

notation

Notation

Symbol	Meaning
s	the space index
t	the time index
$i : 1, 2, \dots, n$	the space index for each individual location
$j : 1, 2, \dots, J$	the time index for each individual timestamp
$j^*, m : 0, 1, \dots, 11$	the time index for indexing time by month
\mathcal{D}_s and \mathcal{D}_t	the parameter space for spatial and temporal
$f_\phi(\cdot)$	the function on temporal processing with parameters ϕ
$g_\theta(\cdot)$	the function on spatial aggregation with parameter θ
$h(\cdot)$	the function on variable transformation, no parameter
$F_\eta(\cdot)$	the PDF to fit the data with parameter η
$\Phi^{-1}(\cdot)$	the quantile (inverse CDF) function

Step	Notation	Notes
Raw data	$\mathbf{X}(\mathbf{s}; \mathbf{t}),$ $x_p(s_i; t_j)$	$\mathbf{s} \in \mathcal{D}_s, \mathcal{D}_s \subseteq \mathbb{R}^2, \mathbf{s} = (s_1, s_2, \dots, s_n)'$ $t \in \mathcal{D}_t, \mathbf{t} = (t_1, t_2, \dots, t_J)'$ $\mathbf{X}(\mathbf{s}; \mathbf{t}) = (x_1(\mathbf{s}; \mathbf{t}), x_2(\mathbf{s}; \mathbf{t}), \dots, x_P(\mathbf{s}; \mathbf{t}))'$ when the pipeline step can be written in univariate case, the data will be referred to as $x(\mathbf{s}; \mathbf{t})$
Variable transfor- mation	$h(x(\mathbf{s}; \mathbf{t}))$	TODO: to be filled

Step	Notation	Notes
Temporal processing	$f_\phi(x(\mathbf{s}; \mathbf{t}))$	<u>Special case 1:</u> aggregate across a time scale of k : $f_k(\mathbf{X}(\mathbf{s}; \mathbf{t})) = \sum_{l=t-k+1}^t \mathbf{X}(\mathbf{s}; \mathbf{t})$ [TODO: check again] <u>Special case 2:</u> aggregate with a kernel weight w_{ij} : $f_{w_{ij}}(\mathbf{X}(s_i; t_j)) = \sum_{l=t-k+1}^t w_{ij} \mathbf{X}(s_i; t_j)$
Spatial aggregation	$g_\theta(x(\mathbf{s}; \mathbf{t}))$	
Normalising	$\Phi^{-1}[F_\eta(x(\mathbf{s}; \mathbf{t}))]$	Special case: When PDF $F(\cdot)$ is separately fitted for each month: $\Phi^{-1}[F_\eta^m(x(\mathbf{s}; t_{j^*}))]$ where j^* is all the indexes that satisfy $j^* \bmod 12 = m$ for each $m = 0, 1, \dots, 11$

TODO:

- look at how temporal aggregation (processing) is written in journals