# Bank Marketing Prediction MA 5790

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# Introduction:

In the current financial setting, a bank's performance is largely determined by how well its marketing campaigns operate, especially when it comes to advertising term deposit services. As new marketing strategies such as phone campaigns take off, financial institutions are under pressure to find new customers quickly and improve the services they provide. In light of this, the application of data mining techniques has attracted a lot of interest, particularly when it comes to accurately and perceptively managing enormous volumes of data.

The goal of this study is to investigate the effectiveness of predictive models in relation to direct marketing campaigns for term deposit subscriptions run by a Portuguese banking company. Using a dataset with several samples and predictive variables, the main objective is to predict whether or not clients would sign up for term deposits. The objective is to identify the best predictive model for customer subscription prediction by analyzing several models, such as Support Vector Machines, Neural Networks, etc.

The methodology involves numerous stages of carefully understanding the data, creating dummy variables for all the categorical columns, resolving imbalance in the dataset, and carefully spending our data into training and testing. The ultimate goal is to identify a best predictive model that can forecast consumer subscriptions with enough accuracy to offer crucial insights to improve customer engagement and future marketing tactics. This study aims to improve marketing precision in the banking industry by utilizing cutting-edge datadriven techniques. This would enable institutions to better customize their tactics and build deeper relationships with their clients.

#### Data:

The dataset involves information about marketing campaigns conducted by a Portuguese bank through phone calls. In these campaigns, multiple contacts with the same client were made to determine whether the client would subscribe to a bank term deposit ('yes') or not ('no'). Here's a simple breakdown:

- Number of Samples: The dataset includes records from 45,210 marketing interactions.
- Number of Variables: There are 17 different aspects of information considered in each interaction.
- ➤ Categorical Predictors: 9 of these variables are categorical, indicating characteristics with distinct categories (e.g., job type, marital status).

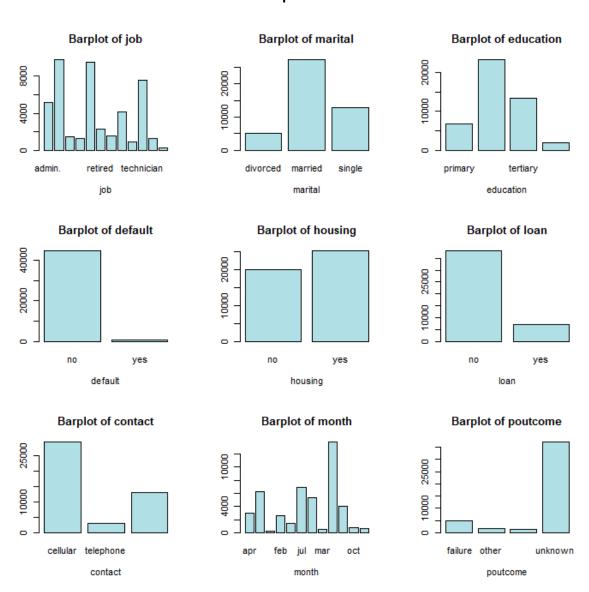
- ➤ **Continuous Predictors:** 7 variables are continuous, representing numerical data (e.g., age, balance).
- ➤ **Target Variable:** There is 1 main variable of interest, which is likely whether the client subscribed to the bank term deposit ('yes') or not ('no').

Below table explains the description of predictors:

Categorical Predictors (Binary)			
Variable Name	Description		
Default	Has credit in default?		
Housing	Has housing loan?		
Loan	Has personal loan?		
<b>Deposit</b> (Target)	has the client subscribed a term deposit?		
Categorical Pro	Categorical Predictors		
Job	Type of job : admin, blue-collar, entrepreneur, etc.		
Marital	Marital Status		
Education	Education level		
Contact	Contact communication type: cellular, telephone		
Month	Last contact month of year		
Poutcome	Outcome of the previous marketing campaignt month of year: failure, nonexistent, success		
Continuous Predictors			
Age	Age		
Balance	average yearly balance		
Day	Last contact day of the week		

Duration	last contact duration, in seconds
Campaign	number of contacts performed during this campaign and for this client
Pdays	number of days that passed by after the client was last contacted from a previous campaign
Previous	number of contacts performed before this campaign and for this client

**Table 1. Description of Predictors** 



**Distribution of Categorical Predictors** 

## Preprocessing:

#### Missing Data

Since our data doesn't have any missing values, we didn't perform any imputation.

#### **Dummy Variables**

Converted categorical predictors into dummy variables using the "dummyVars" function. We got a total of 48 predictors after adding dummy variables.

#### Near Zero Variance

After creating dummy variables, we checked for degenerates and removed them. These are the near zero predictors that we found using "nearZeroVar" function, "default", "pdays", "jobentrepreneur", "jobhousemaid", "jobself-employed", "jobstudent", "jobunemployed", "jobunknown", "educationunknown", "monthdec", "monthjan", "monthmar", "monthoct", "monthsep", "poutcomeother", "poutcomesuccess". We left with 32 predictors, 26 being categorical and 6 are continuous.

#### Correlations

A plot showing the correlation among the remaining 32 predictors was generated to examine how they relate to each other. In the plot, blue indicates positive correlations, while red indicates negative ones. Predictors with correlations greater than 0.65 were removed and those predictors are "contactunknown", "educationtertiary", "poutcomeunknown" "maritalmarried".

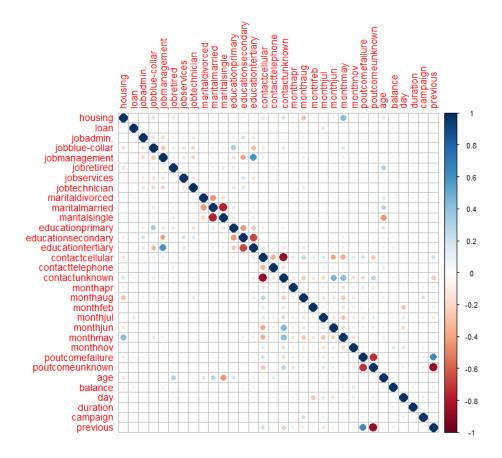


Figure 1. Correlation Plot of 32 predictors

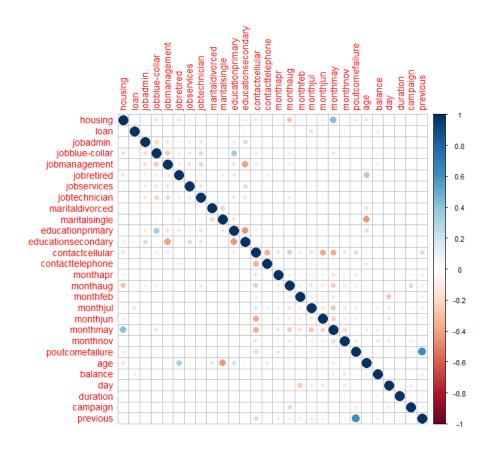


Figure 2. Correlation plot after removing highly correlated predictors.

#### **Transformations**

Before going to the model building, we need to check the distributions of continuous predictors to make sure the distributions have no outliers and are normal.

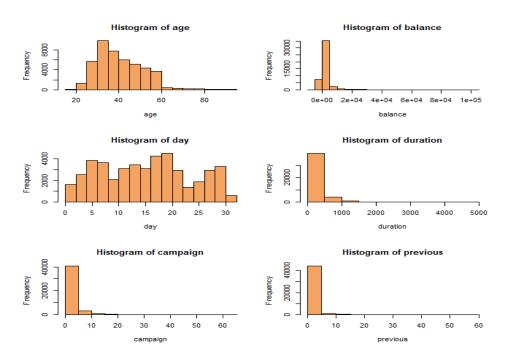


Figure 3. Distribution (Histograms) of continuous predictors.

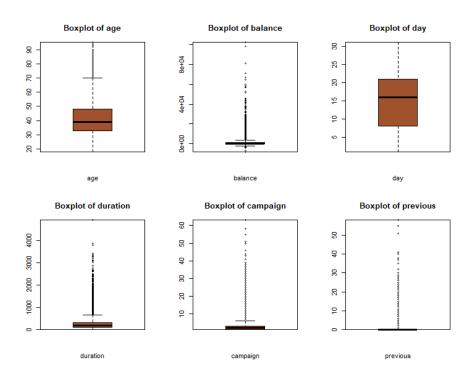


Figure 4. Distribution (Boxplots) of continuous predictors.

Predictor	Skewness	Interpretation
Age	0.68475925	Moderately Right Skewed
Balance	8.35966378	Highly Right Skewed
Day	0.09307122	Approximately Symmetric
Duration	3.14411010	Highly Right Skewed
Campaign	4.89826479	Highly Right Skewed
Previous	7.82957702	Highly Right Skewed

Table 2. Skewness of Predictors.

From the above distributions, we can see that almost all continuous predictors are not normal, and they have outliers in them. We can also confirm this from the skewness values. To correct the skewness of the continuous predictors and make them normalize we performed Box-Cox transformation. We used Spatial Sign transformation to address the outliers in the data. We can the distributions and skewness below after the transformation.

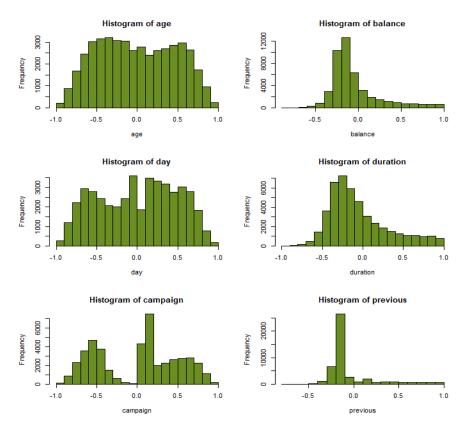


Figure 5. Distribution (Histograms) after the transformation.

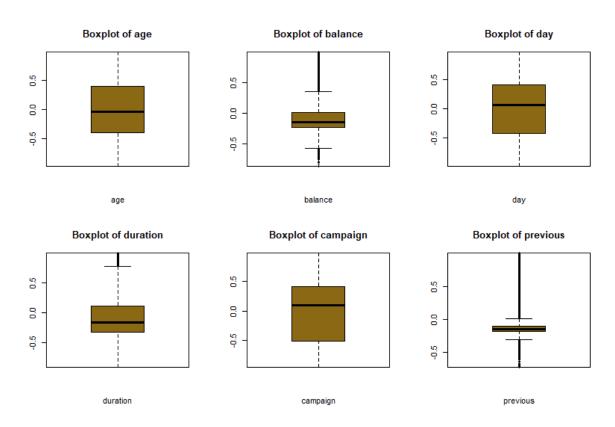


Figure 6. Distribution (Boxplots) after the transformation.

Predictor	Predictor Skewness after Box Cox Skewness after Spat	
Age	0.09889626	0.06354351
Balance	8.35966378	1.62330154
Day	-0.17839430	-0.12294714
Duration	3.14411010	0.96570825
Campaign	0.14909605	-0.07707232
Previous	7.82957702	2.20938085

Table 3. Skewness after Transformations.

# Data Splitting:

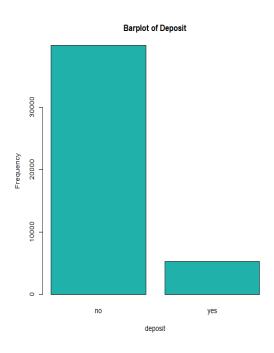


Figure 7. Distribution of Target Variable.

As our target variable is imbalanced, we are using stratified random sampling and going to split the data into 70% train and 30% test data. To check the models effectively, we are using 10-fold cross-validation. After preprocessing we are using 28 predictors for model building and a total number of samples is 45210. Since our data is imbalanced, we are using "Kappa" as a classification statistic.

## Model Building:

#### Models

We're using a variety of models to create our predictive models, covering both linear and non-linear models. In the linear models, we're using logistic regression, linear discriminant analysis (LDA), and partial least squares discriminant analysis (PLSDA), along with penalized models. From non-linear, we have models like nonlinear discriminant analysis, neural networks, flexible discriminant analysis, support vector machines, K-nearest neighbors, and Naive Bayes. These different models give us a range of ways to identify and understand the patterns in our data, contributing to a thorough and strong approach to building our models.

#### Model Summary

We used training set to tune all the models and below table summarizes the models' performance. All the summary statistics and tuning parameters of these models are in the appendix.

Linear Models	Best Tuning Parameter	Accuracy	Карра
Logistic regression	NA	0.8923469	0.3370045
LDA	NA	0.8902299	0.3745043
PLSDA	ncomp = 4	0.8862172	0.08386809
Penalized Models	alpha = 0.1 and lambda = 0.01.	0.8912409	0.272778651
Non-linear Models	Best Tuning Parameter	Accuracy	Карра
NDLA	subclasses = 1	0.8902299	0.3745043
Neural Networks	size = 9 and decay = 1	0.9012575	0.43556644
FDA	degree = 3 and nprune = 14	0.8921263	0.4427430
SVM	sigma = 0.01266439 and C = 0.25	0.8969916	0.4148633
KNN	K = 1	0.8644146	0.3234554
Naïve Bayes	NA	0.8734198	0.357957

**Table 4. Model's Training Summary** 

From the table, we can see that the Kappa value is high for the Linear Discriminant Analysis model from linear models and the Flexible Discriminant Analysis from non-linear models. So, the top two models are Linear Discriminant Analysis and the Flexible Discriminant Analysis.

#### Top two Models

The two best-performing models were then applied to make predictions on the test dataset, and the resulting accuracy and kappa values are provided below.

	Test Set	
Top two Models	Accuracy	Карра
Linear Discriminant Analysis	0.889	0.3562
Flexible Discriminant Analysis	0.8949	0.4444

Table 5. Summary of Top two models.

## Conclusion

#### **Best Model**

Among the top two models, when we compare the test set Kappa value of top models, we can see that the Kappa value is high for the Flexible Discriminant Analysis model. So, we recommend Flexible Discriminant Analysis as the best model for this data.

#### Model Performance

Confusion Matrix

#### Confusion Matrix and Statistics

Reference Prediction no no 11416 866 yes 560 720

Accuracy: 0.8949 95% CI: (0.8896, 0.9) No Information Rate: 0.8831 P-Value [Acc > NIR] : 7.682e-06

Kappa: 0.4444

Mcnemar's Test P-Value : 6.648e-16

Sensitivity: 0.9532 Specificity: 0.4540 Pos Pred Value: 0.9295 Neg Pred Value: 0.5625 Prevalence: 0.8831 Detection Rate: 0.8418

Detection Prevalence: 0.9056 Balanced Accuracy: 0.7036

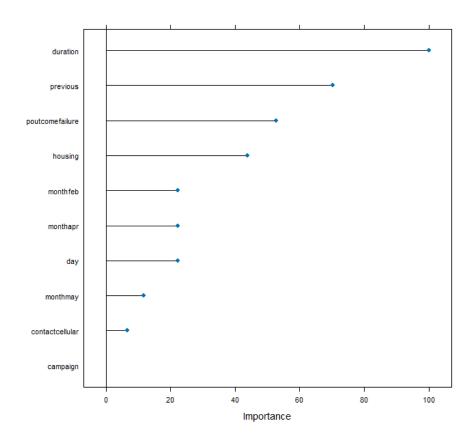
'Positive' Class : no

Important Predictors

Important Predictors	Importance
Duration	100.000
Previous	70.334
Poutcomefailure	52.660
housing	43.794
day	22.297
monthapr	22.297
monthfeb	22.297

monthmay	11.680
contactcellular	6.576
campaign	0.000

**Table 6. FDA variable importance** 



**Figure 8. Important Predictors** 

# References:

Moro,S., Rita,P., and Cortez,P.. (2012). Bank Marketing. UCI Machine Learning Repository. https://doi.org/10.24432/C5K306.

# Appendix: Summary Statistics & Tuning Plot of Models on Train Data

#### **Linear Models**

```
Logistic Regression
```

```
Generalized Linear Model
31648 samples
    28 predictor
     2 classes: 'no', 'yes'
Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results:
  Accuracy Kappa 0.8923469 0.3370045
Linear discriminant analysis (LDA)
Linear Discriminant Analysis
31648 samples
    28 predictor
     2 classes: 'no', 'yes'
Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results:
  Accuracy
  0.8902299 0.3745043
Partial least squares discriminant analysis (PLSDA)
Partial Least Squares
31648 samples
    28 predictor 2 classes: 'no', 'yes'
Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results across tuning parameters:
  ncomp
           Accuracy
                          Карра
           0.8834998
                          0.01044861
  1
           0.8852376
                          0.05410159
  3
           0.8861855
                          0.07513384
                         0.08386809
           0.8862172
```

Kappa was used to select the optimal model using the largest value. The final value used for the model was ncomp = 4.

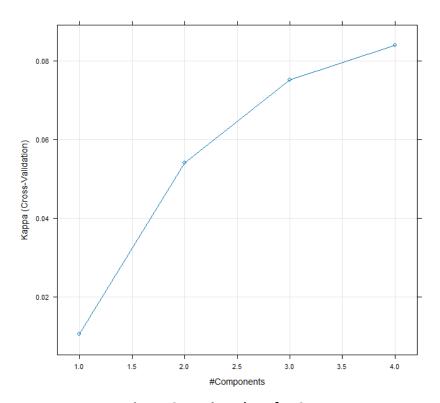


Figure 9. Tuning Plot of PLSDA

#### Penalized models

```
qlmnet
```

```
31648 samples
   28 predictor
2 classes: 'no', 'yes'
Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results across tuning parameters:
  alpha
           lambda
                         Accuracy
                                       Kappa
           0.01000000
                                      0.267737513
0.175524428
  0.0
                         0.8913674
                         0.8894400
  0.0
           0.03111111
                         0.8872915
  0.0
           0.05222222
                                       0.102626521
  0.0
           0.07333333
                         0.8848585
                                       0.042977716
  0.0
           0.09444444
                         0.8839737
                                       0.017879482
  0.0
           0.11555556
                         0.8832470
                                       0.004624647
           0.13666667
                         0.8829942
0.8829942
  0.0
                                       0.00000000
  0.0
           0.15777778
                                       0.00000000
           0.17888889
                         0.8829942
  0.0
                                       0.00000000
  0.0
           0.20000000
                         0.8829942
                                       0.00000000
                                      0.272778651
0.154447621
  0.1
           0.01000000
                         0.8912409
                         0.8888712
  0.1
           0.03111111
           0.05222222
                         0.8855536
  0.1
                                       0.061178569
  0.1
           0.07333333
                         0.8834998
                                       0.010862954
           0.09444444
                         0.8829942
                                       0.00000000
  0.1
                         0.8829942
0.8829942
  0.1
           0.11555556
                                       0.00000000
  0.1
           0.13666667
                                       0.00000000
                         0.8829942
  0.1
           0.15777778
                                       0.00000000
                         0.8829942
  0.1
           0.17888889
                                       0.00000000
           0.2000000
                         0.8829942
                                       0.00000000
  0.1
  0.2
0.2
0.2
           0.01000000
                         0.8911146
                                       0.267154314
                                       0.135281927
           0.03111111
                         0.8881130
                         0.8841949
           0.05222222
                                      0.033011398
```

```
0.2
        0.07333333
                     0.8829942
                                  0.00000000
                     0.8829942
        0.09444444
                                  0.00000000
0.2
0.2
0.2
0.2
0.2
        0.11555556
                     0.8829942
                                  0.00000000
        0.13666667
                     0.8829942
                                  0.00000000
        0.15777778
                     0.8829942
                                  0.00000000
        0.17888889
                     0.8829942
                                  0.00000000
        0.2000000
                     0.8829942
                                  0.00000000
0.4
        0.01000000
                     0.8905143
                                  0.251828682
0.4
        0.03111111
                     0.8865964
                                  0.098816901
                     0.8831522
0.4
        0.05222222
                                  0.003201828
        0.07333333
0.4
                     0.8829942
                                  0.00000000
                     0.8829942
0.8829942
0.8829942
0.4
        0.09444444
                                  0.00000000
        0.11555556
0.4
                                  0.00000000
        0.13666667
0.4
                                  0.00000000
                     0.8829942
                                  0.00000000
0.4
        0.15777778
        0.17888889
                     0.8829942
0.4
                                  0.00000000
0.4
        0.2000000
                     0.8829942
                                  0.00000000
0.6
        0.01000000
                     0.8904511
                                  0.240200794
                     0.8853008
                                  0.069825558
0.6
        0.03111111
0.6
        0.05222222
                     0.8829942
                                  0.00000000
0.6
        0.07333333
                     0.8829942
                                  0.00000000
        0.0944444
                     0.8829942
0.8829942
0.6
                                  0.00000000
        0.11555556
0.6
                                  0.00000000
                                  0.00000000
                     0.8829942
0.6
        0.13666667
                     0.8829942
0.6
        0.15777778
                                  0.00000000
        0.17888889
                     0.8829942
                                  0.00000000
0.6
                     0.8829942
0.6
        0.2000000
                                  0.00000000
0.8
        0.01000000
                     0.8900720
                                  0.226578319
0.8
        0.03111111
                     0.8841000
                                  0.040129809
                     0.8829942
0.8
        0.05222222
                                  0.00000000
        0.0733333\overline{3}
                     0.8829942
0.8829942
0.8
                                  0.00000000
0.8
        0.09444444
                                  0.00000000
                                  0.00000000
                     0.8829942
0.8
        0.11555556
                     0.8829942
0.8
        0.13666667
                                  0.00000000
                     0.8829942
0.8829942
0.8829942
0.8
        0.15777778
                                  0.00000000
        0.17888889
0.8
                                  0.00000000
        0.2000000
0.8
                                  0.00000000
1.0
        0.01000000
                     0.8895350
                                  0.214993642
1.0
        0.03111111
                     0.8832470
                                  0.011925210
                     0.8829942
0.8829942
        0.05222222
                                  0.00000000
1.0
        0.07333333
1.0
                                  0.00000000
                     0.8829942
        0.09444444
1.0
                                  0.00000000
        0.11555556
                     0.8829942
                                  0.00000000
1.0
                     0.8829942
                                  0.00000000
1.0
        0.13666667
                     0.8829942
0.8829942
        0.15777778
1.0
                                  0.00000000
        0.17888889
                                  0.00000000
1.0
        0.20000000
                     0.8829942
1.0
                                  0.00000000
```

Kappa was used to select the optimal model using the largest value. The final values used for the model were alpha = 0.1 and lambda = 0.01.

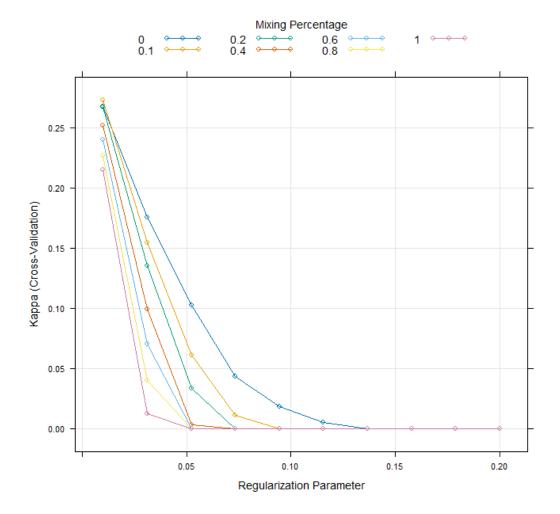


Figure 10. Tuning Plot of Penalized Model

#### Non-linear Models

```
Nonlinear Discriminant Analysis
```

Mixture Discriminant Analysis

```
31648 samples
28 predictor
2 classes: 'no', 'yes'
```

Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results across tuning parameters:

```
Accuracy 0.8902299
                              Kappa
0.3745043
subclasses
 1
2
3
                0.8682687
                              0.2083588
                0.8527572
                              0.2021066
 4
5
6
7
8
9
                0.8504491
                              0.2643869
               0.8512074
0.8553456
0.8593908
                              0.2649004
                              0.2646369
                              0.2912579
                              0.2957629
                0.8527531
                0.8520949
                              0.3280412
                0.8546818
                              0.3224095
```

Kappa was used to select the optimal model using the largest value. The final value used for the model was subclasses = 1.

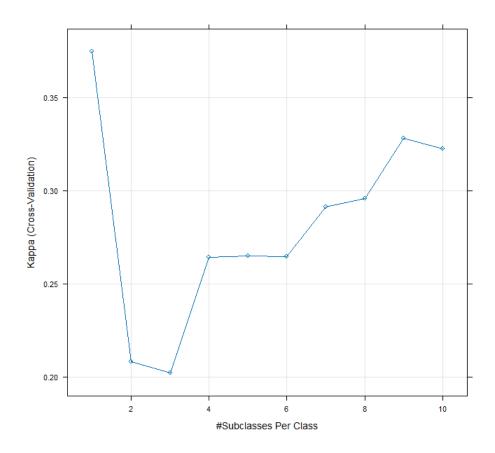
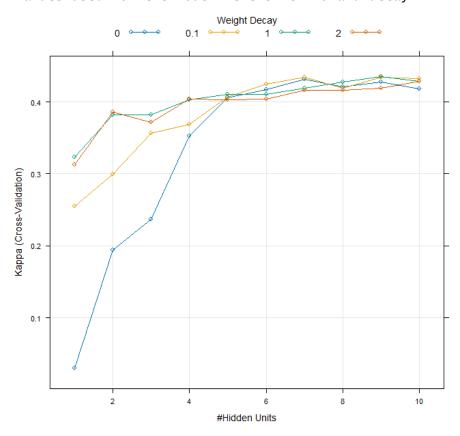


Figure 11. Tuning Plot of NLDA

```
Neural Networks
Neural Network
31648 samples
    28 predictor
2 classes: 'no', 'yes'
Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results across tuning parameters:
   size
           decay
                     Accuracy
                                     Карра
                                     0.03021165
0.25494000
    1
1
           0.0
                     0.8834681
           0.1
                     0.8900086
    112222333344445
           1.0
                     0.8913358
                                     0.32367146
           2.0
                     0.8908302
                                     0.31261132
                     0.8880814
                                     0.19369716
           0.0
                                     0.29951003
           0.1
                     0.8921566
           1.0
                     0.8952222
                                     0.38204436
           2.0
                     0.8961069
                                     0.38553089
                                     0.23659448
           0.0
                     0.8897871
                     0.8938638 \\ 0.8949693
                                     0.35639238
0.38250364
           0.1
           1.0
                     0.8953171
           2.0
                                     0.37121766
                                     0.35288053
                     0.8943688
           0.0
                     0.8964865
                                     0.36858676
           0.1
           1.0
                     0.8982241
                                     0.40316114
                     0.8987609
           2.0
                                     0.40430453
           0.0
                     0.8960754
                                     0.40604025
```

```
0.8981292
                           0.40692228
      0.1
 55566667777888899999
      1.0
              0.8989508
                           0.41041031
      2.0
              0.8992350
                           0.40320778
      0.0
              0.8968018
                           0.41762122
      0.1
              0.8983187
                           0.42499213
      1.0
              0.8992980
                           0.41021093
      2.0
                           0.40404233
              0.8984769
      0.0
              0.8981287
                           0.43183291
      0.1
              0.9004039
                           0.43388006
      1.0
              0.8999302
                           0.41915417
                           0.41645850
              0.9005937
                           0.42120819
              0.8962964
      0.0
              0.8979713
      0.1
                           0.41946017
      1.0
              0.9004676
                           0.42742913
      2.0
              0.9004674
                           0.41603447
      0.0
              0.8973710
                           0.42753499
      0.1
              0.8992978
                           0.43457197
                           0.43556644
      1.0
              0.9012575
      2.0
              0.8998986
                           0.41911086
10
      0.0
              0.8957910
                           0.41794018
10
              0.8987610
      0.1
                           0.43199499
10
              0.9000883
                           0.42833853
      1.0
      2.0
              0.9010679
10
                           0.42903684
```

Kappa was used to select the optimal model using the largest value. The final values used for the model were size = 9 and decay = 1.



**Figure 12. Tuning Plot of Neural Networks** 

# Flexible Discriminant Analysis Flexible Discriminant Analysis 31648 samples 28 predictor

2 classes: 'no', 'yes'

Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28483, 28484, 28484, 28484, 28484, 28483, ...
Resampling results across tuning parameters:

degree 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	nprune 2 3 4 5 6 7 8 9 10 11 12 13 14 15 6 7 8 9 10 11 12 13 14 15 2 3 4 5 6 7 8 9 10 11 12 13 14 15 2 3 4 5 6 7 8 9 10 11 12 13 14 15 15 15 15 15 15 15 15 15 15 15 15 15	Accuracy 0.8751906 0.8790456 0.8807834 0.8886508 0.8911154 0.8913365 0.8916209 0.8909255 0.8919364 0.8914310 0.8906095 0.8920313 0.8913360 0.8920313 0.892313 0.8829942 0.8829942 0.8829942 0.88877346 0.88877346 0.8904204 0.8917788 0.8917788 0.8917788 0.8922528 0.8924109 0.8924109 0.8829942 0.8821414 0.8831847 0.8877346 0.8922528 0.8914629 0.8926637 0.8924109 0.8926637 0.8924109 0.892528 0.8914629 0.8926637 0.8924109	Kappa 0.3006356 0.3192757 0.3227694 0.3988148 0.4177867 0.4200995 0.4211233 0.4202135 0.4255687 0.4262615 0.4237267 0.4305563 0.4268729 0.4241814 0.0000000 0.1502207 0.3102156 0.3756584 0.3809964 0.4014635 0.4076981 0.4186063 0.4179337 0.4261875 0.4274857 0.4255542 0.4358865 0.4355146 0.0000000 0.1502207 0.3102156 0.3756584 0.4076981 0.4194266 0.4217880 0.4294689 0.4363939
3 3 3 3 3	11 12 13 14 15	0.8917157	0.4294689

Kappa was used to select the optimal model using the largest value. The final values used for the model were degree = 3 and nprune = 14.

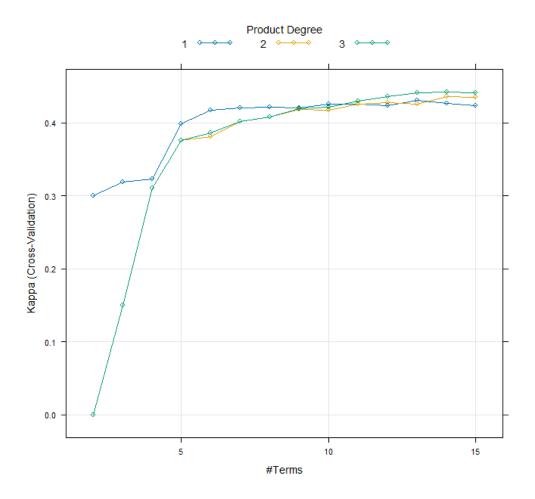


Figure 13. Tuning Plot of FDA

### **Support Vector Machines**

```
Support Vector Machines with Radial Basis Function Kernel
```

```
31648 samples
28 predictor
2 classes: 'no', 'yes'
```

Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results across tuning parameters:

```
C Accuracy Kappa
0.25 0.8969916 0.4148633
1.00 0.8971496 0.3828091
4.00 0.8982551 0.3784174
16.00 0.8959169 0.3581372
```

Tuning parameter 'sigma' was held constant at a value of 0.01266439 Kappa was used to select the optimal model using the largest value. The final values used for the model were sigma = 0.01266439 and C = 0.25.

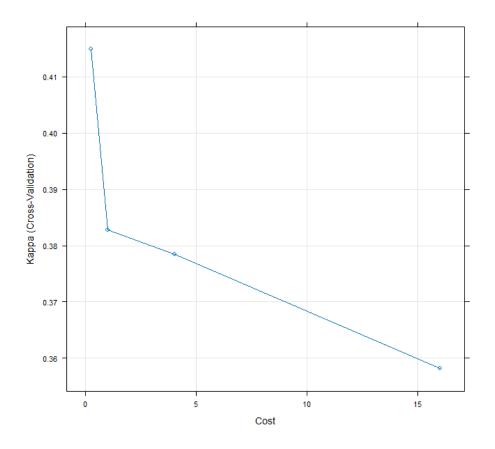


Figure 14. Tuning Plot of SVM

```
K-Nearest Neighbors
k-Nearest Neighbors
31648 samples
   28 predictor
2 classes: 'no', 'yes'
Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results across tuning parameters:
  k
       Accuracy
                     Карра
       0.8644146
                     0.3234554
   1
       0.8624237
                     0.3106057
    3
4
       0.8784436
                     0.3117898
       0.8801187
                     0.3185401
    5
       0.8846367
                     0.3009827
    6
7
       0.8831832
                     0.2883998
                     0.2793152
       0.8860587
    8
       0.8852689
0.8871647
                     0.2694741
    9
                     0.2628467
0.2578917
       0.8869750
  10
       0.8881441
                     0.2530882
  11
                     0.2487129
  12
       0.8878913
  13
       0.8886183
                     0.2389654
  14
       0.8878599
                     0.2296640
  15
       0.8880812
                     0.2151571
       0.8885235
  16
                     0.2177760
       0.8888711
                     0.2112513
```

```
0.2083038
    0.8883971
18
19
    0.8887763
                  0.2016805
20
21
22
    0.8895346
                  0.2045268
    0.8888079
                  0.1908663
    0.8885237
                  0.1866699
23
24
25
26
27
28
    0.8890292
                  0.1854783
    0.8884288
                  0.1790696
    0.8886500
                  0.1768216
    0.8884288
                  0.1741531
    0.8887447
                  0.1712817
    0.8881443
                  0.1657661
29
30
    0.8883656
                  0.1616130
    0.8883338
                  0.1611973
31
    0.8883971
                  0.1569719
32
    0.8886183
                  0.1604321
33
    0.8885234
                  0.1561300
34
    0.8883339
                  0.1519071
    0.8882392
0.8877021
35
                  0.1472698
36
                  0.1408475
37
    0.8875125
                  0.1378084
38
    0.8872597
                  0.1352483
    0.8871965
0.8870384
                  0.1285971
0.1255979
39
40
41
    0.8868804
                  0.1225337
42
    0.8870384
                  0.1242086
43
    0.8873544
                  0.1237608
    0.8874808
0.8871648
44
                  0.1227237
45
                  0.1182114
46
    0.8869753
                  0.1168087
47
    0.8867858
                  0.1116095
    0.8865329
0.8867225
48
                  0.1092905
49
                  0.1091314
50
    0.8865329
                  0.1052568
```

Kappa was used to select the optimal model using the largest value. The final value used for the model was  $k\,=\,1.$ 

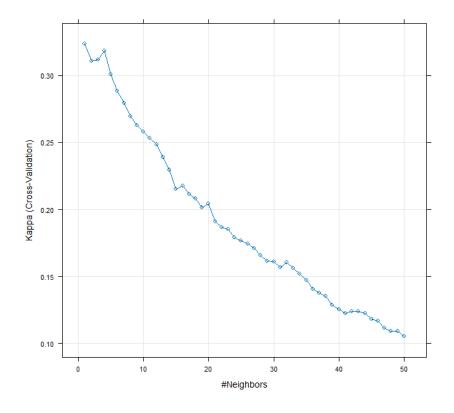


Figure 15. Tuning Plot of KNN

```
Naive Bayes

31648 samples
28 predictor
2 classes: 'no', 'yes'

Pre-processing: centered (28), scaled (28)
Resampling: Cross-Validated (10 fold)
Summary of sample sizes: 28484, 28482, 28483, 28484, 28484, 28482, ...
Resampling results:

Accuracy Kappa
0.8734198 0.357957

Tuning parameter 'fL' was held constant at a value of 2
Tuning parameter 'usekernel' was held constant at a value of TRUE
Tuning parameter 'adjust' was held constant at a value of TRUE
```

```
R Code:
library(mlbench)
library(e1071)
library(caret)
library(dplyr)
library(corrplot)
library(MASS)
dF = read.csv("C:/Users/91938/Desktop/Fall 2023/PM/Project/bank-full.csv", sep = ';')
dim(dF)
head(dF,5)
colnames(dF)[colnames(dF) == "y"] <- "deposit"
table(dF$deposit)
colSums(is.na(dF))
summary(dF)
#####removing oulier##############
max_previous <- max(dF$previous)</pre>
dF <- dF[dF$previous != max_previous, ]</pre>
#########missing values###########
image(is.na(dF), main = "Missing Values", xlab = "Observation", ylab = "Variable",
   xaxt = "n", yaxt = "n", bty = "n")
axis(1, seq(0, 1, length.out = nrow(dF)), 1:nrow(dF), col = "white")
lapply(dF, unique)
continuous_Vars <- names(dF)[sapply(dF, is.numeric)]</pre>
categorical_Vars <- colnames(dF[, !names(dF)%in%continuous_Vars])</pre>
#barplots
par(mfrow=c(3,3))
for (i in categorical_Vars) {
data <- table(dF[[i]])
```

```
barplot(data, main = paste('Barplot of', i), xlab = i, col = 'powderblue')
}
par(mfrow=c(1,1))
barplot(table(dF[, 'deposit']), main = 'Barplot of Deposit', xlab = 'deposit', col = 'lightseagreen', ylab =
'Frequency')
########binary########
binary_columns <- c("default", "housing", "loan")</pre>
head(df)
# Use lapply to apply ifelse to each binary column
dF[,binary_columns] <- lapply(dF[,binary_columns], function(x) ifelse(x == "yes", 1, 0))
#dummy variables
dummy_vars <- dummyVars("~job + marital + education + contact + month + poutcome", data = dF)
df_with_dummies <- predict(dummy_vars, newdata = dF)</pre>
dummy <- c("job", "marital", "education", "contact", "month", "poutcome")</pre>
df <- cbind(dF[, !names(dF)%in%dummy], df_with_dummies)</pre>
df <- df[,-which(names(df) == 'deposit')]</pre>
dim(df)
nearZeroVar(df, names = T)
columns to remove <- c("default", "pdays", "jobentrepreneur", "jobhousemaid", "jobself-
employed", "jobstudent",
 "jobunemployed", "jobunknown", "educationunknown",
 "monthdec", "monthjan", "monthmar", "monthoct", "monthsep", "poutcomeother",
 "poutcomesuccess"
)
# Remove the specified columns from the data frame
df <- df[, !names(df) %in% columns to remove]
dim(df)
continuous_vars <- c("age", "balance", "day", "duration", "campaign", "previous")</pre>
categorical_vars <- colnames(df[, !names(df)%in%continuous_vars])</pre>
```

```
par(mfrow=c(4,4))
for (i in categorical_vars) {
data <- table(df[[i]])
 barplot(data, main = paste('Barplot of', i), xlab = i, col = 'powderblue')
}
par(mfrow=c(1,1))
nearZeroVar(df, names=T)
#histograms
par(mfrow=c(3,2))
for (i in continuous_vars) {
data <- df[[i]]
hist(data, main = paste('Histogram of', i), xlab = i, col = 'sandybrown')
}
par(mfrow=c(1,1))
skewness_values <- apply(df[continuous_vars], 2, skewness)</pre>
skewness_values
#boxplots
par(mfrow=c(2,3))
for (i in continuous_vars) {
data <- df[[i]]
boxplot(data, main = paste('Boxplot of', i), xlab = i, col = 'sienna')
}
par(mfrow=c(1,1))
########BOXCOX############
par(mfrow = c(4, 2))
for (i in continuous_vars){
hist(df[[i]], main = paste("Before Transformation ",i), xlab = i, horiz = TRUE)
 bct_ri = BoxCoxTrans(df[[i]])
```

```
trans <- predict(bct_ri, df[[i]])
 hist(trans, main = paste("After Transformation ",i), xlab = i, horiz = TRUE)
}
par(mfrow = c(1,1))
columns_to_transform <- df[,continuous_vars]</pre>
transDf <- preProcess(columns_to_transform, method = c("BoxCox","center", "scale"))
transDf
#apply transformation
transformed <- predict(transDf, columns_to_transform)
transformed
sapply(transformed, skewness)
#######histograms after trans########
par(mfrow=c(3,2))
for (i in colnames(transformed)) {
 hist(transformed[[i]], main = paste('Histogram of', i), xlab = i, col = 'olivedrab')
}
par(mfrow=c(1,1))
########SS###########
transSS <- spatialSign(transformed[, continuous_vars])</pre>
Transform_spa <- as.data.frame(transSS)</pre>
sapply(Transform_spa, skewness)
#######boxplots after SS########
par(mfrow=c(2,3))
for (i in continuous_vars) {
 data <- Transform_spa[[i]]
 boxplot(data, main = paste('Boxplot of', i), xlab = i, col = 'goldenrod4')
}
```

```
par(mfrow=c(1,1))
par(mfrow=c(3,2))
for (i in colnames(Transform_spa)) {
 hist(Transform_spa[[i]], main = paste('Histogram of', i), xlab = i, col = 'olivedrab')
}
par(mfrow=c(1,1))
#########correlation###########
conPred <- df[, continuous_vars]</pre>
hist(conPred$previous)
correlations <- cor(df[, continuous_vars])</pre>
corrplot(correlations, method = 'color')
correlations1 <- cor(Transform_spa[, continuous_vars])</pre>
corrplot(correlations1, method = 'color')
##########
correlations1 <- cor(dF[, continuous_Vars])</pre>
corrplot(correlations1, method = 'color')
##### Final DF #####
final_df <- cbind(df[, categorical_vars],Transform_spa)</pre>
dim(final_df)
correlations_1 <- cor(final_df)</pre>
corrplot(correlations_1)
highCorr <- findCorrelation(abs(correlations_1), cutoff = .65, names = T)
length(highCorr)
highCorr
final_df[,c(17, 14)]
final <- final_df[, -highCorr]</pre>
corrplot(cor(final))
dim(final)
####### Model Building #######
```

```
dF$deposit <- as.factor(dF$deposit)</pre>
set.seed(5790)
index <- createDataPartition(dF$deposit, p = 0.7, list = FALSE)
x_train <- final[index,]</pre>
x_test <- final[-index,]</pre>
y_train <- dF$deposit[index]</pre>
y_test <- dF$deposit[-index]</pre>
dim(x_test)
length(y_test)
ctrl <- trainControl(method = "cv",
            number= 10,
            summaryFunction = defaultSummary,
            classProbs = TRUE,
            savePredictions = TRUE)
set.seed(5790)
logistic <- train(x_train,</pre>
         y = y_train,
         preProcess = c('center', 'scale'),
         method = "glm",
         metric = "Kappa",
         trControl = ctrl)
logistic
plot(logistic)
pred_logistic <- predict(logistic, x_test)</pre>
confusionMatrix(data = pred_logistic,
         reference = y_test)
## LDA
set.seed(5790)
lda <- train(x_train,</pre>
```

```
y = y_train,
       method = "lda",
       preProcess = c('center', 'scale'),
       metric = "Kappa",
       trControl = ctrl)
lda
plot(lda)
pred_lda <- predict(lda, x_test)</pre>
confusionMatrix(data = pred_lda, y_test)
## PLSDA
set.seed(5790)
plsda <- train(x = x_train,
        y = y_train,
        method = "pls",
        tuneGrid = expand.grid(.ncomp = 1:4),
        preProcess = c("center","scale"),
        metric = "Kappa",
        trControl = ctrl)
plsda
plot(plsda)
pred_plsda <- predict(plsda, x_test)</pre>
confusionMatrix(data = pred_plsda, y_test)
## PM
set.seed(5790)
glmnGrid <- expand.grid(.alpha = c(0, .1, .2, .4, .6, .8, 1),
              .lambda = seq(.01, .2, length = 10))
glmn <- train(x=x_train,
```

```
y = y_train,
method = "glmnet",
tuneGrid = glmnGrid,
preProc = c("center", "scale"),
metric = "Kappa",
trControl = ctrl)
glmn
plot(glmn)
pred_glmn <- predict(glmn, x_test)
confusionMatrix(pred_glmn, y_test)</pre>
```

```
nnetGrid \leftarrow expand.grid(.size = 1:10, .decay = c(0, .1, 1, 2))
maxSize <- max(nnetGrid$.size)</pre>
numWts <- (maxSize * (28 + 1) + (maxSize+1)*2) ## 4 is the number of predictors
set.seed(5790)
library(caret)
nnetFit <- train(x=x_train,</pre>
        y = y_train,
         method = "nnet",
         metric = "Kappa",
         preProc = c("center", "scale"),
         tuneGrid = nnetGrid,
         trace = FALSE,
         maxit = 100,
         MaxNWts = numWts,
         trControl = ctrl)
nnetFit
plot(nnetFit)
pred_nnet<-predict(nnetFit,x_test)</pre>
confusionMatrix(data = pred_nnet,
        reference=y_test)
######## Flexible Discriminant Analysis ##########
marsGrid <- expand.grid(degree = 1:3, nprune = 2:15)
# Train the model
```

fdaTuned <- train(

```
x = x_train,
 y = y_train,
 method = "fda",
 metric = "Kappa",
 preProcess = c('center', 'scale'),
 tuneGrid = marsGrid,
 trControl = trainControl(method = "cv"))
fdaTuned
plot(fdaTuned)
pred_fda <- predict(fdaTuned, x_test)</pre>
confusionMatrix(data = pred_fda,
        reference=y_test)
########## Support Vector Machines #########
set.seed(5790)
library(kernlab)
library(caret)
sigmaRangeReduced <- sigest(as.matrix(x_train))</pre>
svmRGridReduced <- expand.grid(.sigma = sigmaRangeReduced[1],</pre>
                 .C = 2^{(eq(-2, 4, by = 2)))}
set.seed(5790)
svmRModel <- train(x=x_train,</pre>
          y = y_train,
          method = "svmRadial",
          metric = "Kappa",
          preProc = c("center", "scale"),
          tuneGrid = svmRGridReduced,
          fit = FALSE,
          trControl = ctrl)
```

```
svmRModel
plot(svmRModel)
pred_svm <- predict(svmRModel, x_test)</pre>
confusionMatrix(data = pred_svm,
        reference=y_test)
set.seed(5790)
knnFit <- train(x=x_train,
        y = y_train,
        method = "knn",
        metric = "Kappa",
        preProc = c("center", "scale"),
        ##tuneGrid = data.frame(.k = c(4*(0:5)+1, 20*(1:5)+1, 50*(2:9)+1)), ## 21 is the best
        tuneGrid = data.frame(.k = 1:50),
        trControl = ctrl)
knnFit
plot(knnFit)
pred_knn<-predict(knnFit, x_test)</pre>
confusionMatrix(data = pred_knn,
        reference=y_test)
####### Naive Bayes ########
install.packages("klaR")
library(klaR)
set.seed(5790)
nbFit <- train(x_train,</pre>
       y_train,
       method = "nb",
       metric = "ROC",
```

```
preProc = c("center", "scale"),
    ##tuneGrid = data.frame(.k = c(4*(0:5)+1, 20*(1:5)+1, 50*(2:9)+1)), ## 21 is the best
    tuneGrid = data.frame(.fL = 2,.usekernel = TRUE,.adjust = TRUE),
    trControl = ctrl)

nbFit
plot(nbFit) #NO TUNING PARAMETER
pred_nb <- predict(nbFit, x_test)
confusionMatrix(data = pred_nb,
    reference=y_test)

important_pred <- varImp(fdaTuned)
plot(important_pred)
head(x_test)</pre>
```