README

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Language models are probability distributions over sequences of tokens. More formally, we define the sample space Ω^d to be the d-dimensional cartesian product of a set of tokens, the event space \mathcal{F} to be the set of all possible token sentences, and probability measure $\mathbb{P}: \mathcal{F} \mapsto [0,1]$.

Letting the random vector $\mathbf{X} : \Omega^d \to \mathbb{R}^d$, we can encode sentences into \mathbb{R}^d , which is a space that is computable (denotational vs distributional semantics?). To evaluate the probability of an encoded sentence, we compute:

$$p_{\mathbf{X}}(\mathbf{x}) = \mathbb{P}[\mathbf{X} = \mathbf{x}]$$

$$= \mathbb{P}[\mathbf{X}^{-1}(\mathbf{x})]$$

$$= \mathbb{P}[\{\omega \in \Omega^d := \mathbf{X}(\omega) = \mathbf{x}\}]$$
(1)

(autoregressive? markov assumption?)

The goal is to approximate $p_{\mathbf{X}}(\mathbf{x})$ given $\mathcal{D} = (x_1, y_1), ..., (x_n, y_n)$ (assuming (x_i, y_i) p), with some hypothesis $h : \mathcal{X} \mapsto \mathcal{Y}$. With parametric models, this is done by posing parameter estimation as an optimization problem (ERM?) $\operatorname{argmin}_{\theta} \mathcal{L}(\theta)$.

(PAC?, theoretical optimal?)