## Probability and random variables assignment

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## 1 Q 24

Abstract—This section provides the solution to Q24 of EX 15.1 in CBSE class 10th NCERT textbook of mathematics

- 1.1. A die is thrown twice. What is the probability that:
  - (i) 5 will not come up either time?
  - (ii) 5 will come up at least once?

## **Solution:**

Let  $X \in \{1, 2, 3, 4, 5, 6\}$  be a random variable representing the number obtained on the first throw of the dice.

Similarly, Let  $Y \in \{1, 2, 3, 4, 5, 6\}$  be a random variable representing the number obtained on the second throw of the dice.

For our case X is independent of Y.

**TABLE 1.1.1** 

Random variables	Value	Probability
X/Y	1	1/6
X/Y	2	1/6
X/Y	3	1/6
X/Y	4	1/6
X/Y	5	1/6
X/Y	6	1/6

(i) we are required to find  $P((X! = 5) \cap (Y! = 5))$  we know by Conditional probability that:

$$P(A \cap B) = P(A|B) \times P(B)$$
(1.1.1)
$$(1.1.2)$$

$$Let : P = P((X! = 5) \cap (Y! = 5))$$

$$\implies P = P(X! = 5) \times P(Y! = 5)$$
(1.1.4)
$$\implies P = (1 - P(X = 5)) (1 - P(Y = 5))$$
(1.1.5)

Inputting values in (1.1.4) from the table:

$$P = \left(1 - \frac{1}{6}\right) \left(1 - \frac{1}{6}\right) \tag{1.1.6}$$

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$$\implies P = \frac{25}{36} \tag{1.1.7}$$

(ii)

Since the event M(say) = "not getting 5 on either throw of dice" and event N(say) = "getting atleast one 5" are exhaustive events:

$$P(M) + P(N) = 1$$
 (1.1.8)

$$\implies P(N) = 1 - P(M)$$
 (1.1.9)

$$\therefore P(N) = \frac{11}{36} \tag{1.1.10}$$