## notation

## Notation

Symbol	Meaning
$\overline{c_1, c_2, \cdots, c_z}$	the thresholds for simplification
$C_0, C_1, \cdots, C_z$	the groups for simplication
	the function on temporal processing with parameters $\phi$
$f_{\phi}(.) F_{\eta}(.)$	the CDF to fit the data with parameter $\eta$
$g_{\theta}(.)$	the function on spatial aggregation with parameter $\theta$
h(.)	the function on variable transformation, no parameter
$i:1,2,\cdots,n$	the space subscript in the data
$j:1,2,\cdots,J$	the temporal subscript in the data
$j^*$	variation of temporal subscrip in normalising
j'	variation of temporal subscrip in temporal processing
k	time scale in temporal processing
$m:0,1,\cdots,11$	remainder of $j^* \mod 12$ for index monthly data
n	the maximum space index in the data
$p:1,2,\cdots,P$	the (maximum) variable index in the data
$p^*:1,2,\cdots,P^*$	the dimension reduced variable index
$s,\mathcal{D}_s$	the spatial index, and its space, of the data
$t,\mathcal{D}_t$	the temporal index, and its space, of the data
u	the subtracted constant in benchmarking
$\alpha$	the subtracted quantity in scaling
$\gamma$	the divided quantity in scaling
$\eta,\mathrm{H}$	parameters, and its space, in PDF distribution fit
$\theta, \Theta$	additional parameters, and its space, in spatial aggregation
$\lambda$	the PCA factor loadings
$\sigma$	the standard deviation of the data in scaling
au, T	additional parameters, and its space, in variable transformation
$\Phi^{-1}(.)$	the quantile (inverse CDF) function
$\psi,\Psi$	additional parameters, and its space, in temporal processing

Step	Notation	Notes
Raw data	$\mathbf{x}(\mathbf{s};\mathbf{t}),$	$\mathbf{s} \in \mathcal{D}_s,  \mathcal{D}_s \subseteq \mathbb{R}^2,  \mathbf{s} = (s_1, s_2, \cdots, s_n)'$
	$x_p(s_i;t_j)$	$t \in \mathcal{D}_t$ , $\mathbf{t} = (t_1, t_2, \cdots, t_J)'$
		$\mathbf{x}(\mathbf{s};\mathbf{t}) = (x_1(\mathbf{s};\mathbf{t}), x_2(\mathbf{s};\mathbf{t}), \cdots, x_P(\mathbf{s};\mathbf{t}))'$
		when the pipeline step can be written in
		univariate case, the data will be referred to
		as $x(\mathbf{s}; \mathbf{t})$
Spatial	$g_{ heta}(x(\mathbf{s};\mathbf{t}))$	where $\theta \in \Theta \subseteq \mathbb{R}^{d_{\theta}}$ , $d_{\theta}$ is the number of
aggregation		parameter of $\theta$
scaling	$\frac{x(s_i;t_j) - \alpha}{\gamma}$	Example 1: z-score standardisation:
O	γ	$\alpha = \bar{x}(s;t)$ and $\gamma = \sigma(s;t)$ to standardise the
		data by the its mean and standard deviation
		across all time and all space units.
		Example 2: standardise into unit interval:
		$\alpha = \min[x(s_i, t_i)]$ and
		$\gamma = \max[x(s_i, t_j)] - \min[x(s_i, t_j)]$
		where min[.] and max[.] are the minimum
		and maximum value across all spatial and
		temporal units.
Normalising	$\Phi^{-1}[F_{\eta}(x(\mathbf{s};\mathbf{t}))]$	where $\eta \in H \subseteq \mathbb{R}^{d_{\eta}}$ , $d_{\eta}$ is the number of
	<i>- 1</i> / <i>-</i>	parameter of $\eta$
		Example:
		When $\overline{\text{CDF}} F(.)$ is separately fitted for each
		month:
		$\Phi^{-1}[F_{\eta}^{m}(x(\mathbf{s};t_{j^{*}}))]$ where $j^{*}$ is all the indexes
		that satisfy $j^* \mod 12 = m$ for each
		$m=0,1,\cdots,11$
Variable	$h_{\tau}(x(\mathbf{s};\mathbf{t}))$	where $\tau \in T \subseteq \mathbb{R}^{d_{\tau}}$ , $d_{\tau}$ is the number of
transformation		parameter of $\tau$
		TODO: to be filled
Temporal	$f_{\psi}(x(\mathbf{s};\mathbf{t}))$	where $\psi \in \Psi \subseteq \mathbb{R}^{d_{\psi}}$ , $d_{\psi}$ is the number of
processing	* * * * */	parameter of $\psi$
		Example 1:
		aggregate across a time scale of $\psi = k$ :
		$x(s_i; t_{j'}) = \sum_{j=j'-k+1}^{j'} x(s_i; t_j)$
		Example 2:
		aggregate with a kernel weight $\psi = w_{ij}$ :
		$x(s_i; t_{j'}) = \sum_{j=j'-k+1}^{j'} w_{ij} x(s_i; t_j)$
		$\omega(s_i, \iota_{j'}) - \angle_{j=j'-k+1} \omega_{ij}\omega(s_i, \iota_j)$

Step	Notation	Notes
Dimension	$x_{p^*}(\mathbf{s}; \mathbf{t}) \to x_p(\mathbf{s}; \mathbf{t})$	Example: first principal component:
reduction	where $p^* = 1, 2, \dots, P^*$ and $P^* < P$	Example: first principal component: $x_{p^*}(\mathbf{s}; \mathbf{t}) = \sum_{p=1}^{P} \lambda_p x_p(\mathbf{s}; \mathbf{t})$
		where $\lambda_p$ is the loading of the PC1, derived
		from maximising the variance of the data
		given the constraint $\sum_{p=1}^{P} \lambda_p^2 = 1$
benchmarking	$u[x(s_i, t_j)]$	where $u$ is a scalar of interest in the index
	<b>.</b>	constructed, could be a constant or a
		function of the data, i.e. mean.
		Example:
		In SPI, $u = -2$ is the threshold for extreme
		drought.
	$\begin{cases} C_0 & c_1 \leq (s_i;t_j) < c_0 \\ C_1 & c_2 \leq x(s_i;t_j) < c_1 \\ C_2 & c_3 \leq x(s_i;t_j) < c_2 \\ \dots \\ C_z & c_z \leq x(s_i;t_j) \end{cases}$	
	$\begin{array}{ c c } C_1 & c_2 \leq x(s_i; t_j) < c_1 \end{array}$	
Simplification	$\begin{cases} C_2 & c_3 \le x(s_i; t_i) < c_2 \end{cases}$	Example:
		In SPI, four categories are classified: mild
	$C = c \leq r(s \cdot t)$	drought: $[-0.99, 0]$ ; moderate drought:
	$( \circ_z  \circ_z \supseteq \omega(\circ_i, \circ_j)$	•
		and extreme drought: $[-\infty, -2]$ .
		Here $C_0, C_1, C_2, C_3$ are the drought
		categories: mild, moderate, severe, and
		extreme drought $(z=3)$ and
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