

1. Problem Statement:

Using only the first innings data in the given data set, find the best fit 'run production functions' in terms of wickets-in-hand w and overs-to-go u . Assuming that the model follows below curve.

$$Z(u, w) = Z_0(w)[1 - \exp\{-Lu/Z_0(w)\}] \quad (1)$$

Use the sum of squared errors loss function, summed across overs and wickets.

Note: your regression forces all slopes to be equal at $u = 0$. You should provide a plot of the ten functions, and report the (11) parameters associated with the (10) production functions, and the total error.

Dataset: ODI over-by-over data (Taken from the website <http://www.cricketaabstract.com>)

2. Solution

2.1) Data Pre-Processing

The given data file contains data on ODI matches from 1999 to 2011. The file contains 126768 rows and 38 column but we have to estimate our curve using I^{st} innings data only. So, after removing data of II^{nd} innings, the file contains 67794 rows and 38 columns only. To trace the above required curve we need the following data :

- 1) Wickets in hand (from column Wickets.in.Hand)
- 2) Over Remaining (from column Over)
- 3) Run scored (in remaining over) : after subtracting column Total.Runs from column Innings.Total.Runs

2.1) Curve Tracing Approach

I have used the following algorithm to generate the run production functions

Result: Parameter $Z \leftarrow$ list of 10 numbers , 1

Initialization : Intialize Z and l with some initial values;

while *While loss is not minimized* **do**

Predicted Run Score : Calculated using the curve

$Z(u, w) = Z_0(w)[1 - \exp\{-Lu/Z_0(w)\}]$ where Z and l are curve parameter and u is over.;

Loss : (Actual Run score - predicted Run score)² (Sum over all the data points);

Calculate new value of (Z and l) using some method such that the loss is minimized.;

update Z and l ;

end

Algorithm 1: Find curve parameter

To minimize the loss, I have used `scipy.optimize.minimize` function which takes the loss function, Z and l as input and produces the updated value of the parameter and total loss using these parameters.

3. Result

These are the values of the curve parameter Z and L :

The value of parameter L is : 11.54277498

The values of parameters Z are:

Z_0	10.713
Z_1	36.015
Z_2	64.032
Z_3	82.825
Z_4	103.622
Z_5	138.95
Z_6	170.237
Z_7	200.356
Z_8	241.810
Z_9	273.761

Total Loss : 147335263.72064668

Plots:

The plot of 10 functions is as below:

