



# using digital elevation models in glaciology

UNIS Glaciology Course

vår 2017



## Today's Topics

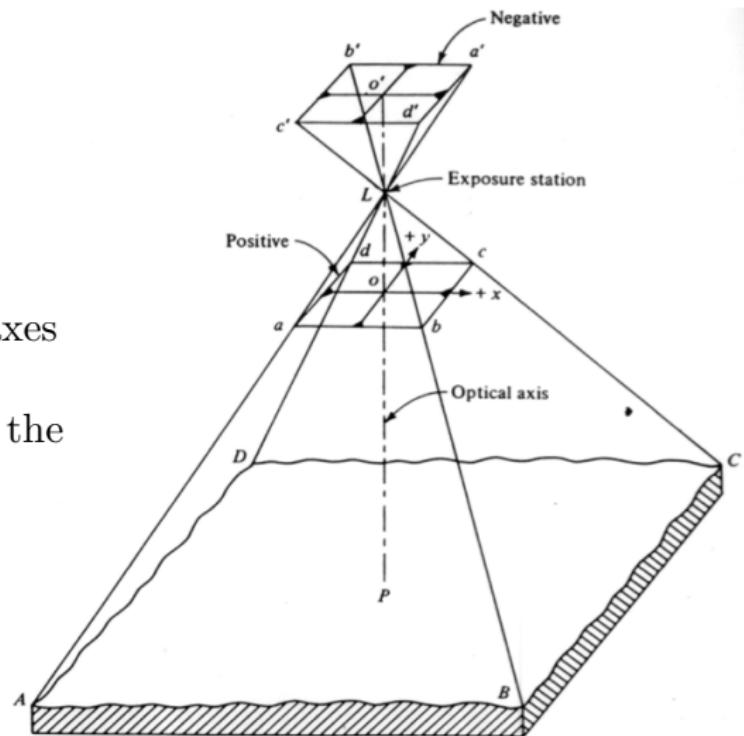
- ▶ principles of stereo photogrammetry
- ▶ dem co-registration
- ▶ dem differencing and geodetic mass balance
- ▶ uncertainty estimation

# what is photogrammetry?

- ▶ **photogrammetry**: the technique of obtaining reliable measurements of objects from photographs
- ▶ **stereo photogrammetry**: the technique of determining 3-D coordinates of points in photographs taken from different locations
- ▶ with stereoscopic images, we can obtain:
  - ▶ precise  $x, y, z$  locations
  - ▶ digital elevation models (**dems**), digital terrain models (**dtms**), digital surface models (**dsms**)
  - ▶ **orthophotos**

# image geometry

photographic coordinate axes  
 $x, y$  radiate from the  
principal point (center) of the  
photo



Wolf, DeWitt, Wilkinson, *Elements of Photogrammetry*



## measuring distance in images

can measure distances in photographs in several ways:

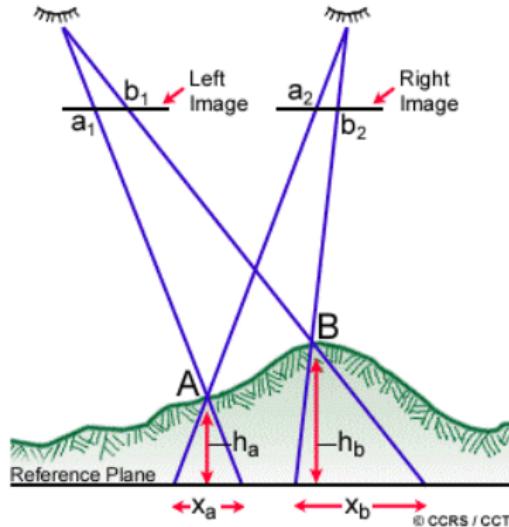
- ▶ comparing apparent size in image to known size on ground
- ▶ calculate scale based on camera properties, distance to target
- ▶ shadow length
- ▶ relief displacement

## parallax

with two cameras (or eyes), we can calculate **parallax**:

- ▶ apparent displacement in object position caused by shift in the position of observation
- ▶ depends on distance between observation point and object
- ▶ can use triangulation to determine distance to various objects
- ▶ can use stereo photos to measure topography

## calculating topography from stereo



- ▶  $x_a, x_b$  are the parallax shifts of  $a, b$
- ▶  $h_a, h_b$  are the heights of  $a, b$
- ▶ using baseline separation  $P$  of acquisition locations:

$$h_a = (H - h) \frac{x_a}{P + x_a},$$

where  $H - h$  is the aircraft height above the ground



## calculating topography from stereo images

in practice we no longer do this manually

- ▶ with two images, find and process **tie points**
- ▶ use correlation to find best matches
- ▶ use knowledge of camera/sensor parameters, orientation, positions
- ▶ as with velocities, contrast is good

## generating dems

can generate dems from single-camera images if we can change the viewing angle

- ▶ satellite imagery (e.g., ASTER, SPOT, Worldview, Planet)
- ▶ aerial photography
- ▶ structure from motion with aerial/terrestrial photos



## errors/uncertainty

sources of error and uncertainty in dems include, but are not limited to:

- ▶ satellite/sensor motion (**jitter**)
- ▶ inability to see features (i.e., snow/ice washes out image)
- ▶ resampling topography
- ▶ georeferencing errors

## dem differencing

- ▶ we want to use multiple dems of glaciers to estimate volume change, mass balance
- ▶ have to select dems separated enough in time to see signal
- ▶ separation depends on:
  - ▶ how much the surface is changing
  - ▶ how good our dems are
- ▶ typically,  $\sim 5$  years is a good rule

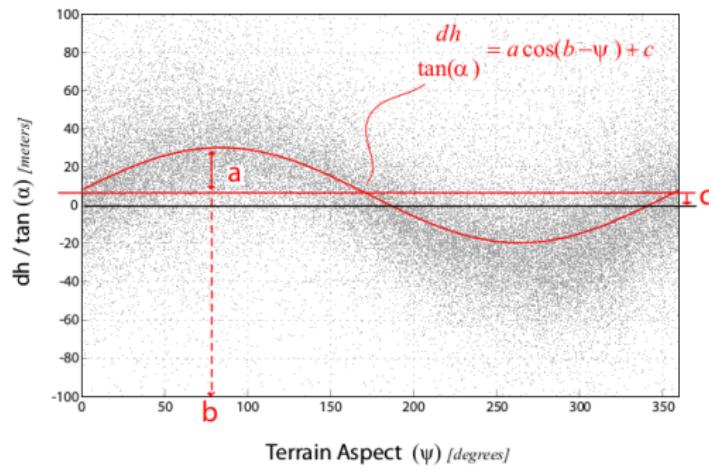
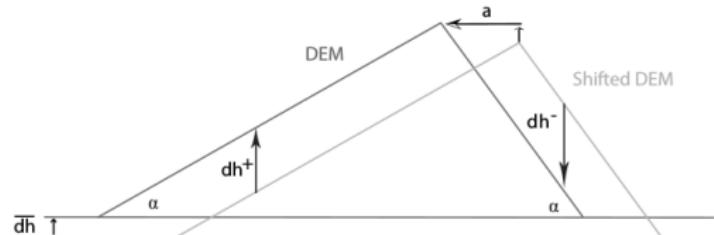


## co-registration

errors in co-registration can occur

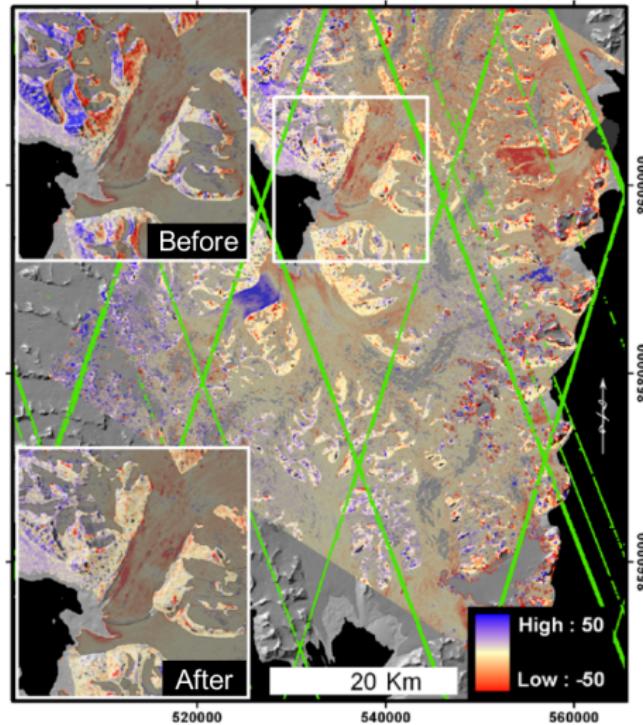
- ▶ these errors become very obvious in difference image
- ▶ dem difference map will resemble hillshade
- ▶ can use offsets, slope, aspect to co-register

## co-registration



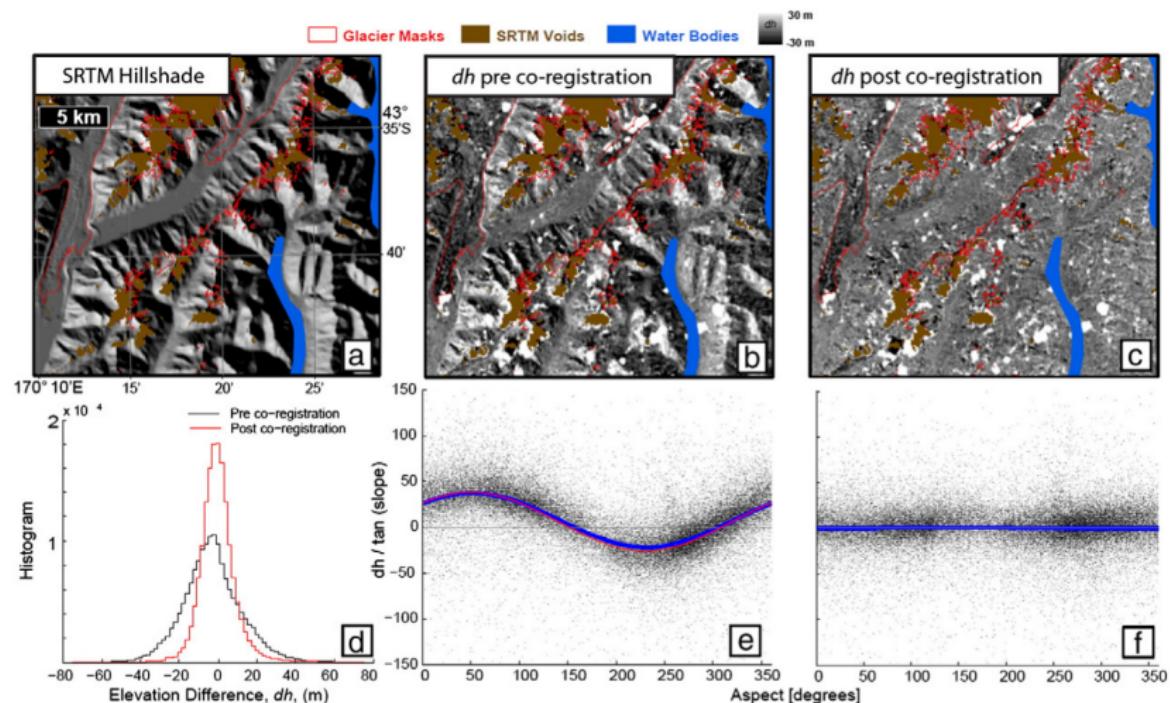
Nuth and Kääb, 2011

## co-registration



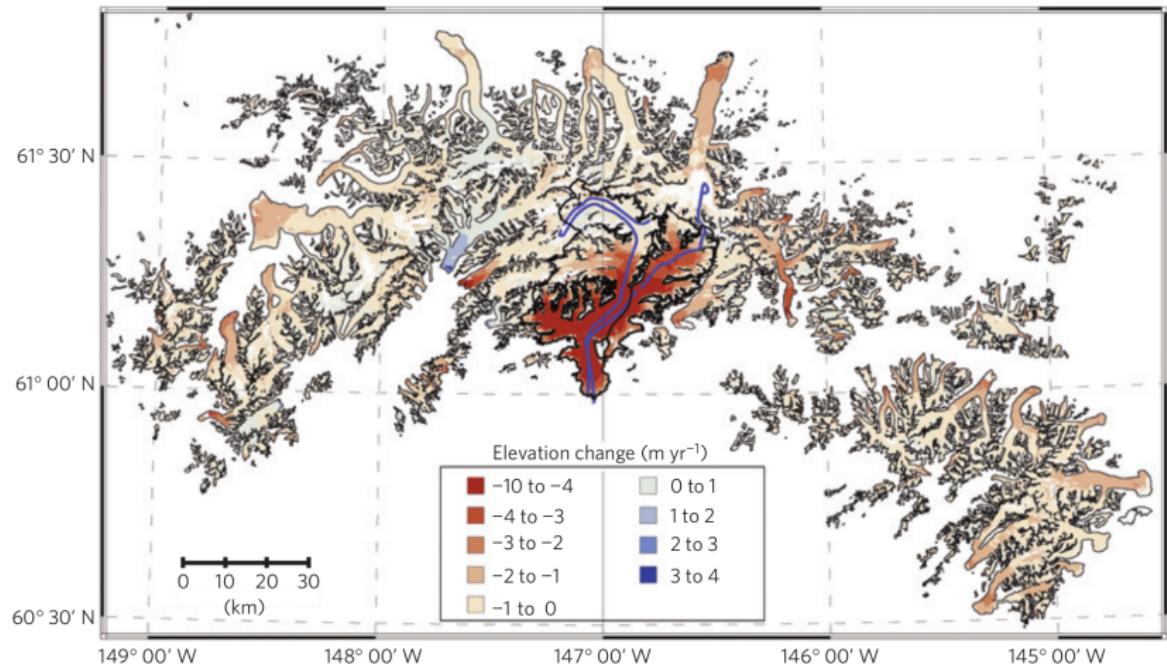
Nuth and Kääb, 2011

## co-registration



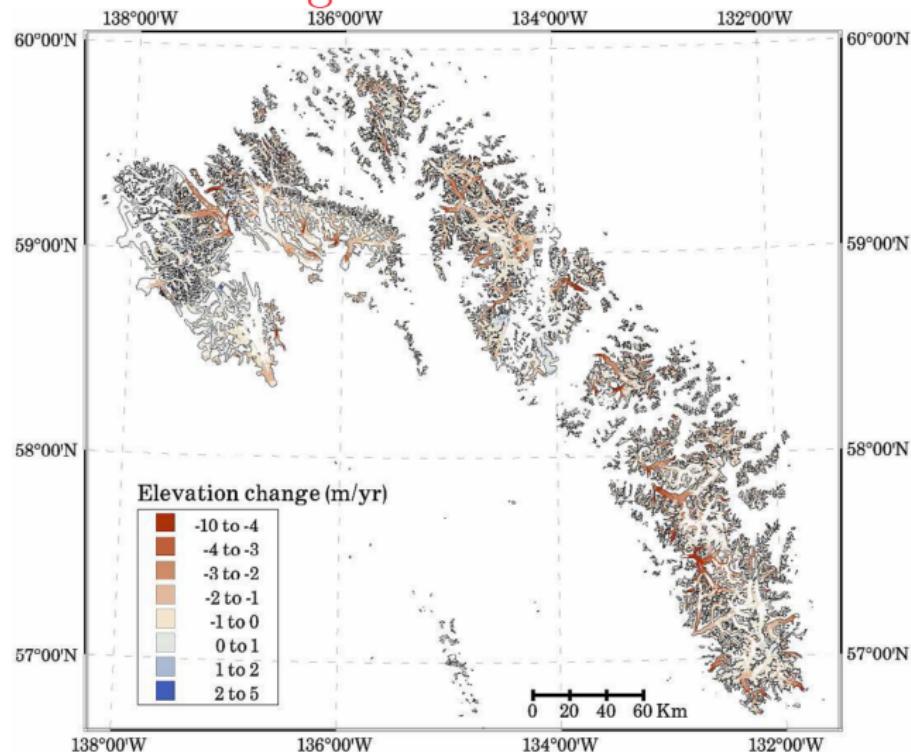
Paul et al., 2015

## glacier elevation changes



Berthier et al., 2010

## glacier elevation changes

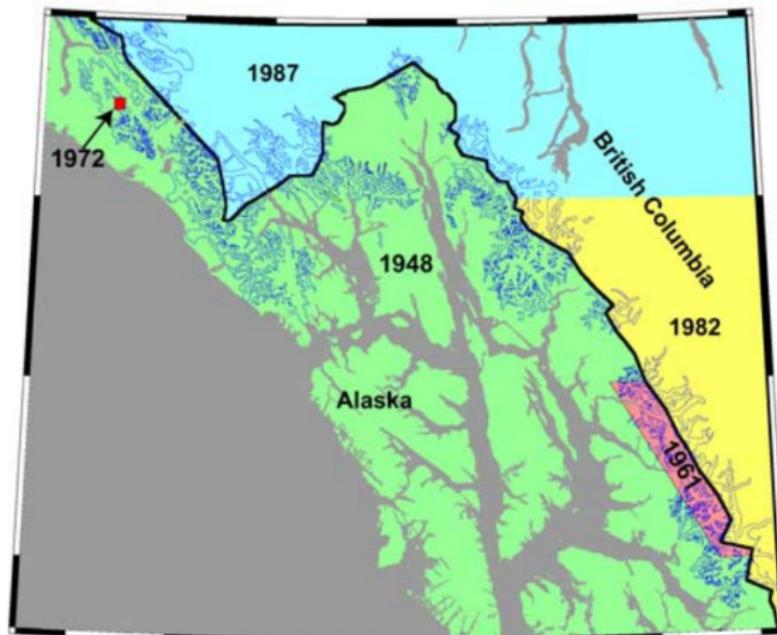


Berthier et al., 2010

## calculating volume changes from elevation changes

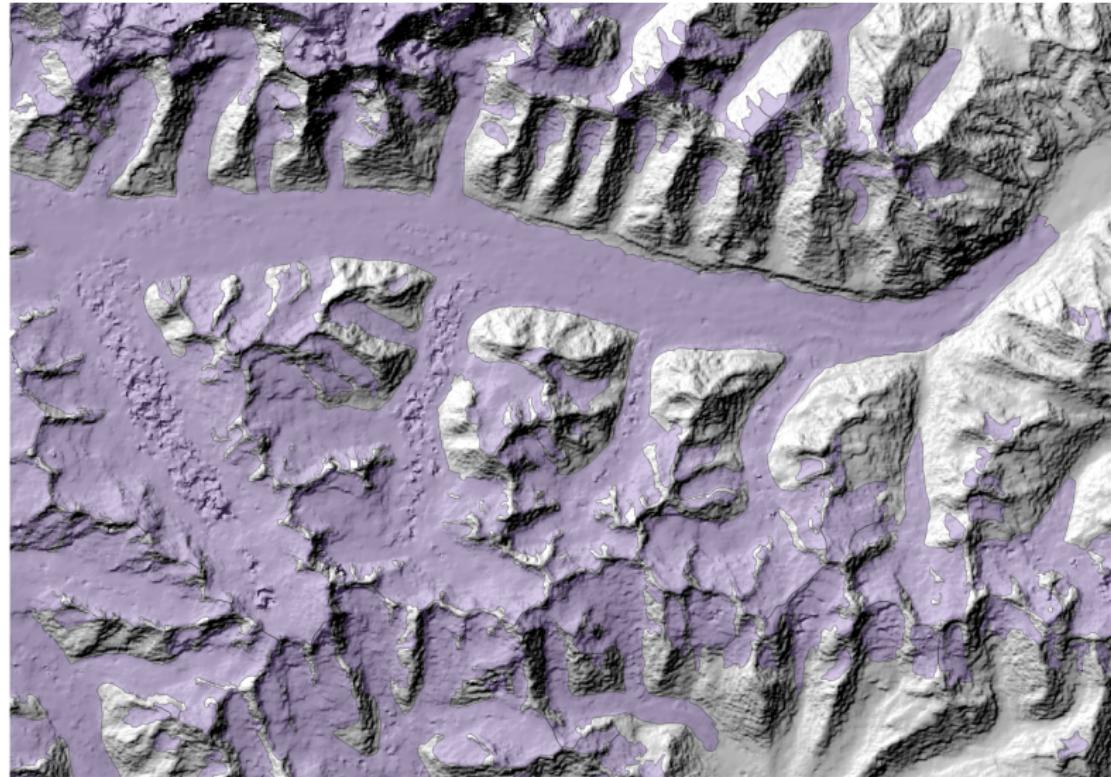
- ▶ dem differencing gives most straightforward way to estimate volume change of glaciers
- ▶ essentially, integrate elevation change map over glacier surface
- ▶ in practice, sum up  $dH$ , multiply by pixel area
- ▶ can still have errors

## handling temporally inconsistent data

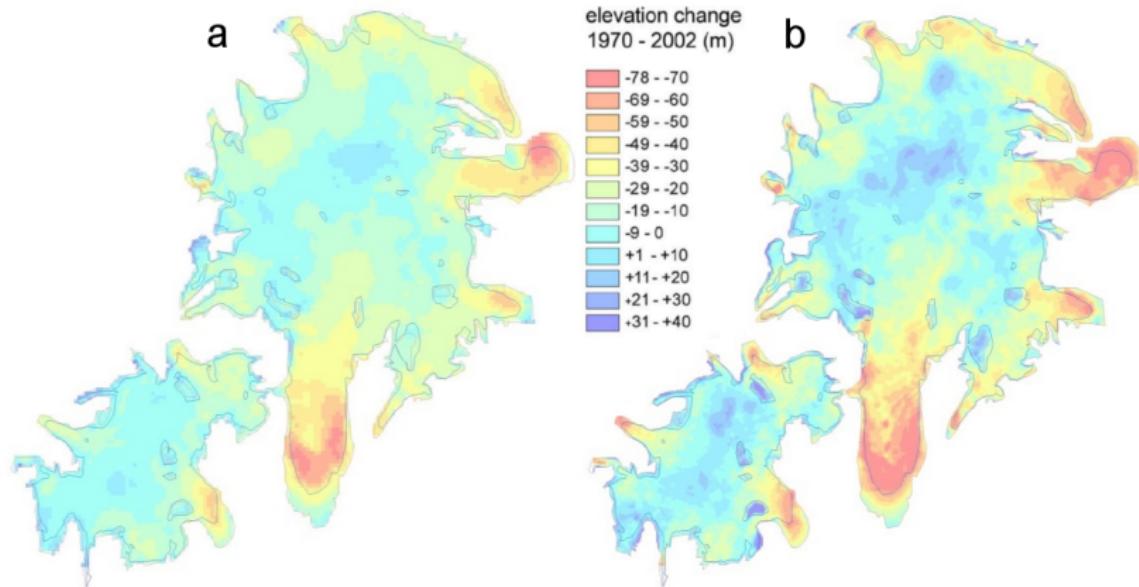


Larsen et al., 2007

## handling spatially incomplete data

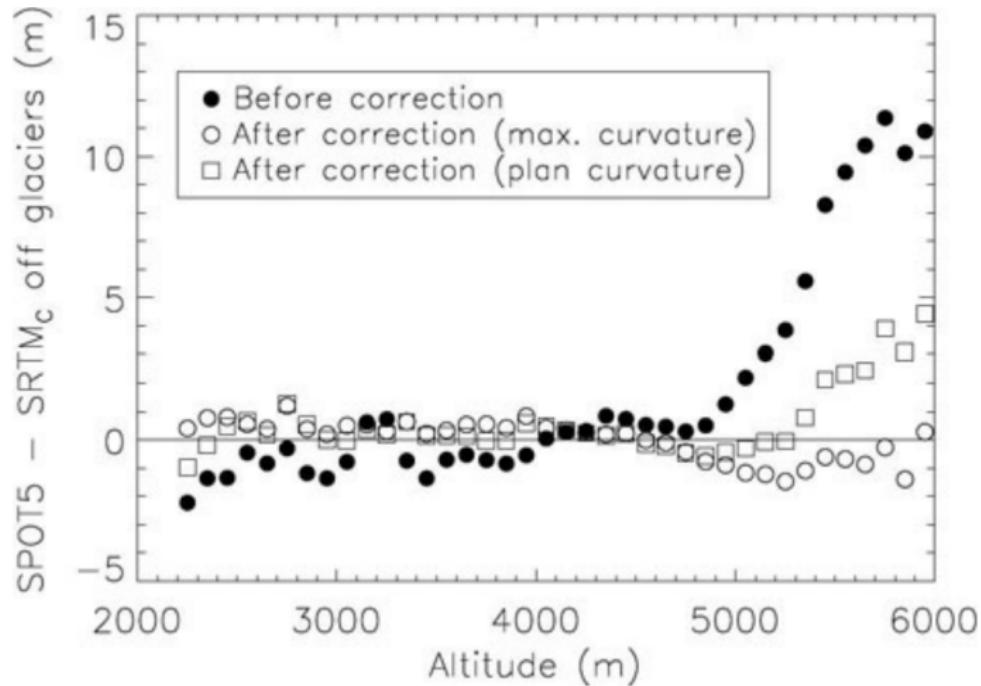


## handling spatially incomplete data



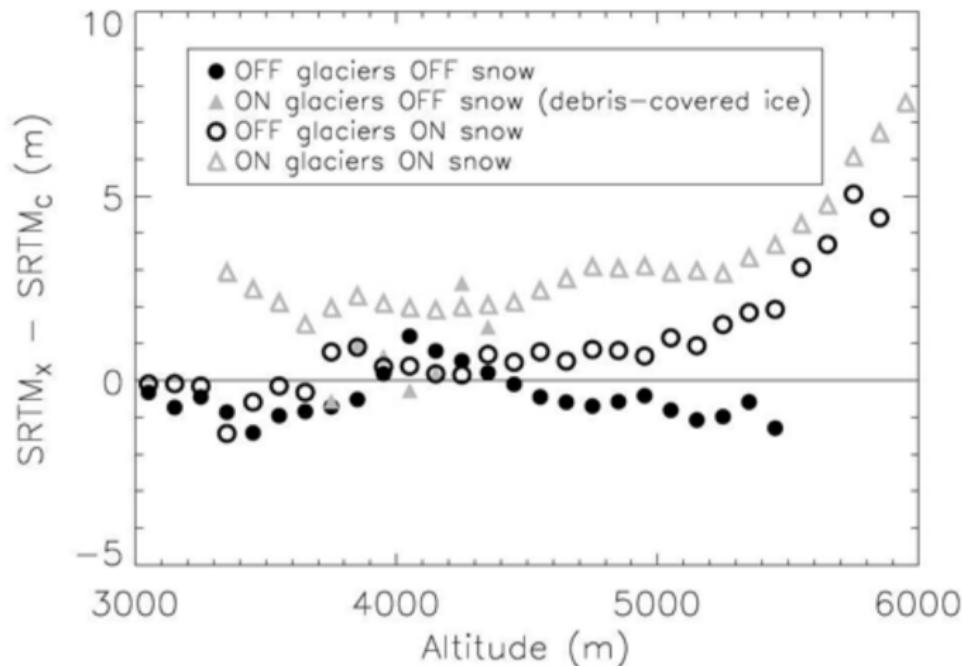
After Kääb, 2008

## curvature errors



Gardelle et al., 2012

# radar signal penetration



Gardelle et al., 2012



## estimating uncertainties

- ▶ compare to a high-resolution dem (if available)
- ▶ compare off-glacier elevations to ICESat elevations
- ▶ if no external data available, estimate RMSE in off-glacier areas from difference map



questions?