

## **BAHRIA UNIVERSITY (KARACHI CAMPUS)**

Department of Software Engineering.
Assignment 04 (Spring 2023)

**Course Title: Linear Algebra** 

Class: BSE 2B

Course Instructor: Muhammad Imran Afridi

Submission: 17 June 2023

Course Code: GSC-121

Shift: Morning Time: 3 Days

**Max Marks: 05 Points** 

## **Assignment No 04**

## **Submitted By:**

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Registrat	ion Number: _	81962	
Section:2		2 B	

$$\begin{bmatrix} 3 & 0 & -1 \\ 2 & 3 & 1 \\ -3 & 4 & 5 \end{bmatrix}$$

solution :-

$$|A-\lambda I|=0$$

$$= \begin{bmatrix} 3-4 & 0 & -1 \\ 2 & 3-4 & 1 \\ -3 & 4 & 5-4 \end{bmatrix}$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -a \\ -a \end{bmatrix} & 08 & -1 \\ x_3 \end{bmatrix} = \begin{bmatrix} -a \\ 0 \end{bmatrix} & 08 & -1 \end{bmatrix} \rightarrow eigenvafo.$$

## Question # 02:

$$A = \begin{bmatrix} 3 & 1 & 1 \\ 0 & 5 & 0 \\ -2 & 0 & 7 \end{bmatrix}$$

$$\begin{bmatrix}
 3 - \lambda & 1 & 1 \\
 0 & 5 - \lambda & 0 & = 0 \\
 -2 & 0 & 7 - \lambda
 \end{bmatrix}$$

$$= 1 \left[ 0 + 2(5 - \lambda) \right] - 0 + (7 - \lambda) \left[ (3 - \lambda) (5 - \lambda) \right]$$

$$= 10 - 2\lambda + (7 - \lambda) \left[ 15 - 5\lambda - 3\lambda + \lambda^{2} \right]$$

$$= 10 - 2\lambda + (7 - \lambda) \left[ 15 - 8\lambda + \lambda^{2} \right].$$

$$= 10 + 21 + 105 - 561 + 71^2 - 151 + 81^2 - 13$$

$$= -(13 - 1512 + 731 - 115) = 0$$

$$\lambda = 3.58$$

$$\lambda = 6.41$$

$$\lambda = 5$$

$$A = 5, 3.58, 6.41$$

$$A = 5$$

$$A = 5, 3.58, 6.41$$

$$A = 5$$

$$A = 5, 3.58, 6.41$$

$$A = 5$$

$$A$$

$$R_3 = 7 - 2x_3 = -2$$
 $R_2 = 1$ 
 $R_2 = 1$ 
 $R_2 = 1$ 
 $R_3 = 1$ 

$$\begin{array}{c|c} P_{2} = 1 & -2x_{3} - 2x_{3} = 0 \\ \hline X_{2} = -1 \end{array}$$

$$R_{1} = 1$$

$$\chi_{1} + 2\chi_{2} + \chi_{3} = 0$$

$$\chi_{1} - 2 + 1 = 0$$

$$\chi_{1} = 1$$

$$\begin{bmatrix} x \end{bmatrix}_{13} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix} = \begin{bmatrix} 7n_5 \\ 1 \end{bmatrix}$$

Question # 041-

$$A = \begin{bmatrix} 2 & 1 & 4 \\ -1 & 2 & -2 \end{bmatrix} = \begin{bmatrix} -1 \\ 3 \\ 4 \end{bmatrix}$$

$$2 & 0 & 5 \end{bmatrix} = \begin{bmatrix} 4 \\ 4 \end{bmatrix}$$

Breaking matix into vectors

$$U_1 = \begin{bmatrix} 2 \\ -1 \end{bmatrix}, \quad U_2 = \begin{bmatrix} 1 \\ 2 \end{bmatrix}, \quad U_3 = \begin{bmatrix} 4 \\ -2 \end{bmatrix}$$

$$U_1 \cdot U_2 = \begin{bmatrix} 2 \\ -1 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

$$U_1 \cdot U_2 = 2 - 2 + 0 = 0$$

$$U_2 \cdot U_3 = \begin{bmatrix} 1 \\ 2 \\ -5 \end{bmatrix}$$

$$\begin{array}{c} O_1 \cdot O_3 = \begin{bmatrix} 2 \\ -1 \end{bmatrix} \cdot \begin{bmatrix} 4 \\ -2 \end{bmatrix} \\ 2 \end{bmatrix}$$

Vectors are orthogonal to each other

$$C_1 = \frac{y \, U_1}{U_1 \, U_1} = \frac{3}{9} = \frac{1}{3}$$

$$C_2 = \frac{y U_2}{U_2 \cdot U_2} = \frac{5}{5} = 1$$

$$C_{3} = \frac{40_{3}}{0_{3}} = \frac{-30}{45} = \frac{-26_{3}}{3}$$

Ans.