

# Package ‘cTMed’

March 19, 2024

**Title** Continuous Time Mediation

**Version** 0.0.0.9000

**Description** Calculates standard errors and confidence intervals  
for the indirect effect in continuous time mediation models.

**URL** <https://github.com/jeksterslab/cTMed>,  
<https://jeksterslab.github.io/cTMed/>

**BugReports** <https://github.com/jeksterslab/cTMed/issues>

**License** MIT + file LICENSE

**Encoding** UTF-8

**LazyData** true

**Roxygen** list(markdown = TRUE)

**Depends** R (>= 3.5.0)

**LinkingTo** Rcpp, RcppArmadillo

**Imports** Rcpp, numDeriv, parallel

**Suggests** knitr, rmarkdown, testthat, simStateSpace, expm

**RoxygenNote** 7.3.1

**NeedsCompilation** yes

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## R topics documented:

confint.ctmeddelta . . . . .	2
confint.ctmedmc . . . . .	3
deboeck2015 . . . . .	4
deboeck2015phi . . . . .	6
DeltaMed . . . . .	7
Direct . . . . .	10

Indirect . . . . .	12
MCMed . . . . .	15
MCPhi . . . . .	18
Med . . . . .	20
plot.ctmeddelta . . . . .	23
plot.ctmedmc . . . . .	24
plot.ctmedmed . . . . .	25
PosteriorMed . . . . .	26
print.ctmeddelta . . . . .	28
print.ctmedeffect . . . . .	30
print.ctmedmc . . . . .	31
print.ctmedmcphi . . . . .	32
print.ctmedmed . . . . .	33
summary.ctmeddelta . . . . .	35
summary.ctmedmc . . . . .	36
summary.ctmedmed . . . . .	37
TestPhi . . . . .	39
Total . . . . .	40
<b>Index</b>	<b>43</b>

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confint.ctmeddelta	<i>Delta Method Confidence Intervals</i>
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**Description**

Delta Method Confidence Intervals

**Usage**

```
## S3 method for class 'ctmeddelta'  
confint(object, parm = NULL, level = 0.95, ...)
```

**Arguments**

- object            Object of class ctmeddelta.
- parm            a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
- level           the confidence level required.
- ...            additional arguments.

**Value**

Returns a matrix of confidence intervals.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```

data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)
confint(delta)

# Range of time-intervals -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
confint(delta)

```

---

confint.ctmedmc

---

*Monte Carlo Method Confidence Intervals*


---

**Description**

Monte Carlo Method Confidence Intervals

**Usage**

```

## S3 method for class 'ctmedmc'
confint(object, parm = NULL, level = 0.95, ...)

```

**Arguments**

object                      Object of class ctmedmc.

<code>parm</code>	a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
<code>level</code>	the confidence level required.
<code>...</code>	additional arguments.

## Value

Returns a matrix of confidence intervals.

## Author(s)

Ivan Jacob Agaloos Pesigan

## Examples

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
confint(mc)

# Range of time-intervals -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
confint(mc)
```

## Description

The data was simulated using `simStateSpace::SimSSMVARFixed()` from a discrete-time vector autoregressive model given by

## Usage

deboeck2015

## Format

Dataframe with Five Columns:

**id** Individual ID.

**time** Time variable.

**x** X variable.

**m** M variable.

**y** Y variable.

## Details

$$\mathbf{y}_{i,t} = \beta \mathbf{y}_{i,t-1} + \boldsymbol{\varepsilon}_{i,t}$$

where  $\mathbf{y}_{i,t}$  and  $\mathbf{y}_{i,t+1}$  represents a vector of observed variables  $X$ ,  $M$ , and  $Y$  for individual  $i$  at time  $t$  and  $t + 1$ ,  $\boldsymbol{\varepsilon}_{i,t}$  a vector of normally distributed random noise with mean vector of zero and covariance matrix  $\Psi$  given by

$$\Psi = \begin{pmatrix} 0.10 & 0 & 0 \\ 0 & 0.10 & 0 \\ 0 & 0 & 0.10 \end{pmatrix}, \quad \text{and}$$

$\beta$  is a matrix of lagged parameters given by

$$\beta = \begin{pmatrix} 0.70 & 0 & 0 \\ 0.50 & 0.60 & 0 \\ -0.10 & 0.40 & 0.50 \end{pmatrix}.$$

The mean vector  $\boldsymbol{\mu}_0$  and covariance matrix  $\Sigma_0$  of the initial condition are given by

$$\boldsymbol{\mu}_0 = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}, \quad \text{and}$$

$$\Sigma_0 = \begin{pmatrix} 1 & 0.20 & 0.20 \\ 0.20 & 1 & 0.20 \\ 0.20 & 0.20 & 1 \end{pmatrix}.$$

## References

Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. [doi:10.1080/10705511.2014.973960](https://doi.org/10.1080/10705511.2014.973960)

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deboeck2015phi

*Drift Matrix*

---

## Description

Parameter estimates and sampling variance-covariance matrix of the continuous-time vector autoregressive model drift matrix using the data set deboeck2015. The model was fitted using the dynr package.

## Usage

deboeck2015phi

## Format

List with Two Elements:

**dynr** Results using the dynr package.

**ctsem** Results using the ctsem package.

The dynr element is a list with the following elements:

**phi** The estimated drift matrix  $\Phi$ .

**vcov** The estimated sampling variance-covariance matrix of  $\text{vec}(\Phi)$ .

The ctsem element is a list with the following elements:

**posterior** Posterior distribution.

**posterior\_phi** Posterior distribution of the drift matrix  $\Phi$ .

**phi** Posterior mean of the drift matrix  $\Phi$ .

**vcov** Posterior variance-covariance matrix of  $\text{vec}(\Phi)$ .

## References

Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. [doi:10.1080/10705511.2014.973960](https://doi.org/10.1080/10705511.2014.973960)

Ou, L., Hunter, M. D., & Chow, S.-M. (2019). What's for dynr: A package for linear and nonlinear dynamic modeling in R. *The R Journal*, 11(1), 91. [doi:10.32614/rj2019012](https://doi.org/10.32614/rj2019012)

DeltaMed

*Delta Method Sampling Variance-Covariance Matrix for the Total, Direct, and Indirect Effects of  $X$  on  $Y$  Through  $M$  Over a Specific Time-Interval or a Range of Time-Intervals*

## Description

This function computes the delta method sampling variance-covariance matrix for the total, direct, and indirect effects of the independent variable  $X$  on the dependent variable  $Y$  through mediator variables  $\mathbf{m}$  over a specific time-interval  $\Delta t$  or a range of time-intervals using the first-order stochastic differential equation model's drift matrix  $\Phi$ .

## Usage

```
DeltaMed(phi, vcov_phi_vec, delta_t, from, to, med, ncores = NULL)
```

## Arguments

phi	Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
vcov_phi_vec	Numeric matrix. The sampling variance-covariance matrix of $\text{vec}(\Phi)$ .
delta_t	Vector of positive numbers. Time interval ( $\Delta t$ ).
from	Character string. Name of the independent variable $X$ in phi.
to	Character string. Name of the dependent variable $Y$ in phi.
med	Character vector. Name/s of the mediator variable/s in phi.
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when the length of delta_t is long.

## Details

See [Total\(\)](#), [Direct\(\)](#), and [Indirect\(\)](#) for more details.

### Delta Method:

Let  $\theta$  be  $\text{vec}(\Phi)$ , that is, the elements of the  $\Phi$  matrix in vector form sorted column-wise. Let  $\hat{\theta}$  be  $\text{vec}(\hat{\Phi})$ . By the multivariate central limit theory, the function  $\mathbf{g}$  using  $\hat{\theta}$  as input can be expressed as:

$$\sqrt{n} \left( \mathbf{g}(\hat{\theta}) - \mathbf{g}(\theta) \right) \xrightarrow{D} \mathcal{N}(0, \mathbf{J}\mathbf{\Gamma}\mathbf{J}')$$

where  $\mathbf{J}$  is the matrix of first-order derivatives of the function  $\mathbf{g}$  with respect to the elements of  $\theta$  and  $\mathbf{\Gamma}$  is the asymptotic variance-covariance matrix of  $\hat{\theta}$ .

From the former, we can derive the distribution of  $\mathbf{g}(\hat{\theta})$  as follows:

$$\mathbf{g}(\hat{\theta}) \approx \mathcal{N}(\mathbf{g}(\theta), n^{-1}\mathbf{J}\mathbf{\Gamma}\mathbf{J}')$$

The uncertainty associated with the estimator  $\mathbf{g}(\hat{\boldsymbol{\theta}})$  is, therefore, given by  $n^{-1}\mathbf{J}\boldsymbol{\Gamma}\mathbf{J}'$ . When  $\boldsymbol{\Gamma}$  is unknown, by substitution, we can use the estimated sampling variance-covariance matrix of  $\hat{\boldsymbol{\theta}}$ , that is,  $\hat{\mathbf{V}}(\hat{\boldsymbol{\theta}})$  for  $n^{-1}\boldsymbol{\Gamma}$ . Therefore, the sampling variance-covariance matrix of  $\mathbf{g}(\hat{\boldsymbol{\theta}})$  is given by

$$\mathbf{g}(\hat{\boldsymbol{\theta}}) \approx \mathcal{N}(\mathbf{g}(\boldsymbol{\theta}), \mathbf{J}\hat{\mathbf{V}}(\hat{\boldsymbol{\theta}})\mathbf{J}').$$

#### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \mathbf{\Lambda}\boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\mathbf{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\mathbf{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}}\mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $(\boldsymbol{\Theta}^{\frac{1}{2}})(\boldsymbol{\Theta}^{\frac{1}{2}})' = \boldsymbol{\Theta}$ .

The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \boldsymbol{\Phi}\boldsymbol{\eta}_{i,t})dt + \boldsymbol{\Sigma}^{\frac{1}{2}}d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\boldsymbol{\Phi}$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

#### Value

Returns an object of class `ctmeddelta` which is a list with the following elements:

**call** Function call.

**args** Function arguments.

**fun** Function used (DeltaMed).

**output** A list with length of `length(delta_t)`.

Each element in the output list has the following elements:

**delta\_t** Time-interval.

**jacobian** Jacobian matrix.,

**est** Estimated total, direct, and indirect effects.,

**vcov** Sampling variance-covariance matrix of the estimated total, direct, and indirect effects.



**Author(s)**

Ivan Jacob Agaloos Pesigan

**References**

Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. doi:10.2307/271028

Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. doi:10.1080/10705511.2014.973960

Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. doi:10.1007/s11336021097670

**See Also**

Other Continuous Time Mediation Functions: [Direct\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [MCPhi\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

**Examples**

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)

# Range of time-intervals -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)

# Methods -----
# DeltaMed has a number of methods including
# print, summary, confint, and plot
print(delta)
summary(delta)
confint(delta, level = 0.95)
```

```
plot(delta)
```

---

Direct

---

*Direct Effect of X on Y Over a Specific Time-Interval*


---

### Description

This function computes the direct effect of the independent variable  $X$  on the dependent variable  $Y$  through mediator variables  $\mathbf{m}$  over a specific time-interval  $\Delta t$  using the first-order stochastic differential equation model's drift matrix  $\Phi$ .

### Usage

```
Direct(phi, delta_t, from, to, med)
```

### Arguments

phi	Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
delta_t	Numeric. Time interval ( $\Delta t$ ).
from	Character string. Name of the independent variable $X$ in phi.
to	Character string. Name of the dependent variable $Y$ in phi.
med	Character vector. Name/s of the mediator variable/s in phi.

### Details

The direct effect of the independent variable  $X$  on the dependent variable  $Y$  relative to some mediator variables  $\mathbf{m}$  is given by

$$\text{Direct}_{\Delta t, i, j, \mathbf{m}} = \exp(\Delta t \mathbf{D} \Phi \mathbf{D})_{i, j}$$

where  $\Phi$  denotes the drift matrix,  $\mathbf{D}$  a diagonal matrix where the diagonal elements corresponding to mediator variables  $\mathbf{m}$  are set to zero and the rest to one,  $i$  the row index of  $Y$  in  $\Phi$ ,  $j$  the column index of  $X$  in  $\Phi$ , and  $\Delta t$  the time-interval.

#### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \mathbf{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\mathbf{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\mathbf{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\Theta^{\frac{1}{2}}\right)\left(\Theta^{\frac{1}{2}}\right)' = \Theta$ . The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \boldsymbol{\Phi}\boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\boldsymbol{\Phi}$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

### Value

Returns an object of class `ctmedeffect` which is a list with the following elements:

**call** Function call.

**args** Function arguments.

**fun** Function used ("Direct").

**output** The direct effect.

### Author(s)

Ivan Jacob Agaloos Pesigan

### References

- Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. doi:[10.2307/271028](https://doi.org/10.2307/271028)
- Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. doi:[10.1080/10705511.2014.973960](https://doi.org/10.1080/10705511.2014.973960)
- Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. doi:[10.1007/s11336021097670](https://doi.org/10.1007/s11336021097670)

### See Also

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [MCPPhi\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

### Examples

```
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
```

```

delta_t <- 1
Direct(
  phi = phi,
  delta_t = delta_t,
  from = "x",
  to = "y",
  med = "m"
)
phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)
Direct(
  phi = phi,
  delta_t = delta_t,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)

```

Indirect

*Indirect Effect of X on Y Through M Over a Specific Time-Interval***Description**

This function computes the indirect effect of the independent variable  $X$  on the dependent variable  $Y$  through mediator variables  $\mathbf{m}$  over a specific time-interval  $\Delta t$  using the first-order stochastic differential equation model's drift matrix  $\Phi$ .

**Usage**

```
Indirect(phi, delta_t, from, to, med)
```

**Arguments**

phi	Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
delta_t	Numeric. Time interval ( $\Delta t$ ).
from	Character string. Name of the independent variable $X$ in phi.
to	Character string. Name of the dependent variable $Y$ in phi.
med	Character vector. Name/s of the mediator variable/s in phi.

### Details

The indirect effect of the independent variable  $X$  on the dependent variable  $Y$  relative to some mediator variables  $\mathbf{m}$  over a specific time-interval  $\Delta t$  is given by

$$\text{Indirect}_{\Delta t} = \exp(\Delta t \Phi)_{i,j} - \exp(\Delta t \mathbf{D}_m \Phi \mathbf{D}_m)_{i,j}$$

where  $\Phi$  denotes the drift matrix,  $\mathbf{D}_m$  a matrix where the off diagonal elements are zeros and the diagonal elements are zero for the index/indices of mediator variables  $\mathbf{m}$  and one otherwise,  $i$  the row index of  $Y$  in  $\Phi$ ,  $j$  the column index of  $X$  in  $\Phi$ , and  $\Delta t$  the time-interval.

#### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \mathbf{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\mathbf{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\mathbf{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\boldsymbol{\Theta}^{\frac{1}{2}}\right) \left(\boldsymbol{\Theta}^{\frac{1}{2}}\right)' = \boldsymbol{\Theta}$ .

The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \Phi \boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\Phi$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

### Value

Returns an object of class `ctmedeffect` which is a list with the following elements:

**call** Function call.

**args** Function arguments.

**fun** Function used ("Indirect").

**output** The indirect effect.

### Author(s)

Ivan Jacob Agaloos Pesigan

## References

- Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. doi:10.2307/271028
- Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. doi:10.1080/10705511.2014.973960
- Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. doi:10.1007/s11336021097670

## See Also

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [MCMed\(\)](#), [MCPhi\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

## Examples

```
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
delta_t <- 1
Indirect(
  phi = phi,
  delta_t = delta_t,
  from = "x",
  to = "y",
  med = "m"
)
phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)
Indirect(
  phi = phi,
  delta_t = delta_t,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)
```

MCMed

*Monte Carlo Sampling Distribution of Total, Direct, and Indirect Effects of  $X$  on  $Y$  Through  $M$  Over a Specific Time-Interval or a Range of Time-Intervals*

## Description

This function generates a Monte Carlo method sampling distribution of the total, direct and indirect effects of the independent variable  $X$  on the dependent variable  $Y$  through mediator variables  $\mathbf{m}$  at a particular time-interval  $\Delta t$  using the first-order stochastic differential equation model drift matrix  $\Phi$ .

## Usage

```
MCMed(
  phi,
  vcov_phi_vec,
  delta_t,
  from,
  to,
  med,
  R,
  test_phi = TRUE,
  ncores = NULL,
  seed = NULL
)
```

## Arguments

phi	Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
vcov_phi_vec	Numeric matrix. The sampling variance-covariance matrix of $\text{vec}(\Phi)$ .
delta_t	Numeric. Time interval ( $\Delta t$ ).
from	Character string. Name of the independent variable $X$ in phi.
to	Character string. Name of the dependent variable $Y$ in phi.
med	Character vector. Name/s of the mediator variable/s in phi.
R	Positive integer. Number of replications.
test_phi	Logical. Check the generated $\Phi$ and generate different values if the test fails. The test includes the following: <ul style="list-style-type: none"> <li>• test that the largest eigen value of <math>\Phi</math> is less than one, and</li> <li>• test that the diagonal values of <math>\Phi</math> are between 0 to negative infinity.</li> </ul>
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when number of replications R is a large value.
seed	Random seed.

## Details

See `Total()`, `Direct()`, and `Indirect()` for more details.

### Monte Carlo Method:

Let  $\boldsymbol{\theta}$  be  $\text{vec}(\boldsymbol{\Phi})$ , that is, the elements of the  $\boldsymbol{\Phi}$  matrix in vector form sorted column-wise. Let  $\hat{\boldsymbol{\theta}}$  be  $\text{vec}(\hat{\boldsymbol{\Phi}})$ . Based on the asymptotic properties of maximum likelihood estimators, we can assume that estimators are normally distributed around the population parameters.

$$\hat{\boldsymbol{\theta}} \sim \mathcal{N}(\boldsymbol{\theta}, \mathbb{V}(\hat{\boldsymbol{\theta}}))$$

Using this distributional assumption, a sampling distribution of  $\hat{\boldsymbol{\theta}}$  which we refer to as  $\hat{\boldsymbol{\theta}}^*$  can be generated by replacing the population parameters with sample estimates, that is,

$$\hat{\boldsymbol{\theta}}^* \sim \mathcal{N}(\hat{\boldsymbol{\theta}}, \hat{\mathbb{V}}(\hat{\boldsymbol{\theta}})).$$

Let  $\mathbf{g}(\hat{\boldsymbol{\theta}})$  be a parameter that is a function of the estimated parameters. A sampling distribution of  $\mathbf{g}(\hat{\boldsymbol{\theta}})$ , which we refer to as  $\mathbf{g}(\hat{\boldsymbol{\theta}}^*)$ , can be generated by using the simulated estimates to calculate  $\mathbf{g}$ . The standard deviations of the simulated estimates are the standard errors. Percentiles corresponding to  $100(1 - \alpha)\%$  are the confidence intervals.

### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \boldsymbol{\Lambda}\boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\boldsymbol{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\boldsymbol{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $(\boldsymbol{\Theta}^{\frac{1}{2}})'(\boldsymbol{\Theta}^{\frac{1}{2}})' = \boldsymbol{\Theta}$ .

The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \boldsymbol{\Phi}\boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\boldsymbol{\Phi}$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

## Value

Returns an object of class `ctmedmc` which is a list with the following elements:



**call** Function call.

**args** Function arguments.

**fun** Function used (MCMed).

**output** A list with length of `length(delta_t)`.

Each element in the output list has the following elements:

**est** A vector of total, direct, and indirect effects.

**thetahatstar** A matrix of Monte Carlo total, direct, and indirect effects.

### Author(s)

Ivan Jacob Agaloos Pesigan

### References

- Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. [doi:10.2307/271028](https://doi.org/10.2307/271028)
- Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. [doi:10.1080/10705511.2014.973960](https://doi.org/10.1080/10705511.2014.973960)
- Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. [doi:10.1007/s11336021097670](https://doi.org/10.1007/s11336021097670)

### See Also

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [Indirect\(\)](#), [MCPHI\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

### Examples

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)

# Range of time-intervals -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
```

```

    delta_t = 1:20,
    from = "x",
    to = "y",
    med = "m",
    R = 5 # use a large value for R in actual research
)

# Methods -----
# MCMed has a number of methods including
# print, summary, confint, and plot
print(mc)
summary(mc)
confint(mc, level = 0.95)
plot(mc)

```

---

MCPhi

---

*Generate Random Drift Matrices Using the Monte Carlo Method*


---

## Description

This function generates random drift matrices  $\Phi$  using the Monte Carlo method.

## Usage

```
MCPhi(phi, vcov_phi_vec, R, test_phi = TRUE, ncores = NULL, seed = NULL)
```

## Arguments

phi	Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
vcov_phi_vec	Numeric matrix. The sampling variance-covariance matrix of $\text{vec}(\Phi)$ .
R	Positive integer. Number of replications.
test_phi	Logical. Check the generated $\Phi$ and generate different values if the test fails. The test includes the following: <ul style="list-style-type: none"> <li>• test that the largest eigen value of <math>\Phi</math> is less than one, and</li> <li>• test that the diagonal values of <math>\Phi</math> are between 0 to negative infinity.</li> </ul>
ncores	Positive integer. Number of cores to use. If ncores = NULL, use a single core. Consider using multiple cores when number of replications R is a large value.
seed	Random seed.

## Details

### Monte Carlo Method:

Let  $\theta$  be  $\text{vec}(\Phi)$ , that is, the elements of the  $\Phi$  matrix in vector form sorted column-wise. Let  $\hat{\theta}$  be  $\text{vec}(\hat{\Phi})$ . Based on the asymptotic properties of maximum likelihood estimators, we can assume that estimators are normally distributed around the population parameters.

$$\hat{\theta} \sim \mathcal{N}(\theta, \mathbb{V}(\hat{\theta}))$$

Using this distributional assumption, a sampling distribution of  $\hat{\theta}$  which we refer to as  $\hat{\theta}^*$  can be generated by replacing the population parameters with sample estimates, that is,

$$\hat{\theta}^* \sim \mathcal{N}(\hat{\theta}, \hat{\mathbb{V}}(\hat{\theta})).$$

### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \mathbf{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\mathbf{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\mathbf{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\boldsymbol{\Theta}^{\frac{1}{2}}\right) \left(\boldsymbol{\Theta}^{\frac{1}{2}}\right)' = \boldsymbol{\Theta}$ . The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \Phi \boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\Phi$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

## Value

Returns a list of simulated drift matrices.

## Author(s)

Ivan Jacob Agaloos Pesigan

## See Also

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

## Examples

```

phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
MCPhi(
  phi = phi,
  vcov_phi_vec = 0.1 * diag(9),
  R = 5
)
phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)
MCPhi(
  phi = phi,
  vcov_phi_vec = 0.1 * diag(16),
  R = 5,
  test_phi = FALSE
)

```

---

Med

---

*Total, Direct, and Indirect Effects of X on Y Through M Over a Specific Time-Interval or a Range of Time-Intervals*


---

## Description

This function computes the total, direct, and indirect effects of the independent variable  $X$  on the dependent variable  $Y$  through mediator variables  $\mathbf{m}$  over a specific time-interval  $\Delta t$  or a range of time-intervals using the first-order stochastic differential equation model's drift matrix  $\Phi$ .

## Usage

```
Med(phi, delta_t, from, to, med)
```

### Arguments

phi	Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
delta_t	Vector of positive numbers. Time interval ( $\Delta t$ ).
from	Character string. Name of the independent variable $X$ in phi.
to	Character string. Name of the dependent variable $Y$ in phi.
med	Character vector. Name/s of the mediator variable/s in phi.

### Details

See [Total\(\)](#), [Direct\(\)](#), and [Indirect\(\)](#) for more details.

#### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \mathbf{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\mathbf{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\mathbf{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\boldsymbol{\Theta}^{\frac{1}{2}}\right) \left(\boldsymbol{\Theta}^{\frac{1}{2}}\right)' = \boldsymbol{\Theta}$ .

The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \boldsymbol{\Phi} \boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\boldsymbol{\Phi}$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

### Value

Returns an object of class `ctmedmed` which is a list with the following elements:

**call** Function call.

**args** Function arguments.

**fun** Function used (Med).

**output** A matrix of total, direct, and indirect effects.

### Author(s)

Ivan Jacob Agaloos Pesigan

## References

- Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. doi:10.2307/271028
- Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. doi:10.1080/10705511.2014.973960
- Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. doi:10.1007/s11336021097670

## See Also

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [MCPhi\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

## Examples

```
# -----
# Example 1 -----
# -----
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")

# Specific time-interval -----
Med(
  phi = phi,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)

# Range of time-intervals -----
med <- Med(
  phi = phi,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
plot(med)

# -----
# Example 2 -----
# -----
```

```

phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)

# Specific time-interval -----
Med(
  phi = phi,
  delta_t = 1,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)

# Range of time-intervals -----
med <- Med(
  phi = phi,
  delta_t = seq(from = 0, to = 5, length.out = 500),
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)

# Methods -----
# Med has a number of methods including
# print, summary, and plot
print(med)
summary(med)
plot(med)

```

---

plot.ctmeddelta

---

*Plot Method for an Object of Class ctmeddelta*


---

## Description

Plot Method for an Object of Class ctmeddelta

## Usage

```

## S3 method for class 'ctmeddelta'
plot(x, alpha = 0.05, ...)

```

**Arguments**

x	Object of class ctmeddelta.
alpha	Numeric. Significance level
...	Additional arguments.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Range of time-intervals -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
plot(delta)
```

---

plot.ctmedmc

---

*Plot Method for an Object of Class ctmedmc*


---

**Description**

Plot Method for an Object of Class ctmedmc

**Usage**

```
## S3 method for class 'ctmedmc'
plot(x, alpha = 0.05, ...)
```

**Arguments**

x	Object of class ctmedmc.
alpha	Numeric. Significance level
...	Additional arguments.

**Author(s)**

Ivan Jacob Agaloos Pesigan



**Examples**

```

data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Range of time-intervals -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
plot(mc)

```

plot.ctmedmed

*Plot Method for an Object of Class ctmedmed***Description**

Plot Method for an Object of Class ctmedmed

**Usage**

```

## S3 method for class 'ctmedmed'
plot(x, ...)

```

**Arguments**

```

x          Object of class ctmedmed.
...        Additional arguments.

```

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```

# -----
# Example 1 -----
# -----
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  )

```

```

    ),
    nrow = 3
  )
  colnames(phi) <- rownames(phi) <- c("x", "m", "y")

  # Range of time-intervals -----
  med <- Med(
    phi = phi,
    delta_t = 1:20,
    from = "x",
    to = "y",
    med = "m"
  )
  plot(med)

  # -----
  # Example 2 -----
  # -----
  phi <- matrix(
    data = c(
      -6, 5.5, 0, 0,
      1.25, -2.5, 5.9, -7.3,
      0, 0, -6, 2.5,
      5, 0, 0, -6
    ),
    nrow = 4
  )
  colnames(phi) <- rownames(phi) <- paste0("y", 1:4)

  # Range of time-intervals -----
  med <- Med(
    phi = phi,
    delta_t = seq(from = 0, to = 5, length.out = 500),
    from = "y2",
    to = "y4",
    med = c("y1", "y3")
  )
  plot(med)

```

---

PosteriorMed

---

*Posterior Distribution of Total, Direct, and Indirect Effects of X on Y  
Through M Over a Specific Time-Interval*


---

## Description

This function generates a posterior distribution of the total, direct and indirect effects of the independent variable  $X$  on the dependent variable  $Y$  through mediator variables  $\mathbf{m}$  at a particular time-interval  $\Delta t$  using the posterior distribution of the first-order stochastic differential equation model drift matrix  $\Phi$ .

**Usage**

```
PosteriorMed(phi, delta_t, from, to, med, ncores = NULL)
```

**Arguments**

<code>phi</code>	List of numeric matrices. Each element of the list is a sample from the posterior distribution of the drift matrix ( $\Phi$ ). Each matrix should have row and column names pertaining to the variables in the system.
<code>delta_t</code>	Numeric. Time interval ( $\Delta t$ ).
<code>from</code>	Character string. Name of the independent variable $X$ in <code>phi</code> .
<code>to</code>	Character string. Name of the dependent variable $Y$ in <code>phi</code> .
<code>med</code>	Character vector. Name/s of the mediator variable/s in <code>phi</code> .
<code>ncores</code>	Positive integer. Number of cores to use. If <code>ncores = NULL</code> , use a single core. Consider using multiple cores when number of replications $R$ is a large value.

**Details**

See [Total\(\)](#), [Direct\(\)](#), and [Indirect\(\)](#) for more details.

**Value**

Returns an object of class `ctmedmc` which is a list with the following elements:

**call** Function call.

**args** Function arguments.

**fun** Function used (`PosteriorMed`).

**output** A list with length of `length(delta_t)`.

Each element in the output list has the following elements:

**est** Mean of the posterior distribution of the total, direct, and indirect effects.

**thetahatstar** Posterior distribution of the total, direct, and indirect effects.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**References**

- Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. [doi:10.2307/271028](#)
- Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. [doi:10.1080/10705511.2014.973960](#)
- Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. [doi:10.1007/s11336021097670](#)

**See Also**

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [MCPPhi\(\)](#), [Med\(\)](#), [TestPhi\(\)](#), [Total\(\)](#)

**Examples**

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$ctsem$posterior_phi

# Specific time-interval -----
PosteriorMed(
  phi = phi,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)

# Range of time-intervals -----
posterior <- PosteriorMed(
  phi = phi,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)

# Methods -----
# PosteriorMed has a number of methods including
# print, summary, confint, and plot
print(posterior)
summary(posterior)
confint(posterior, level = 0.95)
plot(posterior)
```

---

print.ctmeddelta	<i>Print Method for Object of Class ctmeddelta</i>
------------------	--

---

**Description**

Print Method for Object of Class ctmeddelta

**Usage**

```
## S3 method for class 'ctmeddelta'
print(x, alpha = 0.05, digits = 4, ...)
```

**Arguments**

<code>x</code>	an object of class <code>ctmeddelta</code> .
<code>alpha</code>	Numeric vector. Significance level $\alpha$ .
<code>digits</code>	Integer indicating the number of decimal places to display.
<code>...</code>	further arguments.

**Value**

Returns a matrix of time-interval, estimates, standard errors, test statistics, p-values, and confidence intervals.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)
print(delta)

# Range of time-intervals -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
print(delta)
```

---

print.ctmedeffect	<i>Print Method for Object of Class ctmedeffect</i>
-------------------	---

---

**Description**

Print Method for Object of Class ctmedeffect

**Usage**

```
## S3 method for class 'ctmedeffect'
print(x, digits = 4, ...)
```

**Arguments**

x	an object of class ctmedeffect.
digits	Integer indicating the number of decimal places to display.
...	further arguments.

**Value**

Returns the effects.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
delta_t <- 1

# Time-Interval of One -----

## Total Effect -----
total_dt <- Total(
  phi = phi,
  delta_t = delta_t
)
print(total_dt)

## Direct Effect -----
```

```

direct_dt <- Direct(
  phi = phi,
  delta_t = delta_t,
  from = "x",
  to = "y",
  med = "m"
)
print(direct_dt)

## Indirect Effect -----
indirect_dt <- Indirect(
  phi = phi,
  delta_t = delta_t,
  from = "x",
  to = "y",
  med = "m"
)
print(indirect_dt)

```

---

print.ctmedmc	<i>Print Method for Object of Class ctmedmc</i>
---------------	---

---

## Description

Print Method for Object of Class ctmedmc

## Usage

```

## S3 method for class 'ctmedmc'
print(x, alpha = 0.05, digits = 4, ...)

```

## Arguments

x	an object of class ctmedmc.
alpha	Numeric vector. Significance level $\alpha$ .
digits	Integer indicating the number of decimal places to display.
...	further arguments.

## Value

Returns a matrix of estimates, standard errors, number of Monte Carlo replications, and confidence intervals.

## Author(s)

Ivan Jacob Agaloos Pesigan

**Examples**

```

data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
print(mc)

# Range of time-intervals -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
print(mc)

```

---

print.ctmedmcphi	<i>Print Method for Object of Class ctmedmcphi</i>
------------------	--

---

**Description**

Print Method for Object of Class ctmedmcphi

**Usage**

```

## S3 method for class 'ctmedmcphi'
print(x, digits = 4, ...)

```

**Arguments**

x	an object of class ctmedmcphi.
digits	Integer indicating the number of decimal places to display.
...	further arguments.



**Value**

Returns the structure of the output.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
mc <- MCPHi(
  phi = phi,
  vcov_phi_vec = 0.1 * diag(9),
  R = 5
)
print(mc)
```

---

print.ctmedmed

---

*Print Method for Object of Class ctmedmed*


---

**Description**

Print Method for Object of Class ctmedmed

**Usage**

```
## S3 method for class 'ctmedmed'
print(x, digits = 4, ...)
```

**Arguments**

x	an object of class ctmedmed.
digits	Integer indicating the number of decimal places to display.
...	further arguments.

**Value**

Returns a matrix of effects.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```

# -----
# Example 1 -----
# -----
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")

# Specific time-interval -----
med <- Med(
  phi = phi,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)
print(med)

# Range of time-intervals -----
med <- Med(
  phi = phi,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
print(med)

# -----
# Example 2 -----
# -----
phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)

```

```

# Specific time-interval -----
med <- Med(
  phi = phi,
  delta_t = 1,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)
print(med)

# Range of time-intervals -----
med <- Med(
  phi = phi,
  delta_t = 1:10,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)
print(med)

```

---

summary.ctmeddelta	<i>Summary Method for an Object of Class ctmeddelta</i>
--------------------	---

---

## Description

Summary Method for an Object of Class ctmeddelta

## Usage

```
## S3 method for class 'ctmeddelta'
summary(object, alpha = 0.05, ...)
```

## Arguments

object	Object of class ctmeddelta.
alpha	Numeric vector. Significance level $\alpha$ .
...	additional arguments.

## Value

Returns a matrix of effects, time-interval, estimates, standard errors, test statistics, p-values, and confidence intervals.

## Author(s)

Ivan Jacob Agaloos Pesigan

## Examples

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)
summary(delta)

# Range of time-intervals -----
delta <- DeltaMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
summary(delta)
```

---

summary.ctmedmc

*Summary Method for an Object of Class ctmedmc*


---

## Description

Summary Method for an Object of Class ctmedmc

## Usage

```
## S3 method for class 'ctmedmc'
summary(object, alpha = 0.05, ...)
```

## Arguments

object	Object of class ctmedmc.
alpha	Numeric vector. Significance level $\alpha$ .
...	additional arguments.

## Value

Returns a matrix of effects, time-interval, estimates, standard errors, test statistics, p-values, and confidence intervals.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```
data("deboeck2015phi", package = "cTMed")
phi <- deboeck2015phi$dynr$phi
vcov_phi_vec <- deboeck2015phi$dynr$vcov

# Specific time-interval -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
summary(mc)

# Range of time-intervals -----
mc <- MCMed(
  phi = phi,
  vcov_phi_vec = vcov_phi_vec,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m",
  R = 5 # use a large value for R in actual research
)
summary(mc)
```

---

summary.ctmedmed

*Summary Method for an Object of Class ctmedmed*


---

**Description**

Summary Method for an Object of Class ctmedmed

**Usage**

```
## S3 method for class 'ctmedmed'
summary(object, digits = 4, ...)
```

**Arguments**

object            an object of class ctmedmed.  
 digits           Integer indicating the number of decimal places to display.  
 ...              further arguments.

**Value**

Returns a matrix of effects.

**Author(s)**

Ivan Jacob Agaloos Pesigan

**Examples**

```
# -----
# Example 1 -----
# -----
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")

# Specific time-interval -----
med <- Med(
  phi = phi,
  delta_t = 1,
  from = "x",
  to = "y",
  med = "m"
)
summary(med)

# Range of time-intervals -----
med <- Med(
  phi = phi,
  delta_t = 1:20,
  from = "x",
  to = "y",
  med = "m"
)
summary(med)

# -----
# Example 2 -----
# -----
```

```

phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)

# Specific time-interval -----
med <- Med(
  phi = phi,
  delta_t = 1,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)
summary(med)

# Range of time-intervals -----
med <- Med(
  phi = phi,
  delta_t = 1:10,
  from = "y2",
  to = "y4",
  med = c("y1", "y3")
)
summary(med)

```

---

TestPhi

*Test the Drift Matrix*


---

## Description

Both have to be true for the function to return TRUE.

- Test that the largest eigen value of  $\Phi$  is less than one.
- Test that the diagonal values of  $\Phi$  are between 0 to negative infinity.

## Usage

```
TestPhi(phi)
```

## Arguments

phi                      Numeric matrix. The drift matrix ( $\Phi$ ).

Author(s)

Ivan Jacob Agaloos Pesigan

See Also

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [MCPhi\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [Total\(\)](#)

Examples

```
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
TestPhi(phi = phi)
phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)
TestPhi(phi = phi)
```

---

Total	<i>Total Effect Matrix Over a Specific Time-Interval</i>
-------	--

---

Description

This function computes the total effects matrix over a specific time-interval  $\Delta t$  using the first-order stochastic differential equation model's drift matrix  $\Phi$ .

Usage

```
Total(phi, delta_t)
```

Arguments

- phi                    Numeric matrix. The drift matrix ( $\Phi$ ). phi should have row and column names pertaining to the variables in the system.
- delta\_t                Numeric. Time interval ( $\Delta t$ ).



## Details

The total effect matrix over a specific time-interval  $\Delta t$  is given by

$$\text{Total}_{\Delta t} = \exp(\Delta t \Phi)$$

where  $\Phi$  denotes the drift matrix, and  $\Delta t$  the time-interval.

### Linear Stochastic Differential Equation Model:

The measurement model is given by

$$\mathbf{y}_{i,t} = \boldsymbol{\nu} + \mathbf{\Lambda} \boldsymbol{\eta}_{i,t} + \boldsymbol{\varepsilon}_{i,t}, \quad \text{with} \quad \boldsymbol{\varepsilon}_{i,t} \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Theta})$$

where  $\mathbf{y}_{i,t}$ ,  $\boldsymbol{\eta}_{i,t}$ , and  $\boldsymbol{\varepsilon}_{i,t}$  are random variables and  $\boldsymbol{\nu}$ ,  $\mathbf{\Lambda}$ , and  $\boldsymbol{\Theta}$  are model parameters.  $\mathbf{y}_{i,t}$  represents a vector of observed random variables,  $\boldsymbol{\eta}_{i,t}$  a vector of latent random variables, and  $\boldsymbol{\varepsilon}_{i,t}$  a vector of random measurement errors, at time  $t$  and individual  $i$ .  $\boldsymbol{\nu}$  denotes a vector of intercepts,  $\mathbf{\Lambda}$  a matrix of factor loadings, and  $\boldsymbol{\Theta}$  the covariance matrix of  $\boldsymbol{\varepsilon}$ .

An alternative representation of the measurement error is given by

$$\boldsymbol{\varepsilon}_{i,t} = \boldsymbol{\Theta}^{\frac{1}{2}} \mathbf{z}_{i,t}, \quad \text{with} \quad \mathbf{z}_{i,t} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

where  $\mathbf{z}_{i,t}$  is a vector of independent standard normal random variables and  $\left(\boldsymbol{\Theta}^{\frac{1}{2}}\right) \left(\boldsymbol{\Theta}^{\frac{1}{2}}\right)' = \boldsymbol{\Theta}$ .

The dynamic structure is given by

$$d\boldsymbol{\eta}_{i,t} = (\boldsymbol{\iota} + \Phi \boldsymbol{\eta}_{i,t}) dt + \boldsymbol{\Sigma}^{\frac{1}{2}} d\mathbf{W}_{i,t}$$

where  $\boldsymbol{\iota}$  is a term which is unobserved and constant over time,  $\Phi$  is the drift matrix which represents the rate of change of the solution in the absence of any random fluctuations,  $\boldsymbol{\Sigma}$  is the matrix of volatility or randomness in the process, and  $d\mathbf{W}$  is a Wiener process or Brownian motion, which represents random fluctuations.

## Value

Returns an object of class `ctmedeffect` which is a list with the following elements:

**call** Function call.

**args** Function arguments.

**fun** Function used ("Total").

**output** The matrix of total effects.

## Author(s)

Ivan Jacob Agaloos Pesigan

## References

- Bollen, K. A. (1987). Total, direct, and indirect effects in structural equation models. *Sociological Methodology*, 17, 37. [doi:10.2307/271028](https://doi.org/10.2307/271028)
- Deboeck, P. R., & Preacher, K. J. (2015). No need to be discrete: A method for continuous time mediation analysis. *Structural Equation Modeling: A Multidisciplinary Journal*, 23 (1), 61–75. [doi:10.1080/10705511.2014.973960](https://doi.org/10.1080/10705511.2014.973960)
- Ryan, O., & Hamaker, E. L. (2021). Time to intervene: A continuous-time approach to network analysis and centrality. *Psychometrika*, 87 (1), 214–252. [doi:10.1007/s11336021097670](https://doi.org/10.1007/s11336021097670)

**See Also**

Other Continuous Time Mediation Functions: [DeltaMed\(\)](#), [Direct\(\)](#), [Indirect\(\)](#), [MCMed\(\)](#), [MCPPhi\(\)](#), [Med\(\)](#), [PosteriorMed\(\)](#), [TestPhi\(\)](#)

**Examples**

```
phi <- matrix(
  data = c(
    -0.357, 0.771, -0.450,
    0.0, -0.511, 0.729,
    0, 0, -0.693
  ),
  nrow = 3
)
colnames(phi) <- rownames(phi) <- c("x", "m", "y")
delta_t <- 1
Total(
  phi = phi,
  delta_t = delta_t
)
phi <- matrix(
  data = c(
    -6, 5.5, 0, 0,
    1.25, -2.5, 5.9, -7.3,
    0, 0, -6, 2.5,
    5, 0, 0, -6
  ),
  nrow = 4
)
colnames(phi) <- rownames(phi) <- paste0("y", 1:4)
Total(
  phi = phi,
  delta_t = delta_t
)
```

# Index

## \* Continuous Time Mediation Functions

- DeltaMed, [7](#)
- Direct, [10](#)
- Indirect, [12](#)
- MCMed, [15](#)
- MCPhi, [18](#)
- Med, [20](#)
- PosteriorMed, [26](#)
- TestPhi, [39](#)
- Total, [40](#)

## \* cTMed

- DeltaMed, [7](#)
- Direct, [10](#)
- Indirect, [12](#)
- MCMed, [15](#)
- MCPhi, [18](#)
- Med, [20](#)
- PosteriorMed, [26](#)
- TestPhi, [39](#)
- Total, [40](#)

## \* data

- deboeck2015, [4](#)
- deboeck2015phi, [6](#)

## \* effects

- Direct, [10](#)
- Indirect, [12](#)
- Med, [20](#)
- Total, [40](#)

## \* main

- DeltaMed, [7](#)
- MCMed, [15](#)
- Med, [20](#)

## \* methods

- confint.ctmeddelta, [2](#)
- confint.ctmedmc, [3](#)
- plot.ctmeddelta, [23](#)
- plot.ctmedmc, [24](#)
- plot.ctmedmed, [25](#)
- print.ctmeddelta, [28](#)

- print.ctmedeffect, [30](#)
- print.ctmedmc, [31](#)
- print.ctmedmcphi, [32](#)
- print.ctmedmed, [33](#)
- summary.ctmeddelta, [35](#)
- summary.ctmedmc, [36](#)
- summary.ctmedmed, [37](#)

## \* test

- TestPhi, [39](#)

## \* uncertainty

- DeltaMed, [7](#)
- MCMed, [15](#)
- MCPhi, [18](#)
- PosteriorMed, [26](#)

- confint.ctmeddelta, [2](#)

- confint.ctmedmc, [3](#)

- deboeck2015, [4](#)

- deboeck2015phi, [6](#)

- DeltaMed, [7](#), [11](#), [14](#), [17](#), [19](#), [22](#), [28](#), [40](#), [42](#)

- Direct, [9](#), [10](#), [14](#), [17](#), [19](#), [22](#), [28](#), [40](#), [42](#)

- Direct(), [7](#), [16](#), [21](#), [27](#)

- Indirect, [9](#), [11](#), [12](#), [17](#), [19](#), [22](#), [28](#), [40](#), [42](#)

- Indirect(), [7](#), [16](#), [21](#), [27](#)

- MCMed, [9](#), [11](#), [14](#), [15](#), [19](#), [22](#), [28](#), [40](#), [42](#)

- MCPhi, [9](#), [11](#), [14](#), [17](#), [18](#), [22](#), [28](#), [40](#), [42](#)

- Med, [9](#), [11](#), [14](#), [17](#), [19](#), [20](#), [28](#), [40](#), [42](#)

- plot.ctmeddelta, [23](#)

- plot.ctmedmc, [24](#)

- plot.ctmedmed, [25](#)

- PosteriorMed, [9](#), [11](#), [14](#), [17](#), [19](#), [22](#), [26](#), [40](#), [42](#)

- print.ctmeddelta, [28](#)

- print.ctmedeffect, [30](#)

- print.ctmedmc, [31](#)

- print.ctmedmcphi, [32](#)

- print.ctmedmed, [33](#)

`simStateSpace::SimSSMVARFixed()`, [4](#)  
`summary.ctmeddelta`, [35](#)  
`summary.ctmedmc`, [36](#)  
`summary.ctmedmed`, [37](#)  
  
`TestPhi`, [9](#), [11](#), [14](#), [17](#), [19](#), [22](#), [28](#), [39](#), [42](#)  
`Total`, [9](#), [11](#), [14](#), [17](#), [19](#), [22](#), [28](#), [40](#), [40](#)  
`Total()`, [7](#), [16](#), [21](#), [27](#)