

# An integral image approach to performing multi-scale topographic position analysis

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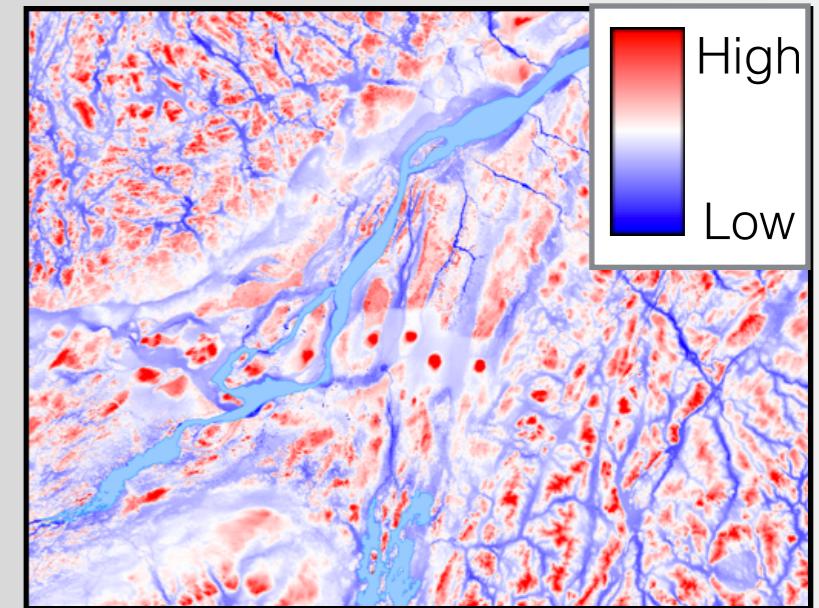
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# Relative topographic position (TP) and landscape ruggedness

Used for landform, soils, veg. and habitat mapping.

Ruggedness (roughness) measures:

- Local relief; Std. dev. of elevation

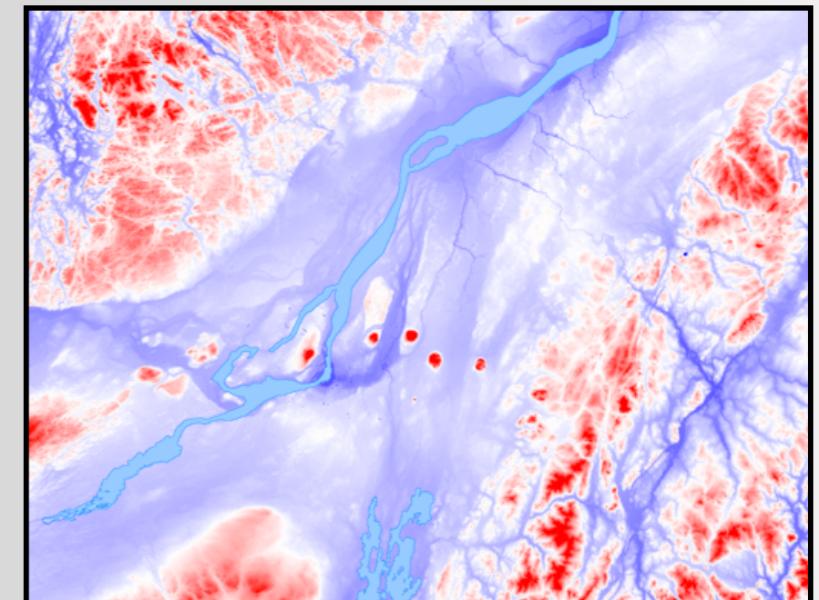


*DEV calculated with 100 x 100 filter*

Topographic position measures:

- Difference from mean elevation
- Deviation from mean elevation (*DEV*)
- Elevation percentile

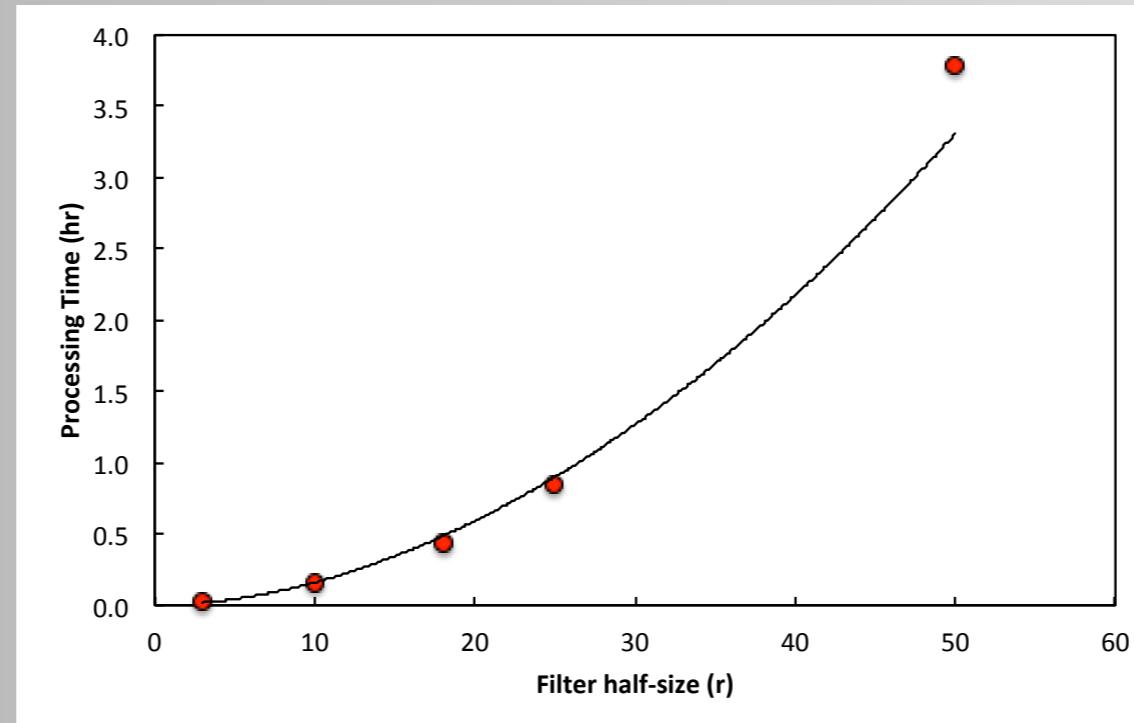
They are inherently scale-dependent.



*DEV calculated with 500 x 500 filter*

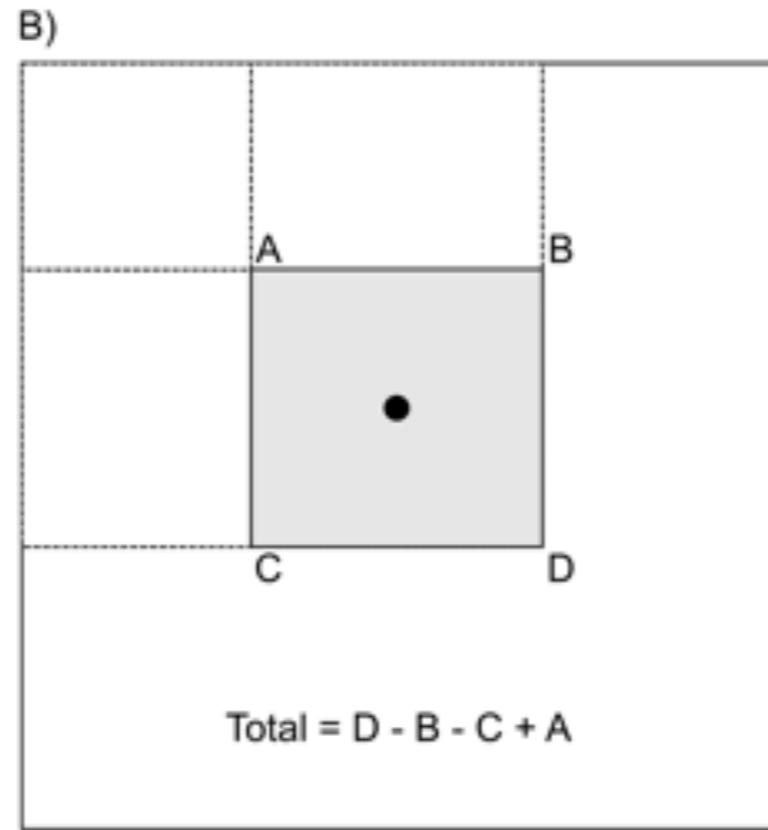
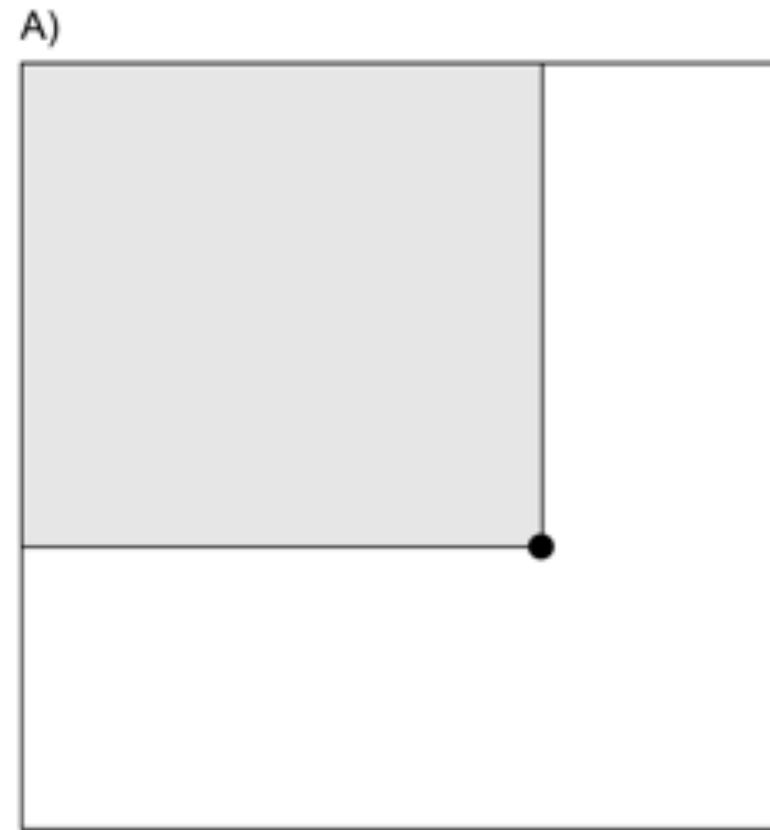
# Multi-scaled analysis of TP/ ruggedness offers substantial value

- The inefficiency of the roving window filter approach makes multi-scaled analyses and applications with massive DEMs very challenging.



- Past work has relied on degrading grid resolution.

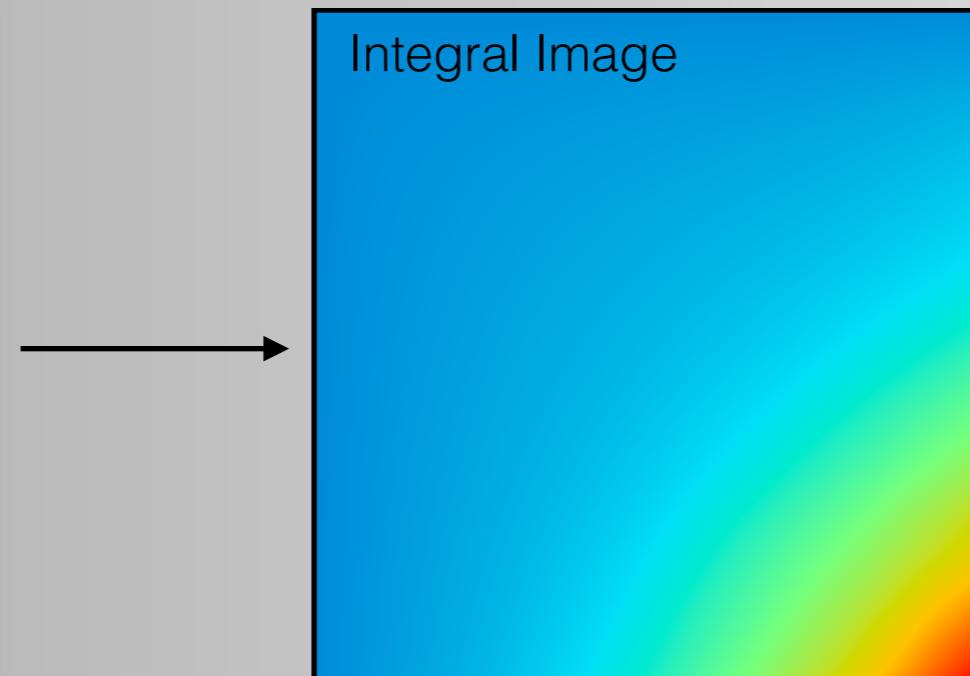
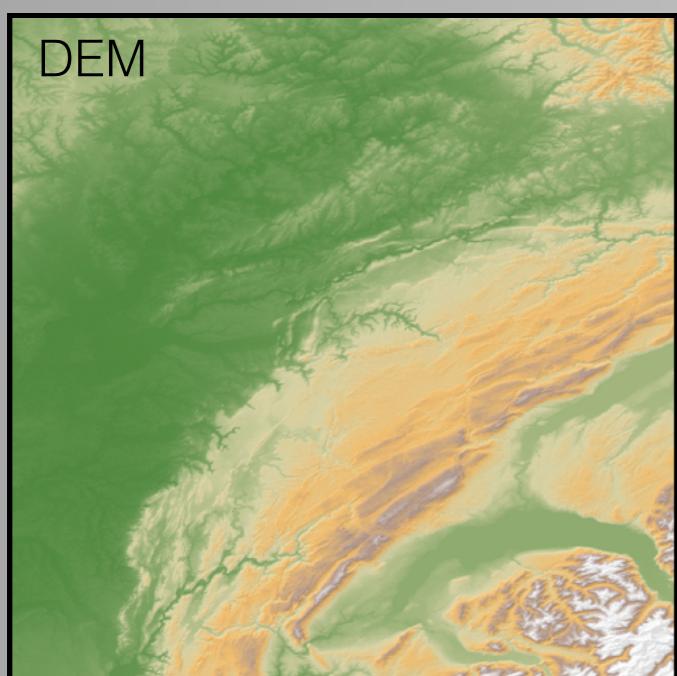
# Integral image transform



Developed by Crow (1984) and now widely used in comp. vision.

Efficiently calculate window sum, mean, variance, etc.

Calculations are independent of roving window size.

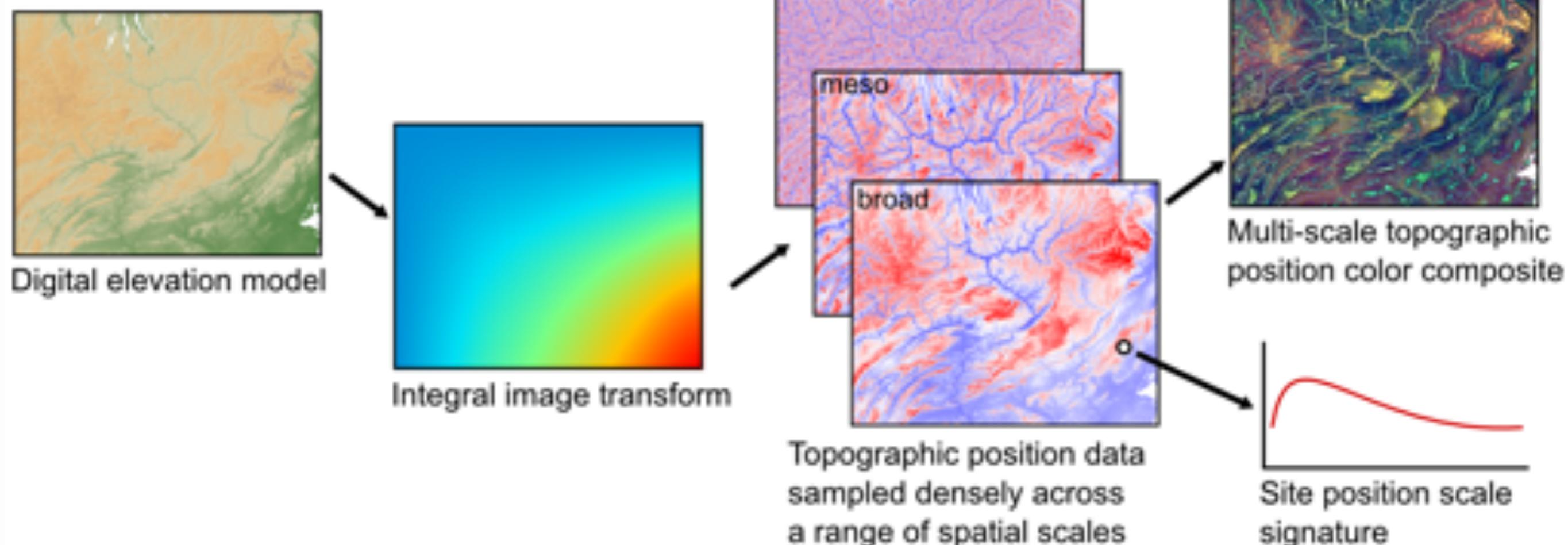


# Case study

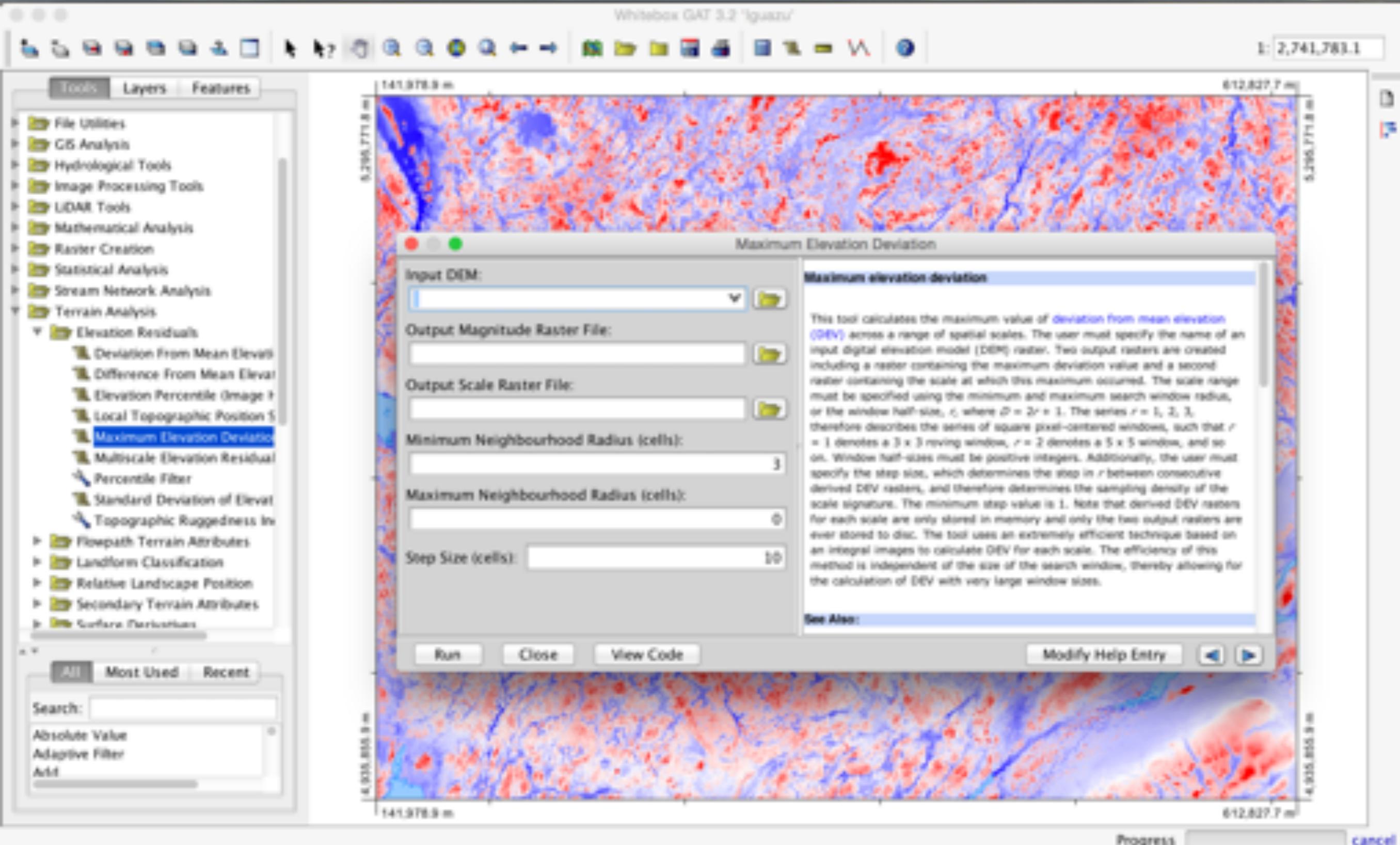


An extensive area of heterogeneous geomorphology and geology.

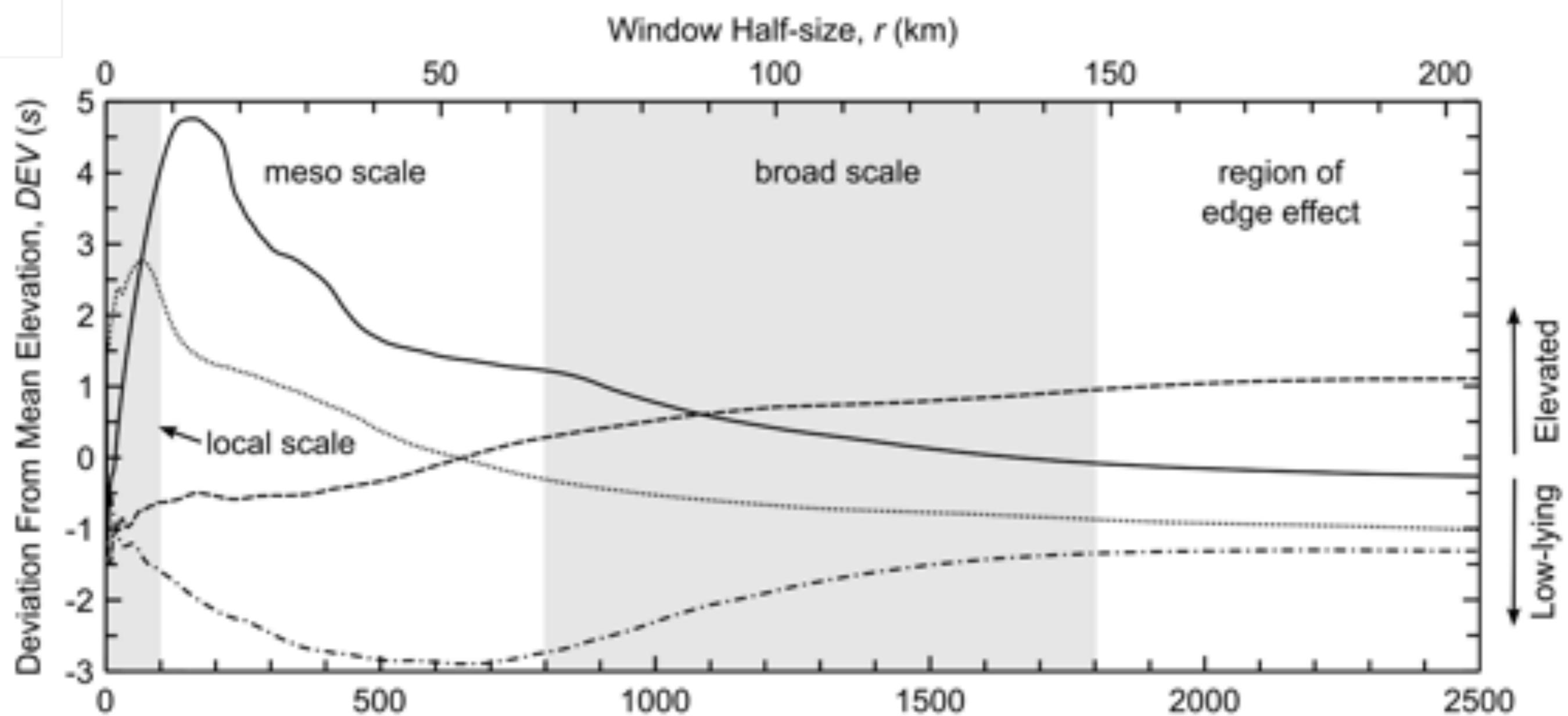
A  $13,692 \times 10,413$  rows by columns (142M grid cells; 544 MB) raster derived from SRTM DEM data.



# Several open-source tools have been created to implement the multi-scale analysis



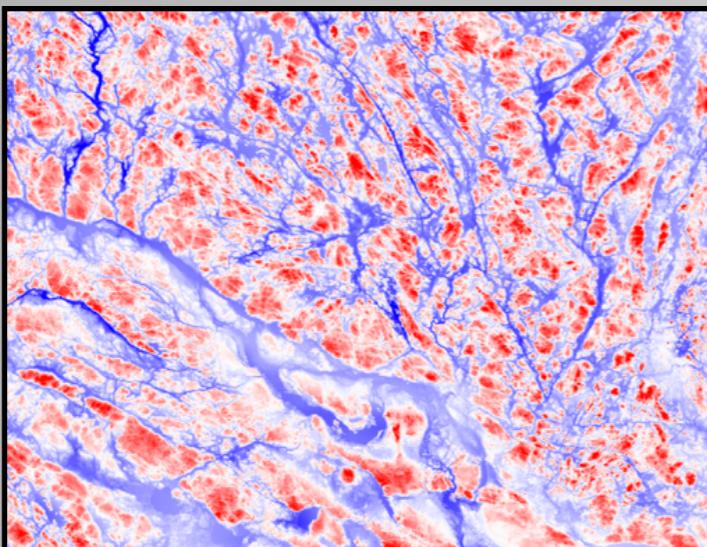
# Scale signatures



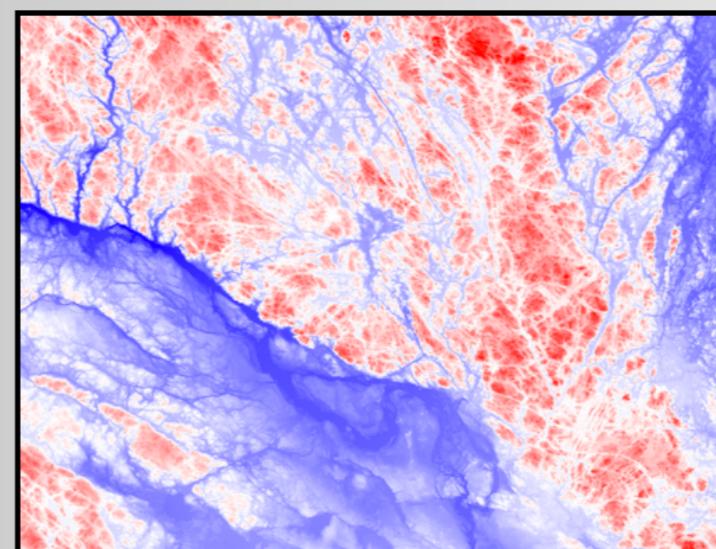
# $DEV_{max}$ and $r_{max}$

- Sample TP across a range of scales and identify the maximally deviated value ( $DEV_{max}$ ) and window size ( $r_{max}$ ) at which it occurs for each raster grid cell.
- Each grid cell's TP is recorded at an optimal scale based on its unique scale signature.
- Effectively allows each cell to self-identify with the feature that it most associates with.

# $DEV_{max}$ and $r_{max}$

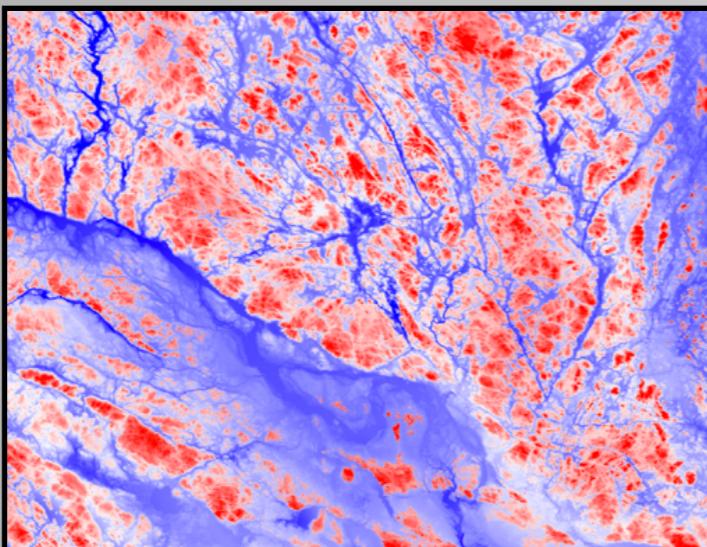


$DEV$  201 x 201 window

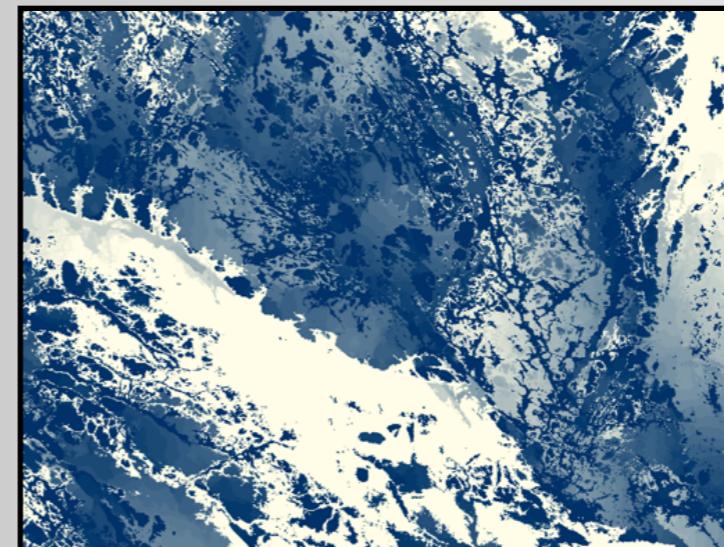


$DEV$  1501 x 1501 window

High  
Low

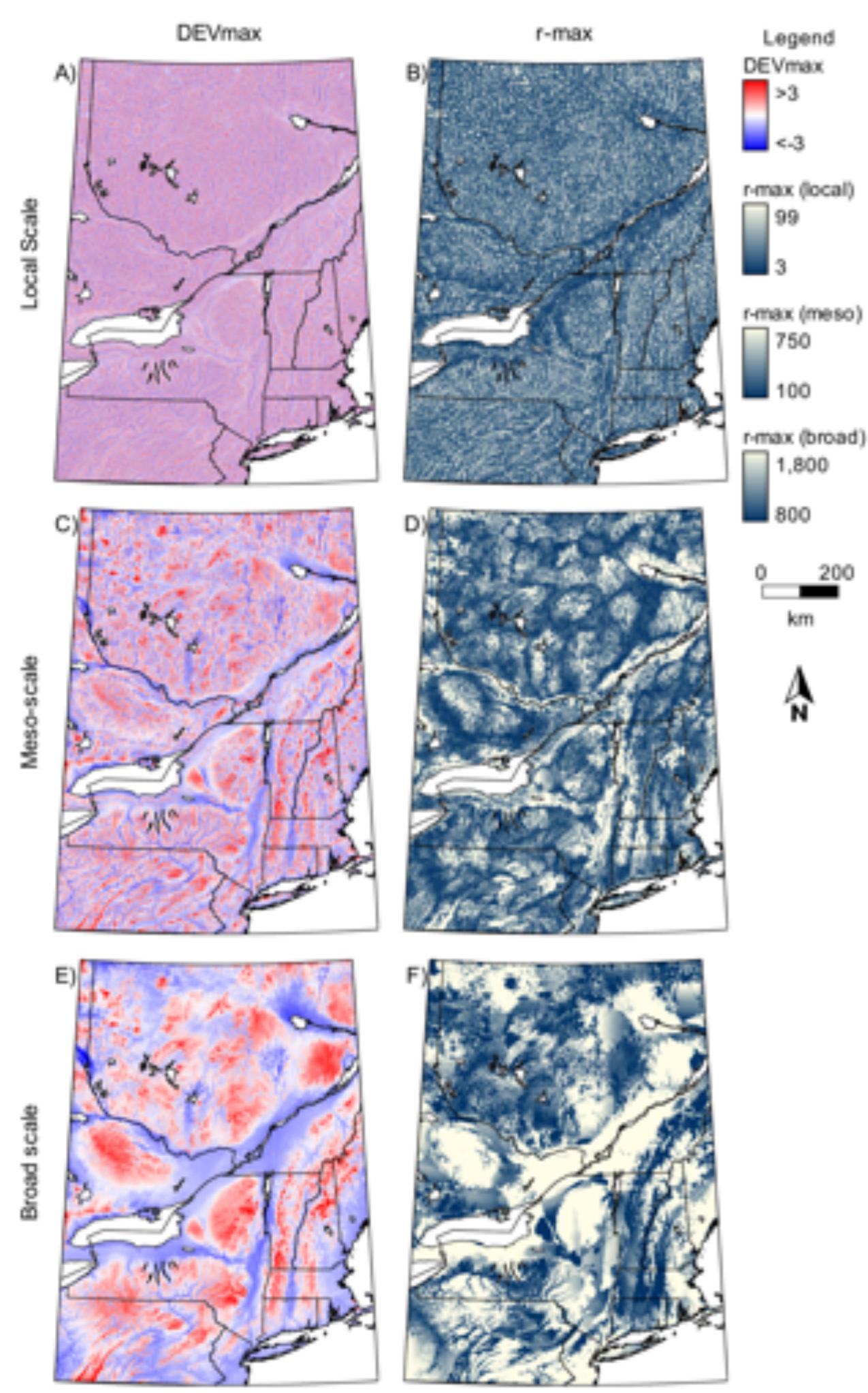


$DEV_{max}$  for windows ranging  
from 201-1501, step = 10



$r_{max}$  for windows ranging  
from 201-1501, step = 10

1501  
201



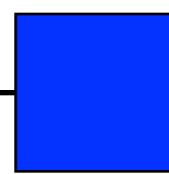
# $DEV_{max}$ and $r_{max}$

- 338 individual  $DEV$  rasters were calculated to create the three  $DEV_{max}$  rasters with window sizes ranging from  $7 \times 7$  to  $3601 \times 360$ .
- 28 minutes to process three scales on a 3.0 GHz system compared with estimated 23.3 years using roving window approach.

Local Scale

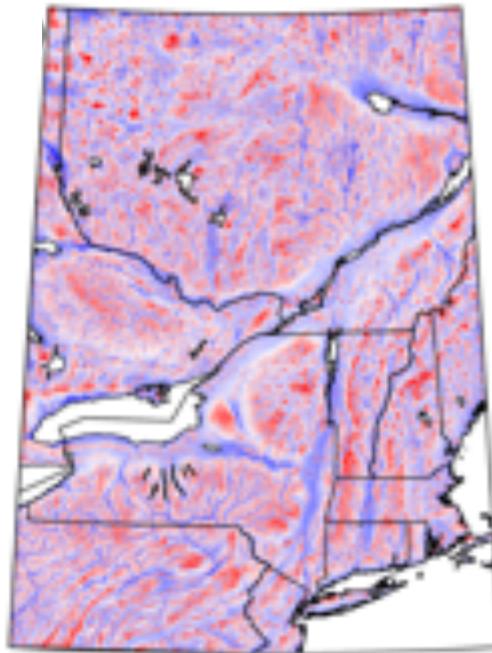


Convert to absolute  
value, rescale 0-255,  
and combine into RGB  
colour composite.

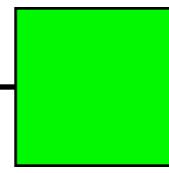


Blue Channel

Meso-scale

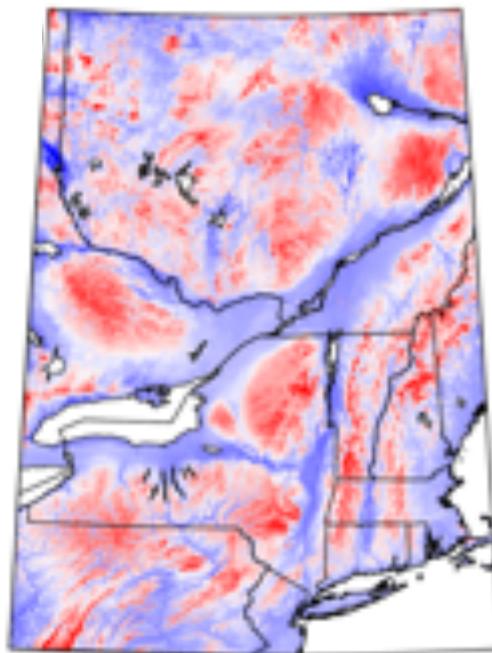


Green Channel

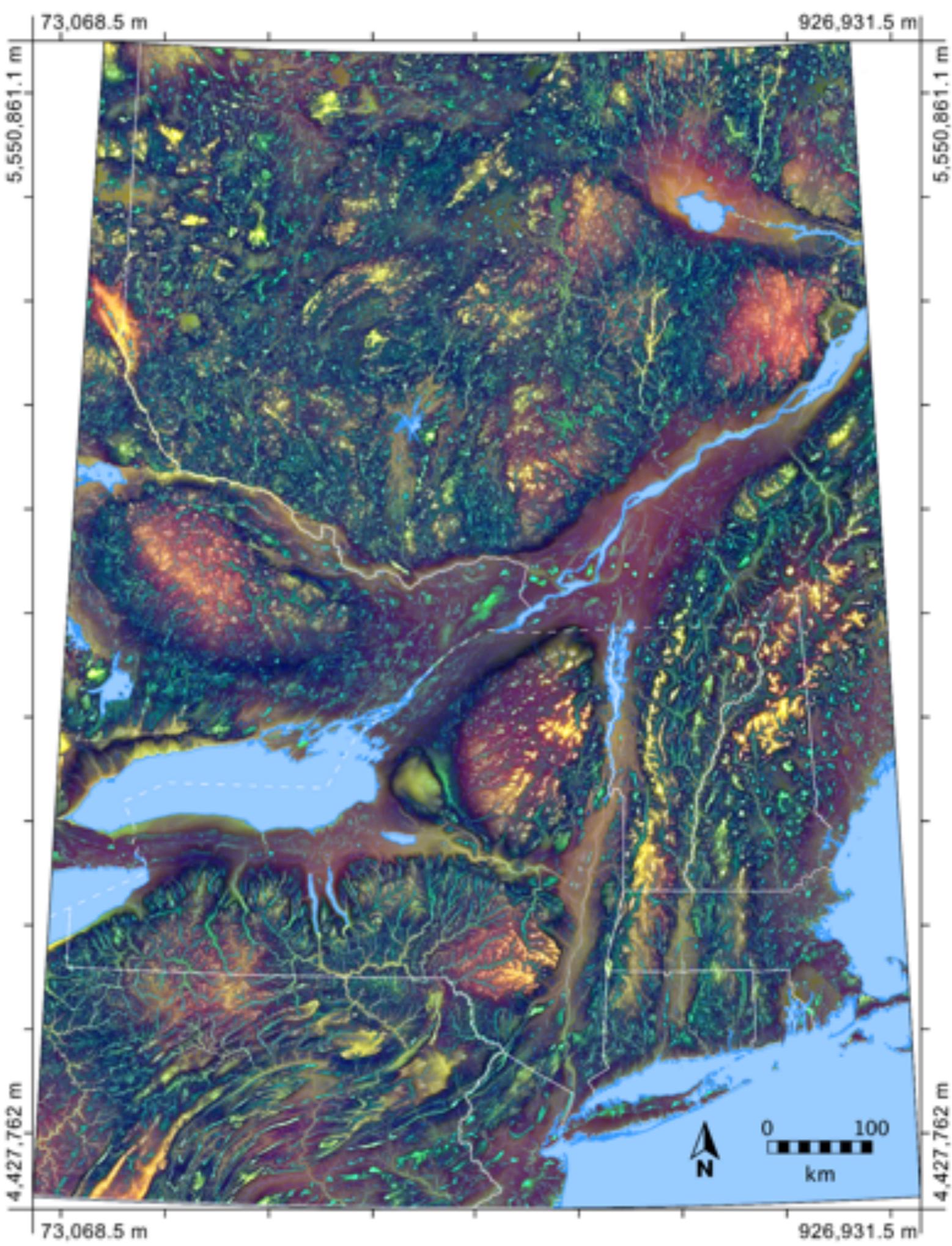
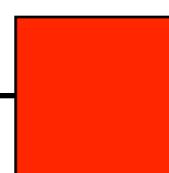


RGB Colour  
Composite

Broad scale

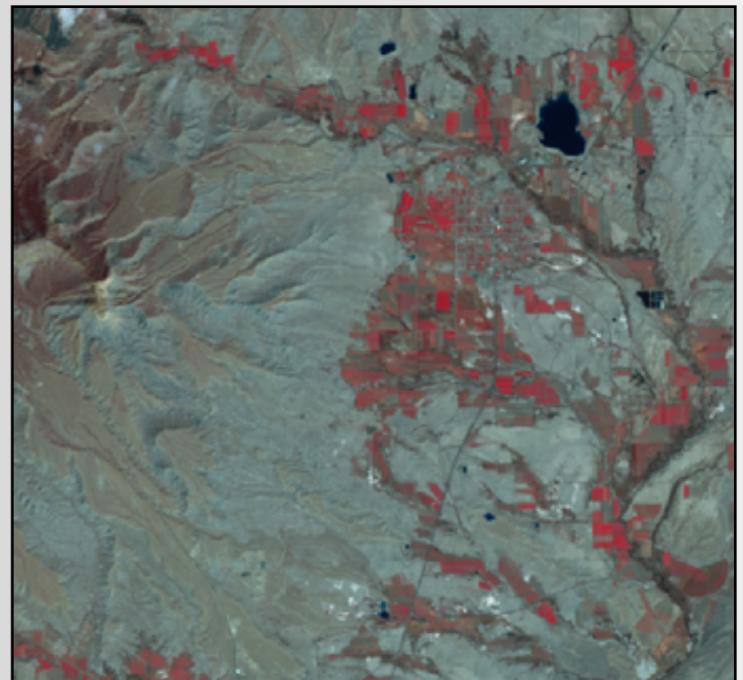


Red Channel



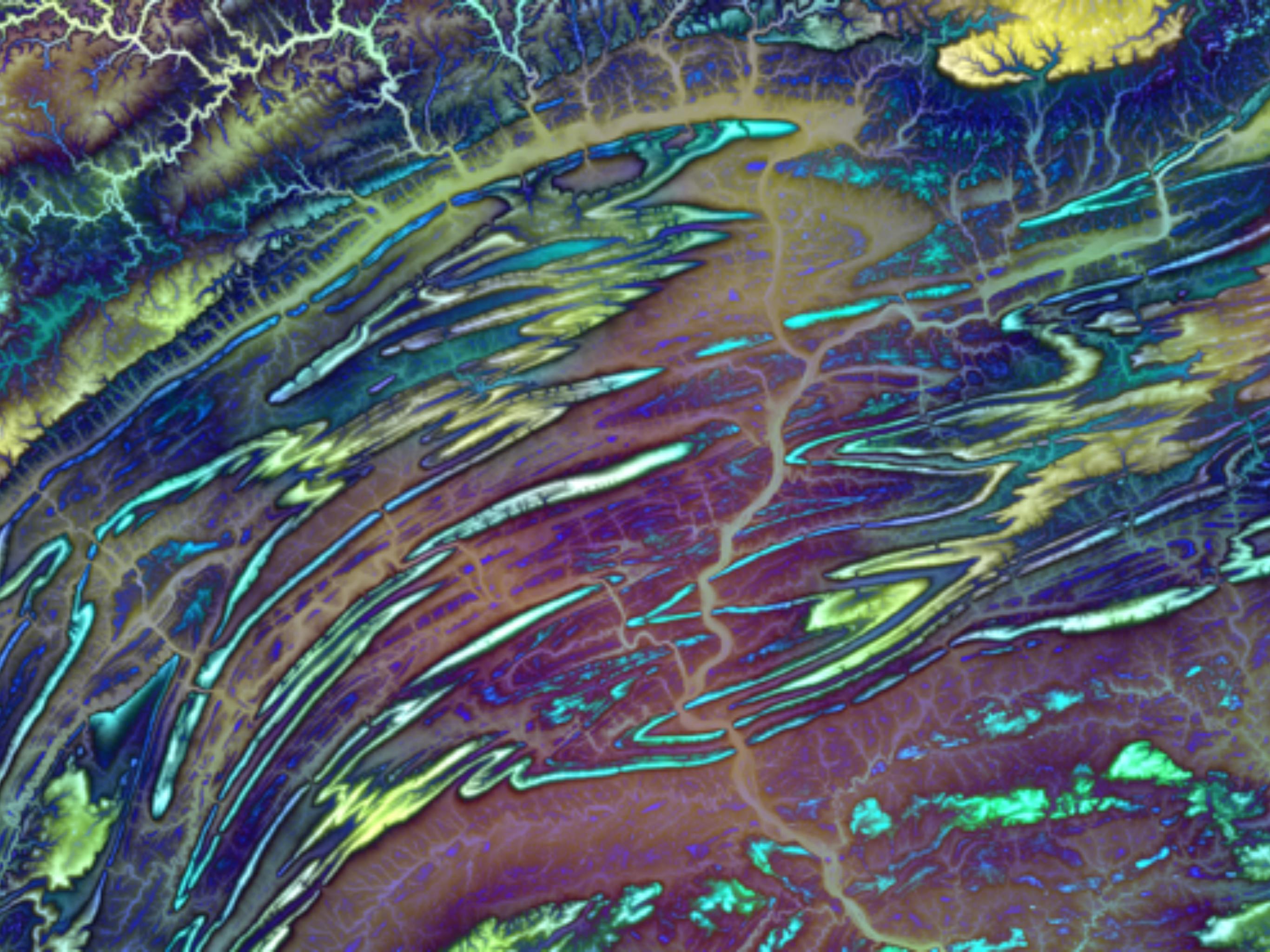
# The MTPCC Image

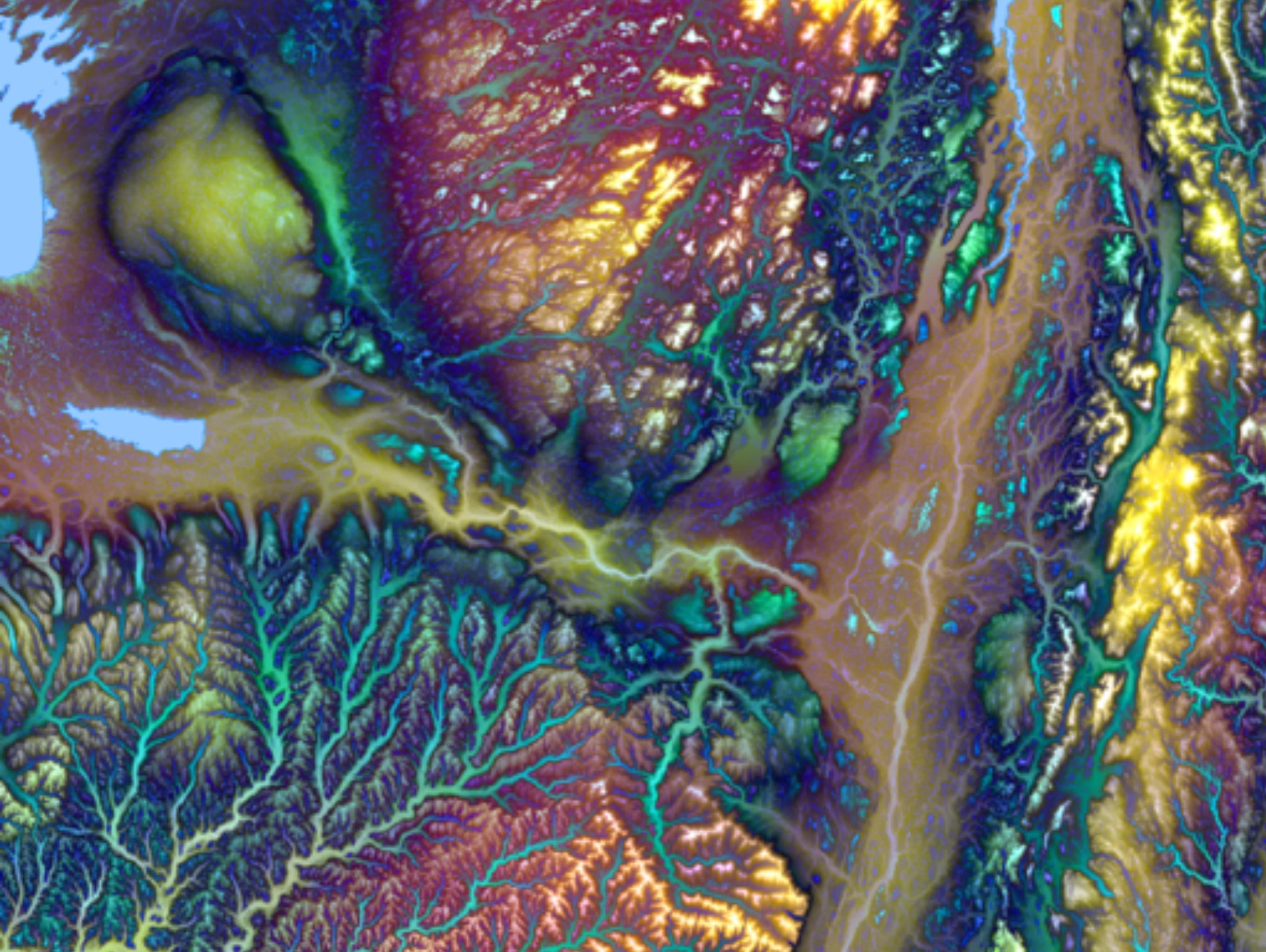
Colour	Multi-scaled TP description	
	Deviated (either elevated or low-lying) local-scale TP; average TP at the two larger scales	
	Deviated meso-scale position; average TP at both the local and broad-scale range	
	Deviated broad-scale position; average TP at both of the shorter scales	
	Deviated TP at both the local and meso-scale range; average TP in the broad-scale range	
	Deviated TP at the meso- and broad-scale ranges; average TP in the local-scale range	
	Deviated TP across a wide range of spatial scales	
	Average TP across a wide range of spatial scales	

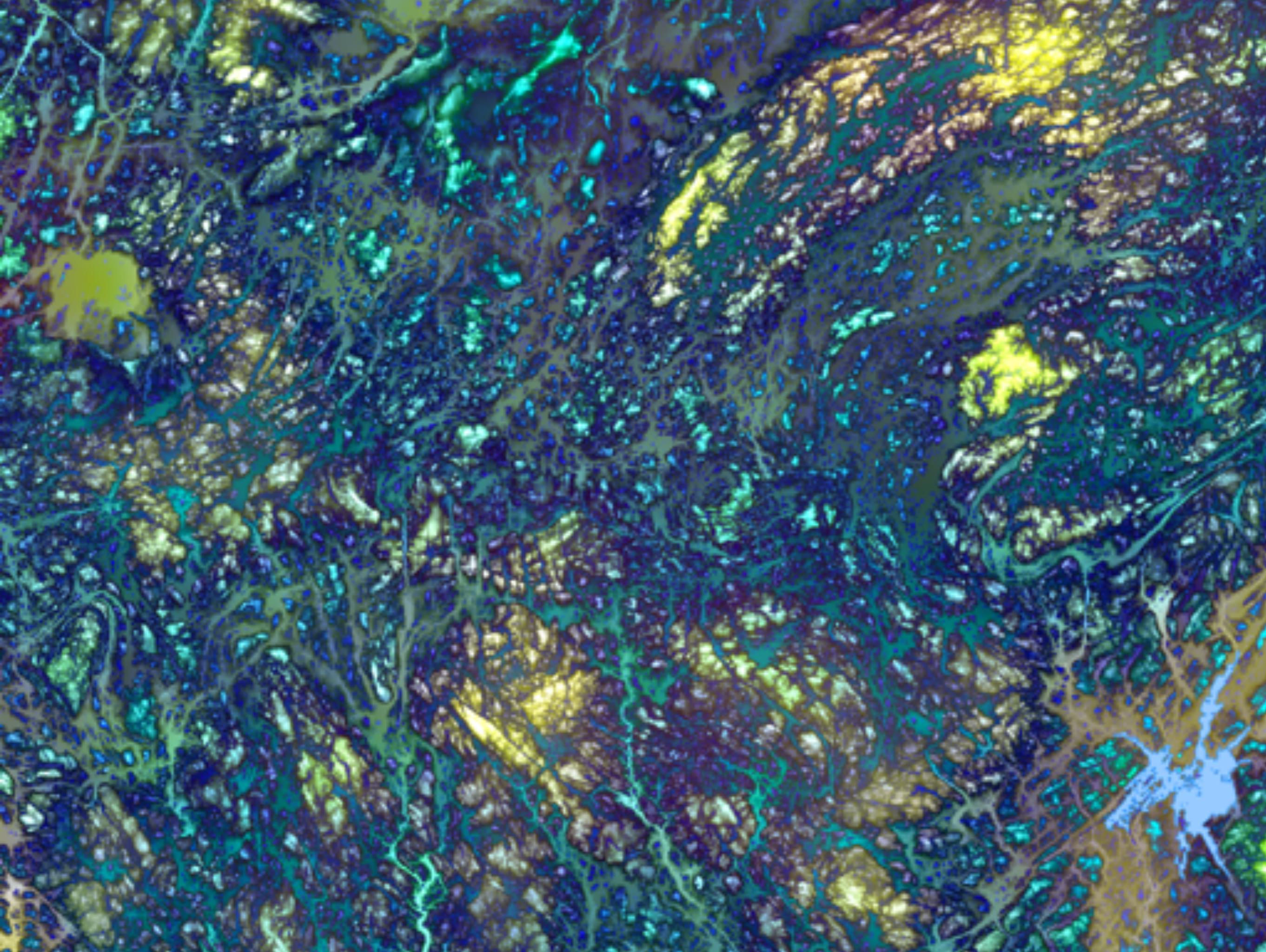


An MTPCC is similar to a colour satellite image created by combining three bands.

A pixel's colour tells you about the site's topographic position across three spatial ranges.







# Conclusions

- An integral image approach allows for the efficient computation of TP and ruggedness indices.
- This provides the opportunity to study the multi-scaled properties of TP and ruggedness at resolutions and scales not previously possible using a roving window approach without resorting to degrading data resolution.
- $DEV_{max}$  provides a valuable means of summarizing topographic position information for each pixel at key spatial scales within a wider range of scales.

# Conclusions

- The MTPCC image, derived by combining three  $DEV_{max}$  rasters into a single colour composite image, provides a convenient means of interpreting the multi-scale properties of locations within the landscape.
- Where from here? Object-based classifications of landscapes; an input to soils and vegetation mapping application; soil moisture modelling.