

Correlations

Correlations is the relationship between any two random variables

They can be described in different ways:

Pearson—linear relationship between continuous variables



two variables as a monotonic function







Correlations in MATLAB



corr — returns a matrix of pairwise correlations between columns



corrcoef — Returns the correlation between vectorized matrices

corr2 — returns correlation coefficient for matrices (i.e., one value for its 2-d inputs)





Reminder: Reshape can help you

Reshape is a useful function to transform any sized matrix into a different shape

Reshape(X, [new dimensions])

Note that the new dimensions need to be consistent with the previous ones i.e., dim1*dim2*dim3 == newdim1*newdim2 etc..













Student t-test allows you to test mean differences between normal distributions

There are many different **flavours** of t's

- one-sample vs two samples
- paired vs unpaired
- one tail vs two



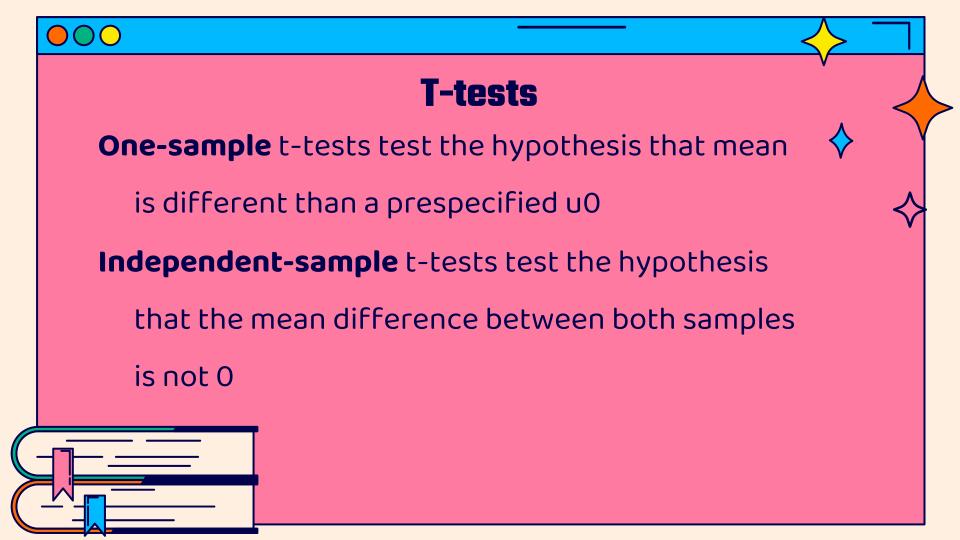


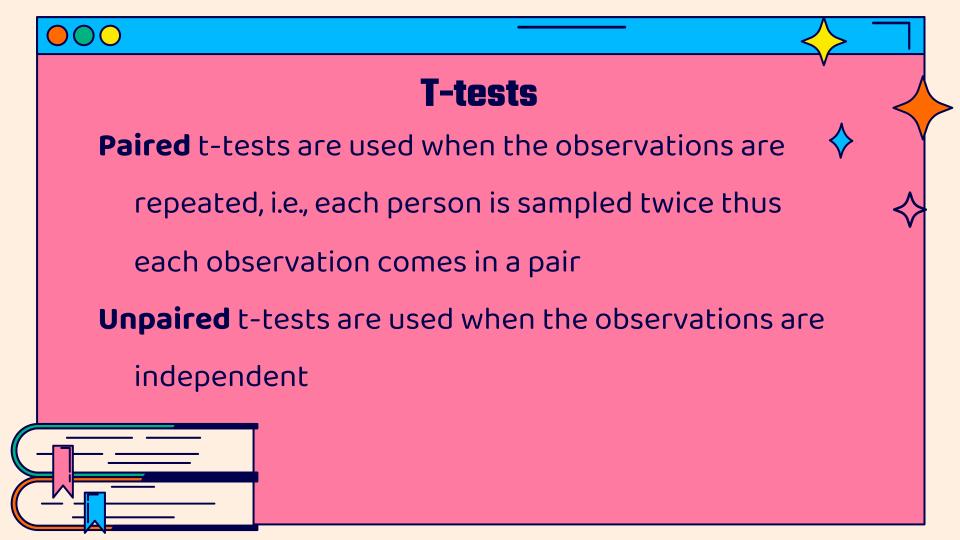


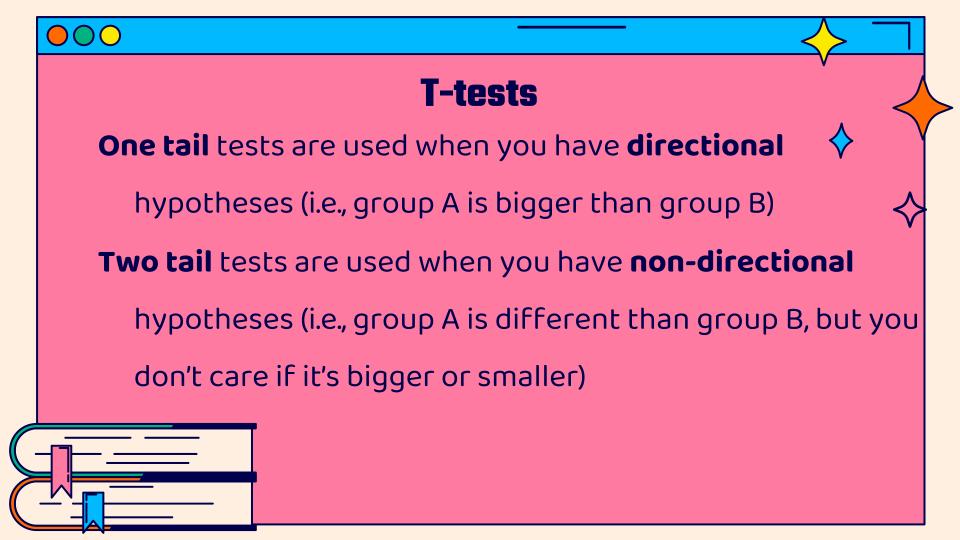


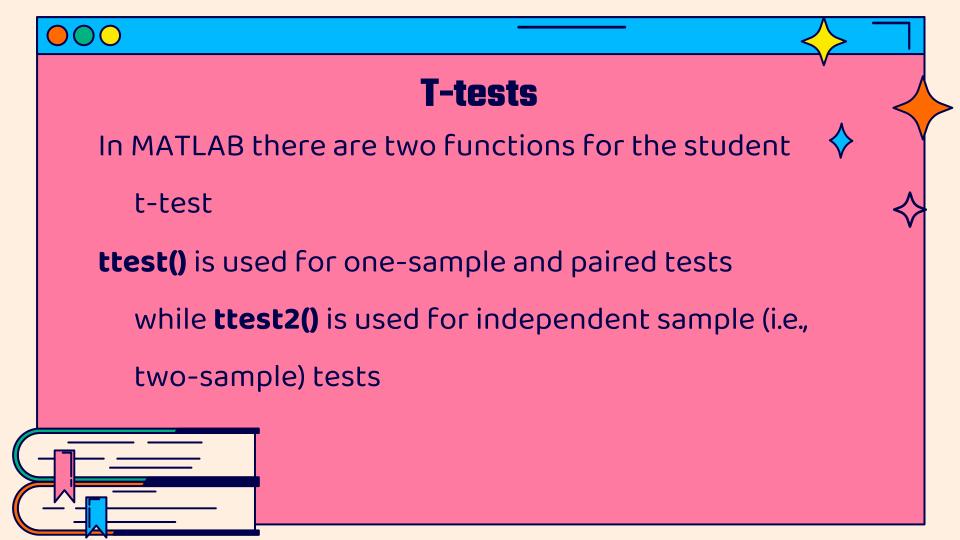
T-tests assume that your data come from a **normal** distribution and the observations are sampled **independently** from one another

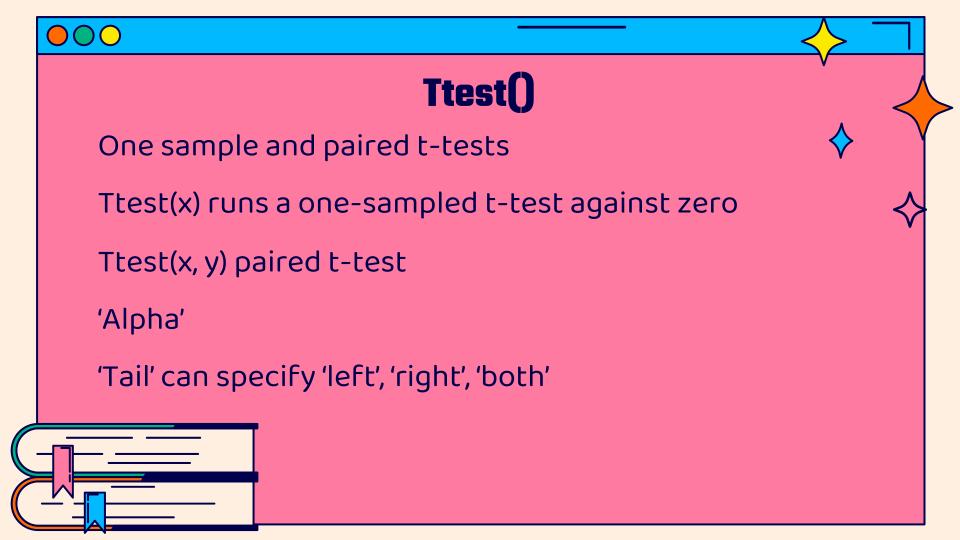
These assumptions apply for both paired and unpaired test

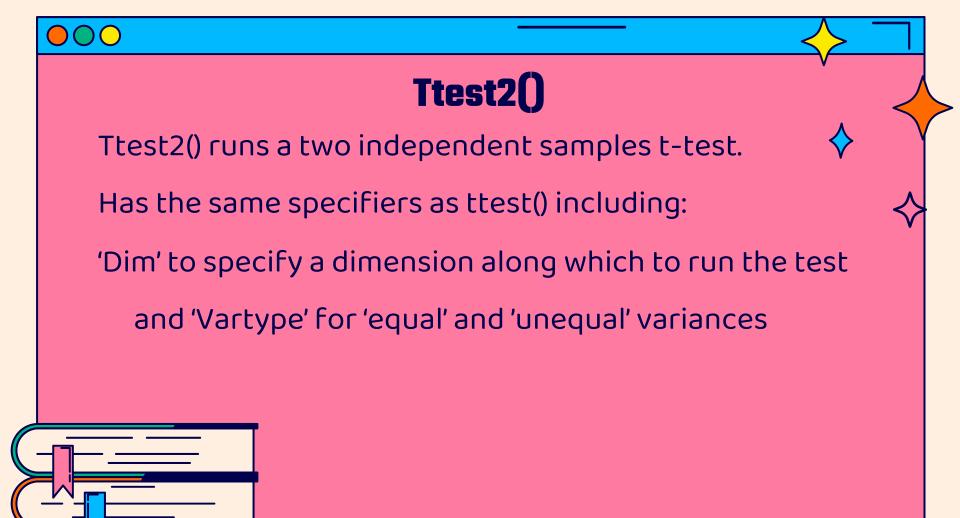


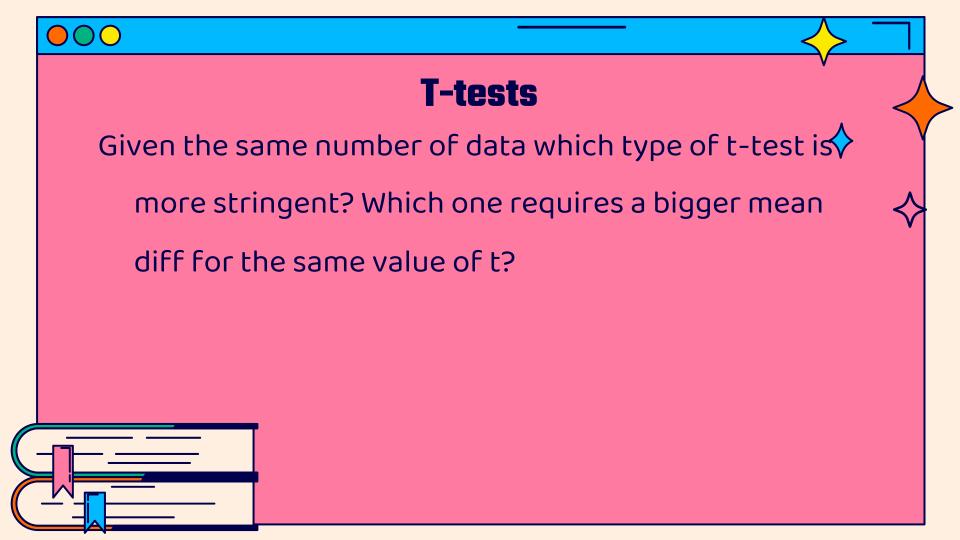














Let us assume we collect data from 20 people (paired)

and observe a mean diff of 3.75, and a sd of 1

Then the t value for a paired test would be:



4	<i>+</i> —	$\frac{mean \ diff}{m}$ with df	with df n	n — 1
	, —	sd	with ai ii	_ 1



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$$t = \frac{3.75}{\frac{1}{\sqrt{20}}}$$
 = with df 19



Let us assume we collect data from 20 people



(independent groups) and observe a mean diff of 3.75,



and a sd of 1 (assuming equal variance)



Then the t value for an unpaired test would be:

$$t = \frac{mean \ diff}{sp * \sqrt{\frac{1}{n1} + \frac{1}{n2}}} \text{ with sp} = \sqrt{\frac{(n1-1)*std1^2 + (n2-1)*std2^2}{n1 + n2 - 2}} \ df \ n1 + n2$$



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Then the t value for an unpaired test would be:

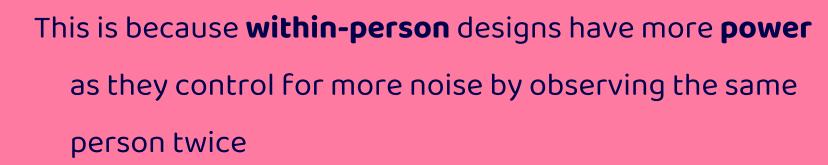
$$sp = \sqrt{\frac{(20-1)*1 + (20-1)*1}{20+20-2}} \qquad t = \frac{3.75}{sp*\sqrt{\frac{1}{20} + \frac{1}{20}}}.$$







T value for paired is larger, in comparison to t values of unpaired or independent tests







Non-parametric tests

In stats there are some tests that are **non-parametric,** by this statisticians mean that the test does not require assuming a specific model or distribution for your data

These are sometimes referred to as **non-distributional** tests

These tests are used when you do not want to assume a specific distribution (e.g., violation), or do not know the distribution of your data



Non-parametric t-tests

Regular t-tests assume your data is normally distributed

There is a non-parametric equivalent of a t-test called the

permutation t-test. This test works on the premise that you

can observe a *null distribution* from your own data by

randomly permuting groups.

Reminder: a null distribution is the distribution when the null

hypothesis is true



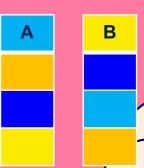
permutations

Permutations build a *null distribution* of data based on your observations under the assumption that randomly shuffling your data will void the effect of interest. Thus, you can measure how surprising the effect you observe is given your data based on the

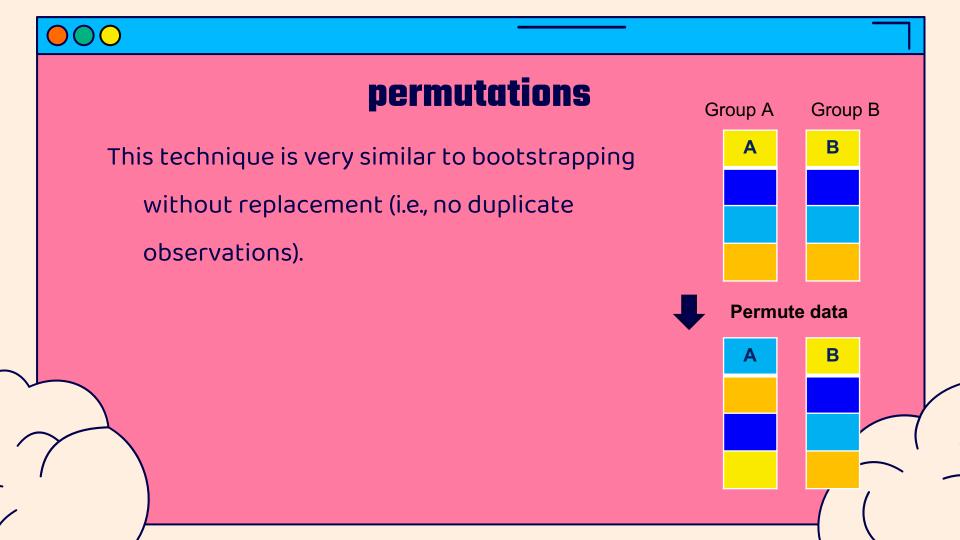
computed null distribution

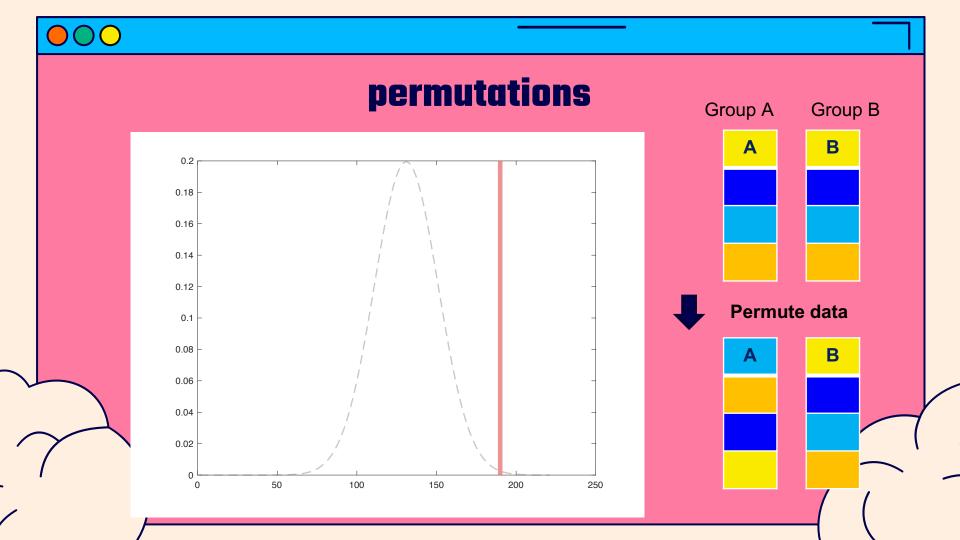
Group A Group B

A B



Permute data







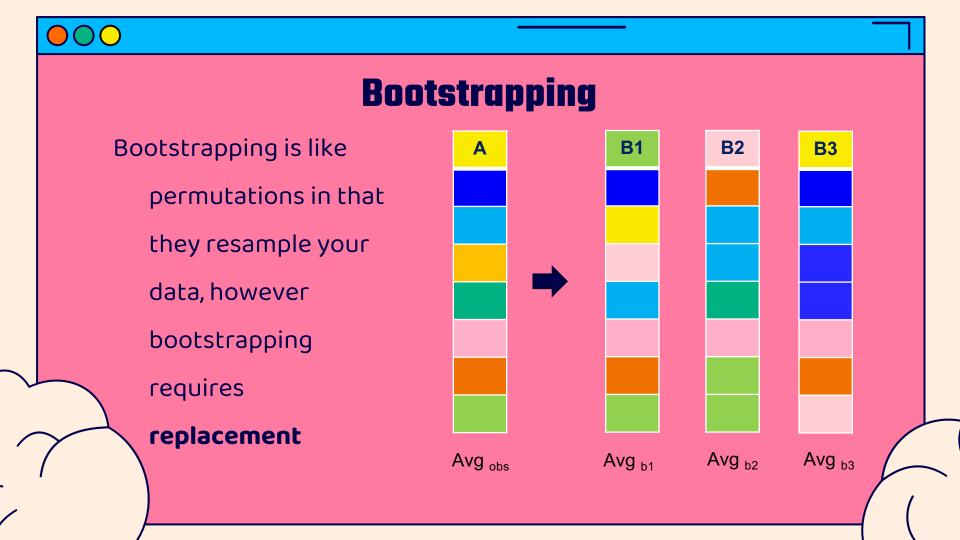
Bootstrapping

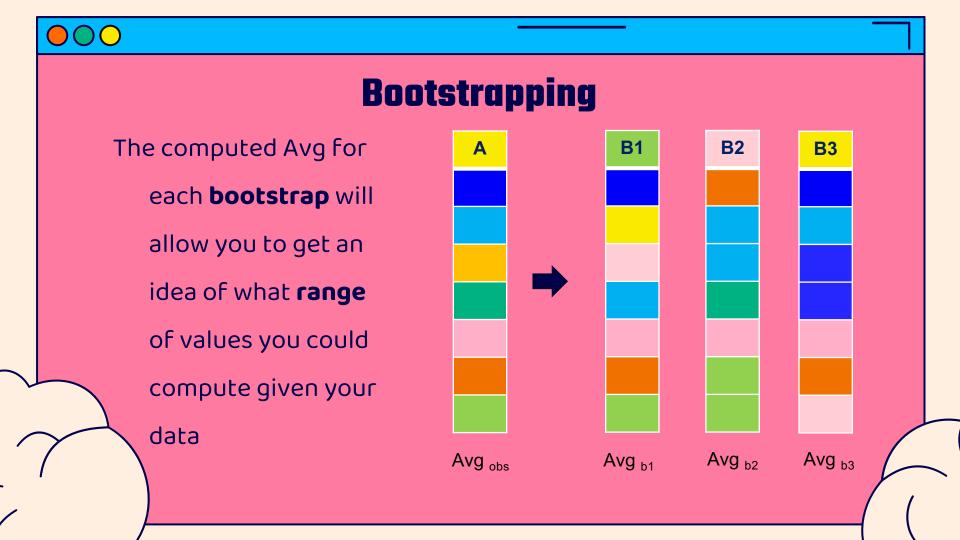
A very similar concept in statistics is the idea of **bootstrapping** to get a measure of uncertainty around an estimate (e.g., CI)

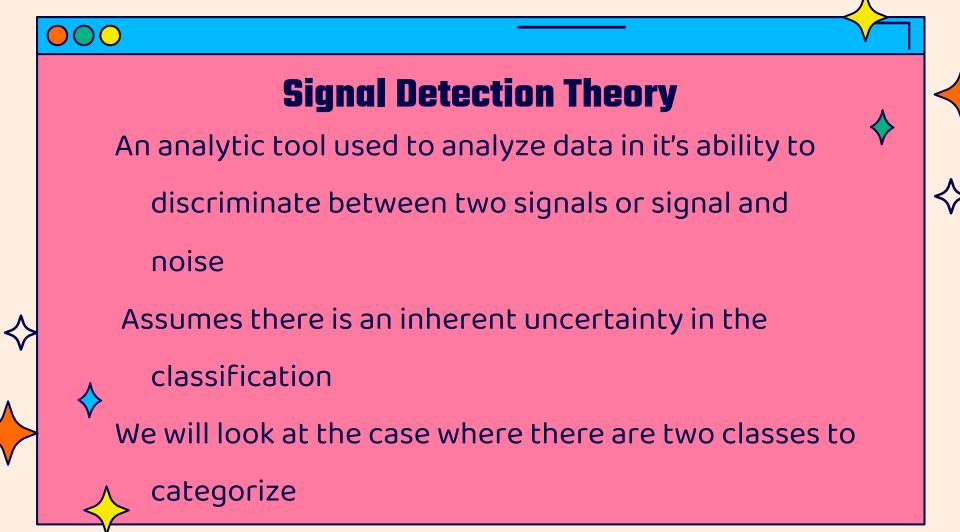
Bootstrapping is like permutations in that they resample your data, however bootstrapping requires **replacement**

It is often used to calculate the error associated to an estimate, effect, or performance of an algorithm and allows you to

know if one given data point is driving the effect you see











detection theory

The criterion: where you draw the boundary between signal and noise



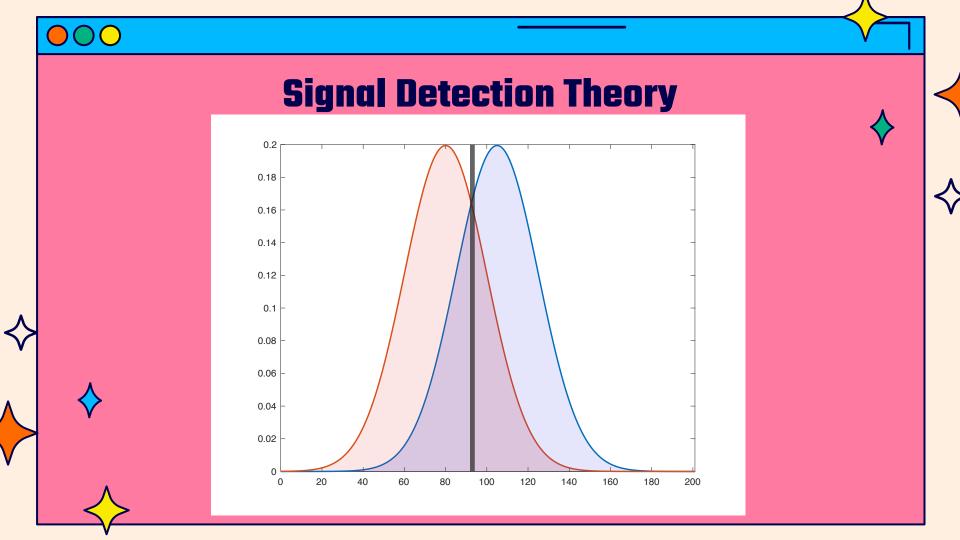
Sensitivity: one's ability to discriminate between signal and noise

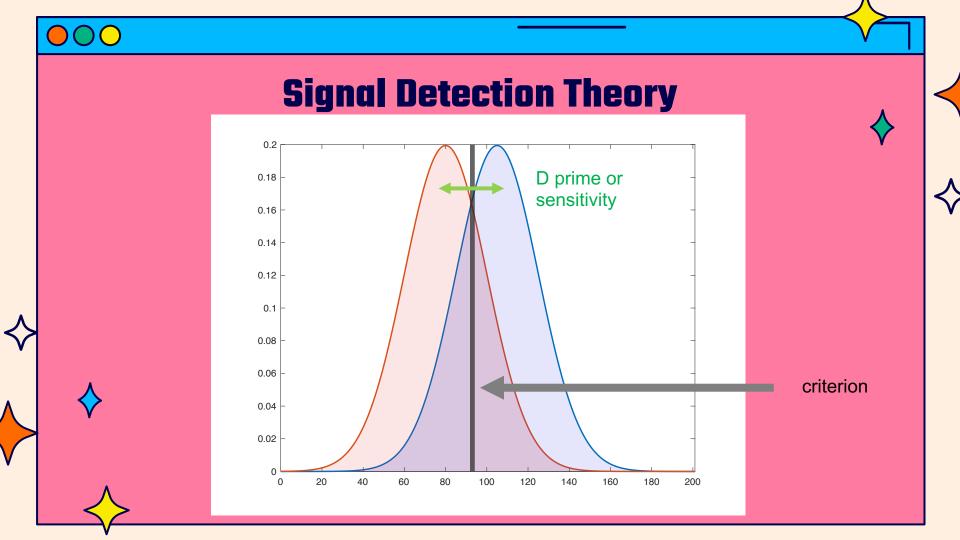






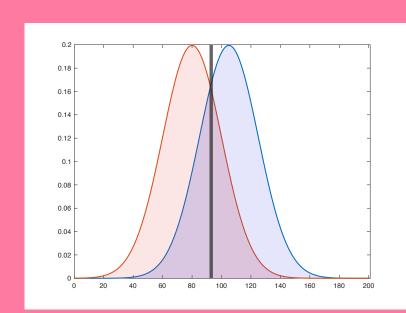












	Signal	Noise
Present	Hits	False Alarms
Absent	Misses	Correct Rejection







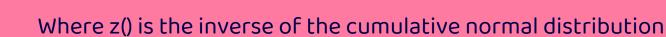






$$c = -\frac{1}{2}(z(Hits) + z(False\ Alarms))$$













What to do when you get values of 0 or 1 as

probabilities?

You cannot take the inverse cumulative normal distribution of 0 or 1 as it returns infinite values.

















We assume that if we double the number of trials, by



answer i.e., if pHIT or pFA =0, then we correct to







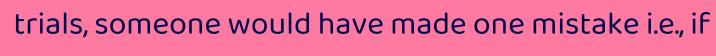




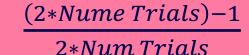




Similarry we assume that if we double the number of



pHIT or pFA =1, then correct with









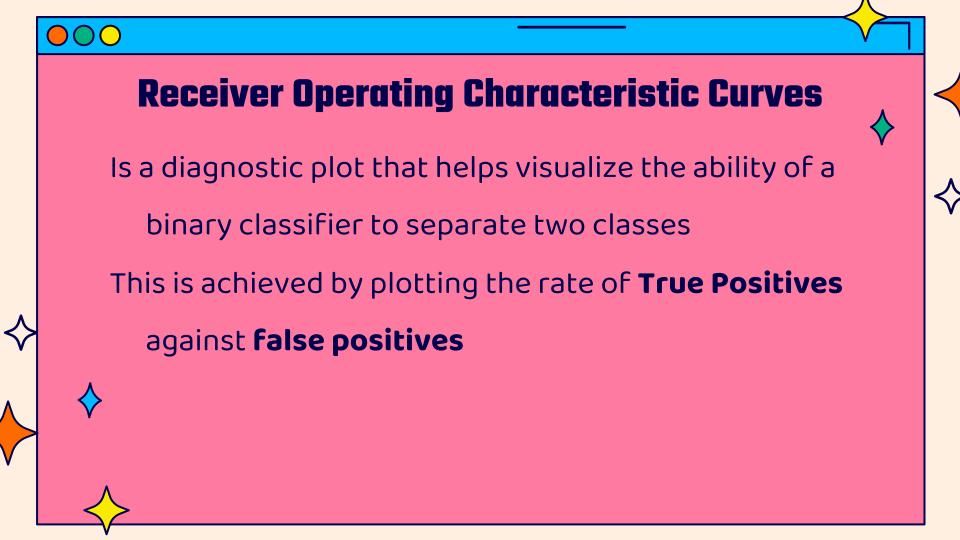




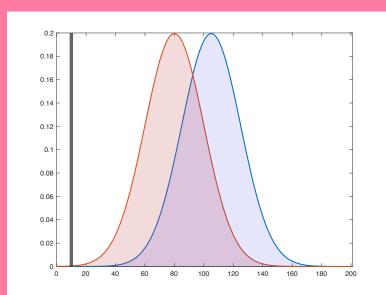


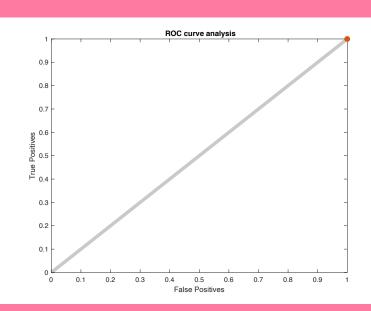










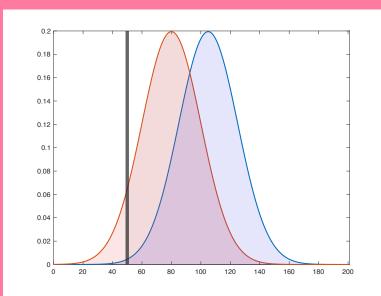


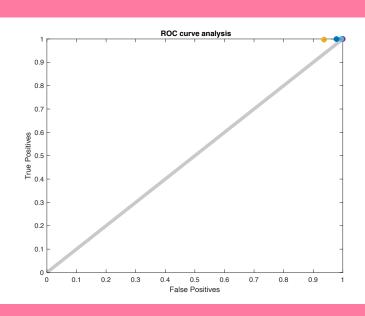








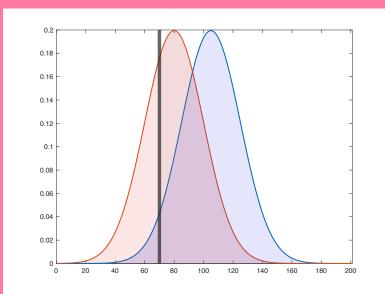


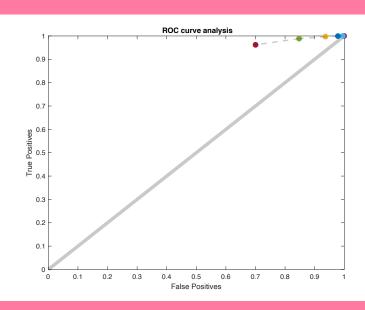










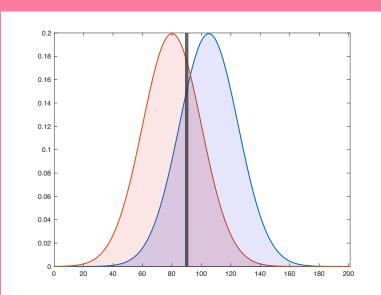


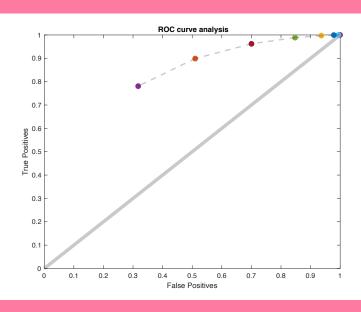










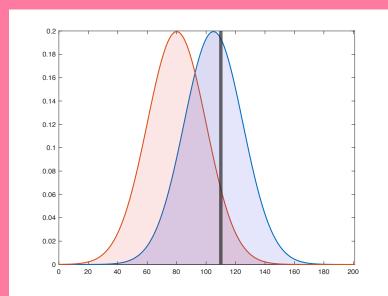


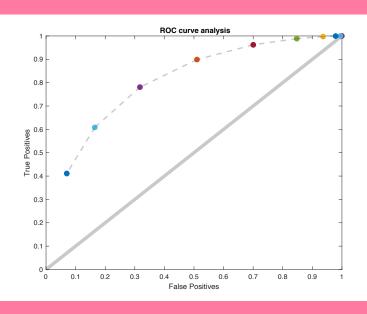






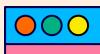


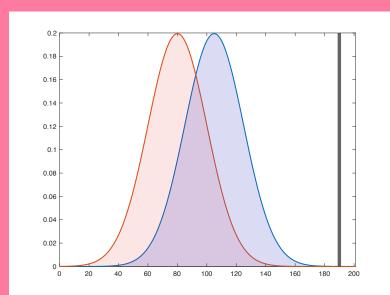


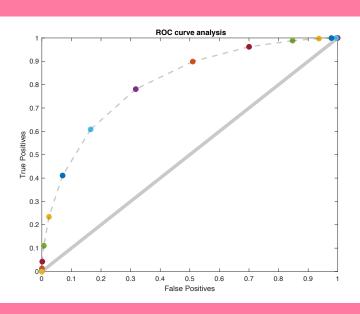








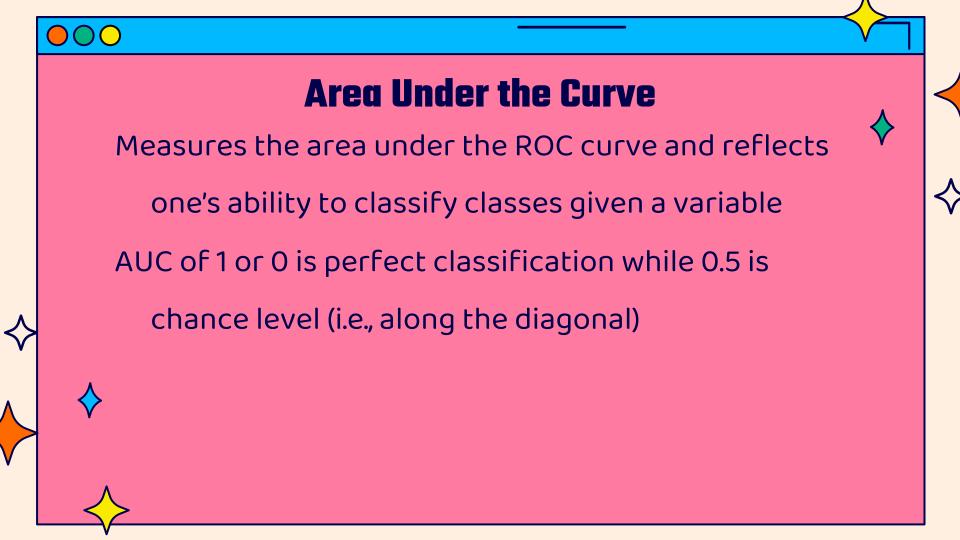


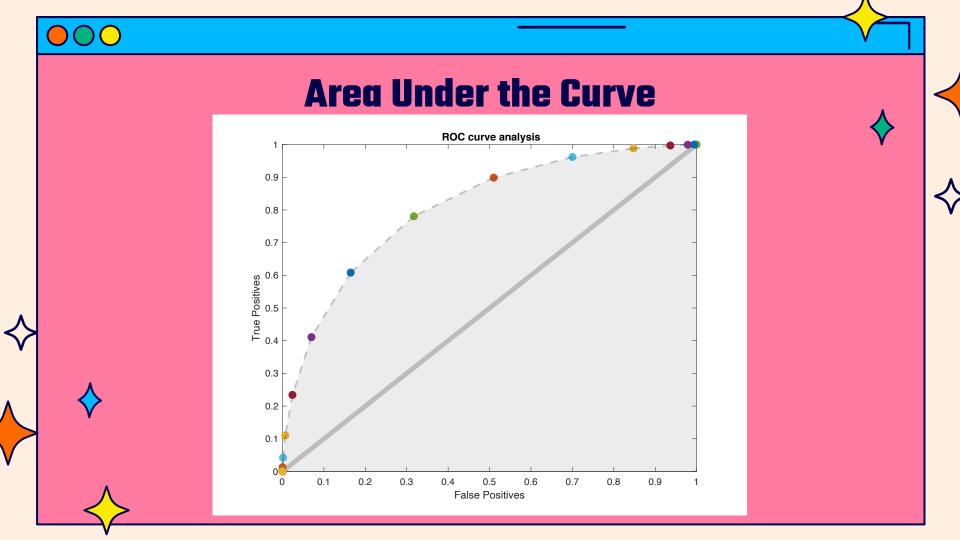


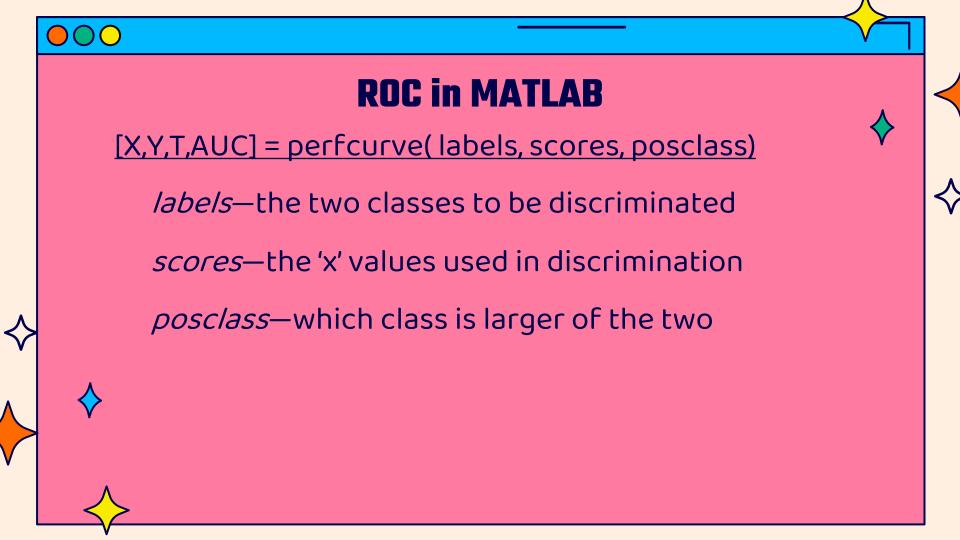












ROC in MATLAB

[X,Y,T,AUC] = perfcurve(labels, scores, posclass)

X— x values of ROC curve

Y— y values of ROC curve

7—array of thresholds used













