#### Hierarchical Linear Models

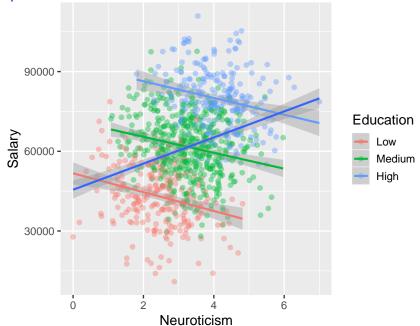
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10/28/2019

#### A Common Challenge Repeated measures

- Multiple measures from the same person who might also be part of a group
- Multiple exposures across people to the same stimuli
- Repeated-measures ANOVA accommodates correlated observations due to differences between people
- Multi-level general linear models go further and explicitly model general grouping effects (e.g., sampled stimuli)
- Addresses Simpson's paradox, where individual trends don't reflect the aggregate trend

Simpson's Paradox



### Useful packages

- library(tidyverse) for ggplot2, dplyr
- library(skimr) for skim, which provides a quick overview of data
- library(lme4) for mixed effect, multi-level general linear models
- library(lmerTest) for extracting p-values
- library(psycho) for extracting APA reportable sentences

#### Effect of Sleep Disruption

```
sleep.df = sleepstudy
ggplot(sleep.df, aes(Days, Reaction)) +
   geom_point() +
   geom_smooth(method = "lm") +
   facet_grid(.~reorder(Subject, Reaction))
 500 -
Reaction
```

```
Uniform Effect of Sleep Disruption?
   sleep.fit = lm(Reaction ~ Days, sleep.df)
   sleep.df$prediction = predict(sleep.fit)
   summary(sleep.fit)
   ##
   ## Call:
   ## lm(formula = Reaction ~ Days, data = sleep.df)
   ##
   ## Residuals:
   ##
          Min 1Q Median
                                    3Q
                                           Max
   ## -110.848 -27.483 1.546 26.142 139.953
   ##
   ## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
   ##
   ## (Intercept) 251.405
                             6.610 38.033 < 2e-16 ***
               10.467
                              1.238 8.454 9.89e-15 ***
   ## Days
```

### Uniform Effect of Sleep Disruption?

```
ggplot(sleep.df, aes(Days, Reaction)) +
  geom point(alpha = .4, size = 1) +
  geom_point(aes(y=prediction), shape = 21) +
  geom_line(aes(y=prediction)) +
  facet_grid(.~reorder(Subject, Reaction))
```

```
Random Effect for Intercept
   sleep_int.fit = lmer(Reaction ~ Days + (1|Subject), sleep.or
   summary(sleep_int.fit)
   ## Linear mixed model fit by REML. t-tests use Satterthwain
   ## lmerModLmerTest]
   ## Formula: Reaction ~ Days + (1 | Subject)
   ##
        Data: sleep.df
   ##
   ## REML criterion at convergence: 1786.5
   ##
   ## Scaled residuals:
   ##
         Min 1Q Median 3Q
                                         Max
   ## -3.2257 -0.5529 0.0109 0.5188 4.2506
   ##
   ## Random effects:
```

960.5 30.99

Groups Name Variance Std.Dev.

Subject (Intercept) 1378.2 37.12

## ##

## Residual

#### Random Effect for Intercept

```
ggplot(sleep.df, aes(Days, Reaction)) +
  geom point(alpha = .4, size = 1) +
  geom_point(aes(y=prediction_int), shape = 21) +
 geom_line(aes(y=prediction_int, group = Subject)) +
 facet_grid(.~reorder(Subject, Reaction))
```

# Random Effect for Intercept and Slope sleep\_int\_slope.fit = lmer(Reaction ~ Days + (Days|Subject)

summary(sleep\_int\_slope.fit) ## Linear mixed model fit by REML. t-tests use Satterthwain ## lmerModLmerTest] ## Formula: Reaction ~ Days + (Days | Subject)

## Data: sleep.df ## ## REML criterion at convergence: 1743.6 ##

## Scaled residuals: ## Min 1Q Median 3Q Max

## -3.9536 -0.4634 0.0231 0.4633 5.1793 ## ## Random effects:

Variance Std.Dev. Corr ## Groups Name

## Subject (Intercept) 611.90 24.737

35.08 5.923 0.07 ## Days

#### Random Effects for Intercept and Slope

```
ggplot(sleep.df, aes(Days, Reaction)) +
  geom point(alpha = .4, size = 1) +
  geom_line(aes(y=prediction_int_slope, group = Subject)) -
  geom_point(aes(y=prediction_int_slope), shape = 21) +
  facet_grid(.~reorder(Subject, Reaction))
Reaction
```

#### Summary for Publication

- The "psycho" package provides functions for summarizing model output
- It creates a publication-ready summary table
- It can even create sentences describing the output
- Parameter estimates can be extracted for plotting

```
library(psycho)
analyze(sleep_int_slope.fit, CI = 95) %>%
  summary(results, round = 2) %>%
  mutate(p = format_p(p)) %>%
  kable()
```

Variable	Effect_Size	Coef	SE	t	df	р	
(Intercept)	NA	251.41	6.82	36.84	17.01	< .001***	
Days	medium	10.47	1.55	6.77	17.00	< .001***	

# Summary for Publication|psycho can create sentences describing the output

```
analyze(sleep_int_slope.fit, CI = 95)
## The overall model predicting Reaction (formula = Reaction)
```

- ## The effect of Days is significant (beta = 10.47, Significant model predicting Reaction (formula = Reaction  $\sim$  Days
- + (Days  $\mid$  Subject)) has an total explanatory power (conditional R2) of 79.92%, in which the fixed effects explain 27.87% of the variance (marginal R2).
- -The model's intercept is at 251.41 (SE = 6.82, 95% CI [237.68, 265.13]). Within this model:
- -The effect of Days is significant (beta = 10.47, SE = 1.55, 95% CI [7.36, 13.58], t(17) = 6.77, p < .001) and can be considered as medium (std. beta = 0.54, std. SE = 0.079).

# Summary for Publication Parameter estimates can also be extracted for plotting

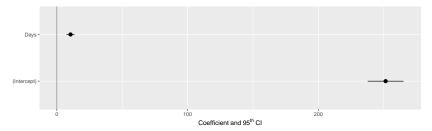
```
CI.lme.df = analyze(sleep_int_slope.fit)$summary
ggplot(CI.lme.df, aes(Variable)) +
    geom hline(yintercept = 0, alpha = .5)+
    geom pointrange(aes(y = Coef, ymin= CI lower, ymax = C)
    coord flip() +
    labs(x = "", y = expression(Coefficient~and~95^{th}~CI)
 Davs -
```

(Intercept) -



## Exercise | Multi-level model fitting

- Fit a multi-level model with Subject as a random variable
- Use the analyze command from psych to extract an summmary of effects
- Plot the effect estimates



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