

# AlphaNet: Improving Long-Tail Classification By Combining Classifiers

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Methods in long-tail learning focus on improving performance for data-poor (rare) classes; however, performance for such classes remains much lower than performance for more data-rich (frequent) classes. Analyzing the predictions of long-tail methods for rare classes reveals that a large number of errors are due to misclassification of rare items as visually similar frequent classes. To address this problem, we introduce AlphaNet, a method that can be applied to existing models, performing post hoc correction on classifiers of rare classes. Starting with a pre-trained model, we find frequent classes that are closest to rare classes in the model’s representation space and learn weights to update rare classifiers with a linear combination of frequent classifiers. AlphaNet, applied on several different models, greatly improves test accuracy for rare classes in multiple long-tail datasets. We then analyze predictions from AlphaNet and find that remaining errors are to often due to fine-grained differences among semantically similar classes (e.g., dog breeds). Evaluating with semantically similar classes grouped together, AlphaNet also improves overall accuracy, showing that the method is practical for long-tail classification problems.

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## 1. Introduction

The significance of long-tailed distributions in real-world applications (such as autonomous driving<sup>[1]</sup> and medical image analysis analysis<sup>[2]</sup>) has spurred a variety of approaches for long-tail classification<sup>[3]</sup>. Learning in this setting is challenging because many classes are “rare” – having only a small number of training samples. Some methods re-sample more data for rare classes in an effort to address data imbalances<sup>[4, 5]</sup>, while other methods adjust learned classifiers to re-weight them in favor of rare classes<sup>[6]</sup>. Both re-sampling

and re-weighting methods provide strong baselines for long-tail classification tasks. However, state-of-the-art results are achieved by more complex methods that, for example, learn multiple experts<sup>[7, 8]</sup>, perform multi-stage distillation<sup>[9]</sup>, or use a combination of weight balancing, data re-sampling, and loss decay<sup>[10]</sup>.

Despite these advances, accuracy on rare classes continues to be significantly worse than overall accuracy using these methods. For example, on the ImageNet-LT dataset, the 6-expert ensemble ‘routing diverse experts’ (RIDE) model<sup>[7]</sup> has an average accuracy of 68.9% on frequent classes, but an average accuracy of 36.5% on rare classes. In addition to significantly reducing overall accuracy, such performance imbalances raise ethical concerns in contexts where unequal accuracy leads to biased outcomes, for instance in medical imaging<sup>[11]</sup> or face detection<sup>[12]</sup>. For example, models trained on chest X-rays consistently under-diagnosed minority groups<sup>[13]</sup>. Similarly, cardiac image segmentation showed significant differences between racial groups<sup>[14]</sup>. For these reasons, our method is aimed at directly improving the accuracy for rare classes in long-tail classification.

To understand the poor rare class performance of long-tail models, we analyzed the predictions of the RIDE model<sup>[7]</sup> on ‘few’ split test samples – classes with limited training samples – in ImageNet-LT<sup>[15]</sup>. Figure 1a shows predictions binned into three groups: 1) samples predicted correctly; 2) samples incorrectly predicted as a visually similar class (e.g., predicting ‘husky’ instead of ‘malamute’); and 3) samples incorrectly predicted as a visually dissimilar class (e.g., predicting ‘car’ instead of ‘malamute’). A significant portion of the misclassifications (about 26%) are to visually similar classes. Figure 1b shows samples from one pair of visually similar classes; the differences are subtle, and can be hard even for humans to identify. We next analyzed the relationship between per-class test accuracy and mean distance of a class to its nearest neighbors (see Section 3 for details). Figure 1c shows a strong positive correlation between accuracy and mean distance – ‘few’ split classes with close neighbors have lower test accuracy than classes with distant neighbors.

Based on these analyses, we introduce a method, AlphaNet, for improving classifiers for rare classes using infor-

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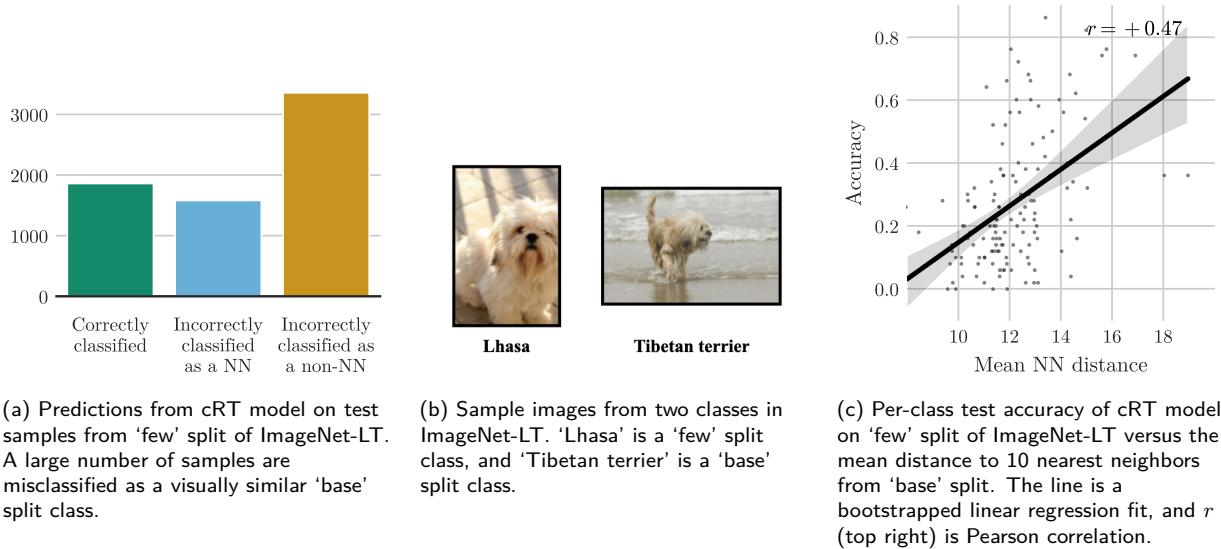


Figure 1: Analysis of test accuracy for ‘few’ split of ImageNet-LT.

mation from visually similar *frequent* classes (Figure 2). At a high level, AlphaNet can be seen as moving the classifiers for rare classes based on their position relative to visually similar classes. Importantly, AlphaNet updates classifiers without making any changes to the representation space, or to other classifiers in the model. It performs a *post-hoc* correction, and as such, is applicable to use cases where existing base classifiers are either unavailable or fixed (e.g., due to commercial interests or data privacy protections). The simplicity of our method lends to computational advantages – AlphaNet can be trained rapidly, and on top of any classification model.

## 2. Related work

Combining, creating, modifying, and learning model weights are concepts that have been implemented in many earlier models. As we review below, these concepts appear frequently in, transfer learning, meta-learning, zero-shot/low-shot learning, and long-tail learning.

### 2.1. Classifier creation

The process of creating new classifiers is captured within meta-learning concepts such as learning-to-learn, transfer learning, and multi-task learning learning [16, 17, 18, 19, 20]. These approaches generalize to novel tasks by learning shared information from a set of related tasks. Many studies find that shared information is embedded within model weights, and, thus, aim to learn structure within learned models to directly modify the weights of a different network [21, 22, 23, 24, 25, 26, 27, 28]. Other studies go even further and instead of modifying net-

works, they create entirely new networks exclusively from training samples samples [29, 30, 31]. In contrast, AlphaNet only combines existing classifiers, without having to create new classifiers or train networks from scratch.

### 2.2. Classifier or feature composition

In various classical approaches, there has been work that learns better embedding spaces for image annotation [32], or uses classification scores as useful features [33]. However, these approaches do not attempt to compose classifiers nor do they address the long-tail problem. Within non-deep methods in classic transfer learning, there have been attempts to use and combine support vector machines (SVMs). In one method [34], SVMs are trained per object instance, and a hierarchical structure is required for combination in the datasets of interest. Such a structure is typically not guaranteed nor provided in long-tailed datasets. Another SVM method uses regularized minimization to learn the coefficients necessary to combine patches from other classifiers [35].

While these approaches are conceptually similar to our method, AlphaNet has the additional advantage of *learning* the compositional coefficients without any hyper-parameters and tuning. Specifically, different novel classes will have their own sets of composition coefficients, and similar novel classes will naturally have similar coefficients. Learning such varying sets of coefficients is difficult in previous classical approaches, which either learn a fixed set of alphas for all novel classes or are forced to introduce more complex group sparsity-like constraints. Finally, in zero-shot learning there exist methods which compose classifiers of known visual concepts to learn

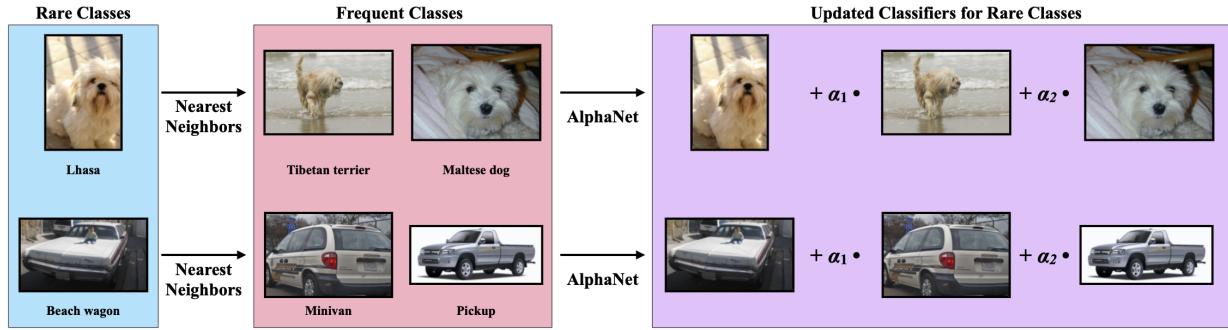


Figure 2: Pipeline for AlphaNet. Given examples from rare classes, we identify the nearest neighbors (visually similar) examples from frequent classes and then update each rare classifier using learned  $\alpha$ 's for each nearest neighbor. The result is an improved classifier for each rare class.

a completely new classifier [30, 36, 37, 38]. However, such composition is often guided by additional attribute supervision or textual description, which are not needed by AlphaNet.

### 2.3. Learning transformations between models and classes

Other studies have demonstrated different ways of learning transformations to modify model weights in an attempt to learn these transformations with stochastic gradient descent (SGD) optimization [39, 40]. Additionally, there is empirical evidence [41] showing the existence of a generic nonlinear transformation from small-sample to large-sample models for different types of feature spaces and classifier models. Finally, in the case where one learns the transformation from the source function to a related target function, there are theoretical guarantees on performance [42]. AlphaNet is similar in that we likewise infer that our target classifier is a transformation from a set of source classifiers.

### 2.4. Zero-shot/low-shot learning

Meta-learning, transfer learning, and learning-to-learn are frequently applied to the domain of low-shot learning [20, 41, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52]. A wide variety of prior studies have attempted to transfer knowledge from tasks with abundant data to completely novel tasks [23, 40, 53]. However, the explicit nature of low-shot learning consisting of tasks with small fixed samples means that these approaches do not generalize well beyond the arbitrary few tasks. This is a significant problem as the visual world clearly involves a wide set of tasks with continuously varying amounts of information.

### 2.5. Long-tail learning

The restrictions of low-shot learning have directly led to the new paradigm referred to as long-tail learning, where data samples are continuously decreasing and the data distribution closely models that of the visual world. Recent work achieves state-of-the-art performance on long-tailed recognition by learning multiple experts [7, 8]. Both of these complex ensemble methods require a two-stage training method. A somewhat different approach re-balances the samples at different stages of model training [5], attempts to transfer features from common classes to rare classes [15], or transfers intra-class variance [54]. However, approaches to knowledge transfer require complex architectures, such as a specialized attention mechanism and memory models [15]. While most studies have largely focused on representation space transferability or complex ensembles, recent work establishes a strong baseline by exploring the potential of operating in classifier space [6]. Results suggest that decoupling model representation learning and classifier learning is a more efficient way to approach long-tailed learning. Specifically, methods normalizing classifiers and adjusting classifiers only using re-sampling strategies achieve good performance. Such successes in working only with classifiers support our general concept that combining strong classifiers in AlphaNet is a natural and direct way to improve upon weak classifiers.

## 3. Methods

### 3.1. Notation

In this work, we will define the distance between two classes as the distance between their average training set representation. Given a classification model, let  $f$  be the function mapping images in  $\mathbb{R}^d$  (typically, this is the output of the

penultimate layer in convolutional networks). For a class  $c$  with training samples  $I_1^c, \dots, I_{n^c}^c$ , let  $z^c \equiv (1/n^c) \sum_i f(I_i^c)$ . Given a distance metric  $\mu : \mathbb{R}^d \times \mathbb{R}^d \rightarrow \mathbb{R}$ , for classes  $c_1$  and  $c_2$ , we define  $m_\mu(c_1, c_2) \equiv \mu(x^{c_1}, x^{c_2})$ .

Given a long-tailed dataset, the ‘few’ split,  $C^F$ , is defined as the set of rare classes (which form the “tail” of the training data distribution). The set of remaining classes forms the ‘base’ split,  $C^B$ . AlphaNet is applied to update the ‘few’ split classifiers using nearest neighbors from the ‘base’ split. For a ‘few’ split class  $c$ , let the  $k$  nearest ‘base’ split neighbors (based on  $m_\mu$ ) be  $q_1^c, \dots, q_k^c$ .

We will use the term ‘classifier’ to denote the linear mapping from feature vectors to class scores. In convolutional networks, the last layer is generally a matrix of all individual classifiers. For a class  $c$ , let  $w^c$  be its classifier, and let  $v_1^c, \dots, v_k^c$  be the classifiers for its nearest neighbors. Finally, let  $\bar{v}^c \in \mathbb{R}^{kd}$  be a vector with the nearest neighbor classifiers concatenated together.

### 3.2. AlphaNet implementation

Figure 2 shows the architecture of our method. AlphaNet is a small fully connected network which maps  $\bar{v}^c$  to a set of coefficients  $\alpha_1^c, \dots, \alpha_k^c$ . The  $\alpha$  coefficients (denoted together as a vector  $\alpha^c$ ), are then scaled to unit 1-norm (the reasoning behind this is explained below):

$$\tilde{\alpha}^c = \alpha^c / |\alpha^c|_1. \quad (1)$$

The scaled coefficients are used to update classifiers through a linear combination:

$$\hat{w}^c \equiv w^c + \sum_{i=1}^k \tilde{\alpha}_i^c v_i^c \quad (2)$$

Due to the 1-norm scaling, we have

$$\begin{aligned} \|\hat{w}^c - w^c\|_2 &\leq \sum_{i=1}^k |\tilde{\alpha}_i^c| \|v_i^c\|_2 \quad (\text{Cauchy-Schwarz inequality}) \\ &\leq \max_{i=1,\dots,k} \|v_i^c\|_2 \sum_{i=1}^k |\tilde{\alpha}_i^c| \\ &= \max_{i=1,\dots,k} \|v_i^c\|_2 \|\tilde{\alpha}^c\|_1 \\ &= \max_{i=1,\dots,k} \|v_i^c\|_2, \end{aligned} \quad (3)$$

that is, a classifier’s change is bound by the norm of its class’s nearest neighbors. Thanks to this, we do not need to update or rescale ‘base’ split classifiers, which may not be possible in certain domains.

A single network is used to generate coefficients for every ‘few’ split class. So, once trained, AlphaNet can be applied even to previously unseen classes.

### 3.3. Training

To train AlphaNet, we have to learn parameters  $\theta$  for the network which maps  $\bar{v}^c$  to  $\alpha^c$ . We also learn a new set of bias values for the ‘few’ split classes,  $\tilde{b}_1, \dots, \tilde{b}_{|C^F|}$ . We train AlphaNet using samples from both the ‘few’ and ‘base’ splits to prevent over-fitting. So, for a sample  $(I, y)$ , the prediction score is given by

$$s(I, y; \theta, \tilde{b}) = \begin{cases} f(I)^T \hat{w}^y + \tilde{b}_y & y \in C^F \\ f(I)^T w^y + b_y & y \in C^B \end{cases} \quad (4)$$

This score is used to compute the softmax cross-entropy loss on a set of training samples, and minimized with respect to  $\theta$  and  $\tilde{b}$  using SGD.

## 4. Experiments

### 4.1. Experimental setup

**Datasets.** We evaluated our method using three long-tailed datasets: ImageNet-LT, Places-LT<sup>[15]</sup>, and CIFAR-100-LT<sup>[10]</sup>. These Datasets are sampled from their respective original datasets, ImageNet<sup>[55]</sup>, Places365<sup>[56]</sup>, and CIFAR-100<sup>[57]</sup> such that the new distributions follow a standard long-tailed distribution. For CIFAR-100-LT, we used an imbalance factor of 100.

The datasets are broken down into three broad splits that indicate the number of training samples per class: 1) ‘many’ contains classes with greater than 100 samples; 2) ‘medium’ contains classes with greater than or equal to 20 samples but less than or equal to 100 samples; 3) ‘few’ contains classes with less than 20 samples. The test set is always balanced, containing an equal number of samples for each class. We use the term ‘base’ split to refer to the combined ‘many’ and ‘medium’ splits.

**Note:** Another popular dataset used for testing long-tail models is iNaturalist<sup>[58]</sup>. Results for this dataset, however, are much more balanced across splits. So it does not represent a valid use case for our proposed method, and we omitted the dataset from our experiments.

**Training data sampling.** In order to prevent over-fitting on the ‘few’ split samples, we used a class balanced sampling approach, using all ‘few’ split samples, and a portion of the ‘base’ split samples. Given  $F$  ‘few’ split samples, and a ratio  $\rho$ , every epoch,  $\rho F$  samples were drawn from the ‘base’ split, with sample weights inversely proportional to the class size. This ensured that all ‘base’ classes had an equal probability of being sampled. As we show in the following section,  $\rho$  allows us to control the balance between ‘few’ and ‘base’ split accuracy. We evaluated AlphaNet with a range of  $\rho$  values; results for  $\rho = 0.5$ ,  $\rho = 1$ , and  $\rho = 1.5$  are shown in the following section, and the full set of results is in the appendix.

Method	Few	Med.	Many	Overall
<b>ImageNet-LT</b>				
Cross entropy	7.7	37.5	65.9	44.4
NCM	28.1	45.3	56.6	47.3
$\tau$ -normalized	30.7	46.9	59.1	49.4
cRT	27.4	46.2	61.8	49.6
$\alpha$ cRT ( $\rho = 0.5$ )	39.7 <sup>1.42</sup>	42.0 <sup>0.66</sup>	58.3 <sup>0.52</sup>	48.0 <sup>0.37</sup>
$\alpha$ cRT ( $\rho = 1$ )	34.6 <sup>1.88</sup>	43.7 <sup>0.51</sup>	59.7 <sup>0.43</sup>	48.6 <sup>0.24</sup>
$\alpha$ cRT ( $\rho = 1.5$ )	32.6 <sup>2.46</sup>	44.4 <sup>0.49</sup>	60.3 <sup>0.38</sup>	48.9 <sup>0.19</sup>
LWS	30.4	47.2	60.2	49.9
$\alpha$ LWS ( $\rho = 0.5$ )	46.9 <sup>0.98</sup>	38.6 <sup>0.87</sup>	52.9 <sup>0.86</sup>	45.3 <sup>0.69</sup>
$\alpha$ LWS ( $\rho = 1$ )	41.6 <sup>1.61</sup>	42.2 <sup>0.53</sup>	56.0 <sup>0.32</sup>	47.4 <sup>0.30</sup>
$\alpha$ LWS ( $\rho = 1.5$ )	40.1 <sup>1.99</sup>	43.2 <sup>0.98</sup>	56.9 <sup>0.76</sup>	48.0 <sup>0.53</sup>
<b>Places-LT</b>				
Cross entropy	8.2	27.3	45.7	30.2
NCM	27.3	37.1	40.4	36.4
$\tau$ -normalized	31.8	40.7	37.8	37.9
cRT	24.9	37.6	42.0	36.7
$\alpha$ cRT ( $\rho = 0.5$ )	31.0 <sup>0.88</sup>	34.5 <sup>0.17</sup>	40.4 <sup>0.29</sup>	35.9 <sup>0.09</sup>
$\alpha$ cRT ( $\rho = 1$ )	27.0 <sup>1.02</sup>	36.1 <sup>0.31</sup>	41.3 <sup>0.13</sup>	36.2 <sup>0.10</sup>
$\alpha$ cRT ( $\rho = 1.5$ )	25.5 <sup>0.89</sup>	36.5 <sup>0.36</sup>	41.6 <sup>0.21</sup>	36.2 <sup>0.11</sup>
LWS	28.7	39.1	40.6	37.6
$\alpha$ LWS ( $\rho = 0.5$ )	37.1 <sup>1.39</sup>	34.4 <sup>0.80</sup>	37.7 <sup>0.52</sup>	36.1 <sup>0.31</sup>
$\alpha$ LWS ( $\rho = 1$ )	34.6 <sup>0.97</sup>	35.8 <sup>0.54</sup>	38.6 <sup>0.39</sup>	36.6 <sup>0.22</sup>
$\alpha$ LWS ( $\rho = 1.5$ )	32.2 <sup>1.17</sup>	37.2 <sup>0.36</sup>	39.5 <sup>0.39</sup>	37.0 <sup>0.11</sup>

Table 1: Mean split accuracy (standard deviation in super-script) of AlphaNet and various baseline methods on ImageNet-LT and Places-LT. cRT and LWS are AlphaNet models applied over cRT and LWS features respectively.

**Training.** All experiments used an AlphaNet module with three 32 unit layers, and Leaky-ReLU activation [59]. Unless stated otherwise, euclidean distance was used to find  $k = 5$  nearest neighbors for each ‘few’ split class. Models were trained for 25 epochs to minimize cross-entropy loss computed using mini-batches of 64 samples. Optimization was performed using AdamW [60] with a learning rate of 0.001, decayed by a factor of 10, every 10 epochs. Model weights were saved after each epoch, and after training, the weights with the best accuracy on validation data were used to report results on the test set. All experiments were repeated 10 times, and we report mean and standard deviation of accuracies across trials.

## 4.2. Long-tail classification results

**Baseline models.** First, we applied AlphaNet on several strong baseline methods [6]. These methods have good overall accuracy, but accuracy for ‘few’ split classes is much lower. On the ImageNet-LT dataset, average accuracy for the classifier re-training (cRT) and learnable weight scaling (LWS) models (using a ResNeXt-50 backbone) is nearly 20 points below the overall accuracy, as seen in Table 1. Using features extracted from these two models, we used AlphaNet to update ‘few’ split classifiers. On both models, we saw a significant increase in the ‘few’ split accuracy for all values of  $\rho$ . For  $\rho = 1$ , average ‘few’ split accuracy was boosted by 7 points for the cRT model, and about 11 points for the LWS model.

We repeated the above experiment on the Places-LT dataset, where again ‘few’ split accuracy for the cRT and

Method	Few	Med.	Many	Overall
<b>ImageNet-LT</b>				
RIDE	36.5	54.4	68.9	57.5
$\alpha$ RIDE ( $\rho = 0.5$ )	43.5 <sup>0.75</sup>	52.3 <sup>0.26</sup>	67.3 <sup>0.17</sup>	56.9 <sup>0.11</sup>
$\alpha$ RIDE ( $\rho = 1$ )	40.8 <sup>1.00</sup>	53.1 <sup>0.21</sup>	67.9 <sup>0.18</sup>	57.1 <sup>0.11</sup>
$\alpha$ RIDE ( $\rho = 1.5$ )	38.2 <sup>1.22</sup>	53.6 <sup>0.25</sup>	68.4 <sup>0.17</sup>	57.2 <sup>0.06</sup>
<b>CIFAR-100-LT</b>				
RIDE	25.8	52.1	69.3	50.2
$\alpha$ RIDE ( $\rho = 0.5$ )	30.9 <sup>1.82</sup>	47.0 <sup>1.25</sup>	65.7 <sup>0.94</sup>	48.7 <sup>0.41</sup>
$\alpha$ RIDE ( $\rho = 1$ )	27.2 <sup>1.69</sup>	49.1 <sup>0.85</sup>	67.4 <sup>0.62</sup>	48.9 <sup>0.30</sup>
$\alpha$ RIDE ( $\rho = 1.5$ )	25.0 <sup>1.15</sup>	50.1 <sup>1.12</sup>	67.9 <sup>1.01</sup>	48.8 <sup>0.63</sup>

Table 2: Mean split accuracy (standard deviation in super-script) on ImageNet-LT and CIFAR-100-LT using the ensemble RIDE model<sup>[7]</sup>. RIDE applies AlphaNet on average features from the ensemble.

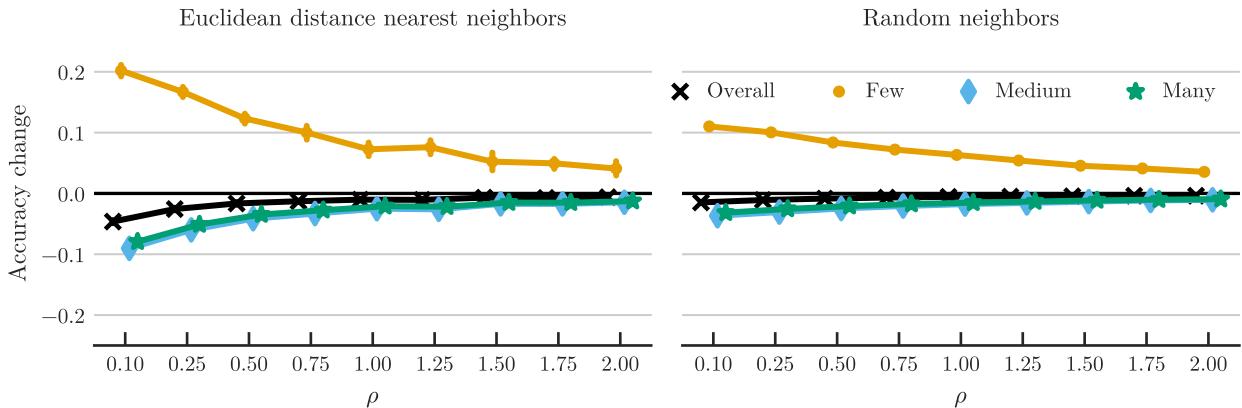


Figure 3: Change in split accuracy for AlphaNet training of cRT model on ImageNet-LT. For each value of  $\rho$ , the two plots show the change in split accuracy for AlphaNet compared to the baseline cRT model, as well as the change in overall accuracy. Left shows the results for normal training with 5 euclidean nearest neighbors, and right shows the results for training with 5 random neighbors for each ‘few’ split class. Training with nearest neighbors leads to a larger increase in ‘few’ split accuracy (especially for small values of  $\rho$ ), which cannot be accounted for by the additional fine-tuning of classifiers.

LWS models is much lower than the overall accuracy (by around 12 and 9 points respectively as seen in Table 1. With  $\rho = 1$ , AlphaNet improved ‘few’ split accuracy by 2 points on average for the cRT model, and about 6 points on average for the LWS model.

**Expert model.** Next, we applied AlphaNet on the 6-expert ensemble RIDE model<sup>[7]</sup>. We provided the combined feature vectors from all 6 experts as input to AlphaNet. The learned ‘few’ split classifiers were split into 6, and used to update the experts. Prediction scores from the experts were averaged to produce the final predictions, as in the original model. For ImageNet-LT, the experts used a ResNeXt-50 backbone, and for CIFAR-100-LT, a ResNet-32 backbone. Table 2 shows the base results for the expert models, along with AlphaNet results for  $\rho = 0.5, 1, 2$ . On ImageNet-LT,

‘few’ split accuracy was increased by up to 7 points, and on CIFAR-100-LT, by 5 points.

#### 4.3. Comparison with control

Our method is based on the core hypothesis that classifiers can be improved using nearest neighbors. In this section, we directly test this hypothesis. Based on the results in the previous section, the improvements in ‘few’ split accuracy could be attributed simply to the extra fine-tuning of ‘few’ split classifiers. So, we repeated the experiments of the previous section with randomly chosen neighbors for each ‘few’ split class, rather than nearest neighbors. This differs from our previous experiments only in the nature of neighbors used, so if our method’s improvements are solely due to extra fine-

tuning, we should see the same results. However, as seen in Figure 3, training with nearest neighbors garners much larger improvements in ‘few’ split accuracy, with similar trends in overall accuracy. This supports our hypothesis that data-poor classes can make use of information from neighbors to improve classification performance.

#### 4.4. Prediction changes

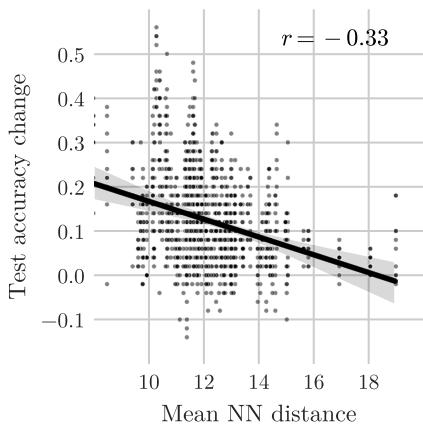


Figure 4: Change in per-class accuracy for AlphaNet applied over cRT features, versus mean Euclidean distance to five nearest neighbors. Comparing with Figure 1c, we can see that AlphaNet provides the largest boost to classes with poor baseline performance, which have close nearest neighbors.

As shown in Section 1, the cRT model frequently misclassifies ‘few’ split classes as visually similar ‘base’ split classes. Using the AlphaNet model with  $\rho = 0.5$ , we performed the same analyses as before. Figure 5a shows the change in sample predictions. A large portion of samples previously misclassified as a nearest neighbor are correctly classified after their classes are updated with AlphaNet. Furthermore, as seen in Figure 4, AlphaNet improvements are strongly correlated to mean nearest neighbor distance. Classes with close neighbors, which had a high likelihood of being misclassified by the baseline model, see the biggest improvement in test accuracy.

#### 4.5. Analysis of AlphaNet predictions

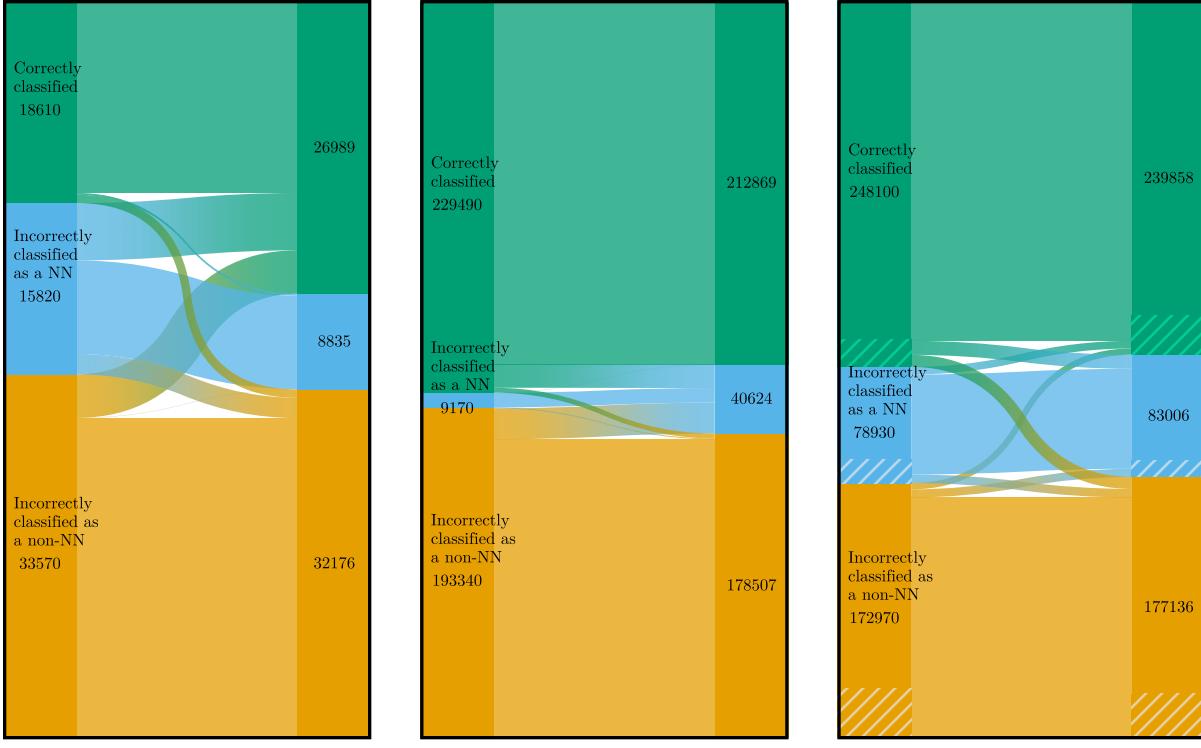
AlphaNet significantly boosts the accuracy of ‘few’ split classes. However, looking at Table 1 and Table 2, we see that the overall accuracy decreases compared to baseline models, particularly for small values of  $\rho$ . It is important to note that the increase in ‘few’ split accuracy is much larger than the decrease in overall accuracy. As discussed earlier, in many applications it is important to have balanced performance across classes, and AlphaNet succeeds in making accuracies more balanced across splits.

However, we further analyzed the prediction changes for ‘base’ split samples. Specifically, Figure 5b shows change in predictions for ‘base’ split samples, with nearest neighbors selected from the ‘few’ split. We see a small increase in misclassifications as ‘few’ split classes. This leads to the slight decrease in overall accuracy, which is also evident in Figure 5c where all predictions are shown, and with nearest neighbors from all classes.

The previous analysis was conducted using nearest neighbors identified based on visual similarity. Since this is dependent on the particular model, we conducted an additional analysis to see the behavior of predictions with respect to *semantically similar* categories. For classes in ImageNet-LT, we defined nearest neighbors using distance in the WordNet hierarchy. Specifically, if two classes (e.g., ‘Lhasa’ and ‘Tibetan terrier’) share a parent at most four levels higher in WordNet (in this example, ‘dog’), we consider them to be nearest neighbors. Figure 6 shows the predictions for AlphaNet with cRT grouped based on these nearest neighbors. As we can see, a large number of predictions which are considered incorrect are among semantically similar categories which can be hard for even humans to distinguish. This suggests that metrics for long-tail classification might need to be re-evaluated for large datasets with many similar classes.

## 5. Conclusion

The long-tailed nature of the world presents a challenge for any model that depends on learning over specific examples. Most long-tailed methods tend to have high overall accuracy, but with unbalanced accuracies where frequent classes are learned well with high accuracies and rare classes are learned poorly with low accuracies. As such, the long-tailed world represents one source of potential bias [11]. To address this problem, typical approaches resort to re-sampling or re-weighting of rare classes but still focus on achieving the highest overall accuracy. Consequently, these methods continue to suffer from low accuracy for data-poor classes, and an accuracy imbalance across data-rich and data-poor classes. In contrast, our method, AlphaNet, provides a rapid 5 minute *post-hoc* correction that can sit on top of any model using classifiers. This simple method greatly improves the accuracy for data-poor classes, and re-balances classification accuracy in a way that overall classification accuracy is preserved. In addition to directly addressing training imbalances, AlphaNet is also applicable to re-balancing accuracies across biases arising from model structure or the prioritization of different model parameters. We analyzed the predictions of our model, and showed that when considering semantically similar classes together, AlphaNet achieves accuracy on par with baselines, while also improving accuracy for data-poor classes significantly. AlphaNet is deployable in any application where the



(a) Predictions on ‘few’ split classes, with nearest neighbors selected from ‘base’ split classes.

(b) Predictions on ‘base’ split classes, with nearest neighbors selected from ‘few’ split classes.

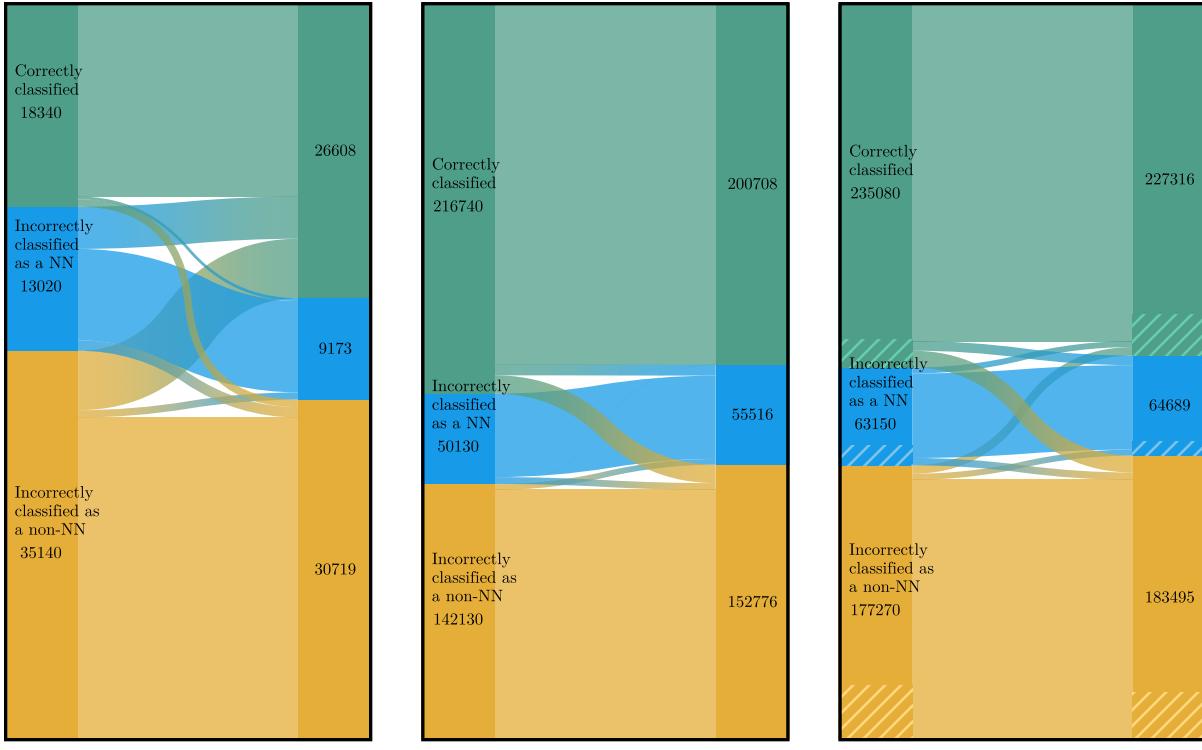
(c) All predictions, with nearest neighbors selected from all classes.

Figure 5: Change in sample predictions for AlphaNet applied for cRT features, with  $k = 10$  nearest neighbors by Euclidean distance. The bars on the left show the distribution of predictions by the baseline model; and the bars on the right show the distribution for AlphaNet. The counts are aggregated from 10 different runs of AlphaNet. The “flow” bands from left to right show the changes in individual sample predictions.

base classifiers cannot be changed, but balanced performance is desirable – thereby making it useful in contexts where ethics, privacy, or intellectual property are concerns.

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(a) Predictions on ‘few’ split classes, with nearest neighbors selected from ‘base’ split classes.

(b) Predictions on ‘base’ split classes, with nearest neighbors selected from ‘few’ split classes.

(c) All predictions, with nearest neighbors selected from all classes.

Figure 6: Change in sample predictions for AlphaNet applied for CRT features, with nearest neighbors identified using WordNet categories. This figure represents the same predictions as Figure 5, but grouped differently.

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Experiment	Few	Med.	Many	Overall
Baseline	27.4	46.2	61.8	49.6
AlphaNet ( $\rho = 0.1$ )	47.6 <sup>1.60</sup>	37.1 <sup>0.76</sup>	53.8 <sup>0.62</sup>	45.0 <sup>0.41</sup>
AlphaNet ( $\rho = 0.2$ )	45.7 <sup>1.56</sup>	39.0 <sup>0.78</sup>	55.7 <sup>0.79</sup>	46.3 <sup>0.52</sup>
AlphaNet ( $\rho = 0.25$ )	44.1 <sup>1.44</sup>	40.2 <sup>0.65</sup>	56.7 <sup>0.57</sup>	47.1 <sup>0.36</sup>
AlphaNet ( $\rho = 0.3$ )	42.9 <sup>1.29</sup>	40.4 <sup>0.72</sup>	57.0 <sup>0.68</sup>	47.1 <sup>0.47</sup>
AlphaNet ( $\rho = 0.4$ )	40.8 <sup>1.85</sup>	41.5 <sup>0.72</sup>	57.8 <sup>0.54</sup>	47.7 <sup>0.36</sup>
AlphaNet ( $\rho = 0.5$ )	39.7 <sup>1.42</sup>	42.0 <sup>0.66</sup>	58.3 <sup>0.52</sup>	48.0 <sup>0.37</sup>
AlphaNet ( $\rho = 0.75$ )	37.4 <sup>1.93</sup>	42.9 <sup>0.46</sup>	59.0 <sup>0.40</sup>	48.3 <sup>0.16</sup>
AlphaNet ( $\rho = 1$ )	34.6 <sup>1.88</sup>	43.7 <sup>0.51</sup>	59.7 <sup>0.43</sup>	48.6 <sup>0.24</sup>
AlphaNet ( $\rho = 1.25$ )	35.0 <sup>1.98</sup>	43.6 <sup>0.70</sup>	59.6 <sup>0.50</sup>	48.6 <sup>0.35</sup>
AlphaNet ( $\rho = 1.5$ )	32.6 <sup>2.46</sup>	44.4 <sup>0.49</sup>	60.3 <sup>0.38</sup>	48.9 <sup>0.19</sup>
AlphaNet ( $\rho = 1.75$ )	32.3 <sup>1.42</sup>	44.4 <sup>0.32</sup>	60.3 <sup>0.18</sup>	48.9 <sup>0.14</sup>
AlphaNet ( $\rho = 2$ )	31.5 <sup>1.99</sup>	44.7 <sup>0.46</sup>	60.5 <sup>0.30</sup>	49.0 <sup>0.12</sup>
AlphaNet ( $\rho = 3$ )	29.0 <sup>2.05</sup>	45.1 <sup>0.36</sup>	60.9 <sup>0.28</sup>	49.0 <sup>0.08</sup>

Table A1: AlphaNet with CRT baseline on ImageNet-LT.

## Appendix A Additional Results

This section contains additional analysis, as well as results on the long-tailed recognition (LTR) model<sup>[10]</sup>. The included results are

- Per-split accuracy with varying number of nearest numbers computed using Euclidean and cosine distance (Figure A1).
- Distribution of  $\alpha$  values across ‘few’ split classes for different number of nearest numbers computed using Euclidean distance (Figure A2).
- Tables of per-split accuracy comparing AlphaNet trained on a range of  $\rho$  values:
  - ImageNet-LT (Table A1, A2, A3).
  - Places-LT (Table A4, A5).
  - CIFAR-100-LT (Table A6, A7).
- Change in per-class accuracy for AlphaNet compared to baseline models:
  - ImageNet-LT (Figure A3, A4, A5).
  - Places-LT (Figure A6, A7).
  - CIFAR-100-LT (Figure A8, A9).
- Per-class test accuracy vs. mean distance to 5 nearest neighbors:
  - ImageNet-LT (Figure A10a, A10b, A10c).
  - Places-LT (Figure A11a, A11b).

– CIFAR-100-LT (Figure A12a, A12b).

- Distribution of  $\alpha$  values across ‘few’ split classes:
  - ImageNet-LT (Figure A13a, A13b, A13c).
  - Places-LT (Figure A14a, A14b).
  - CIFAR-100-LT (Figure A15a, A15b).

Experiment	Few	Med.	Many	Overall
Baseline	30.4	47.2	60.2	49.9
AlphaNet ( $\rho = 0.1$ )	53.9 <sup>0.77</sup>	29.4 <sup>1.22</sup>	44.2 <sup>1.22</sup>	38.5 <sup>1.03</sup>
AlphaNet ( $\rho = 0.2$ )	52.0 <sup>1.21</sup>	33.3 <sup>1.44</sup>	48.0 <sup>1.37</sup>	41.5 <sup>1.08</sup>
AlphaNet ( $\rho = 0.25$ )	51.1 <sup>0.63</sup>	34.4 <sup>1.04</sup>	48.9 <sup>0.99</sup>	42.3 <sup>0.82</sup>
AlphaNet ( $\rho = 0.3$ )	49.8 <sup>2.20</sup>	35.9 <sup>1.59</sup>	50.4 <sup>1.47</sup>	43.4 <sup>1.10</sup>
AlphaNet ( $\rho = 0.4$ )	48.7 <sup>1.17</sup>	37.4 <sup>1.13</sup>	51.6 <sup>0.95</sup>	44.4 <sup>0.80</sup>
AlphaNet ( $\rho = 0.5$ )	46.9 <sup>0.98</sup>	38.6 <sup>0.87</sup>	52.9 <sup>0.86</sup>	45.3 <sup>0.69</sup>
AlphaNet ( $\rho = 0.75$ )	45.3 <sup>1.89</sup>	40.2 <sup>1.28</sup>	54.4 <sup>1.01</sup>	46.3 <sup>0.76</sup>
AlphaNet ( $\rho = 1$ )	41.6 <sup>1.61</sup>	42.2 <sup>0.53</sup>	56.0 <sup>0.32</sup>	47.4 <sup>0.30</sup>
AlphaNet ( $\rho = 1.25$ )	42.5 <sup>1.41</sup>	42.1 <sup>0.74</sup>	56.0 <sup>0.53</sup>	47.5 <sup>0.41</sup>
AlphaNet ( $\rho = 1.5$ )	40.1 <sup>1.99</sup>	43.2 <sup>0.98</sup>	56.9 <sup>0.76</sup>	48.0 <sup>0.53</sup>
AlphaNet ( $\rho = 1.75$ )	39.4 <sup>2.53</sup>	43.5 <sup>0.88</sup>	57.1 <sup>0.70</sup>	48.2 <sup>0.45</sup>
AlphaNet ( $\rho = 2$ )	37.5 <sup>2.94</sup>	44.3 <sup>0.86</sup>	57.9 <sup>0.72</sup>	48.6 <sup>0.32</sup>
AlphaNet ( $\rho = 3$ )	34.5 <sup>1.91</sup>	45.3 <sup>0.54</sup>	58.7 <sup>0.37</sup>	49.0 <sup>0.21</sup>

Table A2: AlphaNet with LWS baseline on ImageNet-LT.

Experiment	Few	Med.	Many	Overall
Baseline	36.5	54.4	68.9	57.5
AlphaNet ( $\rho = 0.1$ )	49.2 <sup>0.69</sup>	49.5 <sup>0.40</sup>	65.4 <sup>0.16</sup>	55.6 <sup>0.19</sup>
AlphaNet ( $\rho = 0.2$ )	47.1 <sup>0.86</sup>	50.5 <sup>0.34</sup>	66.0 <sup>0.20</sup>	56.0 <sup>0.16</sup>
AlphaNet ( $\rho = 0.25$ )	46.8 <sup>0.59</sup>	50.7 <sup>0.29</sup>	66.2 <sup>0.25</sup>	56.2 <sup>0.23</sup>
AlphaNet ( $\rho = 0.3$ )	46.1 <sup>1.16</sup>	51.2 <sup>0.50</sup>	66.5 <sup>0.29</sup>	56.4 <sup>0.21</sup>
AlphaNet ( $\rho = 0.4$ )	44.7 <sup>1.13</sup>	51.7 <sup>0.39</sup>	66.9 <sup>0.24</sup>	56.6 <sup>0.22</sup>
AlphaNet ( $\rho = 0.5$ )	43.5 <sup>0.75</sup>	52.3 <sup>0.26</sup>	67.3 <sup>0.17</sup>	56.9 <sup>0.11</sup>
AlphaNet ( $\rho = 0.75$ )	41.7 <sup>0.63</sup>	52.8 <sup>0.18</sup>	67.7 <sup>0.15</sup>	57.0 <sup>0.12</sup>
AlphaNet ( $\rho = 1$ )	40.8 <sup>1.00</sup>	53.1 <sup>0.21</sup>	67.9 <sup>0.18</sup>	57.1 <sup>0.11</sup>
AlphaNet ( $\rho = 1.25$ )	39.0 <sup>1.28</sup>	53.4 <sup>0.22</sup>	68.2 <sup>0.16</sup>	57.2 <sup>0.05</sup>
AlphaNet ( $\rho = 1.5$ )	38.2 <sup>1.22</sup>	53.6 <sup>0.25</sup>	68.4 <sup>0.17</sup>	57.2 <sup>0.06</sup>
AlphaNet ( $\rho = 1.75$ )	37.7 <sup>0.89</sup>	53.7 <sup>0.14</sup>	68.4 <sup>0.10</sup>	57.2 <sup>0.05</sup>
AlphaNet ( $\rho = 2$ )	37.1 <sup>0.98</sup>	53.8 <sup>0.12</sup>	68.5 <sup>0.11</sup>	57.2 <sup>0.06</sup>
AlphaNet ( $\rho = 3$ )	34.5 <sup>1.23</sup>	54.3 <sup>0.14</sup>	68.8 <sup>0.11</sup>	57.2 <sup>0.08</sup>

Table A3: AlphaNet with RIDE baseline on ImageNet-LT.

Experiment	Few	Med.	Many	Overall
Baseline	24.9	37.6	42.0	36.7
AlphaNet ( $\rho = 0.1$ )	38.2 <sup>1.30</sup>	30.4 <sup>0.84</sup>	37.3 <sup>0.72</sup>	34.4 <sup>0.41</sup>
AlphaNet ( $\rho = 0.2$ )	34.8 <sup>1.42</sup>	32.4 <sup>0.66</sup>	39.0 <sup>0.29</sup>	35.3 <sup>0.15</sup>
AlphaNet ( $\rho = 0.25$ )	34.4 <sup>1.27</sup>	32.8 <sup>0.82</sup>	39.3 <sup>0.34</sup>	35.5 <sup>0.29</sup>
AlphaNet ( $\rho = 0.3$ )	33.2 <sup>1.57</sup>	33.4 <sup>0.75</sup>	39.5 <sup>0.60</sup>	35.6 <sup>0.25</sup>
AlphaNet ( $\rho = 0.4$ )	32.4 <sup>1.47</sup>	33.8 <sup>0.69</sup>	39.8 <sup>0.46</sup>	35.7 <sup>0.22</sup>
AlphaNet ( $\rho = 0.5$ )	31.0 <sup>0.88</sup>	34.5 <sup>0.17</sup>	40.4 <sup>0.29</sup>	35.9 <sup>0.09</sup>
AlphaNet ( $\rho = 0.75$ )	28.6 <sup>1.27</sup>	35.5 <sup>0.40</sup>	41.0 <sup>0.13</sup>	36.1 <sup>0.11</sup>
AlphaNet ( $\rho = 1$ )	27.0 <sup>1.02</sup>	36.1 <sup>0.31</sup>	41.3 <sup>0.13</sup>	36.2 <sup>0.10</sup>
AlphaNet ( $\rho = 1.25$ )	26.9 <sup>1.23</sup>	36.0 <sup>0.47</sup>	41.3 <sup>0.14</sup>	36.1 <sup>0.16</sup>
AlphaNet ( $\rho = 1.5$ )	25.5 <sup>0.89</sup>	36.5 <sup>0.36</sup>	41.6 <sup>0.21</sup>	36.2 <sup>0.11</sup>
AlphaNet ( $\rho = 1.75$ )	25.4 <sup>1.32</sup>	36.5 <sup>0.29</sup>	41.5 <sup>0.23</sup>	36.2 <sup>0.11</sup>
AlphaNet ( $\rho = 2$ )	24.9 <sup>1.38</sup>	36.6 <sup>0.49</sup>	41.5 <sup>0.20</sup>	36.1 <sup>0.10</sup>
AlphaNet ( $\rho = 3$ )	22.3 <sup>1.56</sup>	37.3 <sup>0.28</sup>	41.9 <sup>0.20</sup>	36.1 <sup>0.14</sup>

Table A4: AlphaNet with cRT baseline on Places-LT.

Experiment	Few	Med.	Many	Overall
Baseline	28.7	39.1	40.6	37.6
AlphaNet ( $\rho = 0.1$ )	42.5 <sup>1.03</sup>	29.5 <sup>1.01</sup>	34.4 <sup>0.94</sup>	33.8 <sup>0.58</sup>
AlphaNet ( $\rho = 0.2$ )	41.3 <sup>1.30</sup>	31.0 <sup>0.81</sup>	35.5 <sup>0.81</sup>	34.6 <sup>0.44</sup>
AlphaNet ( $\rho = 0.25$ )	40.5 <sup>2.25</sup>	30.9 <sup>2.92</sup>	35.6 <sup>2.20</sup>	34.4 <sup>1.67</sup>
AlphaNet ( $\rho = 0.3$ )	38.7 <sup>1.13</sup>	33.2 <sup>1.12</sup>	37.0 <sup>0.70</sup>	35.6 <sup>0.51</sup>
AlphaNet ( $\rho = 0.4$ )	38.0 <sup>1.45</sup>	33.6 <sup>1.18</sup>	37.3 <sup>0.65</sup>	35.8 <sup>0.50</sup>
AlphaNet ( $\rho = 0.5$ )	37.1 <sup>1.39</sup>	34.4 <sup>0.80</sup>	37.7 <sup>0.52</sup>	36.1 <sup>0.31</sup>
AlphaNet ( $\rho = 0.75$ )	35.5 <sup>1.25</sup>	35.3 <sup>0.59</sup>	38.5 <sup>0.28</sup>	36.5 <sup>0.16</sup>
AlphaNet ( $\rho = 1$ )	34.6 <sup>0.97</sup>	35.8 <sup>0.54</sup>	38.6 <sup>0.39</sup>	36.6 <sup>0.22</sup>
AlphaNet ( $\rho = 1.25$ )	32.6 <sup>1.28</sup>	36.8 <sup>0.60</sup>	39.3 <sup>0.39</sup>	36.9 <sup>0.19</sup>
AlphaNet ( $\rho = 1.5$ )	32.2 <sup>1.17</sup>	37.2 <sup>0.36</sup>	39.5 <sup>0.39</sup>	37.0 <sup>0.11</sup>
AlphaNet ( $\rho = 1.75$ )	31.7 <sup>1.35</sup>	37.3 <sup>0.43</sup>	39.5 <sup>0.27</sup>	37.0 <sup>0.09</sup>
AlphaNet ( $\rho = 2$ )	30.9 <sup>1.28</sup>	37.6 <sup>0.40</sup>	39.8 <sup>0.18</sup>	37.1 <sup>0.14</sup>
AlphaNet ( $\rho = 3$ )	27.8 <sup>1.94</sup>	38.5 <sup>0.51</sup>	40.2 <sup>0.29</sup>	37.1 <sup>0.10</sup>

Table A5: AlphaNet with LWS baseline on Places-LT.

Experiment	Few	Med.	Many	Overall
Baseline	25.8	52.1	69.3	50.2
AlphaNet ( $\rho = 0.1$ )	38.2 <sup>3.22</sup>	38.1 <sup>5.01</sup>	56.3 <sup>7.65</sup>	44.5 <sup>3.50</sup>
AlphaNet ( $\rho = 0.2$ )	36.0 <sup>4.34</sup>	41.4 <sup>5.41</sup>	59.1 <sup>8.31</sup>	45.9 <sup>3.58</sup>
AlphaNet ( $\rho = 0.25$ )	34.0 <sup>1.70</sup>	44.1 <sup>1.68</sup>	62.6 <sup>1.54</sup>	47.6 <sup>0.76</sup>
AlphaNet ( $\rho = 0.3$ )	32.9 <sup>1.20</sup>	45.3 <sup>1.02</sup>	64.0 <sup>0.78</sup>	48.1 <sup>0.51</sup>
AlphaNet ( $\rho = 0.4$ )	31.1 <sup>1.27</sup>	45.6 <sup>1.63</sup>	64.8 <sup>1.22</sup>	48.0 <sup>0.84</sup>
AlphaNet ( $\rho = 0.5$ )	30.9 <sup>1.82</sup>	47.0 <sup>1.25</sup>	65.7 <sup>0.94</sup>	48.7 <sup>0.41</sup>
AlphaNet ( $\rho = 0.75$ )	28.6 <sup>1.63</sup>	48.3 <sup>0.84</sup>	66.6 <sup>0.65</sup>	48.8 <sup>0.26</sup>
AlphaNet ( $\rho = 1$ )	27.2 <sup>1.69</sup>	49.1 <sup>0.85</sup>	67.4 <sup>0.62</sup>	48.9 <sup>0.30</sup>
AlphaNet ( $\rho = 1.25$ )	26.1 <sup>1.54</sup>	49.8 <sup>0.59</sup>	68.0 <sup>0.47</sup>	49.1 <sup>0.42</sup>
AlphaNet ( $\rho = 1.5$ )	25.0 <sup>1.15</sup>	50.1 <sup>1.12</sup>	67.9 <sup>1.01</sup>	48.8 <sup>0.63</sup>
AlphaNet ( $\rho = 1.75$ )	24.8 <sup>1.09</sup>	50.3 <sup>0.61</sup>	68.4 <sup>0.33</sup>	49.0 <sup>0.27</sup>
AlphaNet ( $\rho = 2$ )	24.3 <sup>1.74</sup>	51.0 <sup>0.55</sup>	68.9 <sup>0.47</sup>	49.2 <sup>0.34</sup>
AlphaNet ( $\rho = 3$ )	22.2 <sup>1.71</sup>	51.6 <sup>0.86</sup>	69.3 <sup>0.58</sup>	49.0 <sup>0.31</sup>

Table A6: AlphaNet with RIDE baseline on CIFAR-100-LT.

Experiment	Few	Med.	Many	Overall
Baseline	33.6	49.4	69.7	51.8
AlphaNet ( $\rho = 0.1$ )	40.9 <sup>4.12</sup>	37.4 <sup>7.63</sup>	62.1 <sup>5.07</sup>	47.1 <sup>3.27</sup>
AlphaNet ( $\rho = 0.2$ )	42.6 <sup>2.47</sup>	32.9 <sup>4.98</sup>	58.7 <sup>3.36</sup>	44.8 <sup>2.43</sup>
AlphaNet ( $\rho = 0.25$ )	42.3 <sup>2.45</sup>	34.4 <sup>6.36</sup>	59.5 <sup>4.83</sup>	45.5 <sup>3.31</sup>
AlphaNet ( $\rho = 0.3$ )	40.9 <sup>3.77</sup>	36.6 <sup>6.76</sup>	61.3 <sup>4.78</sup>	46.6 <sup>3.14</sup>
AlphaNet ( $\rho = 0.4$ )	42.3 <sup>1.73</sup>	33.1 <sup>6.20</sup>	58.9 <sup>4.24</sup>	44.9 <sup>3.25</sup>
AlphaNet ( $\rho = 0.5$ )	43.2 <sup>1.17</sup>	32.1 <sup>4.73</sup>	58.7 <sup>3.55</sup>	44.7 <sup>2.64</sup>
AlphaNet ( $\rho = 0.75$ )	43.1 <sup>1.45</sup>	31.3 <sup>5.14</sup>	57.7 <sup>4.01</sup>	44.1 <sup>2.95</sup>
AlphaNet ( $\rho = 1$ )	42.5 <sup>2.31</sup>	31.3 <sup>6.45</sup>	57.4 <sup>4.50</sup>	43.8 <sup>3.21</sup>
AlphaNet ( $\rho = 1.25$ )	41.7 <sup>4.03</sup>	33.4 <sup>8.11</sup>	59.1 <sup>5.61</sup>	44.9 <sup>3.91</sup>
AlphaNet ( $\rho = 1.5$ )	43.6 <sup>0.87</sup>	31.3 <sup>3.49</sup>	57.8 <sup>2.57</sup>	44.3 <sup>1.95</sup>
AlphaNet ( $\rho = 1.75$ )	42.7 <sup>0.70</sup>	30.0 <sup>4.75</sup>	56.5 <sup>3.51</sup>	43.1 <sup>2.93</sup>
AlphaNet ( $\rho = 2$ )	43.1 <sup>0.79</sup>	28.4 <sup>1.86</sup>	55.4 <sup>1.59</sup>	42.2 <sup>1.39</sup>
AlphaNet ( $\rho = 3$ )	43.2 <sup>0.93</sup>	28.0 <sup>2.00</sup>	55.3 <sup>1.45</sup>	42.1 <sup>1.43</sup>

Table A7: AlphaNet with LTR baseline on CIFAR-100-LT.

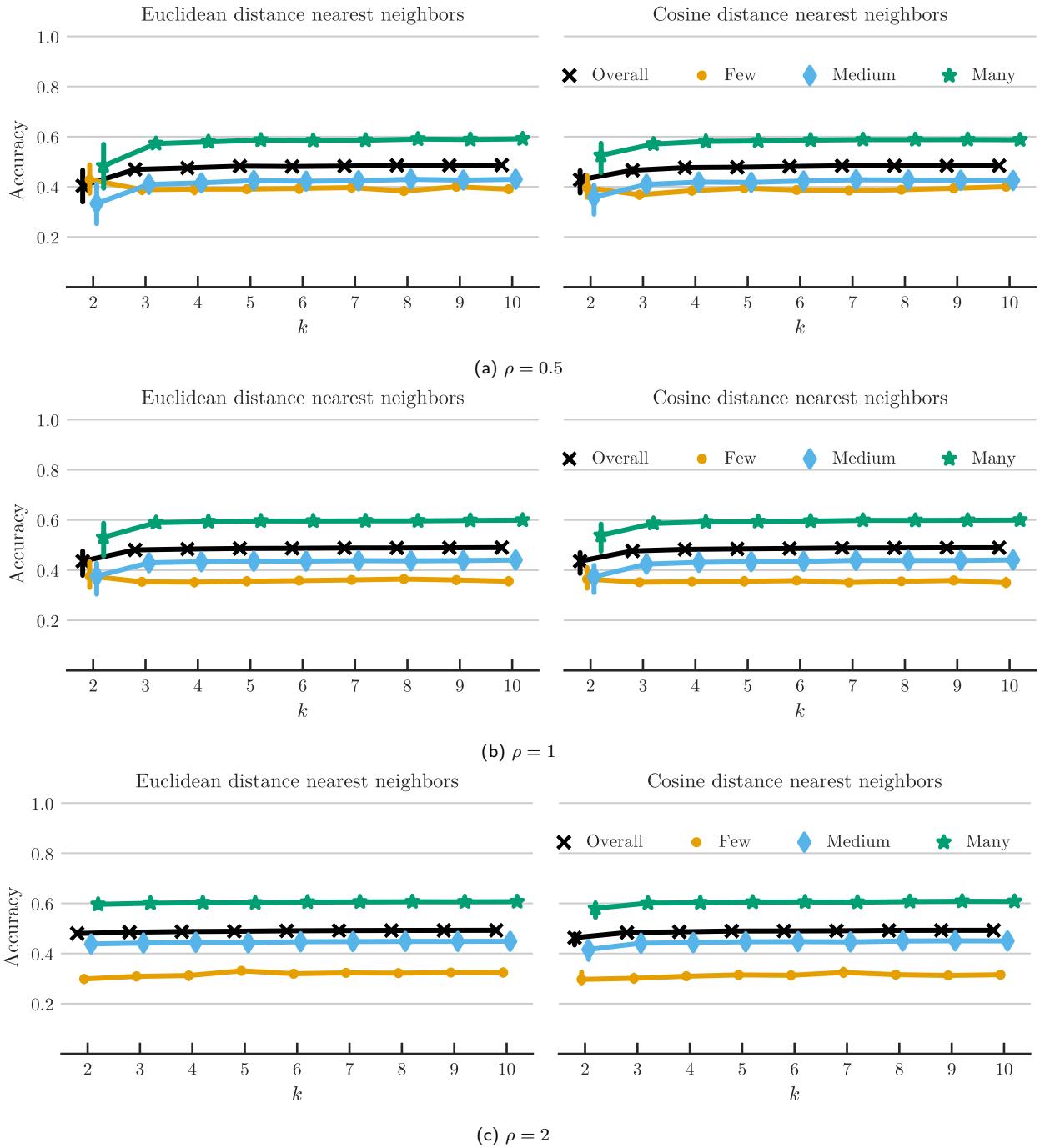


Figure A1: Per-split accuracies on ImageNet-LT with varying number of nearest neighbors for AlphaNet on cRT baseline.

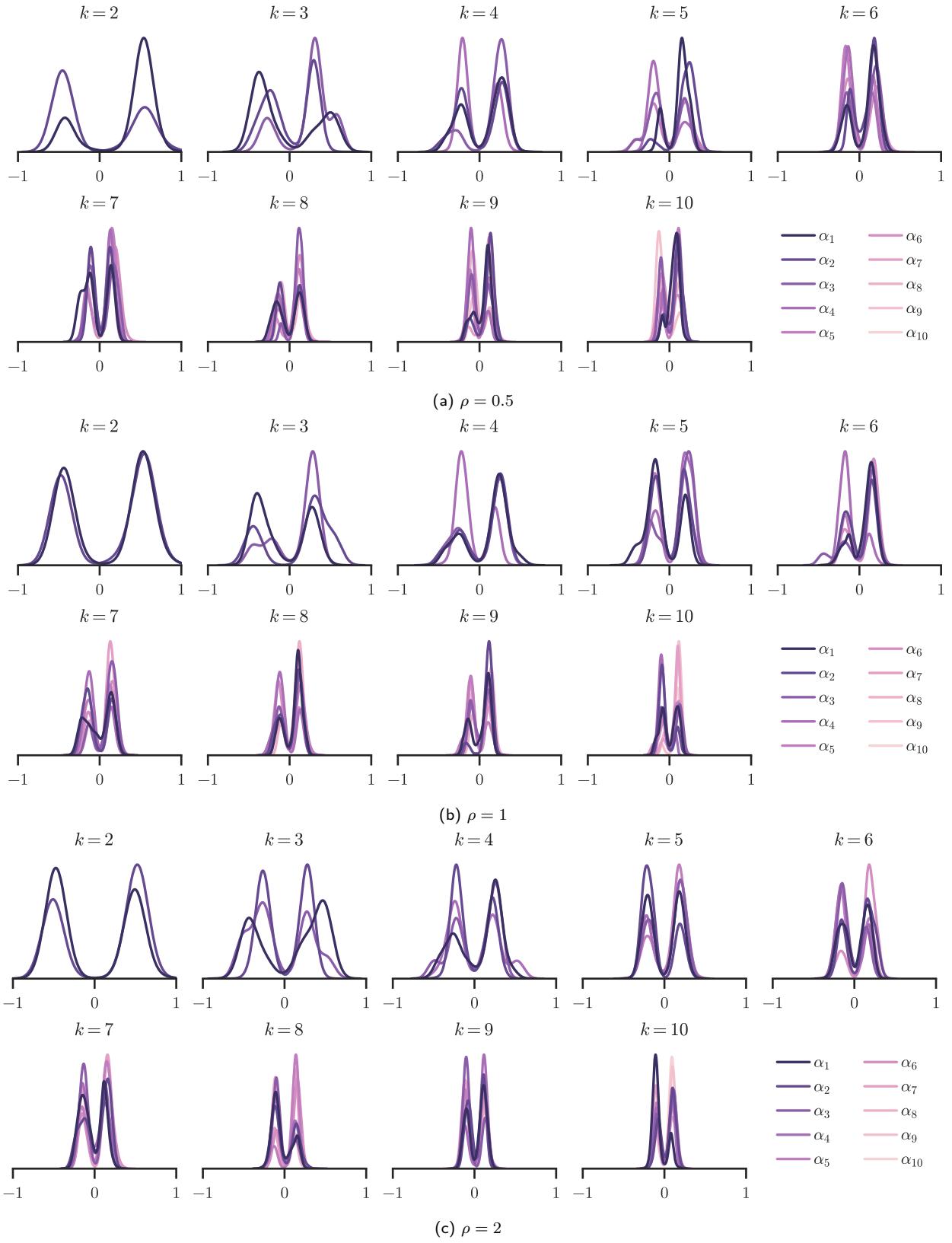


Figure A2: Distribution of  $\alpha$  values across  $k$  for AlphaNet with cRT baseline trained on ImageNet-LT.

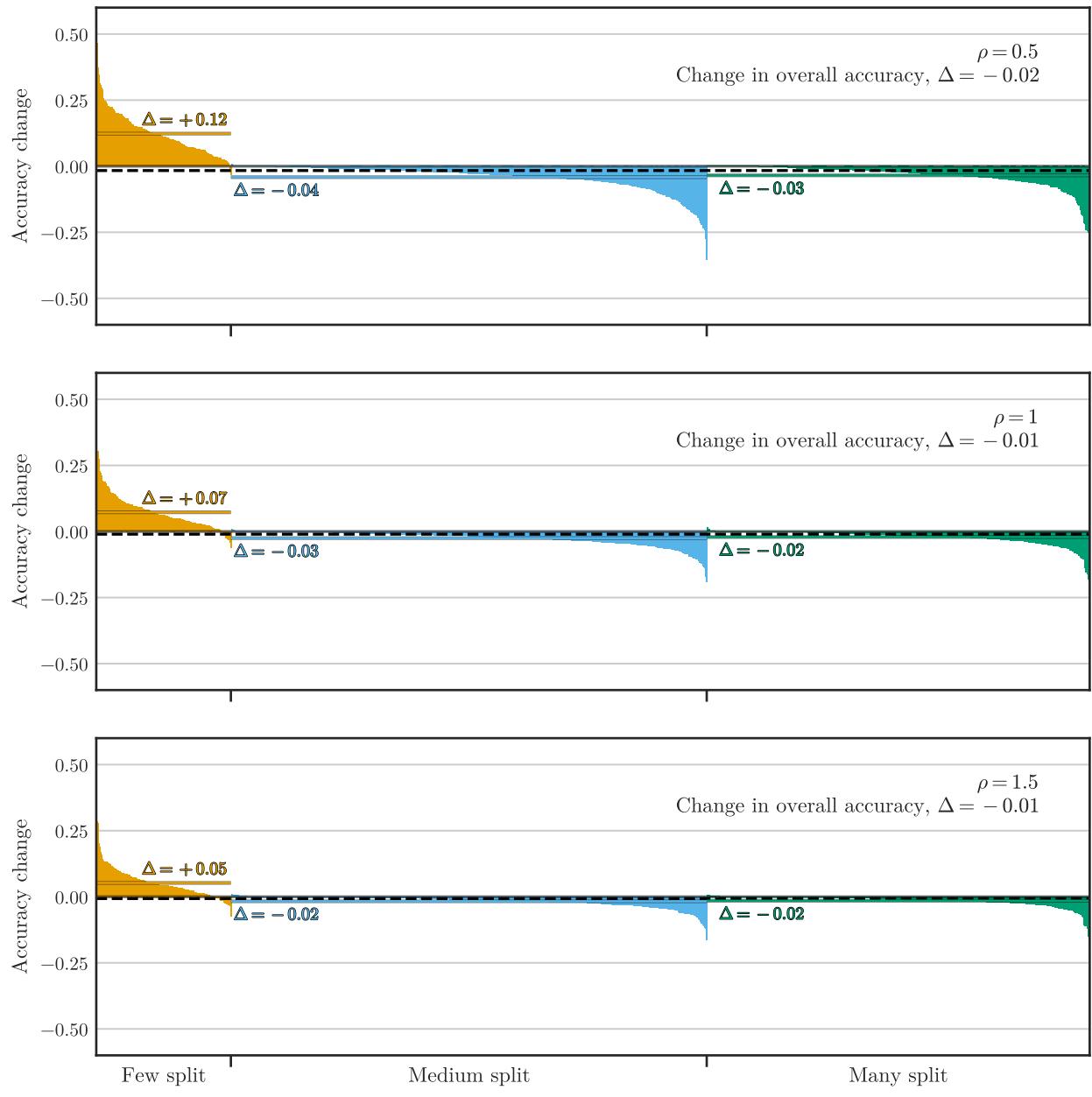


Figure A3: Change in per-class accuracy on ImageNet-LT with AlphaNet on cRT. The  $\Delta$ s indicate the average change in split accuracy.

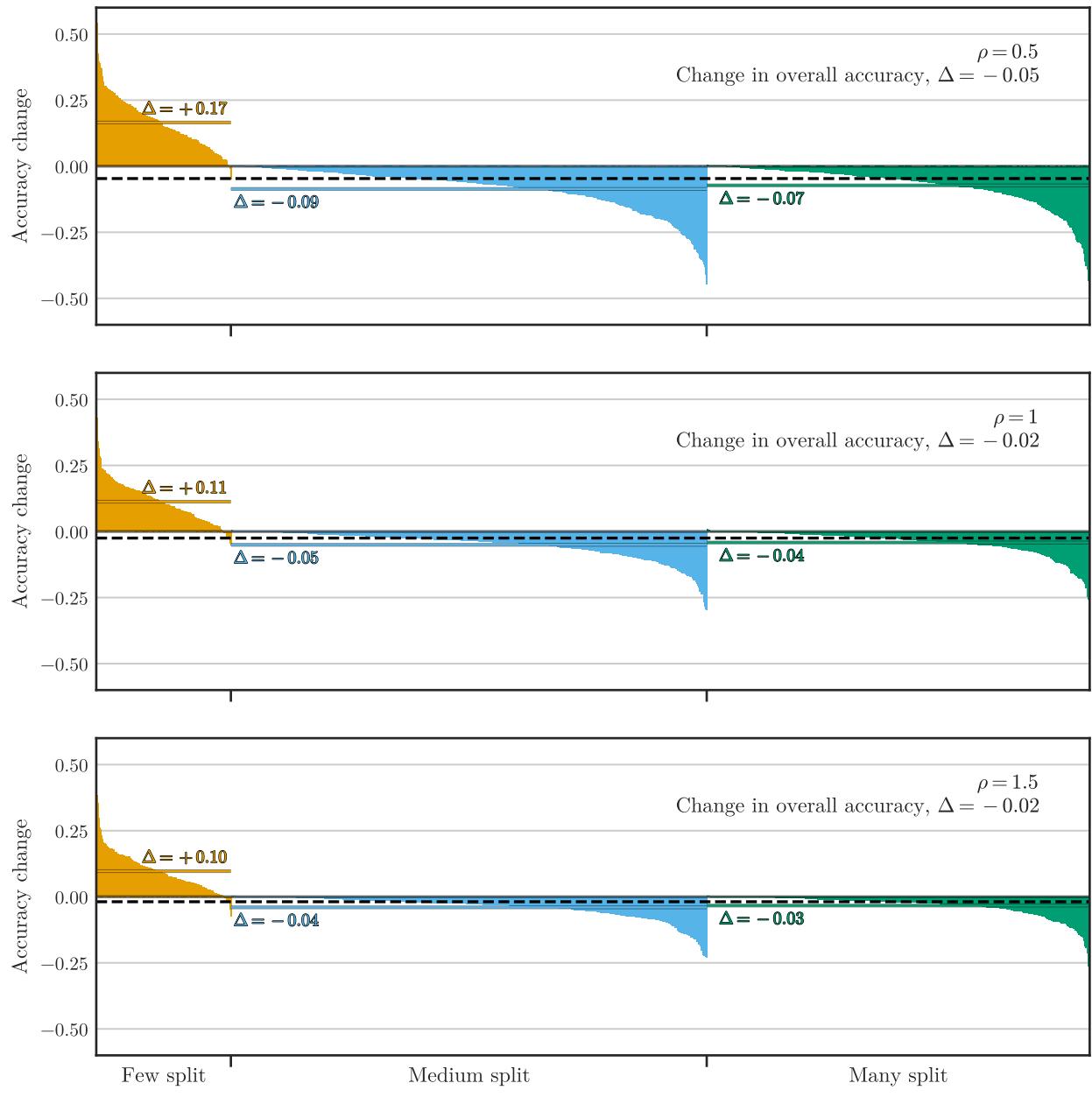


Figure A4: Change in per-class accuracy on ImageNet-LT with AlphaNet on LWS. The  $\Delta$ s indicate the average change in split accuracy.

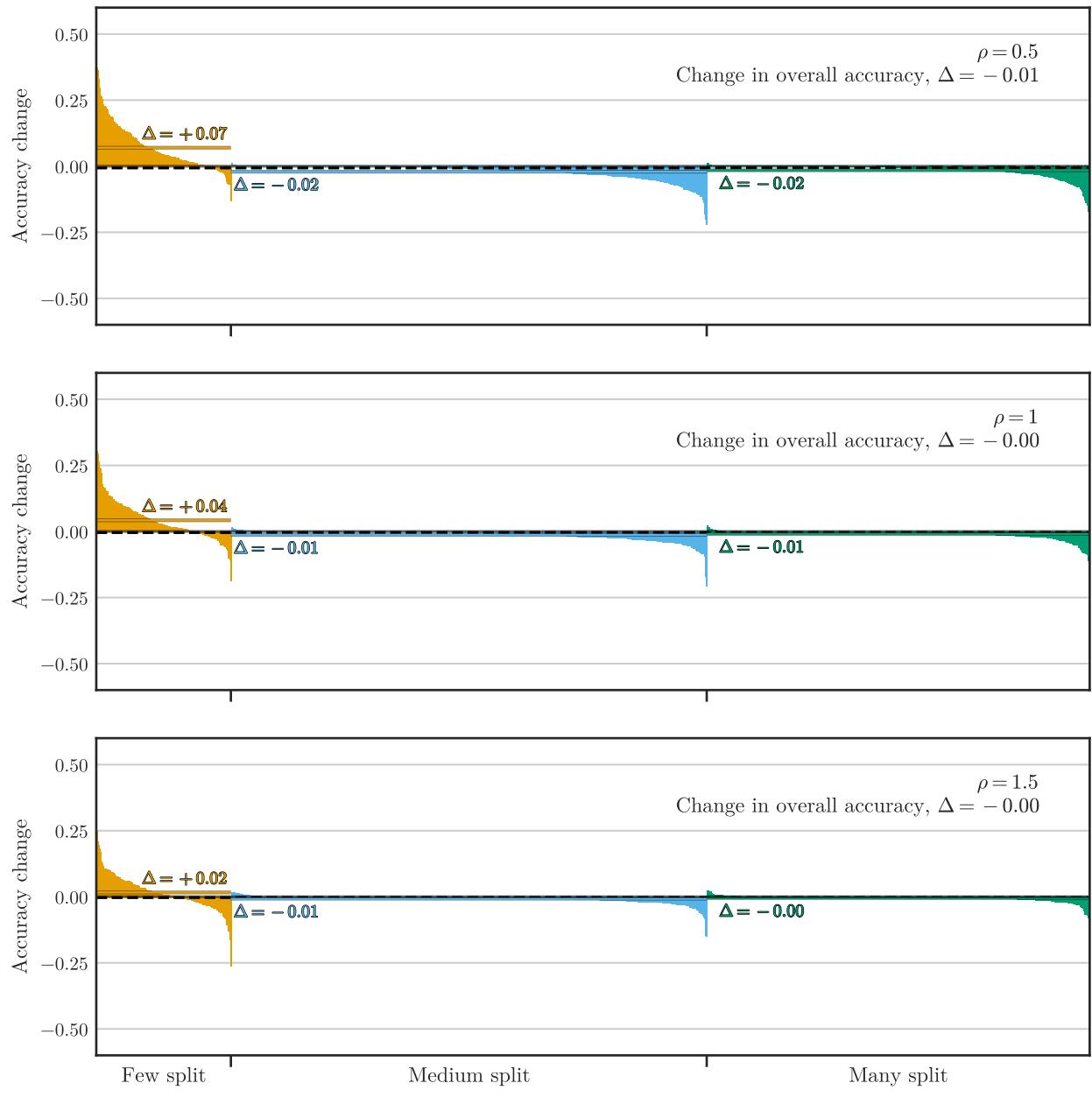


Figure A5: Change in per-class accuracy on ImageNet-LT with AlphaNet on RIDE. The  $\Delta$ s indicate the average change in split accuracy.

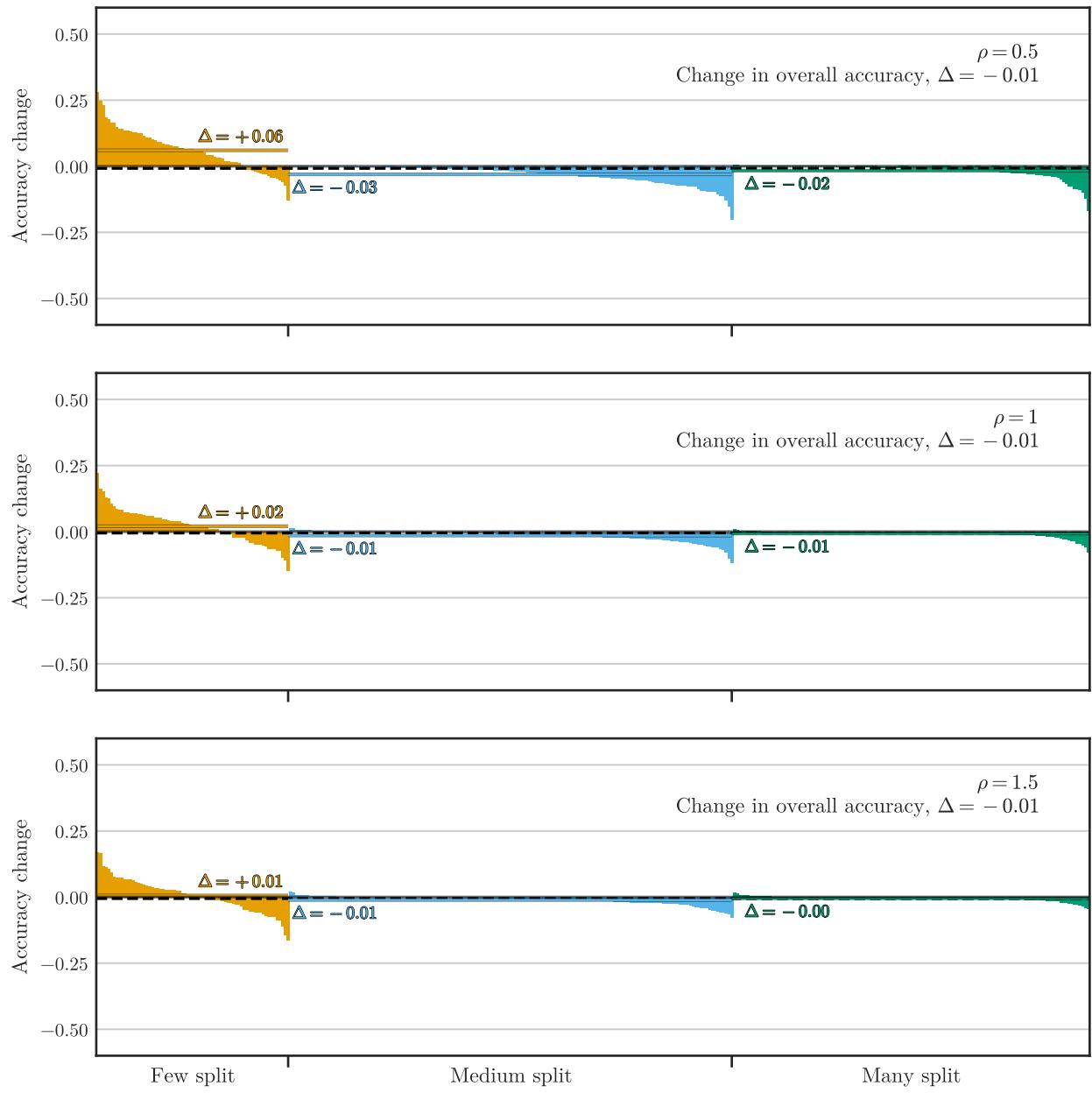


Figure A6: Change in per-class accuracy on Places-LT with AlphaNet on cRT. The  $\Delta$ s indicate the average change in split accuracy.

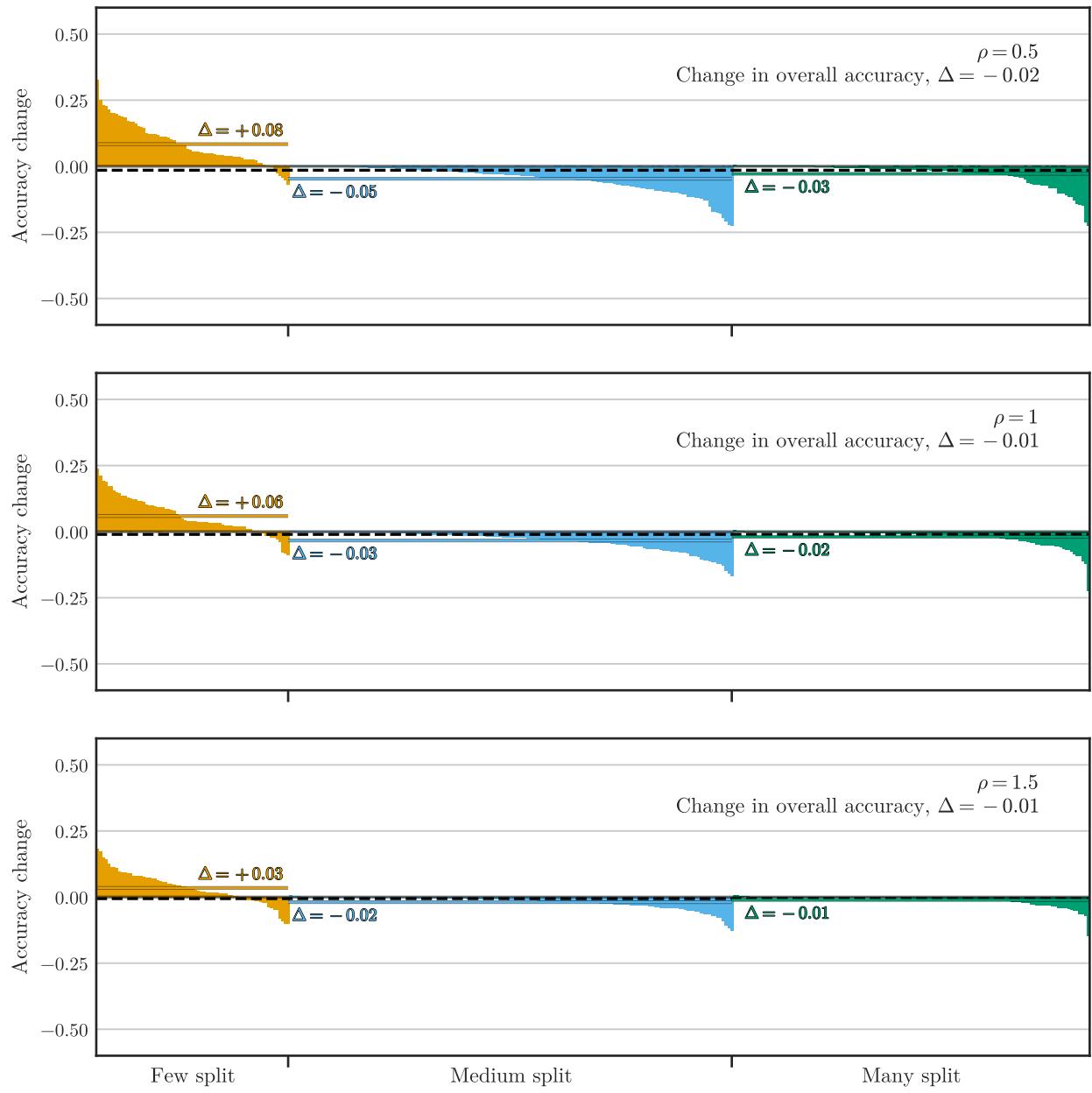


Figure A7: Change in per-class accuracy on Places-LT with AlphaNet on LWS. The  $\Delta$ s indicate the average change in split accuracy.

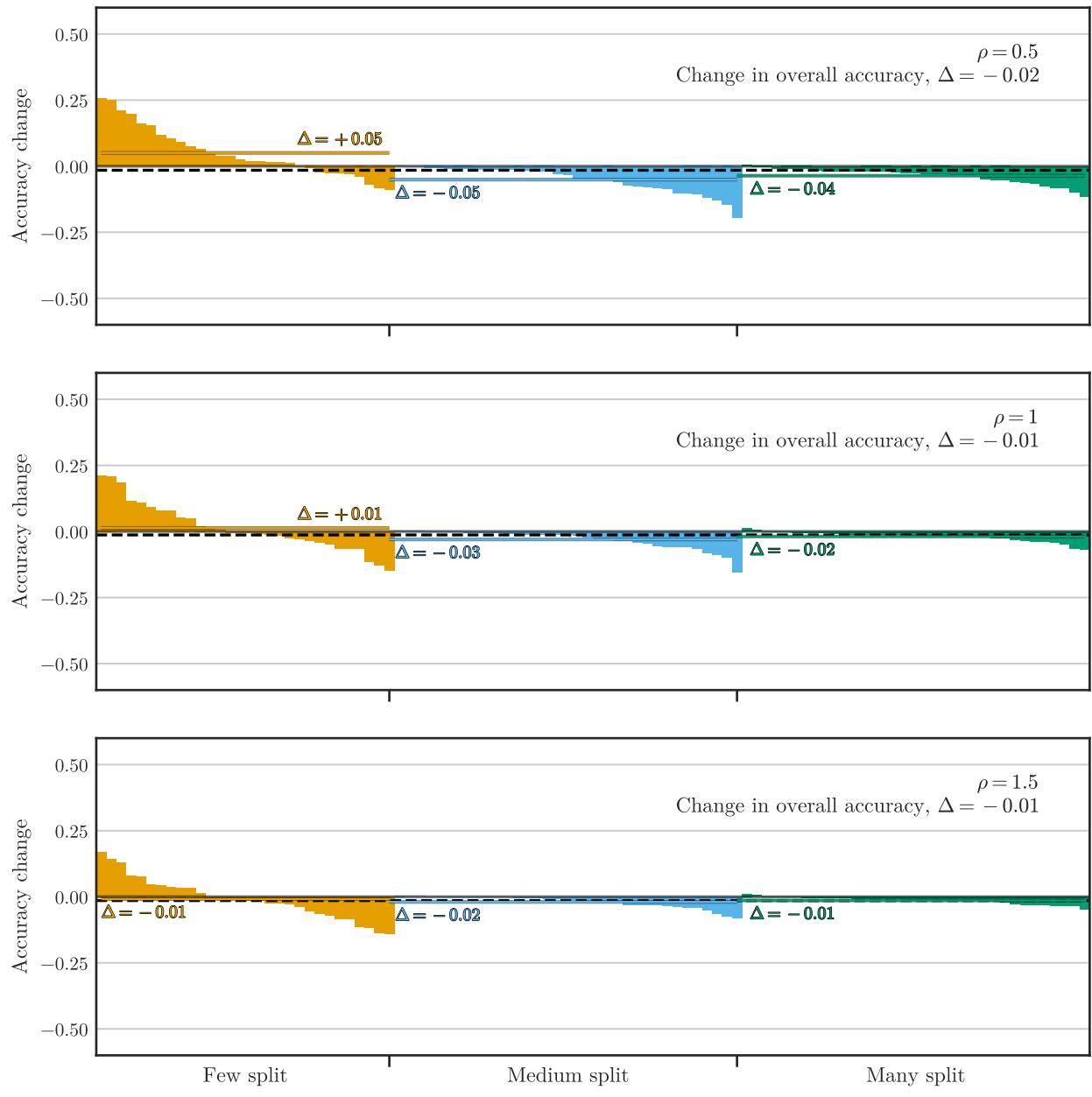


Figure A8: Change in per-class accuracy on CIFAR-100-LT with AlphaNet on RIDE. The  $\Delta$ s indicate the average change in split accuracy.

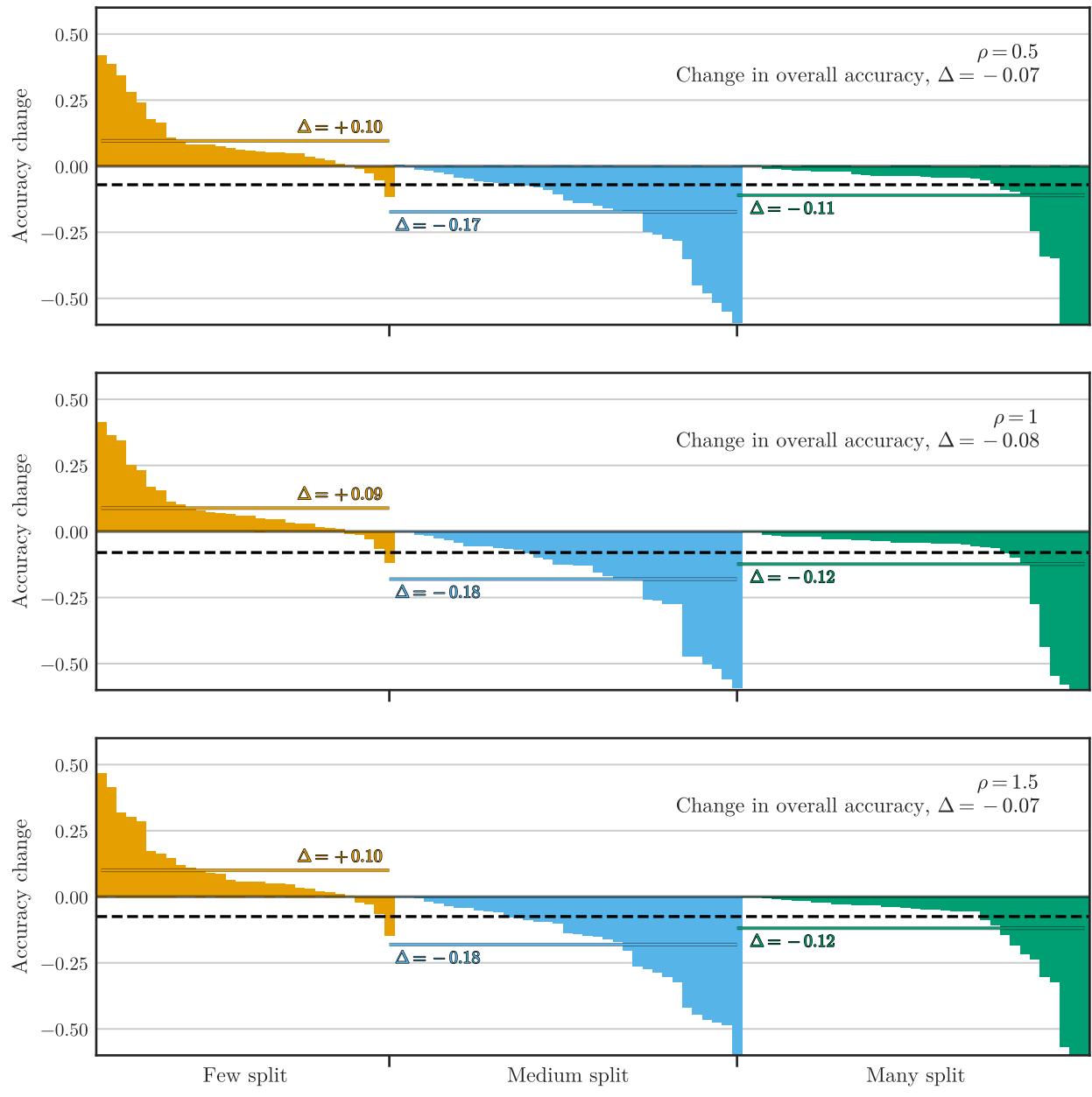


Figure A9: Change in per-class accuracy on CIFAR-100-LT with AlphaNet on LTR. The  $\Delta$ s indicate the average change in split accuracy.

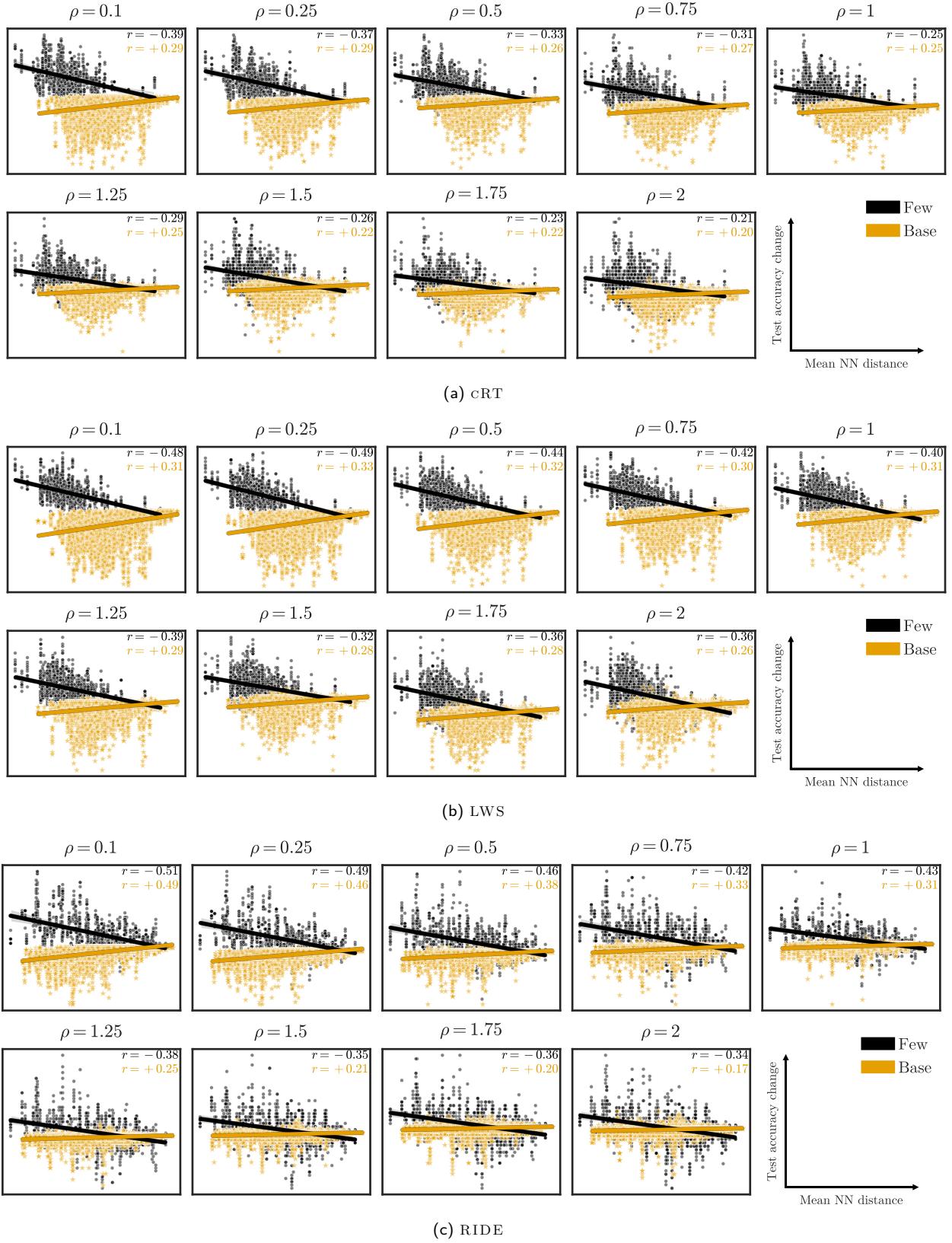


Figure A10: Test accuracy on ImageNet-LT vs. mean nearest neighbor distance for AlphaNet trained with  $k = 5$  neighbors. The lines show regression fits, and the  $r$  values in the upper right are Pearson correlations.

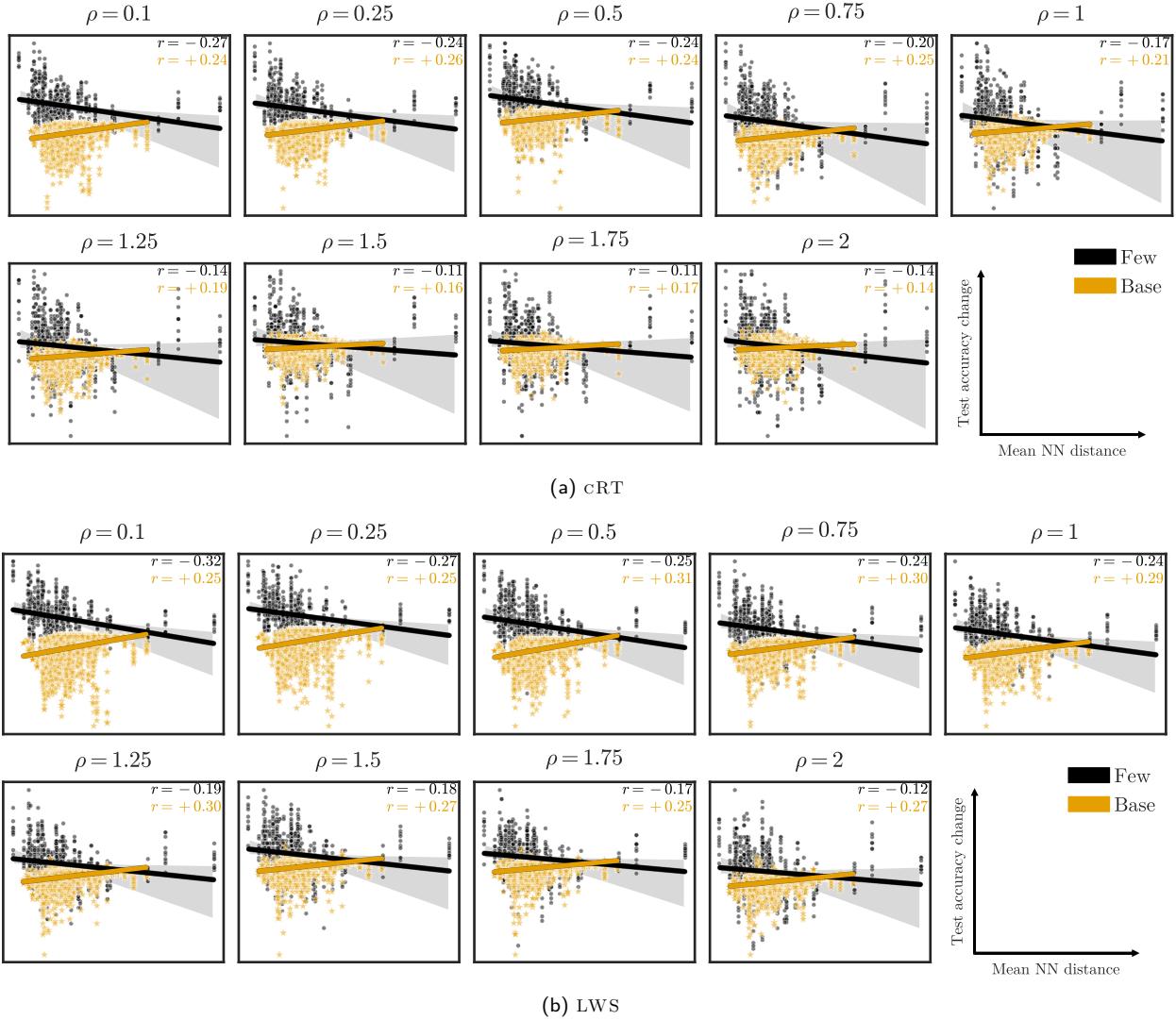


Figure A11: Test accuracy on Places-LT vs. mean nearest neighbor distance for AlphaNet trained with  $k = 5$  neighbors. The lines show regression fits, and the  $r$  values in the upper right are Pearson correlations.

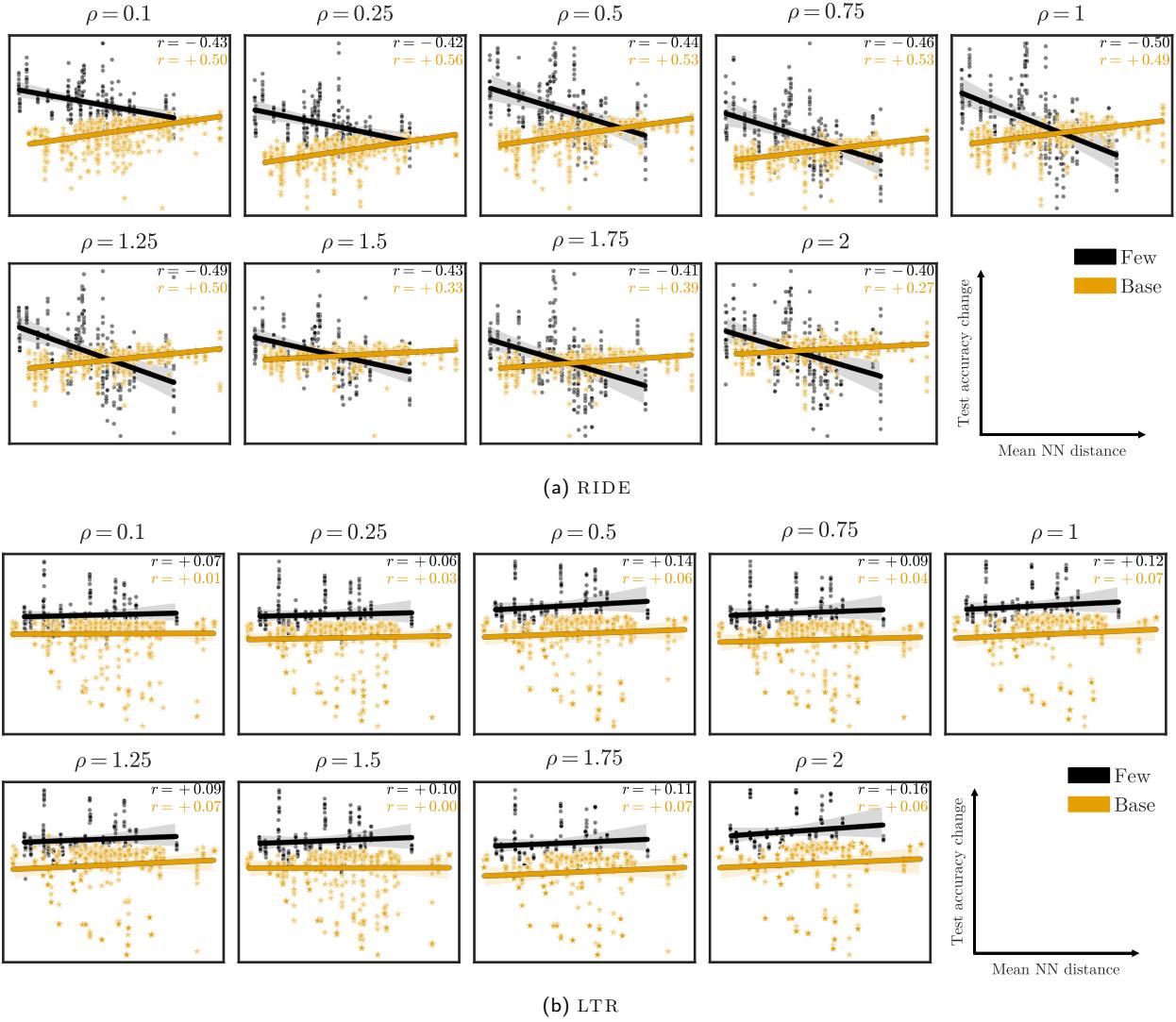


Figure A12: Test accuracy on CIFAR-100-LT vs. mean nearest neighbor distance for AlphaNet trained with  $k = 5$  neighbors. The lines show regression fits, and the  $r$  values in the upper right are Pearson correlations.

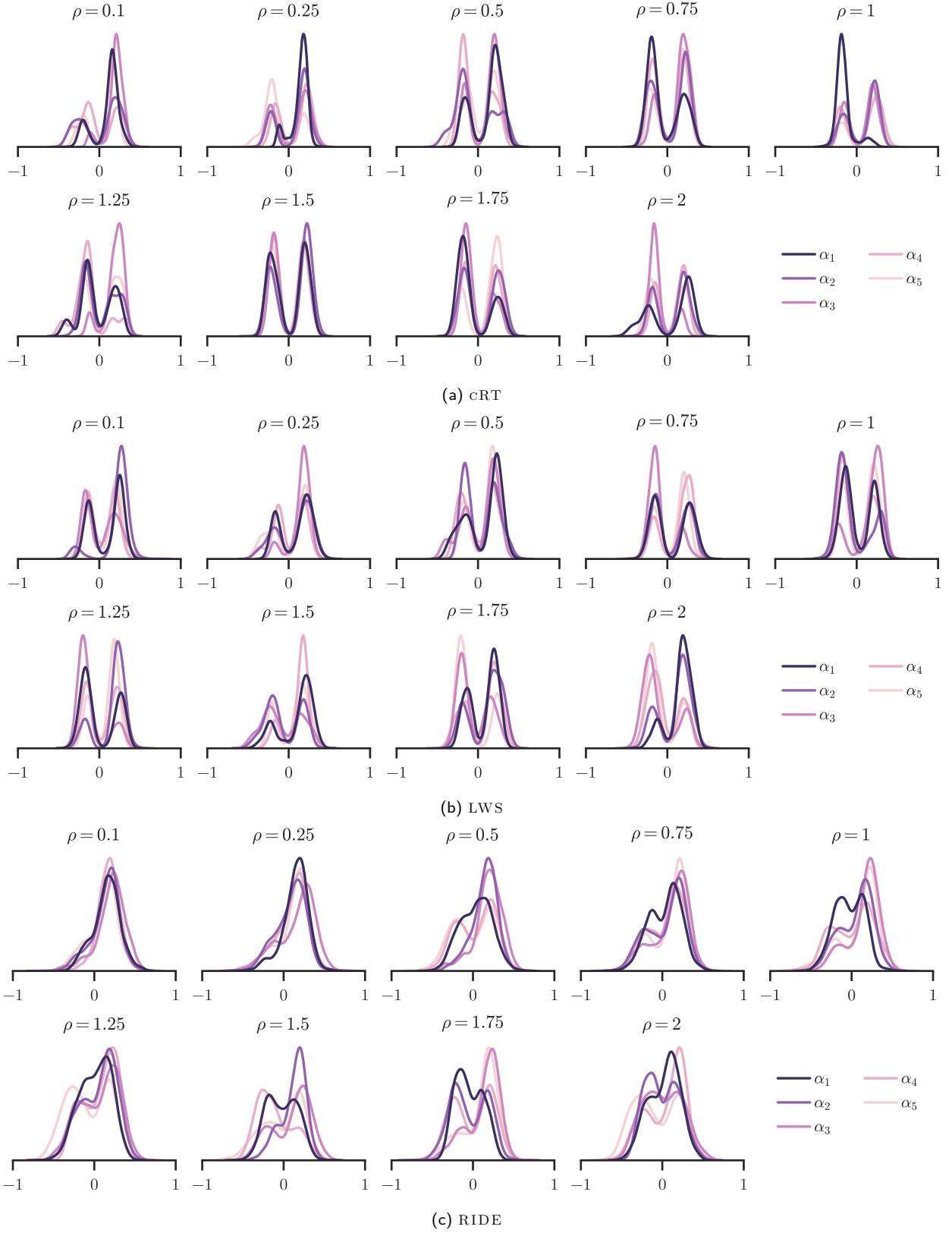


Figure A13: Distribution of  $\alpha$ s for AlphaNet trained on ImageNet-LT.

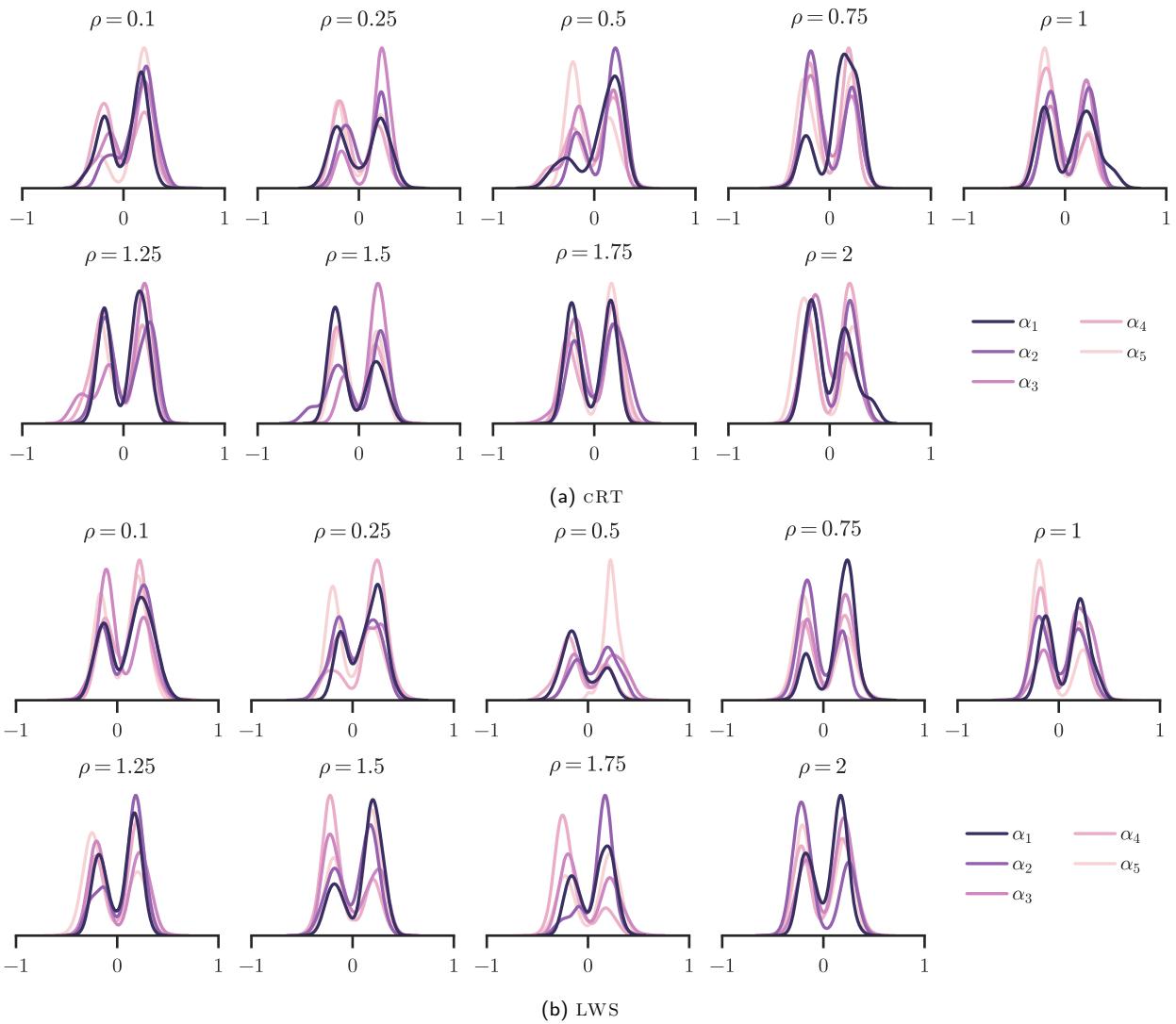


Figure A14: Distribution of  $\alpha$ s for AlphaNet trained on Places-LT.

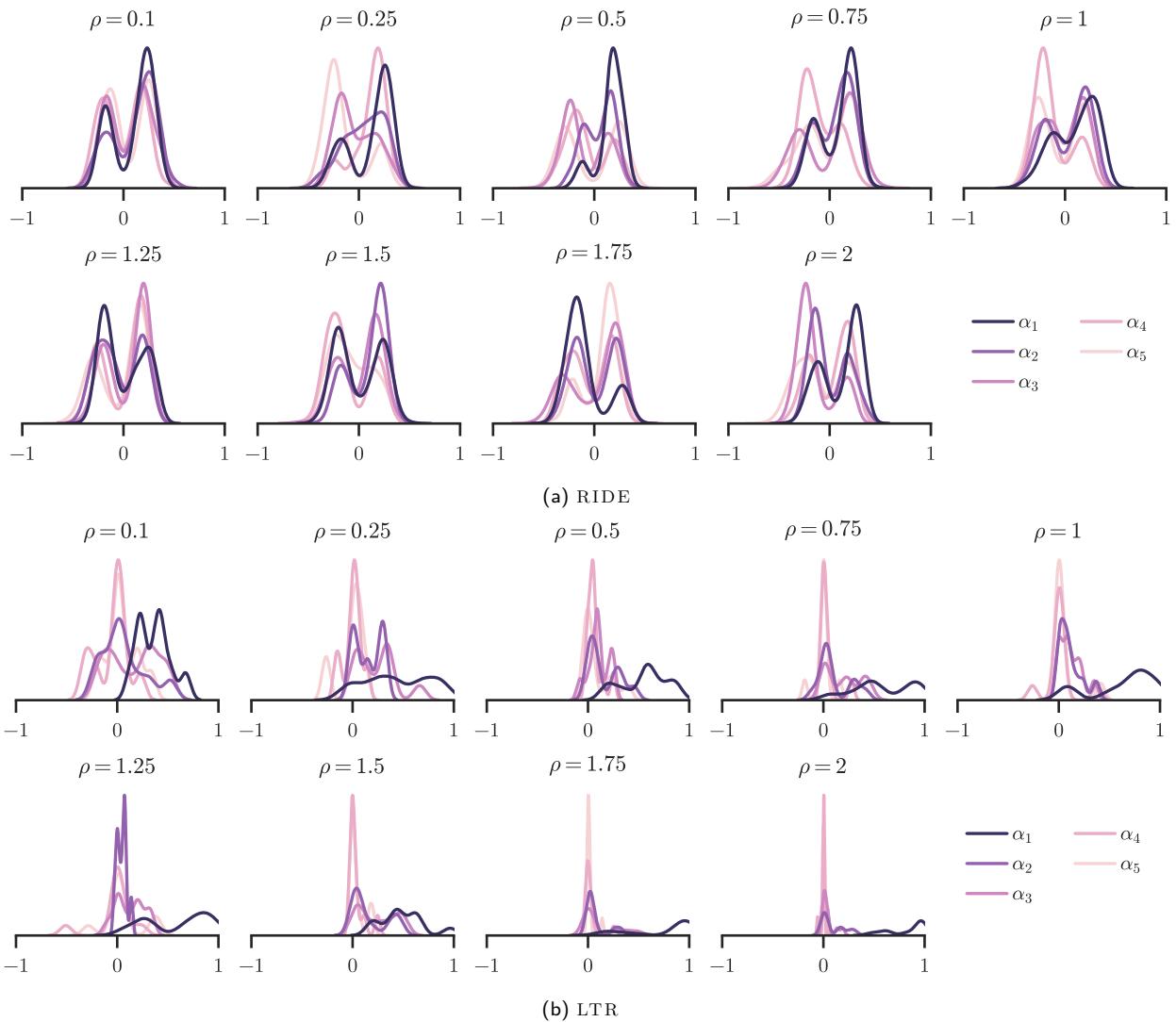


Figure A15: Distribution of  $\alpha$ s for AlphaNet trained on CIFAR-100-LT.