores – sometimes much larger, as in the case of height. 29 out of 33 “raw” effect sizes have a larger absolute value than the corresponding “residualized” effect size. The median proportion between raw and controlled effect sizes is 0.8. Among the children regressions, this no longer holds. Effect sizes are barely affected by controlling for principal components.

Overall, 72.73 per cent of effect sizes are consistently signed across all four regressions (on children and siblings, and with and without residualization).

To get a further insight into this we regress respondents’ and parents’ RLRs on individual principal components. Figure 21 shows the results. Labels show the top principal components. These have larger effect sizes in siblings regressions. One possibility is that the parents’ generation was less geographically mobile, and so geographic patterns of childrearing were more correlated with principal components, which partly capture the location of people’s ancestors.

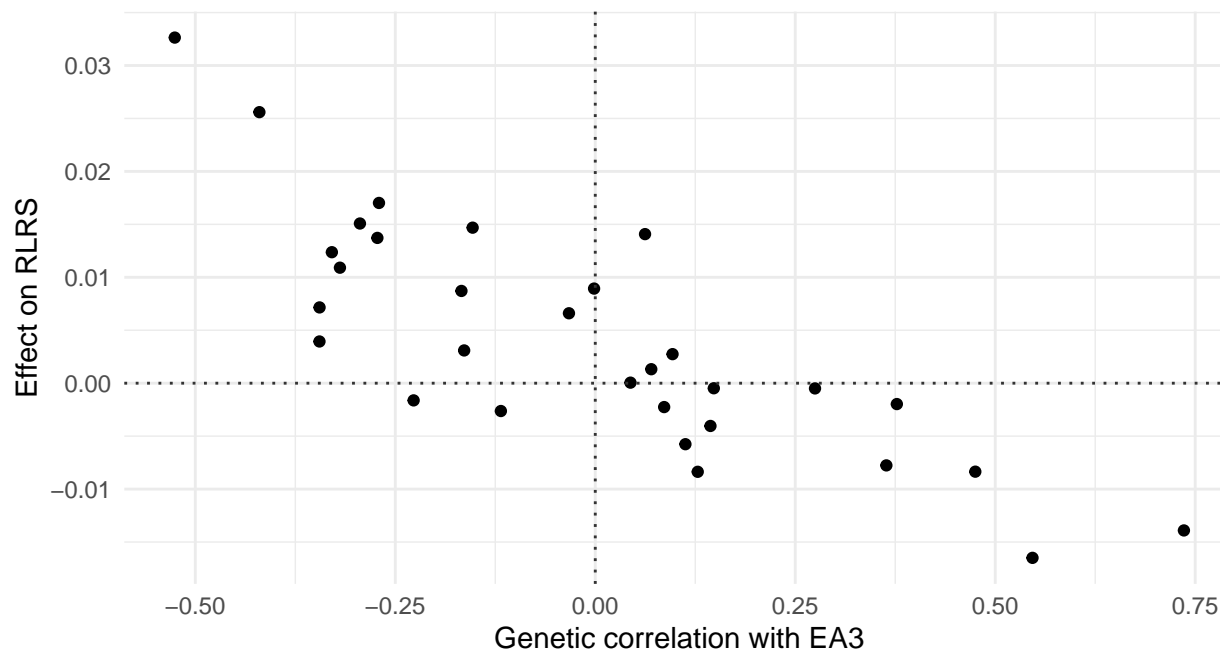


**Figure 20:** Selection effects using unresidualized polygenic scores. Parental generation weights multiplied by 1/number of siblings.



**Figure 21:** Selection effects of 100 principal components of genetic data. Each dot represents one bivariate regression. Sibling estimates weighted by  $1/\text{number of siblings}$ . Absolute effect sizes are plotted. Points are jittered on the  $Y$  axis. Top principal components are labelled.

## 412 7.11.2 Genetic correlations with EA3



**Figure 22:** Selection effects plotted against genetic correlation with EA3.

413 Another way to examine the “earnings” theory of natural selection is to compare selection effects of polygenic scores  
 414 with their genetic correlation with educational attainment (EA3). Since EA3 strongly predicts earnings, if earnings  
 415 drives differences in fertility, we’d expect a correlation between the two sets of results. Figure 22 shows this is so: the  
 416 correlation, after excluding EA2, is  $-0.82$ . Genetic correlations were calculated using LD score regression from GWAS  
 417 summary statistics.

## 418 7.12 Model proofs

### 419 Solution for the one-period model

420 Differentiating and setting  $\frac{dU}{dN} = 0$  gives the first order condition for an optimal choice of children  $N^* > 0$ :

$$\frac{bW}{(W(1 - bN^*))^\sigma} \geq a, \text{ with equality if } N^* > 0.$$

421 Rearranging gives

$$N^* = \max \left\{ \frac{1}{b} \left( 1 - \left( \frac{b}{a} \right)^{1/\sigma} W^{(1-\sigma)/\sigma} \right), 0 \right\}. \quad (5)$$

422 Note that when  $\sigma < 1$ , for high enough  $W$ ,  $N^* = 0$ . Differentiating gives the effect of wages on fertility for  $N^* > 0$ .

423 This is also the fertility-human capital relationship:

$$\frac{dN^*}{dW} = \frac{dN^*}{dW} = -\frac{1}{b} \left( \frac{b}{a} \right)^{1/\sigma} \frac{1-\sigma}{\sigma} W^{(1-2\sigma)/\sigma}. \quad (6)$$

424 This is negative if  $\sigma < 1$ . Also,

$$\frac{d^2 N^*}{dW^2} = -\frac{1}{b} \left( \frac{b}{a} \right)^{1/\sigma} \frac{1-\sigma}{\sigma} \frac{1-2\sigma}{\sigma} W^{(1-3\sigma)/\sigma}$$

425 For  $0.5 < \sigma < 1$ , this is positive, so the effect of fertility on wages shrinks towards zero as wages increase (and becomes

426 0 when  $N^* = 0$ ). Next, we consider the time cost of children  $b$ :

$$\frac{d^2 N^*}{dWdb} = -\left( \frac{1}{a} \right)^{1/\sigma} \left( \frac{1-\sigma}{\sigma} \right)^2 (Wb)^{(1-2\sigma)/\sigma} < 0.$$

427 Lastly we consider the effect of  $a$ . From (5),  $N^*$  is increasing in  $a$ . Differentiating (6) by  $a$  gives

$$\frac{d^2 N^*}{da dW} = b^{1/\sigma-1} \frac{1-\sigma}{\sigma^2} W^{(1-2\sigma)/\sigma} a^{-1/\sigma-1}$$

428 which is positive for  $\sigma < 1$ .



## Solution for the two-period model

Period 1 and period 2 income are:

$$Y_1 = 1 - s - bN_1 \quad (7)$$

$$Y_2 = w(s, h)(1 - bN_2) \quad (8)$$

Write the Lagrangian of utility  $U$  (2) as

$$\mathcal{L}(N_1, N_2, s) = u(Y_1) + u(Y_2) + a(N_1 + N_2) + \lambda_1 N_1 + \lambda_2 N_2 + \lambda_3 \left(\frac{1}{b} - N_2\right) + \mu s$$

Lemma 5 below shows that if  $\sigma > 0.5$ , this problem is globally concave, guaranteeing that the first order conditions identify a unique solution. We assume  $\sigma > 0.5$  from here on.

Plugging (7) and (8) into the above, we can derive the Karush-Kuhn-Tucker conditions for an optimum  $(N_1^*, N_2^*, s^*)$  as:

$$\frac{d\mathcal{L}}{dN_1} = -bY_1^{-\sigma} + a + \lambda_1 = 0, \text{ with } \lambda_1 = 0 \text{ if } N_1^* > 0; \quad (9)$$

$$\frac{d\mathcal{L}}{dN_2} = -bs^*hY_2^{-\sigma} + a + \lambda_2 - \lambda_3 = 0, \text{ with } \lambda_2 = 0 \text{ if } N_2^* > 0, \lambda_3 = 0 \text{ if } N_2^* < \frac{1}{b}; \quad (10)$$

$$\frac{d\mathcal{L}}{ds} = -Y_1^{-\sigma} + h(1 - bN_2^*)Y_2^{-\sigma} + \mu = 0; \quad (11)$$

$$N_1^*, N_2^*, s^*, \lambda_1, \lambda_2, \lambda_3, \mu \geq 0; N_2^* \leq \frac{1}{b}. \quad (12)$$

Note that the Inada condition (that marginal utility of income grows without bound as income approaches zero,  $\lim_{x \rightarrow 0} u'(x) = \infty$ ) for period 1 rules out  $s^* = 1$  and  $N_1 = 1/b$ , so we need not impose these constraints explicitly. Also, so long as  $N_2^* < 1/b$ , the same condition rules out  $s^* = 0$ . We consider four cases, of which only three can occur.

436 **Case 1:**  $N_1^* > 0, N_2^* > 0$

Rearranging (9), (10) and (11) gives:

$$N_1^* = \frac{1}{b} \left( 1 - s^* - \left( \frac{b}{a} \right)^{1/\sigma} \right); \quad (13)$$

$$N_2^* = \frac{1}{b} \left( 1 - \left( \frac{b}{a} \right)^{1/\sigma} (s^* h)^{(1-\sigma)/\sigma} \right); \quad (14)$$

$$s^* = \frac{1 - bN_1^*}{1 + ((1 - bN_2^*)h)^{1-1/\sigma}}. \quad (15)$$

437 Plugging the expressions for  $N_1^*$  and  $N_2^*$  into  $s^*$  gives

$$s^* = \frac{s^* + \left( \frac{b}{a} \right)^{1/\sigma}}{1 + \left( \left( \frac{b}{a} \right)^{1/\sigma} s^{*(1-\sigma)/\sigma} h^{1/\sigma} \right)^{1-1/\sigma}}$$

438 which simplifies to

$$s^* = \left( \frac{b}{a} \right)^{1/(2\sigma-1)} h^{(1-\sigma)/(2\sigma-1)}. \quad (16)$$

Plugging the above into (13) and (14) gives:

$$N_1^* = \frac{1}{b} \left( 1 - \left( \frac{b}{a} \right)^{1/(2\sigma-1)} h^{(1-\sigma)/(2\sigma-1)} - \left( \frac{b}{a} \right)^{1/\sigma} \right);$$

$$N_2^* = \frac{1}{b} \left( 1 - \left( \frac{b}{a} \right)^{1/(2\sigma-1)} h^{(1-\sigma)/(2\sigma-1)} \right).$$

439 Note that that  $N_1^* < N_2^*$ . For these both to be positive requires low values of  $h$  if  $\sigma < 1$  and high values of  $h$  if  $\sigma > 1$ .

440 Also:

$$w(s^*, h) \equiv s^* h = \left( \frac{b}{a} \right)^{1/(2\sigma-1)} h^{\sigma/(2\sigma-1)}.$$

441 Observe that  $w(s^*, h)$  is increasing in  $h$  for  $\sigma > 0.5$ , and convex iff  $0.5 < \sigma < 1$ .

442 While  $N_1^*$  and  $N_2^*$  are positive, they have the same derivative with respect to  $h$ :

$$\frac{dN_t^*}{dh} = -\frac{1}{b} \left( \frac{b}{a} \right)^{1/(2\sigma-1)} \frac{1-\sigma}{2\sigma-1} h^{(1-\sigma)/(2\sigma-1)-1} \quad (17)$$

443 Examining this and expression (16) gives:

444 **Lemma 1.** For  $\sigma < 1$ , case 1 holds for  $h$  low enough, and in case 1,  $N_1^*$  and  $N_2^*$  decrease in  $h$ , while  $s^*$  increases in  $h$ .

445 For  $\sigma > 1$ , case 1 holds for  $h$  high enough, and in case 1  $N_1^*$  and  $N_2^*$  increase in  $h$ , while  $s^*$  decreases in  $h$ .

446  $N_t^*$  is convex in  $h$  for  $\sigma > 2/3$ , and concave otherwise.  $s^*$  is convex in  $h$  if  $\sigma < 2/3$ , and concave otherwise.

447 **Case 2:**  $N_1^* = 0, N_2^* > 0$

448 Replace  $N_1^* = 0$  into the first order condition for  $s^*$  from (11), and rearrange to give:

$$s^* = \frac{1}{1 + ((1 - bN_2)h)^{1-1/\sigma}}.$$

449 Now since  $N_2^* > 0$ , we can rearrange (10) to give

$$N_2^* = \frac{1}{b} \left( 1 - \left( \frac{b}{a} \right)^{1/\sigma} (s^*h)^{(1-\sigma)/\sigma} \right). \quad (18)$$

Plugging this into  $s^*$  gives

$$s^* = \frac{1}{1 + \left( \frac{bh}{a} \right)^{(\sigma-1)/\sigma^2} (s^*)^{-(1-\sigma)^2/\sigma^2}}$$

450 which can be rearranged to

$$(1 - s^*)(s^*)^{(1-2\sigma)/\sigma^2} = \left( \frac{a}{bh} \right)^{(1-\sigma)/\sigma^2}. \quad (19)$$

Differentiate the left hand side of the above to get

$$\begin{aligned} & \frac{1-2\sigma}{\sigma^2} (1 - s^*)(s^*)^{(1-2\sigma)/\sigma^2-1} - (s^*)^{(1-2\sigma)/\sigma^2} \\ &= \frac{1-2\sigma}{\sigma^2} (s^*)^{(1-2\sigma)/\sigma^2-1} - \frac{\sigma^2 + 1 - 2\sigma}{\sigma^2} (s^*)^{(1-2\sigma)/\sigma^2} \\ &= \frac{1-2\sigma}{\sigma^2} (s^*)^{(1-2\sigma)/\sigma^2-1} - \frac{(1-\sigma)^2}{\sigma^2} (s^*)^{(1-2\sigma)/\sigma^2}. \end{aligned} \quad (20)$$

This is negative if and only if

$$s^* > \frac{1-2\sigma}{(1-\sigma)^2}$$

451 which is always true since  $\sigma > 0.5$ . Note also that since  $\sigma > 0.5$ , then the left hand side of (19) approaches infinity as  
452  $s^* \rightarrow 0$  and approaches 0 as  $s^* \rightarrow 1$ . Thus, (19) implicitly defines the unique solution for  $s^*$ .

453 To find how  $s^*$  changes with  $h$ , note that the right hand side of the above decreases in  $h$  for  $\sigma < 1$ , and increases in  $h$  for  
454  $\sigma > 1$ . Putting these facts together: for  $\sigma < 1$ , when  $h$  increases the RHS of (19) decreases, hence the LHS decreases

455 and  $s^*$  increases, i.e.  $s^*$  is increasing in  $h$ . For  $\sigma > 1$ ,  $s^*$  is decreasing in  $h$ .

456 To find how  $N_2^*$  changes with  $h$ , we differentiate (18):

$$\frac{dN_2^*}{dh} = -\frac{1}{b} \left(\frac{b}{a}\right)^{1/\sigma} \frac{1-\sigma}{\sigma} (s^*h)^{(1-2\sigma)/\sigma} \left(s^* + h \frac{ds^*}{dh}\right) \quad (21)$$

457 which is negative for  $\sigma < 1$ , since  $\frac{ds^*}{dh} > 0$  in this case.

458 Differentiating again:

$$\begin{aligned} \frac{d^2N_2}{dh^2} &= -X \left[ \frac{1-2\sigma}{\sigma} (s^*h)^{(1-3\sigma)/\sigma} \left(s^* + h \frac{ds^*}{dh}\right)^2 + (s^*h)^{(1-2\sigma)/\sigma} \left(2 \frac{ds^*}{dh} + h \frac{d^2s^*}{dh^2}\right) \right] \\ &= X (s^*h)^{(1-3\sigma)/\sigma} \left[ \frac{2\sigma-1}{\sigma} \left(s^* + h \frac{ds^*}{dh}\right)^2 - (s^*h) \left(2 \frac{ds^*}{dh} + h \frac{d^2s^*}{dh^2}\right) \right] \end{aligned}$$

459 where  $X = \frac{1}{b} \left(\frac{b}{a}\right)^{1/\sigma} \frac{1-\sigma}{\sigma} > 0$ . Note that  $\frac{d^2N_2}{dh^2}$  is continuous in  $\sigma$  around  $\sigma = 1$ . Note also from (19) that for  $\sigma = 1$ ,  
 460  $s^*$  becomes constant in  $\sigma$ . The term in square brackets then reduces to  $(s^*)^2 > 0$ . Putting these facts together, for  $\sigma$   
 461 sufficiently close to 1,  $\frac{d^2N_2^*}{dh^2} > 0$ , i.e.  $N_2^*$  is convex in  $h$ .

462 This case holds for intermediate values on  $h$ . Equation (21) shows that for  $\sigma < 1$ ,  $N_2$  decreases in  $h$ ; the requirement  
 463 that  $N_2 > 0$  therefore puts a maximum on  $h$ . When  $\sigma > 1$ ,  $N_2$  increases in  $h$  and this puts a minimum on  $h$ . The  
 464 requirement  $N_1 = 0$  provides the other bound. Equation (9) requires  $-bY_1^{-\sigma} + a \leq 0$  since  $\lambda_1$  must be non-negative.  
 465 The LHS is increasing in  $Y_1$ , and hence decreasing in  $s$  as  $Y_1 = 1 - s$  since  $N_1 = 0$ . Lastly, optimal choice of education  
 466  $s^*$  increases in  $h$  for  $\sigma < 1$ , and decreases for  $\sigma > 1$ . Hence for  $\sigma < 1$ , (9) puts a minimum on  $h$ , and for  $\sigma > 1$  it puts a  
 467 maximum on  $h$ .

468 Summarizing:

469 **Lemma 2.** *Case 2 holds for intermediate values of  $h$ . In case 2: for  $\sigma < 1$ ,  $s^*$  is increasing in  $h$  and  $N_2^*$  is decreasing in  $h$ . For  $\sigma > 1$ ,  
 470  $s^*$  is decreasing in  $h$ . For  $\sigma$  close enough to 1,  $N_2^*$  is convex in  $h$ .*

471 **Case 3:**  $N_1^* = 0, N_2^* = 0$

472 We can solve for  $s^*$  by substituting values of  $Y_1$  and  $Y_2$  into (11):

$$-(1-s^*)^{-\sigma} + h(s^*h)^{-\sigma} = 0$$

473 which rearranges to

$$s^* = \frac{1}{1 + h^{(\sigma-1)/\sigma}}. \quad (22)$$

Conditions (9) and (10) become:

$$-b(1 - s^*)^{-\sigma} + a \leq 0$$

$$-bs^*h(s^*h)^{-\sigma} + a \leq 0$$

equivalently

$$\frac{a}{b} \leq (1 - s^*)^{-\sigma}$$

$$\frac{a}{b} \leq s^*h(s^*h)^{-\sigma}$$

474 which can both be satisfied for  $a/b$  close enough to zero. Note from (22) that as  $h \rightarrow \infty$ ,  $s^*$  increases towards 1 for  
 475  $\sigma < 1$ , and decreases towards 0 for  $\sigma > 1$ . Note also that the right hand side of the first inequality above approaches  
 476 infinity as  $s^* \rightarrow 1$ , therefore also as  $h \rightarrow \infty$  for  $\sigma < 1$ . Rewrite the second inequality as

$$\frac{a}{b} < (s^*h)^{1-\sigma} = \left( \frac{h}{1 + h^{(\sigma-1)/\sigma}} \right)^{1-\sigma} = (h^{-1} + h^{-1/\sigma})^{\sigma-1}$$

477 and note that again, as  $h \rightarrow \infty$ , the RHS increases towards infinity for  $\sigma < 1$ , and decreases towards zero otherwise.

478 Thus, for  $\sigma < 1$ , both equations will be satisfied for  $h$  high enough. For  $\sigma > 1$ , they will be satisfied for  $h$  low enough.

479 Summarizing

480 **Lemma 3.** *For  $\sigma < 1$ , case 3 holds for  $h$  high enough, and in case 3,  $s^*$  increases in  $h$ . For  $\sigma > 1$ , case 3 holds for  $h$  low enough and*  
 481  *$s^*$  decreases in  $h$ .*

482 **Case 4:**  $N_1^* > 0, N_2^* = 0$

Rearranging the first order conditions (9) and (10) for  $N_1^*$  and  $N_2^*$  gives

$$\frac{a}{b} = (1 - s^* - bN_1^*)^{-\sigma}$$

$$\frac{a}{b} \leq s^*hY_2^{-\sigma}$$

hence

$$\begin{aligned}
(1 - s^* - bN_1^*)^{-\sigma} &\leq s^* h Y_2^{-\sigma} = (s^* h)^{1-\sigma} \\
\Leftrightarrow (1 - s^* - bN_1^*)^\sigma &\geq (s^* h)^{\sigma-1} \\
\Leftrightarrow 1 - s^* - bN_1^* &\geq (s^* h)^{1-1/\sigma}
\end{aligned}$$

Now rearrange the first order condition for  $s^*$  from (11), noting that since  $N_2^* = 0$ ,  $s^* > 0$  by the Inada condition.

$$\begin{aligned}
h^{1/\sigma-1}(1 - s^* - bN_1^*) &= s^* \\
1 - s^* - bN_1^* &= s^* h^{1-1/\sigma}
\end{aligned}$$

This, combined with the previous inequality, implies

$$\begin{aligned}
(s^* h)^{1-1/\sigma} &\leq s^* h^{1-1/\sigma} \\
\Leftrightarrow (s^*)^{-1/\sigma} &\leq 1
\end{aligned}$$

which cannot hold since  $0 < s^* < 1$ .

## Comparative statics

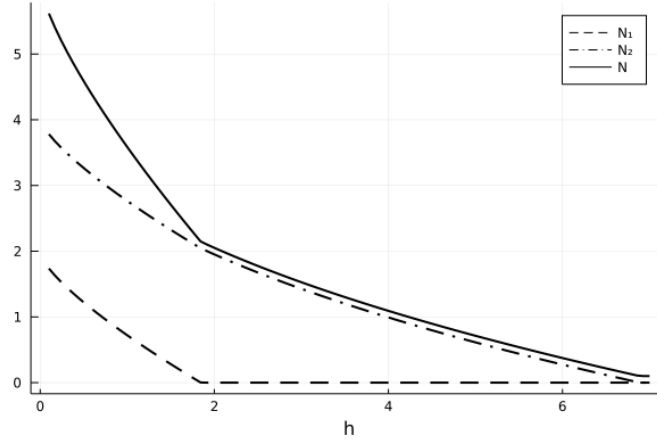
We can now examine how the fertility-human capital relationship

$$\frac{dN^*}{dh}, \text{ where } N^* \equiv N_1^* + N_2^*,$$

changes with respect to other parameters. We focus on the case  $\sigma < 1$ , since it gives the closest match to our observations, and since it also generates “reasonable” predictions in other areas, e.g. that education levels increase with human capital. Figure 23 shows how  $N^*$  changes with  $h$  for  $a = 0.4, b = 0.25, \sigma = 0.7$ .

**Lemma 4.** For  $\sigma < 1$  in a neighbourhood of 1,  $N^*$  is globally convex in  $h$ .

*Proof.* From Lemmas 1, 2 and 3, as  $h$  increases we move from  $N_1^*, N_2^* > 0$  to  $N_1^* = 0, N_2^* > 0$  to  $N_1^* = N_2^* = 0$ . Furthermore, for  $\sigma > 2/3$ ,  $N_1^*$  and  $N_2^*$  are convex in  $h$  when they are both positive, and for  $\sigma$  close enough to 1,  $N_2^*$  is convex in  $h$  when  $N_1^* = 0$ . All that remains is to check that the derivative is increasing around the points where these 3 regions meet. That is trivially satisfied where  $N_2^*$  becomes 0, since thereafter  $\frac{dN^*}{dh}$  is zero. The derivative as  $N_1^*$



**Figure 23:** Fertility vs. human capital in the two-period model with  $a = 0.4, b = 0.25, \sigma = 0.7$ .

approaches zero is twice the expression in (17):

$$-\frac{2}{b} \left(\frac{b}{a}\right)^{1/(2\sigma-1)} \frac{1-\sigma}{2\sigma-1} h^{(1-\sigma)/(2\sigma-1)-1} \quad (23)$$

and the derivative to the right of this point is given by (21):

$$-\frac{1}{b} \left(\frac{b}{a}\right)^{1/\sigma} \frac{1-\sigma}{\sigma} (s^*h)^{(1-2\sigma)/\sigma} (s^* + h \frac{ds^*}{dh}) \quad (24)$$

We want to prove that the former is larger in magnitude (i.e. more negative). Dividing (23) by (24) gives

$$2 \frac{\sigma}{2\sigma-1} \left(\frac{b}{a}\right)^{(1-\sigma)/(\sigma(2\sigma-1))} \frac{h^{(1-\sigma)^2/(\sigma(2\sigma-1))}}{s^*(s^* + h \frac{ds^*}{dh})}$$

Examining (19) shows that as  $\sigma \rightarrow 1$ ,  $s^* \rightarrow 0.5$  and  $\frac{ds^*}{dh} \rightarrow 0$ , and therefore the above approaches

$$2 \frac{1}{(0.5)^2} = 8.$$

□

We can now gather the theoretical predictions stated in Table 1.

**Prediction 1:** for  $\sigma < 1$ , total fertility  $N^* \equiv N_1^* + N_2^*$  is decreasing in human capital  $h$ .

Furthermore, for  $\sigma$  close enough to 1, fertility is convex in human capital, i.e.

**Prediction 2 part 1:** the fertility-human capital relationship is closer to 0 at high levels of  $h$ .

For  $\sigma < 1$ , education levels  $s^*$  increase in  $h$ , and so therefore do equilibrium wages  $w(s^*, h)$ . This, plus fact 1, gives:

**Prediction 2 part 2:** for  $\sigma < 1$  and close to 1, the fertility-human capital relationship is weaker among higher earners.

**Prediction 4:** for  $\sigma < 1$  and close to 1, the fertility-human capital relationship is weaker at high levels of education.

Next, we compare people who start fertility early ( $N_1^* > 0$ ) versus those who start fertility late ( $N_1^* = 0$ ). Again, for  $\sigma < 1$  the former group have lower  $h$  than the latter group. Thus we have:

**Prediction 5:** for  $\sigma < 1$  and close to 1, the fertility-human capital relationship is weaker among those who start fertility late.

Lastly, we prove prediction 3. Differentiating  $dN_t^*/dh$  in (17) with respect to  $b$ , for when  $N_1^* > 0$  gives:

$$\frac{d^2 N_t^*}{dhdb} = \frac{2\sigma - 2}{2\sigma - 1} b^{(3-4\sigma)/(2\sigma-1)} \left(\frac{1}{a}\right)^{1/(2\sigma-1)} \frac{1-\sigma}{2\sigma-1} h^{(\sigma-1)^2/(\sigma(2\sigma-1))}$$

which is negative for  $0.5 < \sigma < 1$ . When  $N_1^* = 0$ , differentiating  $dN_2^*/dh$  in (21) gives:

$$\frac{d^2 N_2^*}{dhdb} = -\frac{1-\sigma}{\sigma} b^{(1-2\sigma)/\sigma} \left(\frac{1}{a}\right)^{1/\sigma} \frac{1-\sigma}{\sigma} (s^* h)^{(1-2\sigma)/\sigma} (s^* + h \frac{ds^*}{dh})$$

which again is negative for  $\sigma < 1$ . Therefore:

**Prediction 3:** for  $\sigma < 1$ , the fertility-human capital relationship is more negative when the burden of childcare  $b$  is larger.

### Including a money cost

The model can be extended by adding a money cost  $m$  per child. Utility is then

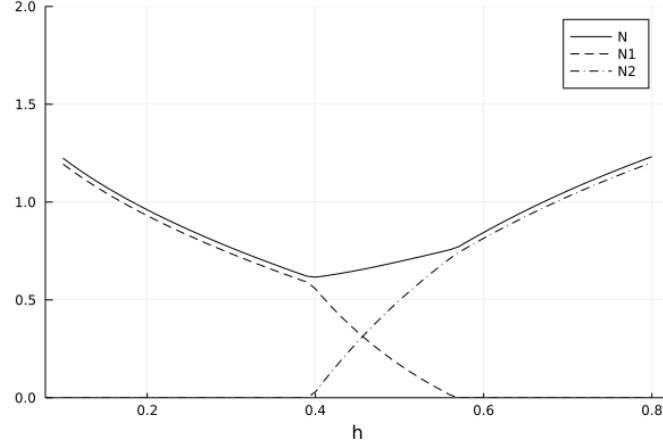
$$U = u(1 - s - bN_1 - mN_1) + u(w(s, h)(1 - bN_2) - mN_2) + a(N_1 + N_2)$$

Figure 24 shows a computed example with  $a = 0.4, b = 0.175, \sigma = 0.7, m = 0.075$ . Fertility first declines steeply with human capital, then rises. In addition, for parents with low AFLB ( $N_1 > 0$ ), the fertility-human capital relationship is negative, while for parents with higher AFLB ( $N_1 = 0$ ) it is positive.

### Concavity

**Lemma 5.** For  $\sigma > 0.5$ ,  $U$  in equation (2) is concave in  $N_1, N_2$  and  $s$ .





**Figure 24:** Fertility vs. human capital in the two-period model with money costs of children.  $a = 0.4, b = 0.175, \sigma = 0.7, m = 0.075$ .

*Proof.* We examine the Hessian matrix of utility in each period. Note that period 1 utility is constant in  $N_2$  and period 2 utility is constant in  $N_1$ . For period 1 the Hessian with respect to  $N_1$  and  $s$  is:

$$\begin{bmatrix} d^2u/dN_1^2 & d^2u/dsdN_1 \\ d^2u/dsdN_1 & d^2u/ds^2 \end{bmatrix} = \begin{bmatrix} -\sigma b^2 & -\sigma b \\ -\sigma b & -\sigma \end{bmatrix} Y_1^{-\sigma-1}$$

with determinant

$$(\sigma^2 b^2 - \sigma^2 b^2) Y_1^{-2\sigma-2} = 0.$$

Thus, first period utility is weakly concave. For period 2 with respect to  $N_2$  and  $s$ , the Hessian is:

$$\begin{bmatrix} d^2u/dN_2^2 & d^2u/dsdN_2 \\ d^2u/dsdN_2 & d^2u/ds^2dN_2 \end{bmatrix} = \begin{bmatrix} -\sigma(bsh)^2 Y_2^{-\sigma-1} & -(1-\sigma)bhY_2^{-\sigma} \\ -(1-\sigma)bhY_2^{-\sigma} & -\sigma[h(1-bN_2^*)]^2 Y_2^{-\sigma-1} \end{bmatrix}$$

with determinant

$$\begin{aligned} & (-\sigma(bsh)^2 Y_2^{-\sigma-1})(-\sigma[h(1-bN_2^*)]^2 Y_2^{-\sigma-1}) - (-(1-\sigma)bhY_2^{-\sigma})^2 \\ &= \sigma^2(bsh)^2[h(1-bN_2^*)]^2 Y_2^{-2\sigma-2} - (1-\sigma)^2(bh)^2 Y_2^{-2\sigma} \\ &= \sigma^2(bh)^2 Y_2^{-2\sigma} - (1-\sigma)^2(bh)^2 Y_2^{-2\sigma}, \text{ using that } Y_2 = (sh)(1-bN) \\ &= (bh)^2 Y_2^{-2\sigma}(\sigma^2 - (1-\sigma)^2) \end{aligned}$$

which is positive if and only if  $\sigma > 0.5$ . Thus, if  $\sigma > 0.5$  then the Hessian is negative definite and thus utility is concave; this combined with weak concavity of period 1, and linearity of  $a(N_1 + N_2)$ , shows that (2) is concave.  $\square$

527 **Effect of  $a$**

528 **Lemma 6.** For  $\sigma < 1$ ,  $d^2 N^*/dadh > 0$ , i.e. the effect of  $a$  increases at higher levels of human capital.

529 *Proof.* Differentiating (17) with respect to  $a$  gives

$$\frac{d^2 N_t^*}{dadh} = -\frac{1}{b} \frac{1}{1-2\sigma} a^{-1} \left(\frac{a}{b}\right)^{1/(1-2\sigma)} \frac{1-\sigma}{2\sigma-1} h^{(1-\sigma)/(2\sigma-1)-1}$$

530 for  $t = 1, 2$  when  $N_1^*, N_2^* > 0$ . For  $\sigma > 0.5$  this is positive.

531 When  $N_1^* = 0, N_2^* > 0$ , differentiating (21) with respect to  $a$  gives

$$\frac{d^2 N_2^*}{dadh} = \frac{1}{b} \frac{1}{\sigma} a^{-1} \left(\frac{a}{b}\right)^{-1/\sigma} \frac{1-\sigma}{\sigma} (s^* h)^{(1-2\sigma)/\sigma} \left(s^* + h \frac{ds^*}{dh}\right)$$

532 which is  $-a^{-1}/\sigma$  times (21) and hence is positive.

533

□

## References

- Abdellaoui, Abdel, David Hugh-Jones, Loïc Yengo, Kathryn E Kemper, Michel G Nivard, Laura Veul, Yan Holtz, et al. 2019. “Genetic Correlates of Social Stratification in Great Britain.” *Nature Human Behaviour* 3 (12): 1332–42.
- Alten, Sjoerd van, Benjamin W Domingue, Titus Galama, and Andries Marees. 2021. “The Effects of Demographic-Based Selection Bias on GWAS Results in the UK Biobank.” *Behavior Genetics* 51 (6): 748–48.
- Barban, Nicola, and Rick Jansen, Ronald de Vlaming, Ahmad Vaez, Jornt J Mandemakers, Felix C Tropf, Xia Shen, et al. 2016. “Genome-Wide Analysis Identifies 12 Loci Influencing Human Reproductive Behavior.” *Nature Genetics* 48 (12): 1462–72. <https://doi.org/10.1038/ng.3698>.
- Baron, Reuben M, and David A Kenny. 1986. “The Moderator–Mediator Variable Distinction in Social Psychological Research: Conceptual, Strategic, and Statistical Considerations.” *Journal of Personality and Social Psychology* 51 (6): 1173.
- Baudin, Thomas, David De La Croix, and Paula E Gobbi. 2015. “Fertility and Childlessness in the United States.” *American Economic Review* 105 (6): 1852–82.
- Beauchamp, Jonathan P. 2016. “Genetic Evidence for Natural Selection in Humans in the Contemporary United States.” *Proceedings of the National Academy of Sciences* 113 (28): 7774–79.
- Becker, Gary S. 1960. “An Economic Analysis of Fertility.” *National Bureau Committee for Economic Research* 209.
- . 1964. “Human Capital.”
- . 1981. “A Treatise on the Family.” *NBER Books*.
- Becker, Gary S, and Nigel Tomes. 1976. “Child Endowments and the Quantity and Quality of Children.” *Journal of Political Economy* 84 (4, Part 2): S143–62.
- Belsky, Daniel W, Benjamin W Domingue, Robbee Wedow, Louise Arseneault, Jason D Boardman, Avshalom Caspi, Dalton Conley, et al. 2018. “Genetic Analysis of Social-Class Mobility in Five Longitudinal Studies.” *Proceedings of the National Academy of Sciences* 115 (31): E7275–84.
- Benton, Mary Lauren, Abin Abraham, Abigail L. LaBella, Patrick Abbot, Antonis Rokas, and John A. Capra. 2021. “The Influence of Evolutionary History on Human Health and Disease.” *Nature Reviews Genetics*.
- Bycroft, Clare, Colin Freeman, Desislava Petkova, Gavin Band, Lloyd T Elliott, Kevin Sharp, Allan Motyer, et al. 2018. “The UK Biobank Resource with Deep Phenotyping and Genomic Data.” *Nature* 562 (7726): 203–9.
- Caucutt, Elizabeth M, Nezih Guner, and John Knowles. 2002. “Why Do Women Wait? Matching, Wage Inequality, and the Incentives for Fertility Delay.” *Review of Economic Dynamics* 5 (4): 815–55.
- Cohen, Alma, Rajeev Dehejia, and Dmitri Romanov. 2013. “Financial Incentives and Fertility.” *Review of Economics and Statistics* 95 (1): 1–20.
- Conley, Dalton, Thomas Laidley, Daniel W Belsky, Jason M Fletcher, Jason D Boardman, and Benjamin W Domingue.

2016. “Assortative Mating and Differential Fertility by Phenotype and Genotype Across the 20th Century.” *Proceedings of the National Academy of Sciences* 113 (24): 6647–52.
- Davey Smith, George, and Shah Ebrahim. 2003. “‘Mendelian Randomization’: Can Genetic Epidemiology Contribute to Understanding Environmental Determinants of Disease?” *International Journal of Epidemiology* 32 (1): 1–22.
- Fieder, Martin, and Susanne Huber. 2022. “Contemporary Selection Pressures in Modern Societies? Which Factors Best Explain Variance in Human Reproduction and Mating?” *Evolution and Human Behavior* 43 (1): 16–25. <https://doi.org/https://doi.org/10.1016/j.evolhumbehav.2021.08.001>.
- Fisher, RA. 1930. “The Genetical Theory of Natural Selection.”
- Flynn, James R. 1987. “Massive IQ Gains in 14 Nations: What IQ Tests Really Measure.” *Psychological Bulletin* 101 (2): 171.
- Fry, Anna, Thomas J Littlejohns, Cathie Sudlow, Nicola Doherty, Ligia Adamska, Tim Sprosen, Rory Collins, and Naomi E Allen. 2017. “Comparison of Sociodemographic and Health-Related Characteristics of UK Biobank Participants With Those of the General Population.” *American Journal of Epidemiology* 186 (9): 1026–34. <https://doi.org/10.1093/aje/kwx246>.
- Gauthier, Anne H. 2007. “The Impact of Family Policies on Fertility in Industrialized Countries: A Review of the Literature.” *Population Research and Policy Review* 26 (3): 323–46.
- Harden, Kathryn Paige. 2021. *The Genetic Lottery: Why DNA Matters for Social Equality*. Princeton University Press.
- Hotz, V Joseph, Jacob Alex Klerman, and Robert J Willis. 1997. “The Economics of Fertility in Developed Countries.” *Handbook of Population and Family Economics* 1 (Part A): 275–347.
- Howe, Laurence J, Michel G Nivard, Tim T Morris, Ailin F Hansen, Humaira Rasheed, Yoonsu Cho, Geetha Chittoor, et al. 2021. “Within-Sibship GWAS Improve Estimates of Direct Genetic Effects.” *bioRxiv*. <https://doi.org/10.1101/2021.03.05.433935>.
- HRS. 2020. [https://hrs.isr.umich.edu/data-products/genetic-data/products?\\_ga=2.248005447.1729788711.1602771602-1571093872.1602771602](https://hrs.isr.umich.edu/data-products/genetic-data/products?_ga=2.248005447.1729788711.1602771602-1571093872.1602771602).
- Jones, Larry E, Alice Schoonbroodt, and Michele Tertilt. 2008. “Fertility Theories: Can They Explain the Negative Fertility-Income Relationship?”
- Jones, Larry E, and Michèle Tertilt. 2006. “An Economic History of Fertility in the US: 1826-1960.” *NBER Working Paper*, no. w12796.
- Kong, Augustine, Michael L Frigge, Gudmar Thorleifsson, Hreinn Stefansson, Alexander I Young, Florian Zink, Gudrun A Jonsdottir, et al. 2017. “Selection Against Variants in the Genome Associated with Educational Attainment.” *Proceedings of the National Academy of Sciences* 114 (5): E727–32.
- Kong, Augustine, Gudmar Thorleifsson, Michael L Frigge, Bjarni J Vilhjalmsen, Alexander I Young, Thorgeir E Thorgeirsson, Stefania Benonisdottir, et al. 2018. “The Nature of Nurture: Effects of Parental Genotypes.” *Science*

359 (6374): 424–28.

Lee, James J, Robbee Wedow, Aysu Okbay, Edward Kong, Omeed Maghzian, Meghan Zacher, Tuan Anh Nguyen-Viet, et al. 2018. “Gene Discovery and Polygenic Prediction from a Genome-Wide Association Study of Educational Attainment in 1.1 Million Individuals.” *Nature Genetics* 50 (8): 1112–21.

Lumley, Thomas. 2020. “Survey: Analysis of Complex Survey Samples.”

Lundberg, Shelly, and Robert A Pollak. 2007. “The American Family and Family Economics.” *Journal of Economic Perspectives* 21 (2): 3–26.

Lynn, Richard, and Marian Van Court. 2004. “New Evidence of Dysgenic Fertility for Intelligence in the United States.” *Intelligence* 32 (2): 193–201.

Mills, Melinda C, Felix C Tropf, David M Brazel, Natalie van Zuydam, Ahmad Vaez, Tune H Pers, Harold Snieder, et al. 2021. “Identification of 371 Genetic Variants for Age at First Sex and Birth Linked to Externalising Behaviour.” *Nature Human Behavior*.

Mincer, Jacob. 1958. “Investment in Human Capital and Personal Income Distribution.” *Journal of Political Economy* 66 (4): 281–302.

Monstad, Karin, Carol Propper, and Kjell G Salvanes. 2008. “Education and Fertility: Evidence from a Natural Experiment.” *Scandinavian Journal of Economics* 110 (4): 827–52.

Reeve, Charlie L, Michael D Heeney, and Michael A Woodley of Menie. 2018. “A Systematic Review of the State of Literature Relating Parental General Cognitive Ability and Number of Offspring.” *Personality and Individual Differences* 134: 107–18.

Rimfeld, Kaili, Eva Krapohl, Maciej Trzaskowski, Jonathan R. I. Coleman, Saskia Selzam, Philip S. Dale, Tonu Esko, Andres Metspalu, and Robert Plomin. 2018. “Genetic Influence on Social Outcomes During and After the Soviet Era in Estonia.” *Nature Human Behaviour* 2 (4): 269–75. <https://doi.org/10.1038/s41562-018-0332-5>.

Robertson, Alan. 1966. “A Mathematical Model of the Culling Process in Dairy Cattle.” *Animal Science* 8 (1): 95–108.

Sanjak, Jaleal S, Julia Sidorenko, Matthew R Robinson, Kevin R Thornton, and Peter M Visscher. 2018. “Evidence of Directional and Stabilizing Selection in Contemporary Humans.” *Proceedings of the National Academy of Sciences* 115 (1): 151–56.

Sarraf, Matthew Alexandar, Colin Feltham, et al. 2019. *Modernity and Cultural Decline: A Biobehavioral Perspective*. Springer Nature.

Selzam, Saskia, Stuart J Ritchie, Jean-Baptiste Pingault, Chandra A Reynolds, Paul F O’Reilly, and Robert Plomin. 2019. “Comparing Within-and Between-Family Polygenic Score Prediction.” *The American Journal of Human Genetics* 105 (2): 351–63.

Social Security Committee. 1999. “Fourth Report.”

Townsend, Peter. 1987. “Deprivation.” *Journal of Social Policy* 16 (2): 125–46.

<sup>632</sup> Willis, Robert J. 1973. "A New Approach to the Economic Theory of Fertility Behavior." *Journal of Political Economy* 81  
<sup>633</sup> (2, Part 2): S14–64.