Tabular and Graphical Methods for Displaying and Summarizing Relationships Between Two Variables (along with some other related remarks)

I. DISPLAYING the Relationship

a. <u>Crosstab(ulation)s</u>:

• Y is typically displayed by row; X by column

| ousehold Income, | | | | ears of Edu | cation | | | | |
|-----------------------|----|-----|-----|-------------|--------|-----|-----|------|------|
| 2004 | 0 | 2.5 | 5.5 | 7.5 | 9 | 10 | 11 | 11.5 | Tota |
| 2500 | 2 | 0 | 4 | 7 | 4 | 12 | 11 | 2 | 13 |
| 6250 | 2 | 6 | 5 | 6 | 7 | 13 | 9 | 0 j | 11 |
| 8250 | 0 | 3 | 4 | 16 | 5 | 8 | 9 | 2 | 12 |
| 11500 | 0 | 2 | 5 | 10 | 11 | 9 | 16 | 5 j | 16 |
| 13750 | 0 | 1 | 3 | 10 | 13 | 7 | 8 | 0 j | 14 |
| 17500 | 1 | 5 | 6 | 14 | 17 | 21 | 14 | 6 j | 23 |
| 22500 | 1 | 2 | 7 | 15 | 21 | 14 | 19 | 5 j | 32 |
| 27500 | 1 | 1 | 4 | 16 | 14 | 16 | 21 | 3 | 33 |
| 32500 | 4 | 2 | 8 | 9 | 19 | 20 | 11 | 3 | 34 |
| 37500 | 2 | 3 | 4 | 9 | 12 | 12 | 17 | 3 | 32 |
| 45000 | 2 | 1 | 6 | 12 | 20 | 16 | 22 | 14 | 55 |
| 55000 | 3 | 4 | 2 | 9 | 12 | 20 | 17 | 8 | 56 |
| 67500 | 0 | 0 | 0 | 8 | 12 | 14 | 11 | 13 | 62 |
| 87500 | 0 | 0 | 1 | 8 | 16 | 19 | 21 | 2 | 63 |
| 125000 | 0 | 0 | 1 | 6 | 10 | 13 | 16 | 2 | 47 |
| Total | 18 | 30 | 60 | 155 | 193 | 214 | 222 | 68 | 5,00 |

| Household | | | | | | | |
|-----------|-------|-----|-------------|--------|-----|----|-------|
| Income, | | Υ | ears of Edu | cation | | | |
| 2004 | 12 | 13 | 14 | 16 | 18 | 22 | Total |
| | | | | | | | |
| 2500 | 40 | 27 | 7 | 13 | 5 | 0 | 134 |
| 6250 | 31 | 27 | 1 | 4 | 1 | 0 | 112 |
| 8250 | 48 | 9 | 6 | 9 | 1 | 0 | 120 |
| 11500 | 65 | 22 | 9 | 9 | 2 | 0 | 165 |
| 13750 | 62 | 24 | 7 | 5 | 0 | 0 | 140 |
| 17500 | 105 | 20 | 6 | 16 | 1 | 0 | 232 |
| 22500 | 120 | 54 | 22 | 36 | 9 | 1 | 326 |
| 27500 | 124 | 63 | 28 | 34 | 5 | 0 | 330 |
| 32500 | 115 | 62 | 28 | 46 | 12 | 1 | 340 |
| 37500 | 131 | 56 | 25 | 36 | 11 | 3 | 324 |
| 45000 | 185 | 96 | 52 | 81 | 40 | 4 | 551 |
| 55000 | 150 | 110 | 47 | 84 | 32 | 3 | 501 |
| 67500 | 185 | 128 | 65 | 131 | 50 | 4 | 621 |
| 87500 | 140 | 116 | 53 | 155 | 93 | 10 | 634 |
| 125000 | 67 | 85 | 47 | 138 | 68 | 17 | 470 |
| Total | 1,568 | 899 | 403 | 797 | 330 | 43 | 5,000 |

• Often more informative to provide column percents. Note that convention is typically to provide *column*, not *row*, percents. Include 100s at the bottom so reader can quickly see that columns add up to 100:

| . tab faminc | educyears, c | ol nofr | | | | | | | |
|----------------------------------|--------------|---------|-------|-------------|---------------|------|------|-------|-------|
| Household Income, 2004 | 0 | 2.5 | 5.5 | Years of Ed | lucation 9 | 10 | 11 | 11.5 | Total |
| 2500 | 11.11 | 0.00 | 6.67 | 4.52 | 2.07 | 5.61 | 4.95 | 2.94 | 2.68 |
| 6250 I | 11.11 | 20.00 | 8.33 | 3.87 | 3.63 | 6.07 | 4.95 | 0.00 | 2.24 |
| | | | | | | | | | |
| 8250 | 0.00 | 10.00 | 6.67 | 10.32 | 2.59 | 3.74 | 4.05 | 2.94 | 2.40 |
| 11500 | 0.00 | 6.67 | 8.33 | 6.45 | 5.70 | 4.21 | 7.21 | 7.35 | 3.30 |
| 13750 | 0.00 | 3.33 | 5.00 | 6.45 | 6.74 | 3.27 | 3.60 | 0.00 | 2.80 |
| 17500 | 5.56 | 16.67 | 10.00 | 9.03 | 8.81 | 9.81 | 6.31 | 8.82 | 4.64 |
| 22500 | 5.56 | 6.67 | 11.67 | 9.68 | 10.88 | 6.54 | 8.56 | 7.35 | 6.52 |
| 27500 | 5.56 | 3.33 | 6.67 | 10.32 | 7.25 | 7.48 | 9.46 | 4.41 | 6.60 |
| 32500 | 22.22 | 6.67 | 13.33 | 5.81 | 9.84 | 9.35 | 4.95 | 4.41 | 6.80 |
| 37500 | 11.11 | 10.00 | 6.67 | 5.81 | 6.22 | 5.61 | 7.66 | 4.41 | 6.48 |
| 45000 | 11.11 | 3.33 | 10.00 | 7.74 | 10.36 | 7.48 | 9.91 | 20.59 | 11.02 |
| 55000 | 16.67 | 13.33 | 3.33 | 5.81 | 6.22 | 9.35 | 7.66 | 11.76 | 10.02 |
| 67500 | 0.00 | 0.00 | 0.00 | 5.16 | 6.22 | 6.54 | 4.95 | 19.12 | 12.42 |
| 87500 | 0.00 | 0.00 | 1.67 | 5.16 | 8.29 | 8.88 | 9.46 | 2.94 | 12.68 |
| 125000 | 0.00 | 0.00 | 1.67 | 3.87 | 5.18 | 6.07 | 7.21 | 2.94 | 9.40 |

Total | 100.00 100.00 100.00 100.00 100.00 100.00 100.00 100.00 | 100.00

| Household | | | | | | | |
|-----------|--------|--------|-------------|----------|--------|--------|--------|
| Income, | | | Years of Ed | ducation | | | |
| 2004 | 12 | 13 | 14 | 16 | 18 | 22 | Total |
| 2500 | 2.55 | 3.00 | 1.74 | 1.63 | 1.52 | 0.00 | 2.68 |
| 6250 | 1.98 | 3.00 | 0.25 | 0.50 | 0.30 | 0.00 | 2.24 |
| 8250 | 3.06 | 1.00 | 1.49 | 1.13 | 0.30 | 0.00 | 2.40 |
| 11500 | 4.15 | 2.45 | 2.23 | 1.13 | 0.61 | 0.00 | 3.30 |
| 13750 | 3.95 | 2.67 | 1.74 | 0.63 | 0.00 | 0.00 | 2.80 |
| 17500 | 6.70 | 2.22 | 1.49 | 2.01 | 0.30 | 0.00 | 4.64 |
| 22500 | 7.65 | 6.01 | 5.46 | 4.52 | 2.73 | 2.33 | 6.52 |
| 27500 | 7.91 | 7.01 | 6.95 | 4.27 | 1.52 | 0.00 | 6.60 |
| 32500 | 7.33 | 6.90 | 6.95 | 5.77 | 3.64 | 2.33 | 6.80 |
| 37500 | 8.35 | 6.23 | 6.20 | 4.52 | 3.33 | 6.98 | 6.48 |
| 45000 | 11.80 | 10.68 | 12.90 | 10.16 | 12.12 | 9.30 | 11.02 |
| 55000 | 9.57 | 12.24 | 11.66 | 10.54 | 9.70 | 6.98 | 10.02 |
| 67500 | 11.80 | 14.24 | 16.13 | 16.44 | 15.15 | 9.30 | 12.42 |
| 87500 | 8.93 | 12.90 | 13.15 | 19.45 | 28.18 | 23.26 | 12.68 |
| 125000 | 4.27 | 9.45 | 11.66 | 17.31 | 20.61 | 39.53 | 9.40 |
| Total | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 |

• Lots of categories of both X and Y, so maybe you recode:

```
. gen educ_rc = educyears
```

```
. recode educ_rc (0/7.5 = 1) (9/11.5 = 2) (12=3) (13/14=4) (16=5) (18/22=6) (educ_rc: 5000 changes made)
```

- . label def educ_rc 1 "< 8th grade" 2 "< H.S" 3 "HS Diploma" 4 "Some college" 5 "B.A." 6 "Post-grad"
- . label values educ_rc educ_rc
- . tab educ_rc

| educ_rc | Freq. | Percent | Cum. |
|--------------|---------|---------|--------|
| | | | |
| < 8th grade | 263 | 5.26 | 5.26 |
| < H.S | 697 | 13.94 | 19.20 |
| HS Diploma | 1,568 | 31.36 | 50.56 |
| Some college | 1,302 | 26.04 | 76.60 |
| B.A. | 797 | 15.94 | 92.54 |
| Post-grad | 373 | 7.46 | 100.00 |
| Total | 5,000 | 100.00 | |

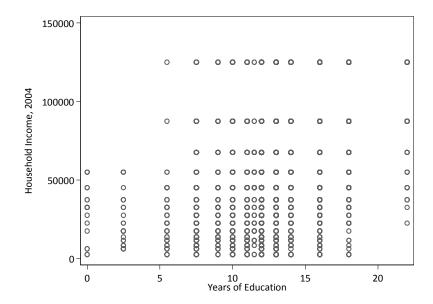
- . gen faminc_rc = famincome
- . recode faminc_rc (0/20000 = 1) (21000/40000=2) (41000/70000=3) (71000/max=4) $(faminc_rc: 5000 changes made)$
- . label def faminc_rc 1 "<\$20K" 2 "\$21-\$40K" 3 "\$41-\$70K" 4 ">\$70K"
- . label values faminc_rc faminc_rc
- . tab faminc_rc

| faminc_rc | Freq. | Percent | Cum. |
|---|--------------------------------|----------------------------------|-----------------------------------|
| <pre><\$20K \$21-\$40K \$41-\$70K >\$70K </pre> | 903 1,320 1,673 1,104 | 18.06 26.40 33.46 22.08 | 18.06 44.46 77.92 100.00 |
| Total | 5,000 | 100.00 | |

- This crosstab is now easier to read (though of course we've lost some information).
- To detect a relationship between X and Y, see how the column percents change within rows (note how it's now easier to do this than it was on the bigger crosstab earlier):
- . tab faminc_rc educ_rc, col nofr

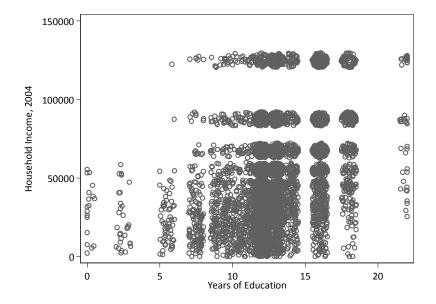
| ĺ | | | edu | c_rc | | | |
|------------|-----------|--------|-----------|-----------|--------|-----------|--------|
| faminc_rc | < 8th gra | < H.S | HS Diplom | Some coll | B.A. | Post-grad | Total |
| <\$20K | 42.59 | 29.99 | 22.39 | 12.67 | 7.03 | 2.68 | 18.06 |
| \$21-\$40K | 33.46 | 30.13 | 31.25 | 25.96 | 19.07 | 11.26 | 26.40 |
| \$41-\$70K | 17.87 | 25.68 | 33.16 | 38.25 | 37.14 | 35.66 | 33.46 |
| >\$70K | 6.08 | 14.20 | 13.20 | 23.12 | 36.76 | 50.40 | 22.08 |
| Total | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 | 100.00 |

- b. <u>Scatterplots</u> (both variables at interval-level or higher):
- . twoway (scatter famincome educyears)



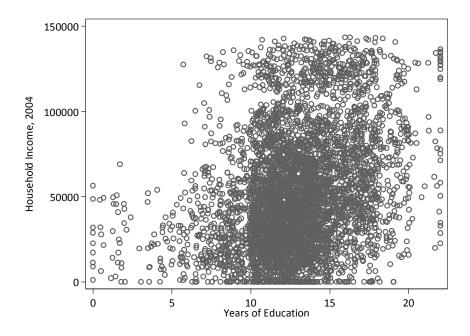
Not very informative, so let's jitter, adding noise to each marker that is equivalent to 5% of area of graph:

twoway (scatter famincome educyears, jitter(5))

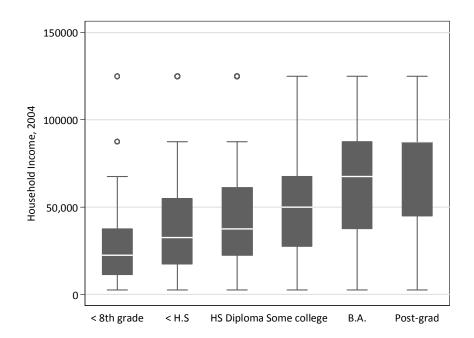


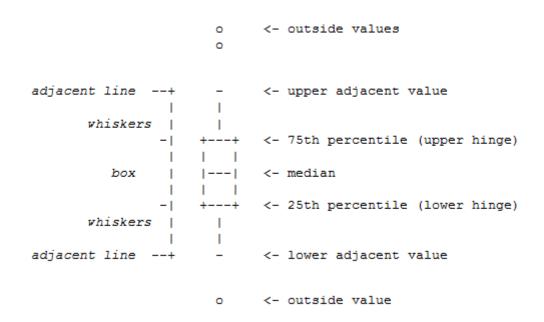
Still not so good, let's try 20%:

twoway (scatter famincome educyears, jitter(20))



c. <u>Boxplots</u> (appropriate when Y is at interval-level, and X has few categories and/or is less than interval level):





OK, but what's an "adjacent value"? From Stata manual:

The upper and lower adjacent values are as defined by Tukey (1977):

Let x represent a variable for which adjacent values are being calculated. Define $x_{(i)}$ as the ith ordered value of x, and define $x_{[25]}$ and $x_{[75]}$ as the 25th and 75th percentiles.

Define U as $x_{[75]} + \frac{3}{2}(x_{[75]} - x_{[25]})$. The upper adjacent value is defined as x_i , such that $x_{(i)} \leq U$ and $x_{(i+1)} > U$.

Define L as $x_{[25]}-\frac{3}{2}(x_{[75]}-x_{[25]})$. The lower adjacent value is defined as x_i , such that $x_{(i)}\geq L$ and $x_{(i-1)}< L$.

d. "Binning out" X and then displaying the mean Y in each "bin" of X. Good when X is continuous/takes on many values but Y is dichotomous. From Egan & Mullin (2012):

. sum getwarm01, d

Belief that there is "solid evidence" for global warming (0 = No, 1 = Yes)

| | Percentiles | Smallest | | |
|-----|-------------|----------|-------------|-----------|
| 1% | 0 | 0 | | |
| 5% | 0 | 0 | | |
| 10% | 0 | 0 | 0bs | 7224 |
| 25% | 0 | 0 | Sum of Wgt. | 7224 |
| 50% | 1 | | Mean | .732835 |
| | | Largest | Std. Dev. | .4425099 |
| 75% | 1 | 1 | | |
| 90% | 1 | 1 | Variance | .195815 |
| 95% | 1 | 1 | Skewness | -1.052411 |
| 99% | 1 | 1 | Kurtosis | 2.107569 |

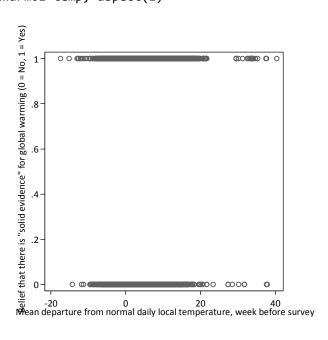
[.] sum temp, d

Mean departure from normal daily local temperature, week before survey

| | Percentiles | Smallest | | |
|-----|-------------|-----------|-------------|----------|
| 1% | -7 | -17.42857 | | |
| 5% | -4.285714 | -15.14286 | | |
| 10% | -2.714286 | -14.28571 | 0bs | 7971 |
| 25% | 1428571 | -13 | Sum of Wgt. | 7971 |
| | | | | |
| 50% | 2.571429 | | Mean | 3.536448 |
| | | Largest | Std. Dev. | 5.728437 |
| 75% | 6.285714 | 37.57143 | | |
| 90% | 11.57143 | 37.57143 | Variance | 32.815 |
| 95% | 14.28571 | 37.71429 | Skewness | .9993781 |
| 99% | 18.28572 | 40.28571 | Kurtosis | 5.503608 |
| | | | | |

Here, a scatterplot is virtually worthless:

twoway scatter getwarm01 temp, aspect(1)



So we "bin out" our X (temp), creating equal-sized bins of temp. Do-file below does this for any x (called 'x-var' in the do-file)

*this do-file creates a user-specified total # of "bins" of the variable xvar, each with an approximately equal number of observations. the bins are found in a new variable named the (name of your xvar) + suffix "bin".

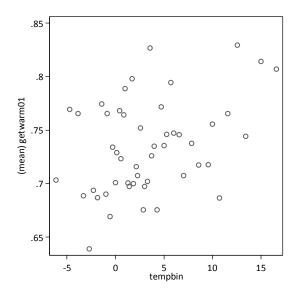
```
*user fills in following three local macros:
local xvar xvargoeshere
local yvar yvargoeshere
local bins numberofbinsdesiredgoeshere
local binsminus1 = `bins'-1
local binsminus2 = `bins'-2
_pctile `xvar', n(`bins')
gen `xvar'bin = .
replace `xvar'bin = 0 if `xvar' <= `r(r1)'
forvalues i = 1(1)`binsminus2' {
       local j = i'+1
       replace `xvar'bin = `r(r`i')' if `xvar' > `r(r`i')' & `xvar' <= `r(r`j')'</pre>
replace `xvar'bin = `r(r`binsminus1')' if `xvar' > `r(r`binsminus1')'
replace `xvar'bin = . if `xvar'==.
save, replace
*now if you wanted to create the dataset you'd use to create the graph (where means of
yvar are plotted against the bin values), you might do the following:
collapse (mean) `yvar', by(`xvar'bin race)
save bindata, replace
twoway (scatter `yvar' `xvar'bin) (lowess `yvar' `xvar'bin)
*etc.
```

Here, I've created 50 bins of temp. Note that because of lumpiness of data they don't all have exactly equal numbers of obs. Not a big deal for our purposes.

| tempbin | Freq. | Percent | Cum. |
|------------------------|--------------|--------------|--------------|
| 6 442057 | t | 2.07 | 2.07 |
| -6.142857 -4.714286 | 165 | 2.07 2.31 | 2.07 4.38 |
| -3.857143 | 184 90 | 1.13 | 4.38 5.51 |
| -3.285714 | 242 | 3.04 | 8.54 |
| -2.714286 | 94 | 1.18 | 9.72 |
| -2.285714 | 153 | 1.92 | 11.64 |
| -1.857143 | 149 | 1.87 | 13.51 |
| -1.428571 | 256 | 3.21 | 16.72 |
| | 98 | 1.23 | 17.95 |
| 8571429 | 174 | 2.18 | 20.14 |
| 5714286 | 172 | 2.16 | 22.29 |
| 2857143 | 205 | 2.57 | 24.87 |
| | 277 | 3.48 | 28.34 |
| .1428571 | 197 | 2.47 | 30.81 |
| .4285714 | 106 | 1.33 | 32.14 |
| .5714286 | 232 | 2.91 | 35.05 |
| .8571429 | 126 | 1.58 | 36.63 |
| | 108 | 1.35 | 37.99 |
| 1.271429 | 206 | 2.58 | 40.57 |
| 1.428571 | 176 | 2.21 | 42.78 |
| 1.714286 | 121 | 1.52 | 44.30 |
| 1.857143 | 217 | 2.72 | 47.02 |
| 2.142857 | j 99 | 1.24 | 48.26 |
| 2.285714 | j 97 | 1.22 | 49.48 |
| 2.571429 | 286 | 3.59 | 53.07 |
| 2.857143 | j 91 | 1.14 | 54.21 |
| 3 | j 164 | 2.06 | 56.27 |
| 3.285714 | j 112 | 1.41 | 57.67 |
| 3.571429 | J 93 | 1.17 | 58.84 |
| 3.714286 | 254 | 3.19 | 62.02 |
| | j 182 | 2.28 | 64.31 |
| 4.285714 | j 181 | 2.27 | 66.58 |
| 4.714286 | 140 | 1.76 | 68.34 |
| 5 | 133 | 1.67 | 70.00 |
| 5.285714 | 198 | 2.48 | 72.49 |
| 5.714286 | 125 | 1.57 | 74.06 |
| 6 | 189 | 2.37 | 76.43 |
| 6.571429 | 126 | 1.58 | 78.01 |
| 7.033163 | 168 | 2.11 | 80.12 |
| 7.857143 | 157 | 1.97 | 82.09 |
| 8.571428 | 187 | 2.35 | 84.43 |
| 9.571428 | 134 | 1.68 | 86.11 |
| | 134 | 1.68 | 87.79 |
| 10.71429 | 188 | 2.36 | 90.15 |
| 11.57143 | 180 | 2.26 | 92.41 |
| 12.57143 | 130 | 1.63 | 94.04 |
| 13.42857 | 176 | 2.21 | 96.25 |
| 15 | 156 | 1.96 | 98.21 |
| 16.57143 | 143 | 1.79 | 100.00 |
| Total | + 7,971 | 100.00 | |

Now generate new file:

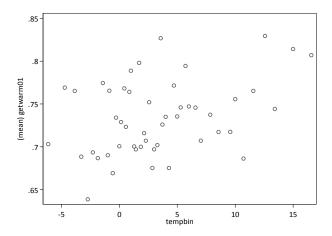
collapse (mean) getwarm01, by (tempbin)
twoway scatter getwarm01 tempbin, aspect(1)



So much better, right?

One other thing: note that I use the option aspect(1). This forces Stata to produce a graph with aspect ratio (i.e. ratio of height:width) of 1. Otherwise, Stata's default is the "golden ratio," which is approx 1:1.6. This produces a picture that "stretches out" X, leading the eye to underestimate the strength of the relationship between X and Y:

twoway scatter getwarm01 tempbin



II. SUMMARIZING the Relationship NON-PARAMETRICALLY

a. Table: Summary Statistics for Y by Values of X

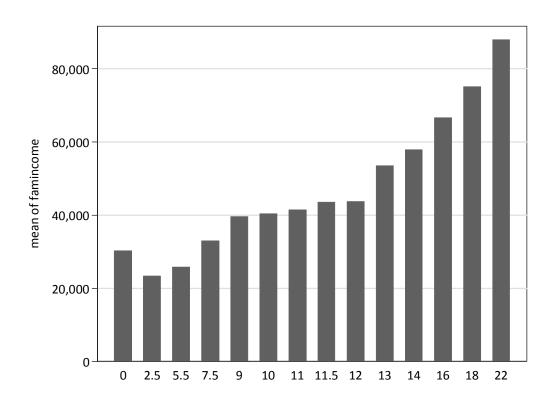
. table educyears, c(mean famincome median famincome sd famincom)

| Years of Education | mean(faminc~e) | med(faminc~e) | sd(faminc~e) |
|-----------------------|----------------|---------------|--------------|
| 0 | 30277.78 | 32500 | 17690.95 |
| 2.5 | 23383.33 | 17500 | 16861.47 |
| 5.5 | 25800 | 22500 | 20889.18 |
| 7.5 | 33012.9 | 22500 | 28464.15 |
| 9 | 39599.74 | 32500 | 30232.96 |
| 10 | 40429.91 | 32500 | 32337.82 |
| 11 | 41450.45 | 32500 | 33324.25 |
| 11.5 | 43551.47 | 45000 | 25684.93 |
| 12 | 43733.9 | 37500 | 28895.93 |
| 13 | 53493.88 | 45000 | 33180.55 |
| 14 | 57854.84 | 55000 | 32961.58 |
| 16 | 66617.31 | 67500 | 34944.65 |
| 18 | 75098.48 | 67500 | 32904.3 |
| 22 | 87965.12 | 87500 | 34723.64 |

b. FIGURES (generally appropriate when X, Y or both are at interval-level or higher)

i. a **BAR CHART** displaying central tendencies of Y by values of X:

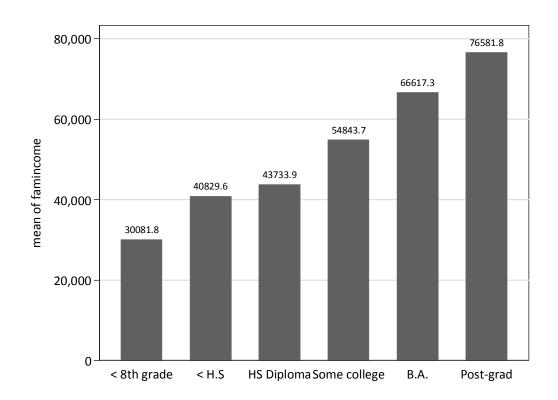
. graph bar (mean) famincome, over(educyears)



(Note: not ideal because gives false impression that intervals between bars are equally sized.)

Another way, with bar heights labeled:

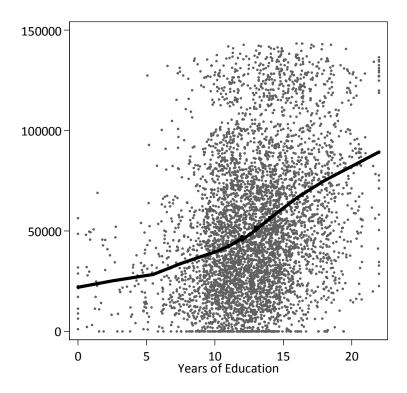
. graph bar (mean) famincome, over(educ_rc) blabel(bar)



ii. <u>SCATTERPLOT WITH SMOOTHER</u> displaying mean of Y by values of X (both X,Y interval-level or higher):

(We'll hold off on discussing details of how the smoother is constructed. For now, simply note that it requires very little in terms of parametric assumptions.)

. twoway (scatter famincome educyears, jitter(20) msize(tiny)) (lowess famincome educyears, clc(black) clw(thick)), legend(off)



III. SUMMARIZING the relationship PARAMETRICALLY

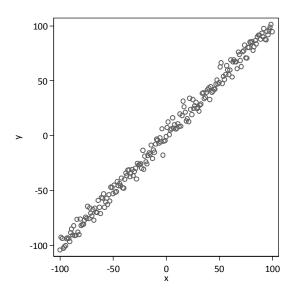
i. The correlation coefficient

Sometimes it acts like we want it to. Very strong here, as it should be:

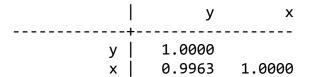
*generate 201 x values ranging from -100 to 100 in steps of 1: . egen x = fill(-100/100)

*generate 201 y values equal to x plus a bit of noise:

- . gen y = x + rnormal(0,5)
- . scatter y x, aspect(1)

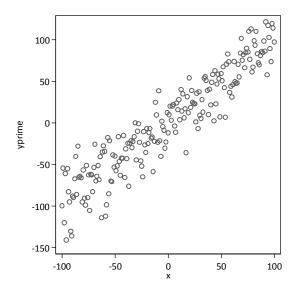


. corr y x (obs=201)



A little weaker here, as we would expect (and want):

- *generate 201 y values equal to x plus a lot more noise:
- . gen yprime = x + rnormal(0,20)
- . scatter yprime x, aspect(1)

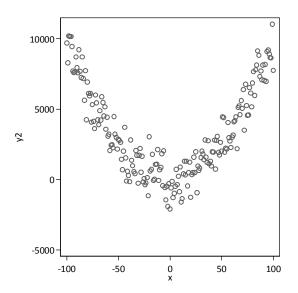


. corr yprime x
(obs=201)

But is terrible at detecting non-linear relationships, no matter how strong:

*generate 201 y values equal to x-squared plus noise:

- . gen $y2 = x^2 + rnormal(0,1000)$
- . scatter y2 x, aspect(1)



. corr y2 x (obs=201)

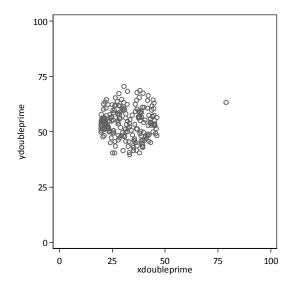
And is very sensitive to outliers. Here there is no relationship between x and y in obs 1 through 99. See how adding just one additional observation changes the correlation coefficient:

- . set obs 100
- . gen xdoubleprime = 33
- . egen ydoubleprime = fill(50 52 54 56 58 50 52 54 56 58)
- *note no relationship betw x and y among these observations; *now let's change obs # 100 as follows:
- . replace xdoubleprime = 80 in 100
 (1 real change made)
- . replace ydouble =75 in 100
 (1 real change made)
- . list xdoubleprime ydoubleprime

. . .

| 91. | 33 | 50 |
|------|----|----|
| 92. | 33 | 52 |
| 93. | 33 | 54 |
| 94. | 33 | 56 |
| 95. | 33 | 58 |
| | | |
| 96. | 33 | 50 |
| 97. | 33 | 52 |
| 98. | 33 | 54 |
| 99. | 33 | 56 |
| 100. | 80 | 75 |
| | | |

. scatter ydouble xdouble, xsize(3) ysize(3) xlabel(0(25)100) ylabel(0(25)100) jitter(20)



. corr y x (obs=100)

| | ydoubl~e | |
|--------------|----------|--------|
| ydoubleprime | ! | |
| xdoubleprime | 0.5988 | 1.0000 |

That's a pretty darn high correlation, considering we have nothing but random covariation in obs 1-99!