

BAHRIA UNIVERSITY (KARACHI CAMPUS)

Department of Software Engineering.
Assignment 04 (Spring 2023)

Course Title: Linear Algebra

Class: BSE 2A

Course Instructor: Muhammad Imran Afridi

Submission: 17 June 2023

Course Code: GSC-121

Shift: Morning Time: 3 Days

Max Marks: 05 Points

Assignment No 04

Submitted By:

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Registrat	ion Number:	81965			
Section:	,	2 A			

Overtion # 01 8-

$$\begin{pmatrix} 3 & 0 & -1 \\ 2 & 3 & 1 \\ -3 & 4 & 5 \end{pmatrix}$$

$$\begin{bmatrix} -1 & 0 & -1 \\ 2 & -1 & 1 \\ -3 & 4 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & -1 & 0 \\ 2 & -1 & 1 & 0 \\ -3 & 4 & 1 & 0 \end{bmatrix}$$

(-1	0	- 1	10	
0	-1	-1	0	
lo	4	U	0] .

V3: free column.

The system has non toival solution so
$$\lambda = 4$$
 is the eigen value of $\begin{bmatrix} 3 & 0 & -1 \\ 2 & 3 & 1 \end{bmatrix}$ $\begin{bmatrix} -3 & 4 & 5 \end{bmatrix}$

$$R_2 = \frac{7 - 1/2 - 9 = 0}{1/2 = -9}$$

Overtion It 02

$$\theta = \begin{pmatrix} 3 & 1 & 1 \\ 0 & 5 & 0 \\ -2 & 0 & 7 \end{pmatrix}$$

(3)

Solution:

$$\begin{bmatrix}
1A - \lambda I & 1 & 1 \\
3 - \lambda & 1 & 1 \\
0 & 5 - \lambda & 0 \\
-2 & 0 & 7 - \lambda
\end{bmatrix}$$

=
$$1[0 + 2(5 - \lambda)] - 0 + (7 + \lambda)[(3 - \lambda)(5 - \lambda)]$$

= $10 - 2\lambda + (7 - \lambda)[(15 - 5\lambda - 3\lambda + \lambda^2]$

$$[10-2\lambda+(7-\lambda)[15-8\lambda+\lambda^2]$$

$$= -\lambda^3 + 15\lambda^2 - 73\lambda + 115=0$$

Question # 3

$$b_1 = \begin{pmatrix} 1 \\ 1 \\ 3 \end{pmatrix}$$
 $b_2 = \begin{pmatrix} 2 \\ 0 \\ 8 \end{pmatrix}$, $b_3 = \begin{pmatrix} 1 \\ -1 \\ 3 \end{pmatrix}$, $\chi = \begin{pmatrix} 0 \\ 0 \\ -2 \end{pmatrix}$

Solution :-

$$= \begin{bmatrix} 1 & 2 & 1 & 0 \\ 1 & 0 & -1 & 0 \\ 3 & 8 & 3 & -2 \end{bmatrix} \begin{array}{c} R_2 - R_1 \\ R_3 - 3R_1 \end{array}$$

$$= \begin{pmatrix} 1 & 2 & 1 & 0 \\ 0 & -2 & -2 & 0 \\ 0 & 2 & 0 & -2 \end{pmatrix} \begin{array}{c} R_3 + R_2 \\ 0 & 2 & 0 & -2 \end{array}$$

$$= \begin{bmatrix} 1 & 2 & 1 & 0 \\ 0 & -2 & -2 & 0 \\ 0 & 0 & -2 & -2 \end{bmatrix}$$

$$R_3 = 7 - 2 \chi_3 = -2$$
 $\chi_3 = 11$

$$\mathcal{K}_2 = -1$$

2x2 + 2/3=0 7h

$$\begin{bmatrix} \chi \end{bmatrix}_{13} = \begin{bmatrix} \chi \\ \chi_{2} \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix} A_{13}$$

$$\begin{bmatrix} \chi_{2} \\ \chi_{3} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Question # 04

Solution: matrix into rectors. Braking

$$U_1 = \begin{bmatrix} 2 \\ -1 \\ 2 \end{bmatrix}$$

$$0 \quad 2 = \begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix}$$

$$0 \quad 3 = \begin{bmatrix} 4 \\ -2 \\ -5 \end{bmatrix}$$

cheeking the vectors are ofthogonal or not

$$0, 0, 0 = \begin{bmatrix} 2 \\ -1 \\ 2 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} U_2 \cdot U_3 & = \begin{bmatrix} 1 \\ 2 \\ 0 \end{bmatrix} \cdot \begin{bmatrix} 4 \\ -2 \\ -5 \end{bmatrix}$$

$$\begin{array}{c}
U_1 - U_3 = \begin{bmatrix} 2 \\ -1 \\ 2 \end{bmatrix} \cdot \begin{bmatrix} 4 \\ -2 \\ -5 \end{bmatrix}$$

OT,

FOS CI

$$\frac{(1901 - 3 - 1}{01.01}$$

6

For Cz

$$C_2 = \frac{9}{9} \frac{02}{02} = \frac{5}{5} = 1$$

FO6 C 3

$$C_3 = 9U_3 = -30 = -2$$
 $U_3U_3 = 45 = 3$

(BK)

dura