



## IMD0033 - Probabilidade Aula 14 - Distribuições de Frequência

Ivanovitch Silva Abril, 2019

## Agenda

- Tabelas de distribuição de frequências
- Ordenação de tabelas de distribuição de frequências (nominal, ordinal, intervalar, razão)
- Proporções e porcentagens
- Percentil e classificação de percentis
- Agrupamento de tabelas de distribuição de frequência
- Perda de informação



## Atualizar o repositório

git clone https://github.com/ivanovitchm/imd0033\_2019\_1.git

Ou ....

git pull



# PREVIOUSLY ON...

(1) collecting data (2) understanding its structure and how it's measured

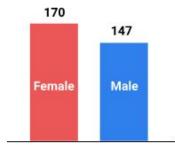


Id	Name	Salary	 Gender
1	Mary Ann	\$35 000	 Female
2	Marc Downey	\$55 000	 Male
 51	 Juliet Ali	\$45 000	 Female
 317	 Jane Ace	\$95 000	 Female

Understand how the data is **structured** and **measured** 







Visualize the patterns

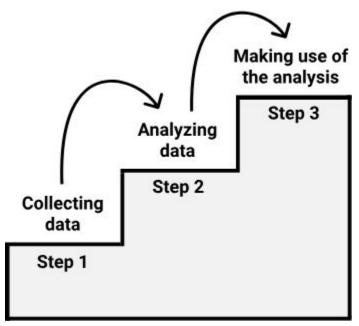
Gender	Frequency
Male	147
Female	170

Organize the data in comprehensible forms to find patterns

## Simplifying Data

We collect data to analyze it, and we analyze it for different purposes:

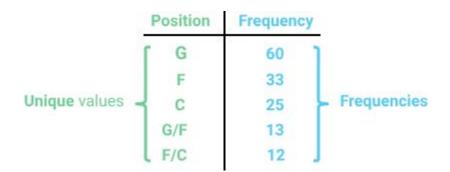
- To describe phenomena in the world (science).
- To make better decisions (industries).
- To improve systems (engineering).
- To describe different aspects of our society (data journalism); etc.





## Frequency Distribution Tables

Our capacity to understand a data set just by looking at it in a table format is limited



-	Name	Team	Pos	Height	Weight	BMI	Birth_Place	Birthdate	Age	College	Experience	Games Played	MIN
0	Aerial Powers	DAL	F	183	71.0	21.200991	US	January 17, 1994	23	Michigan State	2	8	173
1	Alana Beard	LA	G/F	185	73.0	21.329438	US	May 14, 1982	35	Duke	12	30	947
2	Alex Bentley	CON	G	170	69.0	23.875433	US	October 27, 1990	26	Penn State	4	26	617
3	Alex Montgomery	SAN	G/F	185	84.0	24.543462	US	December 11, 1988	28	Georgia Tech	6	31	721
4	Alexis Jones	MIN	G	175	78.0	25.469388	US	August 5, 1994	23	Baylor	R	24	137





## Sorting Frequency Distribution Tables

```
wnba.Pos.value counts()
        60
        33
        13
        12
      Pos, dtype:
Name:
                    int64
       Nominal Scale
```

```
1 wnba.Height.value counts()
188
        20
193
        18
                How many players are under
175
        16
                170 cm?
185
        15
                How many players are very tall
191
        11
                (over 185)?
183
        11
                Are there any players below
173
        11
                160 cm?
196
178
180
                      Ratio Scale
170
         6
198
                       We can tell the
201
168
                   direction of difference
206
165
Name: Height, dtype: int64
```

## Sorting Tables for Ordinal Variables

The sorting techniques learned in the previous screen can't be used for ordinal scales where the measurement is done using words.

Condition	Label		
points <= 20	very few points		
20 < points <= 80	few points		
80 < points <= 150	many points		
points > 150	a lot of points		

	Name	PTS	PTS_ordinal_scale
0	Aerial Powers	93	many points
1	Alana Beard	217	a lot of points
2	Alex Bentley	218	a lot of points
3	Alex Montgomery	188	a lot of points
4	Alexis Jones	50	few points

## Sorting Tables for Ordinal Variables

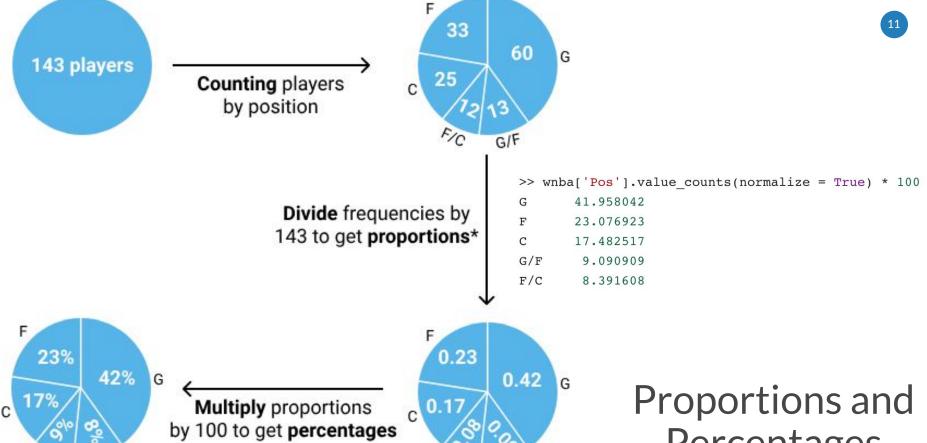
```
>> wnba['PTS ordinal scale'].value counts()
a lot of points
                   79
few points
                   27
many points
                   25
                   12
very few points
dtype: int64
>> wnba['PTS ordinal scale'].value counts().sort index()
a lot of points
                    79
few points
                    27
many points
                   25
                    12
very few points
dtype: int64
```



## Sorting Tables for Ordinal Variables

```
>> wnba['PTS ordinal scale'].value counts()
a lot of points
                   79
few points
                  27
many points
                  25
                  12
very few points
dtype: int64
>> wnba['PTS ordinal scale'].value counts().iloc[[3, 1, 2, 0]]
very few points
                   12
few points
                   27
many points
                   25
a lot of points
                   79
dtype: int64
```





G/F

## Percentages



#### Percentiles and Percentile Ranks

```
percentages = wnba['Age'].value counts(normalize = True).sort index() * 100
  2 percentages
21
        1.398601
22
        6.993007
23
      10.489510
                          19% of the ages
                                                          "What percentage of players are
24
      11,188811
                         in the dataset are
25
      10.489510
                           23 or lower
                                                          23 years or younger?"
26
        8.391608
                                       A • means 0.7%
27
        9.090909
28
        9.790210
29
        5.594406
30
        6.293706
31
        5.594406
                                                                                                       years
32
        5.594406
                                    23
                                                              30
                                                                                     36
                         20
                            21
                                                                                                    40
33
        2.097902
        3.496503
34
                                        23 has a percentile rank
35
        2.797203
                        Minimum age
                                        of 19%. This means 23 is
                                                                                Maximum age
36
                        in our data set
                                          the 19th percentile.
                                                                                in our data set
        0.699301
```

#### Percentiles and Percentile Ranks

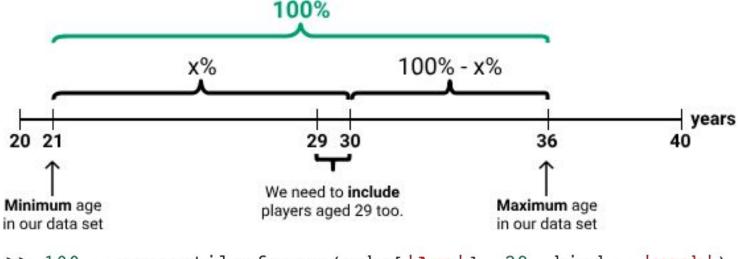
"What percentage of players are 23 years or younger?"

```
>> from scipy.stats import percentileofscore
>> percentileofscore(a = wnba['Age'], score = 23, kind = 'weak')
18.88111888111888
```



#### Percentiles and Percentile Ranks

"What percentage of players are 30 years or older?"



>> 100 - percentileofscore(wnba['Age'], 29, kind = 'weak')
26.573426573426573



## Finding Percentiles with Pandas

```
>> wnba['Age'].describe()
         143,000000
count
          27.076923
mean
           3.679170
std
min
          21.000000
25%
          24.000000
50%
          27.000000
75%
          30.000000
          36.000000
max
Name: Age, dtype: float64
```

```
>>wnba['Age'].describe().iloc[3:]
min 21.0
25% 24.0
50% 27.0
75% 30.0
max 36.0
Name: Age, dtype: float64
```



## Finding Percentiles with Pandas

```
>> wnba['Age'].describe(percentiles = [.1, .15, .33, .5, .592, .85, .9]).iloc[3:]
           21.0
min
10%
           23.0
15%
           23.0
                                        0%
                                                      25%
                                                                    50%
                                                                                 75%
                                                                                              100%
33%
           25.0
50%
           27.0
                                            25% of ages
                                                         50% of ages
                                                                       75% of ages
                                                                                    100% of ages
                                           are 24 or less
                                                         are 27 or less
                                                                       are 30 or less
                                                                                    are 36 or less
59.2%
           28.0
85%
           31.0
                                                      24
                                                                    27
                                                                                 30
                                                                                               36
90%
           32.0
           36.0
max
                                     Minimum age
                                                                                          Maximum age
                                     in our data set
                                                                                          in our data set
Name: Age, dtype: float64
```



## **Grouped Frequency Distribution Tables**

```
>> wnba['Weight'].value counts(bins = 10).sort index()
(54.941, 60.8]
                     5
(60.8, 66.6)
                    21
(66.6, 72.4]
                    10
(72.4, 78.2]
                    33
                              5.8
(78.2, 84.0]
                    31
                                60.8
                                      66.6
                                            72.4
                                                  78.2
                                                        84.0
                                                              89.8
                                                                    95.6
                                                                          101.4 107.2
                    24
(84.0, 89.8)
(89.8, 95.6]
                    10
                                                        58 kg
(95.6, 101.4]
                     3
(101.4, 107.2]
(107.2, 113.0]
```



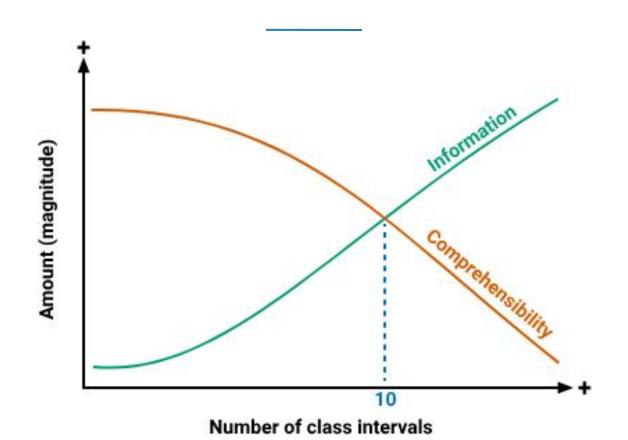
#### **Information Loss**

```
>> wnba['PTS'].value counts(bins = 10)
(1.417, 60.2]
                   30
(60.2, 118.4)
                   24
                   17
(118.4, 176.6)
                            wnba['PTS'].value counts(bins = 5).sort index()
(176.6, 234.8)
                   20
                            (1.417, 118.4]
                                              54
                   17
(234.8, 293.0]
                            (118.4, 234.8)
                                              37
(293.0, 351.2]
                            (234.8, 351.2]
                                              25
(351.2, 409.4)
                   10
                            (351.2, 467.6)
                                              18
(409.4, 467.6]
                    8
                            (467.6, 584.0]
                                               9
(467.6, 525.8)
(525.8, 584.0)
```

Name: PTS, dtype: int64

 $\langle \rangle$ 

### **Information Loss**





## Readability for Grouped Frequency Tables

```
wnba['PTS'].value counts(bins = 5).sort index()
(1.417, 118.4)
                   54
                                    (0,100]
                                                   49
                   37
(118.4, 234.8]
(234.8, 351.2]
                   25
                                    (100,200)
                                                   28
                   18
                                    (200,300)
(351.2, 467.6]
                                                  32
(467.6, 584.0)
                    9
                                    (300,400]
                                                   17
                   int64
Name: PTS, dtype:
                                    (400,500)
                                                   10
                                    (500,600]
```



## Readability for Grouped Frequency Tables

```
>> intervals = pd.interval range(start = 0, end = 600, freq = 100)
>> intervals
IntervalIndex([(0, 100], (100, 200], (200, 300], (300, 400], (400, 500], (500, 600]]
               closed='right',
               dtype='interval[int64]')
                                                                          >> gr freq table
                                                                          (0, 100)
                                                                                       49
                                                                          (100, 200)
                                                                                       28
>> qr freq table = pd.Series([0,0,0,0,0,0], index = intervals)
                                                                          (200, 300]
                                                                                       32
>> gr freq table
                                                                          (300, 400]
                                                                                       17
(0, 100)
                         >> for value in wnba['PTS']:
                                                                          (400, 500]
                                                                                       10
(100, 200)
                                 for interval in intervals:
                                                                          (500, 6001
                                                                                        7
(200, 300]
                                     if value in interval:
(300, 400]
(400, 500]
                                          gr freq table.loc[interval] += 1
(500, 600)
                                          break
dtype: int64
```

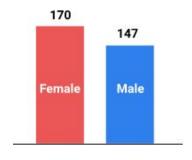


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