

Question # 01 (A):

1) There are exactly four red books.

$$\begin{aligned} & \exists a \exists b \exists c \exists d \text{ book}(a) \wedge \text{red}(a) \wedge \text{book}(b) \wedge \text{red}(b) \\ & \wedge \text{book}(c) \wedge \text{red}(c) \wedge \text{book}(d) \wedge \text{red}(d) \wedge \neg(a=b) \\ & \wedge \neg(a=c) \wedge \neg(a=d) \wedge (b=c) \wedge \neg(b=d) \wedge \neg \\ & (c=d) \wedge \forall x (\text{book}(x) \wedge \text{red}(x)) \rightarrow ((a=x) \vee (b=x)) \vee \\ & (c=x) \vee (d=x)) \end{aligned}$$

2) There are at least four red books

$$\begin{aligned} & \exists a \exists b \exists c \exists d \text{ book}(a) \wedge \text{red}(a) \wedge \text{book}(b) \wedge \text{red}(b) \\ & \wedge \text{book}(c) \wedge \text{red}(c) \wedge \text{book}(d) \wedge \text{red}(d) \wedge \neg(a=b) \\ & \wedge \neg(a=c) \wedge \neg(a=d) \wedge (b=c) \wedge \neg(b=d) \wedge \neg(c=d) \end{aligned}$$

3) There are at most four red books.

$$\begin{aligned} & \exists a \exists b \exists c \exists d \text{ book}(a) \wedge \text{red}(a) \wedge \text{book}(b) \wedge \text{red}(b) \\ & \wedge \text{book}(c) \wedge \text{red}(c) \wedge \text{book}(d) \wedge \text{red}(d) \wedge \forall x \\ & (\text{book}(x) \wedge \text{red}(x)) \rightarrow (a=x) \vee (b=x) \vee (c=x) \vee (d=x). \end{aligned}$$

Question # 01 (B):

1) C is true or not

$$(A \wedge B) \vee D \Rightarrow C \quad \text{_____ (i)}$$

$$B \wedge K \quad \text{_____ (ii)}$$

$$A \vee K \quad \text{_____ (iii)}$$

$$\sim N \quad \text{_____ (iv)}$$

• By applying unit resolution rule on statement (ii) and (iv), we know that

A is true

• By Applying and elimination we know that B is true

• from above, we came to know that A and B are true
∴ C is true.

2) E is true or not

$$(A \vee B) \wedge (C \vee D) \Rightarrow E \quad \rightarrow I$$

$$A \wedge K \quad \rightarrow II$$

$$\sim K \quad \rightarrow III$$

$$C \wedge T \quad \rightarrow IV$$

• By applying and Elimination on II we came to know that A is true

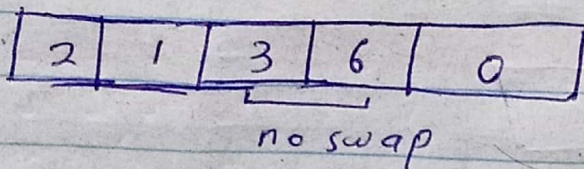
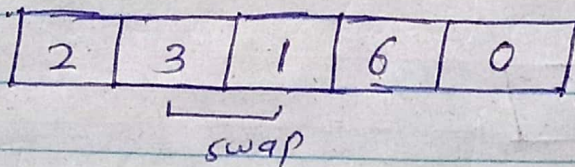
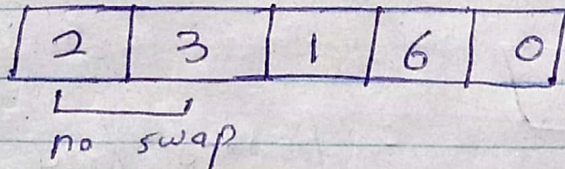
• By applying And elimination on IV, we know that C is true

• from above we come to know that E is true

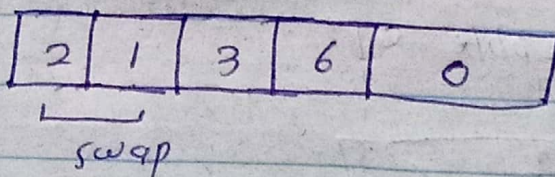
Question # 02 (A):

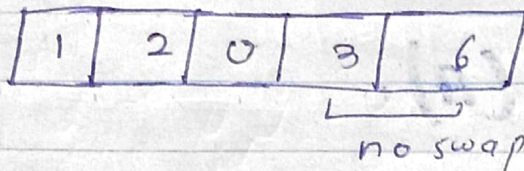
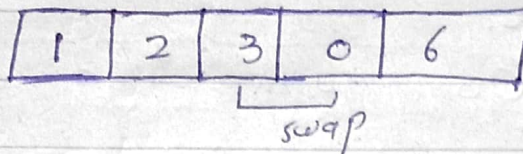
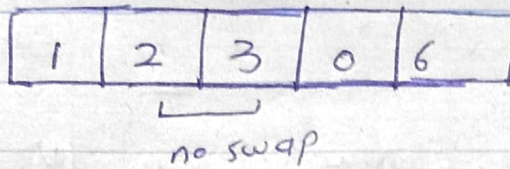
• Bubble sort

2, 3, 1, 6, 0

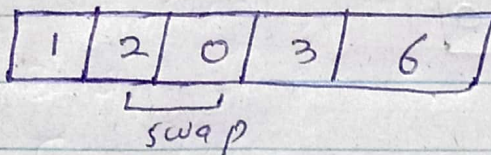
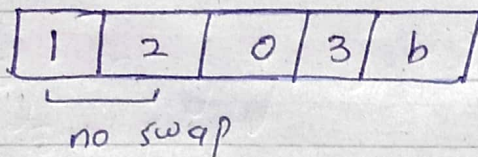


= finished sort

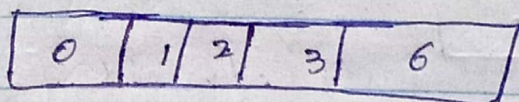
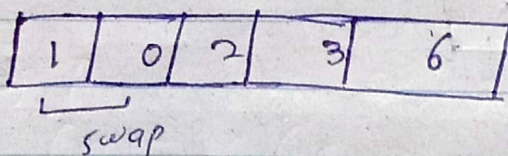




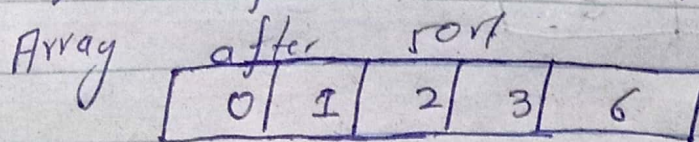
> finished second



= finished third



= finished fourth "bubble up"



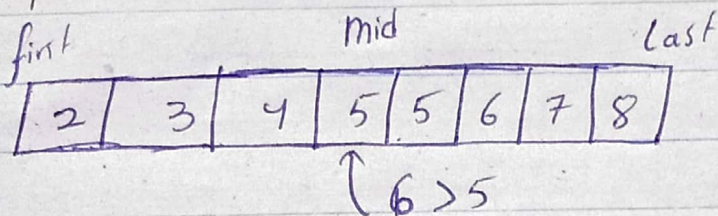
Question # 02 (B):

- Binary search

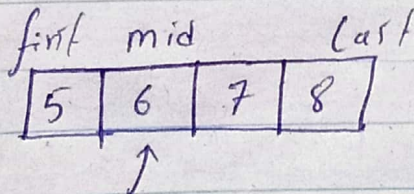
2, 3, 4, 5, 5, 6, 7, 8

Target = 6

step 1



step 2



In this case,

(`data[index] == value`)

return index;

Question # 2(c):-

- for big O of following code
for ($i=1$ to $5N$)
 for ($j=1$ to $6m$)
 print("hello")

solution,

Big O notation for the above
Code is

$$O(m \times n).$$