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DATA MINING IN DER MEDIZIN**



Bachelor Thesis
in Computer Science

Attention in Mixed-Type Clustering

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Declaration of Authorship

I hereby declare that the thesis submitted is my own unaided work. All direct or indirect sources used are acknowledged as references.

This paper was not previously presented to another examination board and has not been published.

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Abstract

This document serves as a model for the development of a thesis at the Department of Database Systems at the Institute for Computer Science at the LMU Munich. The abstract should not contain more than 300 words.

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Chapter 1

Introduction

1.1 Introduction

Clustering is an unsupervised machine learning method that groups similar observations together. Due to its ability to find patterns in an unlabeled dataset, it's an essential task in Data Mining and Knowledge Discovery. A *cluster* is a group of similar observations that belongs to a *centroid* (center point of a cluster). Distance-based clustering algorithms use distance measures such as Euclidean distance to calculate the similarity of datapoints. Hierarchical methods partition the observations and merge (agglomerative) or split them into bigger or smaller clusters. Many other methods exist, but this work focuses on methods for clustering *mixed-type* data. [1]

1.2 k-means

The most well known distance-based clustering method is k-means [5]. The goal is defined as follows: Suppose we have a finite set of n observations $S = \{p_1, p_2, \dots, p_n\} \in \mathbb{R}^m$ for a dataset with m features, the target of k-means is to find $k(\leq n)$ optimal centroids $B = \{b_1, b_2, \dots, b_k\} \subseteq \mathbb{R}^m$ that minimize the sum of the squared Euclidean distance of each point in S to its nearest centroid. Formally

$$\sum_{i=1}^n d(p_i, B)$$

has to be minimized, where d is the Euclidean distance from a point $p_i \in S$ to the nearest centroid in B ; $d(p_i, B) = \min_{1 \leq j \leq k} d(p_i, b_j)$ [6]. The Euclidean distance between two points p and q in an n -dimensional Euclidean space is

defined as

$$d(p, q) = \|p - q\| = \sqrt{(p_1 - q_1)^2 + (p_2 - q_2)^2 + \dots + (p_n - q_n)^2}$$

Finding the optimal centroids is a NP-hard problem, even for $d = 2$, as shown by Mahajan et al. [6]. The most common algorithm used for the k-means problem is a iterative refinement technique proposed by Lloyd [4]. It is defined as follows:

1. Randomly set k initial cluster centroids $b_1^{(1)}, \dots, b_k^{(1)}$.
2. Assign each obseration p_i to the nearest centroid using squared Euclidean distance. This splits our observations into S into k sets $\{S_1^{(t)}, \dots, S_k^{(t)}\}$.
3. Recalculate the optimal position of each centroid using the mean distance to each observation assigned to the centroid:

$$b_i^{(t+1)} = \frac{1}{|S_i^{(t)}|} \sum_{p_j \in S_i^{(t)}} p_j$$

4. Repeat steps 2. and 3. until the centroid assignments no longer change.

1.3 Mixed-type data

In many real-world scenarios, besides continuous, numerical data, *categorical* data exists. While Euclidean distance or other distance measures work well with continuous data, categorical data is different. Suppose we have categories $\{A, B, C\}$ of a given feature, we would encode them into numeric values to allow for computation of a distance measure:

$$\{A, B, C\} \equiv \{1, 2, 3\}$$

While A and C can share the same semantic similarity as A and B , numerically category A and Category C are now $|1 - 3| = 2$ apart, while Category A and B are only $|1 - 2| = 1$ apart. During clustering, this could lead to observations being assigned to centroids based on a wrong distance assumption.

A possible solution is to use *one-hot encoding*, also known as *dummy coding* in classical statistics. One-hot encoding turns a discrete feature containing k mutually exclusive categories into a vector x of length k , in which only one of the elements x_k equals 1 and all remaining elements equal 0 [2]. For an observation B of a feature having $k = 3$ separate categories $\{A, B, C\}$, the one-hot vector x would be represented by $x = (0, 1, 0)^\top$.

1.3.1 k-modes

According to Huang [3], one-hot encoding has two drawbacks:

1. In real-world applications, categorical features with hundreds or thousands of categories are encountered. This would result in a large number of binary features in the one-hot encoded representation, which will increase cost and space of computation.
2. The centroid value of a certain one-hot encoded feature, given by a real value between 0 and 1, cannot indicate the characteristics of the according cluster, since the feature only describes the presence or absence of one category.

1.4 Methodology

In this work we use 8 mixed-type datasets from the UC Irvine Machine Learning Repository [7]. All observations containing missing values were removed. Categorical columns were standardized by removing the mean and scaling to unit variance, using the scikit-learn Python API [8]. The standardized score z of a sample x from a feature is calculated as:

$$z = \frac{(x - \mu)}{\sigma}$$

where μ is the mean of the samples x_1, \dots, x_N from a feature of length N , defined as

$$\mu = \frac{1}{N} \sum_{i=1}^N x_i$$

and σ is the standard deviation of the samples of a feature, defined as

$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2}$$

| | Naive k-means | k-means one-hot | k-prototypes | Gower distance |
|-----------------|-----------------|-----------------|-----------------|----------------|
| Soybean Disease | 0.679950 | 0.674068 | 0.694658 | 0.669526 |
| Heart Disease | 0.198871 | 0.193008 | 0.153387 | 0.140792 |
| Breast Cancer | 0.748214 | 0.734909 | 0.587960 | 0.537113 |
| Bank Marketing | 0.017640 | 0.029666 | 0.017566 | 0.000356 |
| Census Income | 0.072767 | 0.146271 | 0.022475 | 0.000507 |
| Credit Approval | 0.225376 | 0.161375 | 0.114664 | 0.003465 |

Figure 1.1: Comparison of Normalized Mutual Information (NMI) of classical methods on clustering mixed-type data. Naive k-means and k-means with one-hot encoding were calculated 100 times and the average NMI was taken. After calculating the Gower distance matrix, Agglomerative Clustering with average linkage between sets of observation was used. Due to high runtime and memory consumption, the "Bank Marketing" and "Census Income" datasets were downsampled to the first 2000 instances.

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