# Iowa Social Science Research Center 2020-21 Workshop series

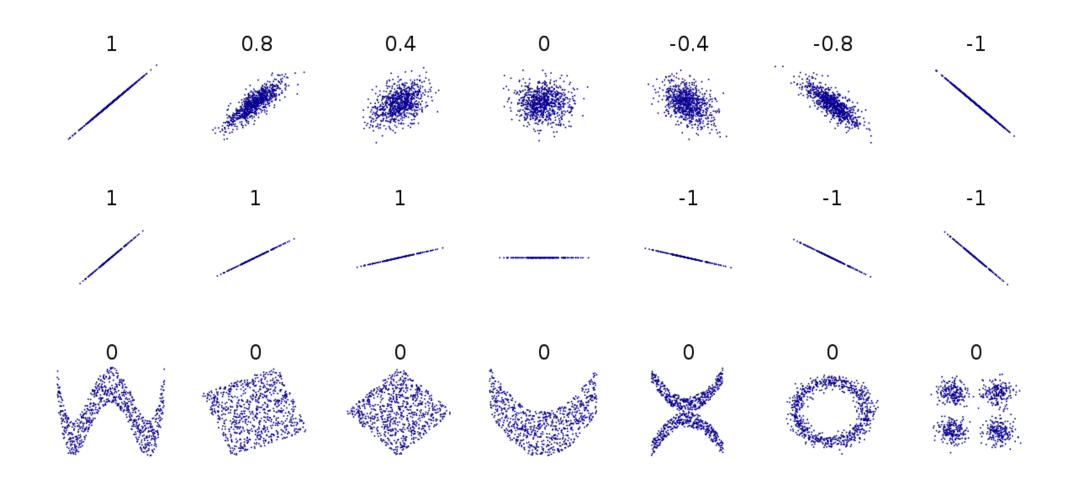


#### Advanced Spatial analysis with R

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Geographical and Sustainability Sciences

#### Correlation



#### Regression

 A set of statistical processes for estimating the relationships between a dependent variable and one or more independent variables

- Goals
  - Identify the statistically significant predictors
    - Education, Epidemiology,...
  - Prediction

# Ordinary Least Squares Regression (OLS)

- $y_i$  is the <u>response variable</u>
  - a.k.a. Dependent variable
- $x_i$  is the **explanatory variable** or **predictor variable** 
  - a.k.a. Independent variable

 We are using X to explain some or most of the variability of y, in particular, the non-random part of y's variability

#### Steps for linear regression

- Response variable
  - Type of variable
    - Continuous: Simple or multiple regression
    - Count data: Poisson regression or negative binomial regression
    - Binary: Logistic/Probit regression
  - Independent?
    - Study design
    - Ex) School, classroom, students
- Linear relationship between response and predictor(s)
  - Scatter plot

# Steps for linear regression (cont.)

- Predictor
  - Check multicollinearity
    - Correlation matrix
    - Variance Inflation Factor (VIF)
- Error
  - Normality
    - Q-Q plot
    - Shapiro-Wilk test
      - $H_0$ : The population is normally distributed
  - Heteroscedasticity
    - Plot (studentized) residuals vs. predicted y
    - Breusch-Pagan test
      - $H_0$ : Homoskedasticity
  - Autocorrelation
    - Plot
    - Burbin-Watson test

## The first law of geography

- Waldo Tobler
  - "Everything is related to everything else, but near things are more related than distant things."
- Spatial dependence
  - The co-variation of properties within geographic space
  - Weather map (Kriging)
  - Spatial autocorrelation

#### Back to regression analysis

- Response variable
  - Type of variable
    - Continuous: Simple or multiple regression
    - Count data: Poisson regression or negative binomial regression
    - Binary: Logistic regression
  - Independent? (Spatially independent?)
    - Study design
    - Ex) School, classroom, students

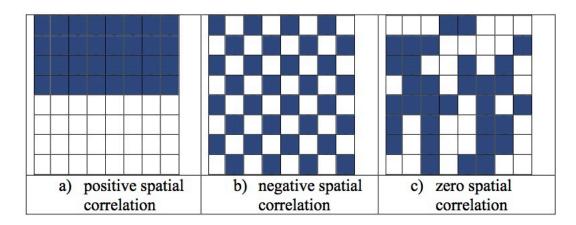
#### Back to regression analysis

#### • Error

- Normality
  - Q-Q plot
  - Shapiro-Wilk test
- Heteroscedasticity
  - Plot (studentized) residuals vs. predicted y
  - Breusch-Pagan test
- Autocorrelation (Spatial autocorrelation)
  - Plot
  - Burbin-Watson test

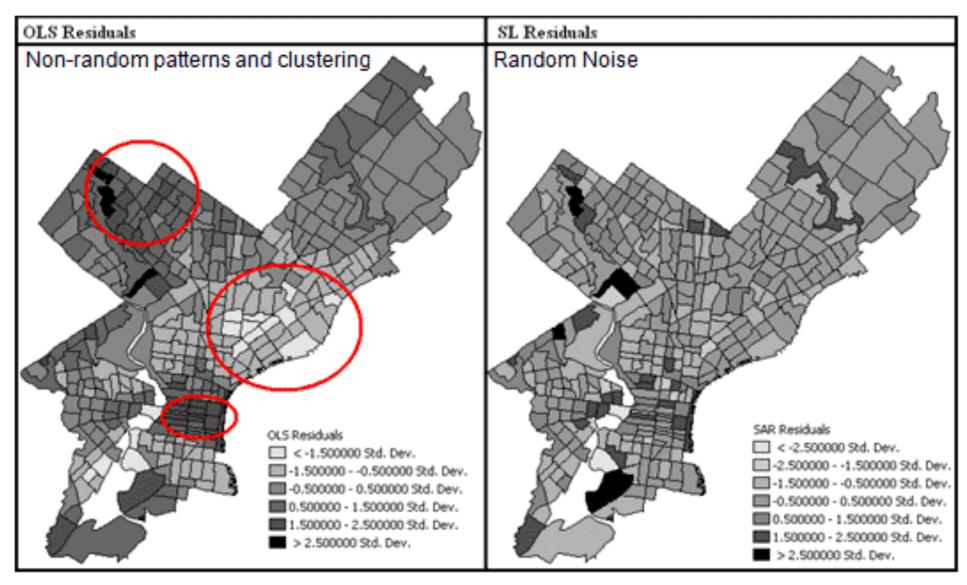
### Check Spatial dependence

- Moran's I
  - A measure of spatial autocorrelation



A summary statistic with p-value from bootstrapping

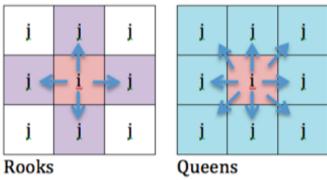
## Check Spatial dependence – residual map



### Spatial Weight matrix

- The spatial relationships that exist among the features in your dataset
- NxN matrix
- Two ways to determine neighbors
  - Rooks case
  - Queens case

**Spatial Weights Matrix** 



### Spatial regression models

#### Spatial Lag model

- Assumes that dependencies exist directly among the levels of the response variable
- Used when we know the structure of spatial dependence
- $Y = \rho WY + X\beta + \varepsilon$

#### Spatial Error model

- Error term has dependence
- Used when structure of dependence is unknown
- $Y = X\beta + \lambda W\varepsilon + \xi$

#### Data Structures

#### Vectors

- A 1-dimensional object that consists of indexed elements of the same data type
- Numeric / Character / Date / Logical / Factors
- X <- c(1, 2, 3, 4, ...)
- X[i]

#### Matrix

- A 2-dimensional object that consists of indexed elements of the same data type
- X[i, j]

#### Data Structures

- Data frame
  - A 2-dimensional object that consists of indexed elements
  - Elements within a given column are of the same type, but types may differ between columns.
  - x[i, j]
  - x[i,] ## Extract a row
  - x[, j] ## Extract a column

#### R Studio

