

FLsp - a Surplus Production model in FLR

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1 Introduction

This package implements the surplus production described in Polacheck REF. At the moment only the model including observation error is implemented. The Pella Tomlinson shape is used (which defaults to Schaeffer) Tested against the three data sets in the paper. Accurate gradients and hessian are returned using automatic differentiation (implemented using ADOLC REF)

2 The Model

Following the Polacheck paper Assumptions: Observation error Only r and k are estimated σ and q are approximated as described in the paper The initial biomass is k

The general equation for the biomass through time is:

$$B_{y+1} = B_y + g(B_y) - C_y \quad (1)$$

where B is the stock biomass at the start of year y , C is the catch during the year and g is surplus production as a function of biomass.

Here we implement the Pella-Tomlinson form of surplus production:

$$g(B) = \frac{r}{p} B (1 - (B/K)^p) \quad (2)$$

where r is the intrinsic growth rate parameter and K is the average biomass level prior to exploitation. By default, p is set to 1 making the surplus production formulation the same as a Schaefer model.

The biomass is related to an index of abundance:

$$I_y = q B_y \quad (3)$$

Where I is an index of relative abundance in year y and q is the catchability coefficient.

Here we assume that errors are introduced through observation. The population dynamics are assumed to be deterministic and all of the error occurs in the relationship between stock biomass and the index of abundance. It is assumed that the error is multiplicative and log-normal with a constant coefficient of variation. The estimates of the model parameters are (B_0 , r , K and q) are obtained by maximising the likelihood function:

$$L = \prod \exp(\hat{v}_y^2 / (2\hat{\sigma}_v^2)) / (\sqrt{2\pi}\hat{\sigma}_v) \quad (4)$$

where the product is over all years for which CPUE data are available and:

$$\hat{v}_y = \log(C/E)_y - \log(\hat{C}/\hat{E})_y \quad (5)$$

$$\hat{\sigma}_v^2 = \sum \hat{v}_y^2 / n \quad (6)$$

where n is the number of data points.

The value of q which maximises the likelihood is given by:

$$\hat{q} = \exp\left(\frac{1}{n} \sum_y \log(I_y / \hat{B}_y)\right) \quad (7)$$

Following Polacheck et al B_0 is set to K . This means that only two parameters need to be estimated: r and K . In *FLsp* the estimation is performed using the *DEoptim* package REF.

3 The FLsp class

The *FLsp* class extends the *FLModel* class by including slots to store the catch and index time series. Catch is represented as an *FLQuant* and index is represented as an *FLQuants* object. This allows multiple indices to be used (not yet implemented).

To estimate the parameters r and K , an *FLsp* object must be created with catch and index data. The method *fitsp()* is then called. Once the object has been fitted, the biomass trajectory and other variables of interest (e.g. σ^2 and \hat{q} can be calculated).

4 Creating and fitting FLsp objects

Here we show how to create and fit a surplus production model using *FLsp*. The data set is New Zealand Rock Lobster, taken from Polcheck REF.

```
> # Load the library
> library(FLsp)
> # Load the New Zealand Rock Lobster data set
> data(nzrl)
> # This is a dataframe with year, catch and cpue
> # Take a look at the top of it
> head(nzrl)
> # Make FLQuant objects of the catch and cpue series
> catch <- FLQuant(nzrl$catch, dimnames=list(year=nzrl$year))
> index <- FLQuant(nzrl$cpue, dimnames=list(year=nzrl$year))
> # Create the FLsp object
> nzrl <- FLsp(catch=catch, index=index)
```

After creating our object we are ready to fit the parameters.

```
> nzrl <- fitsp(nzrl)
```

The published values for this data set are: $r = 0.0659$, $K = 129000$, $\hat{q} = 2.461\text{e-}5$, $\sigma = 0.207$, $B_{current} = 21150$. These can be compared to our results by interrogating the *FLsp* object.

```
> # Look at the fitted parameters
```

```
> params(nzrl)
```

```
An object of class "FLPar"
```

```
params
```

```
      r      k
```

```
4.9407e-02 1.4236e+05
```

```
units: NA
```

```
> # qhat
```

```
> qhat(nzrl)
```

```
An object of class "FLQuant"
```

```
, , unit = unique, season = all, area = unique
```

```
      year
```

```
quant 1
```

```
all 2.2126e-05
```

```
units: NA
```

```
> # sigma2
```

```
> sqrt(sigma2(nzrl))
```

```
An object of class "FLQuant"
```

```
, , unit = unique, season = all, area = unique
```

```
      year
```

```
quant 1
```

```
all 0.20695
```

```
units: NA
```

```
> # returns the full biomass timeseries
```

```
> biomass(nzrl)
```

```
An object of class "FLQuant"
```

```
, , unit = unique, season = all, area = unique
```

```
      year
```

```
quant 1945  1946  1947  1948  1949  1950  1951  1952  1953  1954
```

```
all 142355 141546 140732 139892 138652 136958 134542 132073 129221 125650
```

```
      year
```

```
quant 1955  1956  1957  1958  1959  1960  1961  1962  1963  1964
```

```
all 120837 116731 111222 107374 104231 101592 99267 96710 93659 90688
```

```
      year
```

```
quant 1965  1966  1967  1968  1969  1970  1971  1972  1973  1974
```

```
all 87717 84397 80799 77743 74512 71480 68540 65818 64071 62028
```

```
      year
```

```
quant 1975  1976  1977  1978  1979  1980  1981  1982  1983  1984
```

```
all 60114 58843 57237 55691 53948 51554 48988 46518 43734 40846
```

```
      year
```

```
quant 1985  1986  1987  1988  1989  1990
```

```
all 37374 33880 30498 27182 25141 422846
```

	New Zealand Rock Lobster		South Atlantic Albacore		Northern Namibian Hake	
Measure	FLsp	Published	FLsp	Published	FLsp	Published
r	0.0494	0.0659	0.32	0.328	0.37	0.379
K ('000 t)	142	129.0	243	239.6	2820	2772.6
σ	0.207	0.207	0.11	0.111	0.125	0.124
\hat{q}	2.21e-05	2.461e-05	0.264	0.2671	0.000427	4.360e-04
$B_{current}$	22.8	21.15	75	75.51	1660	1646.3
MSY	0	2133.74	0	19.65	0	263.2

Table 1: Comparing the published results with those from *FLsp* for three data sets.

It can be seen that there is good agreement between the published results and those generated with *FLsp*. The differences are likely caused by the precision of the printed data set in the Polcheck paper (REF) and the fitting method used.

5 Testing FLsp against the other data sets

The results fitted with *FLsp* are in good agreement with the published results.

6 Plotting results

There is no generic plot for FLsp at the moment. However, it is possible to look at the fitted index and residuals using relatively simple code. For example, to plot the indices with the fitted indices you can use (see Figure 1):

```
> fitted <- cbind(as.data.frame(nzrl@fitted_index),type="fitted")
> index <- cbind(as.data.frame(nzrl@index),type="index")
> index <- rbind(index,fitted)
> print(xyplot(data ~ year | qname, group=type, data=index, type="b",auto.key=TRUE))
```

To look at the residuals and put a loess function through them use (see Figure 2):

```
> residuals <- as.data.frame(nzrl@residuals_index)
> print(xyplot(data ~ year | qname, data = residuals, panel = function(x,
+   y) {
+     panel.xyplot(x, y)
+     panel.loess(x, y, span = 1)
+   }))
```

7 Profiling the fit

You can explore how good the fit is by looking at the likelihood profile. This is easily done by using the *profile()* method (see Figure 3).

Notice that the profile plot has a banana shaped flat section which contains the optimum solution. This is because the parameters r and K are correlated, making them difficult to estimate unless there is sufficient information in the data. The profile plot also includes the gradient of the log likelihood as r and K change

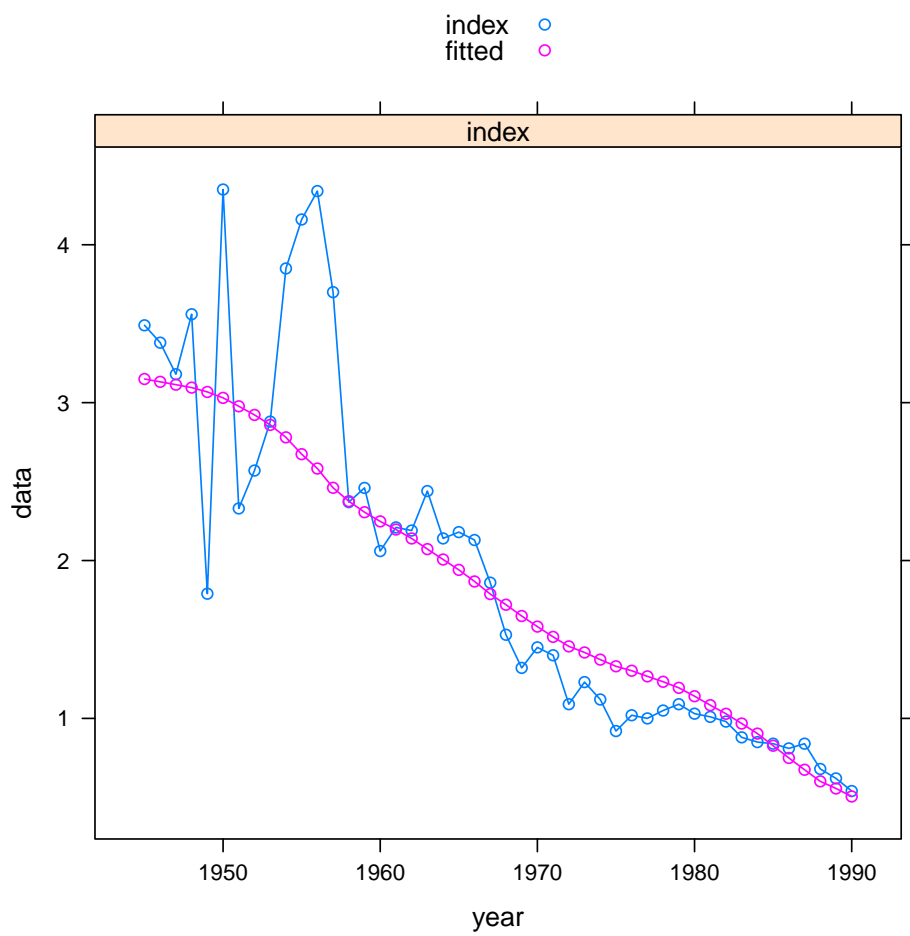


Figure 1: Indices and fitted indices for New Zealand rock lobster

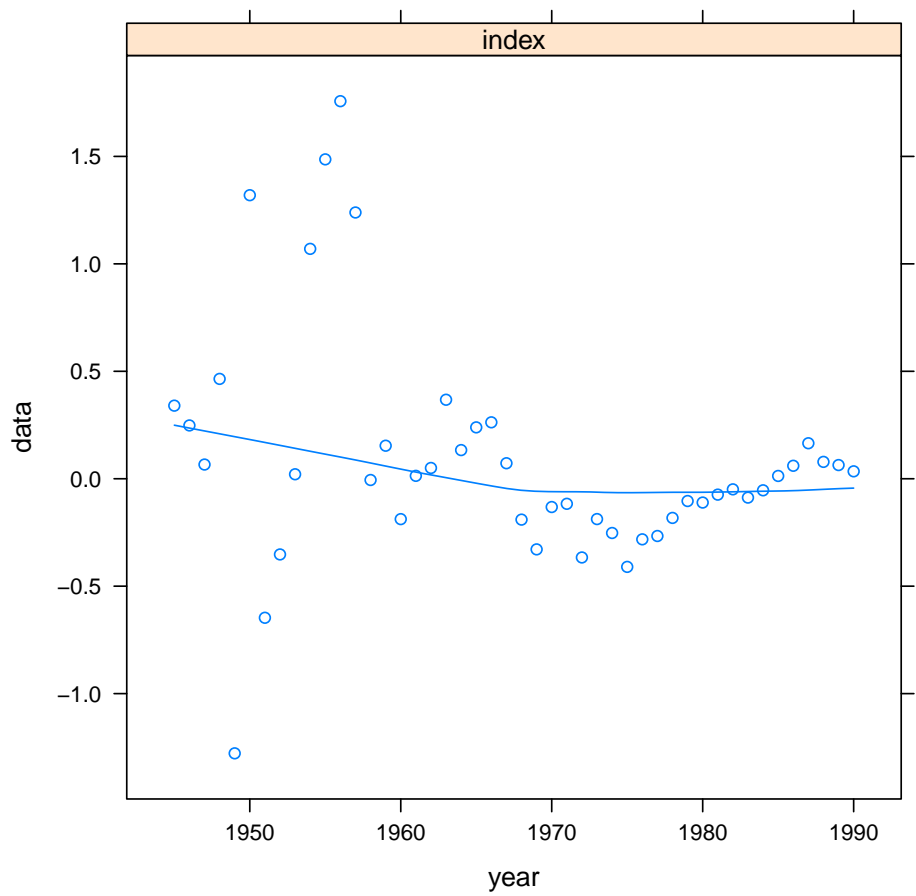


Figure 2: Residuals for New Zealand rock lobster

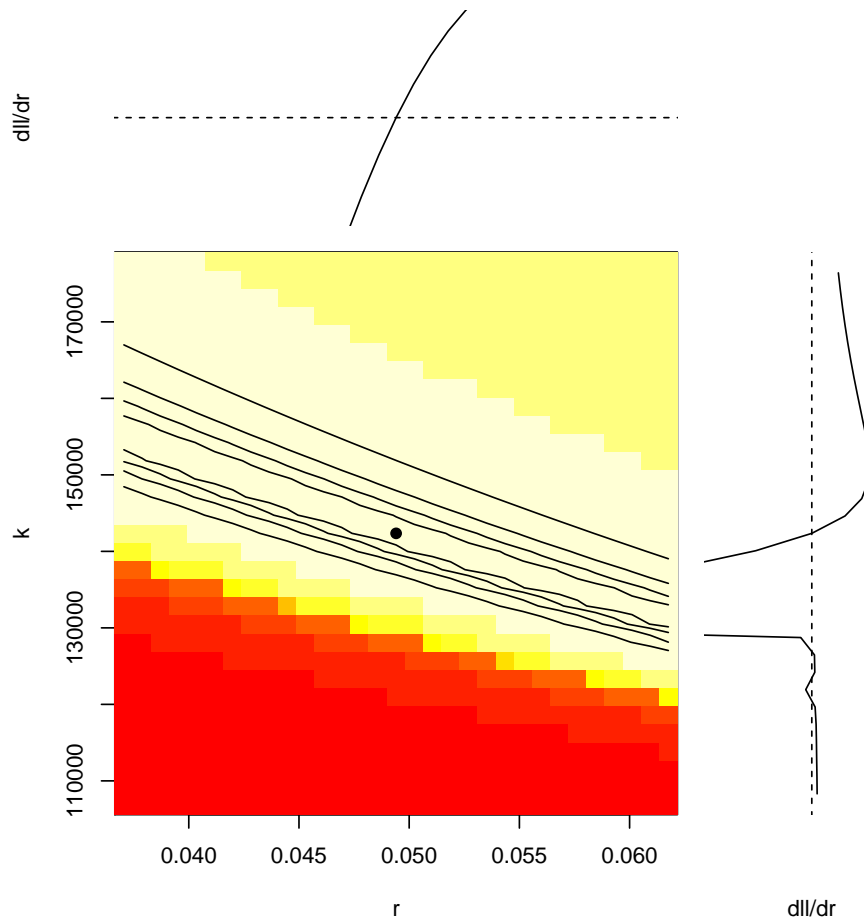


Figure 3: Profile plot for New Zealand rock lobster

(keeping K and r fixed at the estimated value found by the optimiser respectively). The dashed line is at a gradient of 0. If the fitting has worked, the gradient should be 0 at the estimated parameter values. It is just another simple way to check that the results of from the fitting process are sensible.

```
> profile(nzrl, maxsteps = 31, range = 0.25)
```

8 Uncertainty