

# Multi-Stage Ensemble and Feature Engineering for MOOC Dropout Prediction

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## ABSTRACT

In this paper, we present the winning solution of KDD Cup 2015, where participants are asked to predict dropouts in a Massive Open Online Course (MOOC) platform. Our approach demonstrates best practices in feature engineering dealing with complex real world data, and pushes forward state-of-the-art for ensemble methods. We began with feature engineering. We extracted the hand-crafted and autoencoder features from raw student activity logs, course enrollment, and course material data. Then, we trained 64 classifiers with 8 different algorithms and different subsets of extracted features. Lastly, we blended predictions of classifiers with the multi-stage ensemble framework. Our final solution achieved AUC scores of 0.90918 and 0.90744 on the public and private leaderboards respectively, and put us to the 1st place out of 821 teams.

## CCS Concepts

•Computing methodologies → Supervised learning by classification; Ensemble methods; *Cross-validation*;

## Keywords

KDD Cup, Feature Engineering, Ensemble Learning

## 1. INTRODUCTION

Since 1997, KDD Cup has been one of the most prestigious competitions in knowledge discovery and data mining, where experts around the world from both industry and academia compete with each other with best modeling practices to solve real world challenges in complex data sets.

The task of KDD Cup 2015 was to predict dropouts of students in a Massive Open Online Course (MOOC) platform. MOOC platforms aim at providing the mass population with open access to quality education. Despite of

their initial success in some courses, MOOC platforms have struggled with extremely high dropout rates. Perna et al. reported that the average completion rate is 4% among 1 million students across 16 Coursera courses offered by the University of Pennsylvania from June 2012 to June 2013 [17]. If we identify those who are likely to drop out, we can engage with and help them complete courses successfully. For this task, XuetangX, one of the largest MOOC platforms in China provides the student activity logs, course enrollment, and course material data.

Student dropout in MOOC can be viewed as customer churn, which is a prevailing problem in publishing, financial services, insurance, electric utilities, health care, banking, Internet, telephone, and cable service industries [14]. There are previous competitions related to churn prediction. The task of Teradata Center for CRM (TCC)-Duke Competition was to predict churn with 171 variables provided by a major wireless telecommunication company [14]. The winning solution of TCC-Duke Competition was the ensemble of TreeNet (or MART [7]) models [1]. The task of KDD Cup 2009 was to predict churn, appetency and up-selling with 15,000 variables provided by the French telecommunication company Orange [8]. The winning solution of KDD Cup 2009 was the ensemble of single models trained with 10 base algorithms [15].

Both competitions focused on predictive modeling rather than feature engineering by providing preprocessed variables instead of raw data as in KDD Cup 2015. However, in practice, feature engineering is inevitable and crucial in predictive modeling. For example, Morik and Köpcke showed significant improvements in churn prediction performance of 4 different algorithms when time intervals for the states of variables are added to original variables [13]. Furthermore, winning solutions of both competitions used simple ensemble methods: an average of single model predictions at TCC-Duke Competition [1] and ensemble selection [3], which averages single model predictions with stepwise greedy forward selection, at KDD Cup 2009 [15].

Our final solution is a joint work from 9 data scientists, distributed around the world. The pipeline from raw data to final solution is as follows:

- Feature engineering - both hand crafted and automated.
- Single model training with feature sets.
- Stage-1 ensemble with single model predictions.

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KDD '16 August 13–17, 2016, San Francisco, CA, USA

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DOI: 10.1145/1235

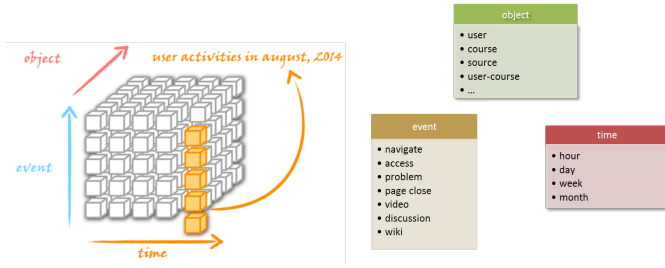


Figure 1: Data cube.

- Stage-2 ensemble with stage-1 ensemble model predictions.
- Stage-3 ensemble with all model predictions.

The rest of the paper is organized as follows. Section 2 describes our feature engineering approach. Section 3 introduces various classification algorithms used. Section 4 presents our multi-stage ensemble framework. Section 5 shows our final solution. Section 6 concludes the paper.

## 2. FEATURE ENGINEERING

Our team members extracted 7 feature sets, namely F1, F2, F3, F4, F5, F6, and F7 from raw data independently.

### 2.1 Data Sets

Activity logs of 200,906 enrollments from 112,448 students across 39 courses are provided. Each activity is described by 6 fields of the username, course ID, timestamp, source, event, and object. For each object, 3 additional fields of the category, children, and start date are provided. The training set consists of 8,157,278 logs from 120,543 enrollments with the target variable indicating if a student dropped out. The test set consists of 5,387,848 logs from 80,363 enrollments. The full description of the data sets is available in [2]. In general, this data can be organized in 3 dimensional space of object, time, and event as shown in Figure 1. Feature engineering tasks were carried out based on these views.

### 2.2 Common Features

There are common features across 7 feature sets, F1 through F7 as follows:

- Number of objects
- Number of events
- Aggregation features of features above

The common features can be generated using cube operations. Figure 2 shows an example how weekly and monthly count features are calculated. First, the data is cut along with the object dimension. In this case, we choose to generate feature for users. Next, we select an event "navigate" in the event space to generate a time series presenting "navigate" event over the time. Finally, the drill-down operation is used to generate monthly or weekly count features.

### 2.3 F1

The feature set F1 is generated by Chen and Ozaki and includes features as follows:

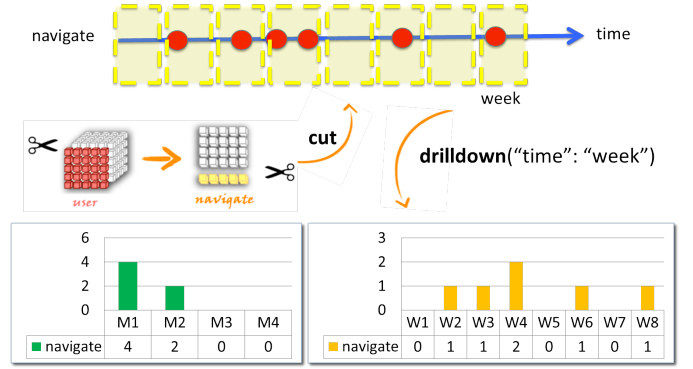


Figure 2: Data slice and dice.

- Enrollment-based features
- Username-based features
- Username-based features for each courses
- Features based on 10 days after the end date of course
- Features based on 1 day after the end date of a course
- Day-level features

Table A1 in Appendix shows the full list of features in F1.

### 2.4 F2

The feature set F2 is generated by Yan and Zhou and includes features as follows:

- Visit time(hour, day) set features (including time span and max absent days)
- Act(event, object) counting features (some uses missed content counts)
- Course drop rate
- Number of courses the user enrolled
- Minimum time interval between time points(first visit, last visit, course begin, course end, 10 days after course end) of current course and another enrolled course
- Active days between course end and 10 days after course end
- Active days between last visit and course end
- Number of courses ended after current course end

Table A2 in Appendix shows the full list of features in F2.

### 2.5 F3

The feature set F3 is generated by Nguyen, and are categorized into 3 groups of the count, aggregation, and date features.

#### 2.5.1 Count Features

There are a few entities such as user, course, and object in the training dataset. Combining these entities together, we have user activities or events. The simplest way to generate features from these events is to count the number of times an entity engaging in the event. The motivation is that the more a user participate in course, the less likely she drop out the course. Table 1 shows the list of count features in F3.

**Table 1: List of count features in F3.**

No.	Description
1	The log count of each user
2	The log count of each course
3	The log count of each event
4	The log count of each user per week
5	The log count of each user per two weeks
6	The log count of each user per weekday
7	The log count of each user per month
8	The log count of each course per week
9	The log count of each course per two weeks
10	The log count of each course per weekday
11	The log count of each course per month
12	The log count of each event per week
13	The log count of each event per two weeks
14	The log count of each event per weekday
15	The log count of each event per month

### 2.5.2 Aggregation Features

Aggregation features are calculated based on count features. Usually, each course would have a fixed schedule for users to study. Therefore, students enrolled in the course must have consistent activity patterns. Aggregation features would measure the stability of course engagement. These features are minimum, mean, median, maximum, and standard deviation of count features on date basis such as weekly, monthly, etc.

### 2.5.3 Date Features

To capture how often users participate in a certain course, we generated date features. Date features can be time span among user activities as well as time span from last activity and last course date.

## 2.6 F4

The feature set F4 is generated by Jahrer, and includes features as follows:

- User ID
- Course ID
- User ID count
- Enrollment ID count
- Enrollment ID  $\rightarrow$  Source ID count
- Enrollment ID  $\rightarrow$  Event ID
- Enrollment ID  $\rightarrow$  Object ID count
- Enrollment ID  $\rightarrow$  Timestamp count
- User ID:  $\text{floor}(\log(\text{timespan}^2 + 1))$
- User ID  $\rightarrow \log(\text{timespan} \text{ to obj start} + 1)$
- Enrollment ID  $\rightarrow$  timespan statistics

## 2.7 F5

The feature set F5 is generated by Bay, and includes features as follows:

- Course ID - One-hot-encoded course\_id
- Source time counts by enrollment - The log count of each source type per day for each enrollment
- Source time counts by course id - The log count of each source type per day for each course id

- Event time counts by enrollment - The log count of each event type per day for each enrollment
- Event time counts by course id - The log count of each event type per day for each course id

## 2.8 F6

The feature set F6 is generated by Lee, and includes features as follows:

- User ID - One-hot-encoded username. Usernames appearing less than 100 times in training log data are grouped together as one user ID.
- Course ID - One-hot-encoded course\_id.
- Source Event - One-hot-encoded combination of source and event.
- Object ID - One-hot-encoded object. Objects appearing less than 100 times in training log data are grouped together as one object ID.
- Count - Number of log entries for an hour\_id.
- Object Category - Number of log entries with an object category for an enrollment\_id.
- Number of Children Objects - One-hot-encoded total number of object's children for an enrollment\_id.
- Object Timespan - One-hot-encoded timespan in days between object's start date and last day of the class
- Day of Class - One-hot-encoded day of the class
- Week of Class - One-hot-encoded week of the class
- End Month of Class - One-hot-encoded end month of the class
- Object Started in Dropout Period - Binary variable that is 1 if object started after but before 10 days after last day of the class and 0 otherwise.

## 2.9 F7

The feature set F7 is generated by Ozaki, and encodes target variables for each days. By adding F7 features, the best CV and public leaderboard score of our single model improved by 0.000846 and 0.001404 respectively.

- For 10 days after the end date of each course, number of active enrollment\_id, which target variables are 1 in the training set, enrolled by a username.
- For 10 days after the end date of each course, number of active enrollment\_id, which target variables are 0 in the training set, enrolled by a username.
- For 10 days after the end date of each course, number of active enrollment\_id (in this case, days between last access and the end date of the course are also counted for active days), which target variables are 1 in the training set, enrolled by a username.
- For 10 days after the end date of each course, number of active enrollment\_id (in this case, days between last access and the end date of the course are also counted for active days), which target variables are 0 in the training set, enrolled by a username.
- For 14 days before the end date of each course, number of active enrollment\_id, which target variables are 1 in the training set, enrolled by a username.

- For 14 days before the end date of each course, number of active enrollment\_id, which target variables are 0 in the training set, enrolled by a username.
- For 14 days before the end date of each course, number of active enrollment\_id (in this case, days between last access and the end date of the course are also counted for active days), which target variables are 1 in the training set, enrolled by a username.
- For 14 days before the end date of each course, number of active enrollment\_id (in this case, days between last access and the end date of the course are also counted for active days), which target variables are 0 in the training set, enrolled by a username.

## 2.10 Denoising Autoencoder Features

We generate denoising autoencoder (DAE) [9] features from feature sets above and use those as additional features. We experiment with two autoencoder networks:

- **Deep Stack** [21]: It is an architecture with input- $x$ - $x$ -input, where  $x = 1,000$  for example. The resulting feature dimensionality is  $3 \times x$ . We extract outputs from all layers as new features.
- **Bottleneck** [19]: It is an architecture with one layer with significantly fewer neurons such as input-1000-1000-30-1000-1000-input for example, which results in 30 features.

Both variants are trained with stochastic mini-batch SGD on the original training and test feature set. We use the rectified linear unit (ReLU) [6] transfer function in hidden layers and the linear function in the output and bottleneck layers.

## 3. CLASSIFICATION ALGORITHMS

We selected algorithms that achieve good predictive performance, process large sparse data sets efficiently (with exception of K-Nearest Neighbors) and differ from other algorithms. The 8 classification algorithms selected are as follows:

- **Gradient Boosting Machine (GBM)**: We trained GBM classifiers using the Scikit-Learn Python package [16] and XGBoost [5]. We used various tree structures of 4 to 10 maximum depths and 0.004 to 0.05 shrinkage rates.
- **Neural Networks (NN)**: We trained NN classifiers with the dropout [20], ReLU transfer function and sigmoid activation function. We used various network architectures of 1 to 3 hidden layers and 16 to 500 hidden units per layer. We wrote our own C++ NN implementation optimized for sparse data sets.
- **Factorization Machine (FM)**: We trained FM classifiers using libFM [18] and libFFM [11]. We used 2-way interaction dimensions of 4 to 20. We transformed count variables  $x$  into  $\log(1 + x)$ .
- **Logistic Regression (LR)**: We trained LR classifiers using the Scikit-Learn Python package [16] and Vowpal Wabbit [12]. We used the regularization parameter  $C = 0.01$ . We transformed count variables  $x$  into  $\log(1 + x)$ .

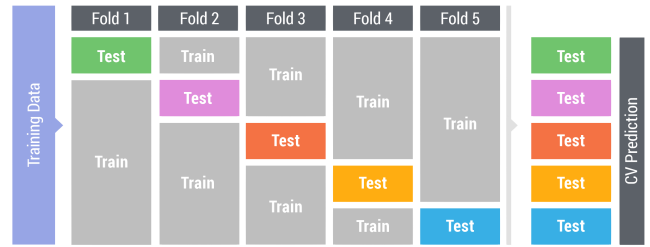


Figure 3: 5-fold CV.

- **Kernel Ridge Regression (KRR)**: We trained KRR classifiers using our own C++ implementation. We used the ridge regression constant  $\lambda = 1.5e - 3$  with the Gaussian kernel. We transformed count variables  $x$  into  $\log(1 + x)$ .
- **Extremely Randomized Trees (ET)**: We trained ET classifiers using the Scikit-Learn Python package [16].
- **Random Forests (RF)**: We trained RF classifiers using the Scikit-Learn Python package [16]. Besides training classifiers, we used RF for feature selection. We trained an RF model and selected features with high variable importance.
- **K-Nearest Neighbors (KNN)**: We trained KNN classifiers using our own C++ implementation. We used  $k = 124$  with the Euclidean distance. We transformed count variables  $x$  into  $\log(1 + x)$ .

## 4. LEARNING FRAMEWORK

At previous KDD Cups, winning solutions either combined only single models without further combining ensemble models [8, 24, 10] or combined ensemble models based on public leaderboard scores, which are not available in practice [4, 23].

However, we were able to combine ensemble models in multiple stages without overfitting to training data or using public leaderboard scores by using our learning framework. Our learning framework consists of the stratified cross validation (CV) and multi-stage ensemble.

### 4.1 Model Validation

We used stratified 5-fold CV for model validation and ensemble. As shown in Figure 3, training data were split into 5 folds while the sample size and dropout rate were preserved across the folds.

For validation, each of single and ensemble models was trained 5 times. Each time, 1 fold was held out and the remaining 4 folds were used for training. Then, predictions for the hold-out folds were combined and formed the model's CV prediction. CV predictions were used as inputs for ensemble model training as well as the model's CV score calculation.

For test, each of single and ensemble models was retrained with whole training data. Then predictions for test data were used as inputs for ensemble prediction as well as for submission.

### 4.2 Multi-Stage Ensemble

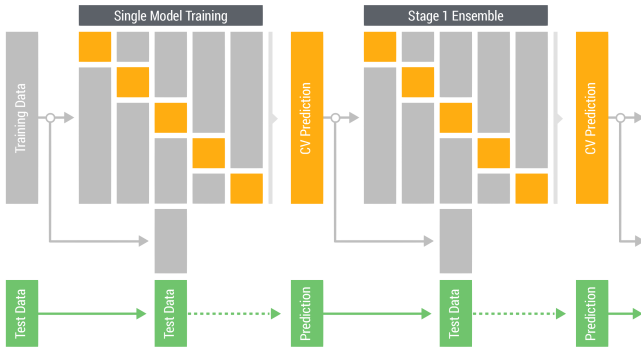


Figure 4: 5-fold CV stacked generalization ensemble.

We used the multi-stage ensemble with stacked generalization [22] to blend predictions of various models. At each stage, we train ensemble models with 5-fold CV, and use the CV and test predictions of models in the previous stage as inputs. Then, we pass the CV and test predictions of the ensemble models to the next stage as inputs. Figure 4 illustrates the process of multi-stage ensemble with 5-fold CV stacked generalization.

We stopped adding an additional ensemble stage when we saw no improvement in CV.

## 5. FINAL SOLUTION

Our final solution is a stage-3 ensemble model trained with the multi-stage ensemble method described in Section 4.2 as follows:

- **Single Model Training:** First, we trained 64 single models with the 8 different algorithms and different subsets of 7 feature sets and DAE features. Out of 64 models, there were 26 GBM, 14 NN, 12 FM, 6 LR, 2 KRR, 2 ET, 1 RF, and 1 KNN models. Some of single models used RF feature selection, where we trained an RF model and selected features with high variable importances.
- **Stage-1 Ensemble:** Second, we trained 15 stage-1 ensemble models with different subsets of CV predictions of 64 single models. Out of 15 models, there were 7 GBM, 4 NN, 2 LR, 1 FM, and 1 ET models. Some of stage-1 ensemble models used rank orders between single models as additional inputs.
- **Stage-2 Ensemble:** Third, we trained 2 stage-1 ensemble models with different subsets of CV predictions of 15 stage-1 ensemble models. We used a LR with stepwise greedy forward selection and a GBM.
- **Stage-3 Ensemble:** Lastly, we trained a stage-3 ensemble model with CV predictions of all models. We used LR with stepwise greedy forward selection, and it selected 5 models out of total 81 models: 1 stage-2 ensemble models, 3 stage-1 ensemble models and 1 single model. Table 2 shows the list of models selected by the final stage-3 ensemble model.

Figure 6 shows the end-to-end pipeline for the final solution. Details of the single and ensemble models trained are available in Table A3 and A4 in Appendix.

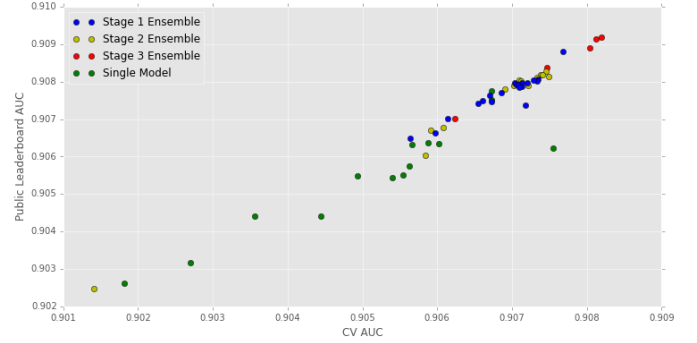


Figure 5: CV vs. public leaderboard AUC scores.

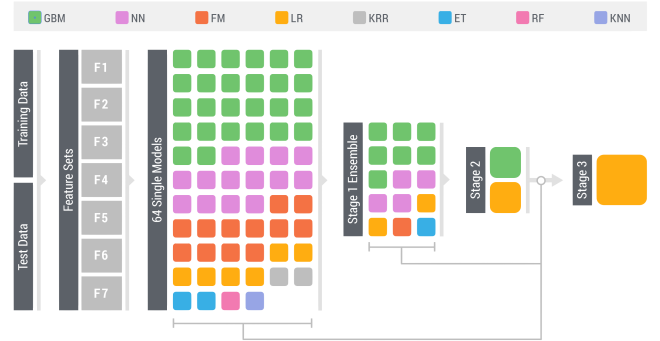


Figure 6: End-to-end pipeline for the final solution

Our final solution achieved AUC scores of 0.90918 and 0.90744 on the public and private leaderboards respectively, and put us to the 1st place out of 821 teams.

At KDD Cup 2015, we made some observations as follows:

- As shown in Figure 5, our CV scores were very consistent with public leaderboard scores. Therefore we used CV scores to determine (1) whether to add more ensemble stage or not and (2) whether to include a model for ensemble or not.
- GBM outperformed other algorithms. Our top 8 single models as well as top 2 stage-1 ensemble models are GBM models. NN and FM were next best algorithms. LR with stepwise greedy forward selection worked well in ensemble stages.
- Biggest performance improvement was from the stage-1 ensemble, and as we added more ensemble stages, we observed diminishing improvements. The stage-1, -2, and -3 ensembles improved the best CV score by 0.00967, 0.00028, and 0.000226 respectively. However, it was the improvement from the stage-2 and -3 ensemble that allowed us to finish the 1st.

## 6. CONCLUSIONS

In this paper, we demonstrated a comprehensive pipeline from the raw data to the final dropout prediction with best practices in predictive modeling. It started from feature engineering that extracts both hand crafted and automated features. At this step, discovering key features (such as F7

**Table 2: Models selected in the stage-3 ensemble.**

ID	Stage	Algorithm	5-CV	Weight
S1	Single	GBM	0.906721	1.1703
E4	1	GBM	0.907878	1.9626
E8	1	NN	0.907567	0.7871
E18	1	ET	0.906207	0.4580
E2	2	LR	0.907968	1.6146

in Section 2.9) played a key role for us to proceed close to the top. Then, we trained 64 single models with 8 classification algorithms. Lastly, the multi-stage ensemble allows us to fully harness predictive signals in the extracted features and trained single models, and to finish the 1st at KDD Cup 2015.

Here we made 2 major contributions. First, our feature engineering approach can be useful for customer churn prediction in publishing, financial services, insurance, electric utilities, health care, banking, Internet, telephone, and cable service industries, where similar customer log data are available. Second, we push forward current state-of-the-art for ensemble methods with our multi-stage ensemble framework.

## APPENDIX

**Table A1: List of features in the feature set F1.**

No.	Description
1	Course.id encoded by 1-of-N coding
2	Number of requests by an enrollment_id
3	Number of unique object by an enrollment_id
4	Number of unique problem object of event by an enrollment_id
5	Number of active days by an enrollment_id
6	Number of active hours by an enrollment_id
7	Time of first access in hours by an enrollment_id
8	Time of last access in hours by an enrollment_id
9	Number of enrollments by an username
10	Number of requests by an username
11	Number of unique objects by an username
12	Number of unique problem object of event by an username
13	Number of active days by an username
14	Number of active hours by an username
15	Time of first access in hours by an username
16	Time of last access in hours by an username
17	Time of first problem access in hours by an username
18	Time of last problem access in hours by an username
19	For each course, number of requests by an username
20	For each course, number of unique object by an username
21	For each course, number of unique problem object by an username
22	For each course, number of active days by an username
23	For each course, number of active hours by an username
24	For each course, time of first access in hours
25	For each course, time of last access in hours
26	Number of enrollment_ids during 10 days after the end date of course by an username
27	For each course, number of access logs during 10 days after the end date of course by an username
28	For each course, number of unique objects during 10 days after the end date of course by an username
29	For each course, number of unique problem objects during 10 days after the end date of course by an username
30	For each course, number of active hours during 10 days after the end date of course by an username
31	For each course, difference between first and last access during 10 days after the end date of course by an username
32	For each course, time of first access in hours during 10 days after the end date of course by an username
33	For each course, time of last access in hours during 10 days after the end date of course by an username
34	For each course, time of first access to an problem object in hours during 10 days after the end date of course by an username
35	For each course, time of last access to an problem object in hours during 10 days after the end date of course by an username
36	Number of enrollment_ids during 1 day after the end date of course by an username
37	For each course, number of access logs during 1 day after the end date of course by an username
38	For each course, number of unique objects during 1 day after the end date of course by an username
39	For each course, number of unique problem objects during 1 day after the end date of course by an username
40	For each course, number of active hours during 1 day after the end date of course by an username
41	For each course, difference between first and last access during 1 day after the end date of course by an username
42	For each course, time of first access in hours during 1 day after the end date of course by an username
43	For each course, time of last access in hours during 1 day after the end date of course by an username
44	For each course, time of first access to an problem object in hours during 1 day after the end date of course by an username
45	For each course, time of last access to an problem object in hours during 1 day after the end date of course by an username
46	For each days of the course, which date is provided in date.csv, number of unique active courses by an username

**Table A2: List of features in the feature set F2.**

No.	Description
1	act counts
2	hourset length in last 2 days
3	last month
4	max absent days
5	day set length
6	hour set length
7	average hours per day
8	event wiki counts
9	event discussion counts
10	event access counts
11	event video counts
12	event problem counts
13	obj chapter not visited
14	obj chapter visited ratio
15	obj video not visited
16	obj video visited ratio
17	obj problem not visited
18	obj problem visited ratio
19	obj set length
20	total time span
21	days from last act to course end
22	course drop rate
23	number of courses enrolled
24	min days between first visit and next course begin
25	min days between 10 days after last visit and next course begin
26	min days between last visit and next course end
27	min days between previous course end and last visit
28	min days between 10 days after current course end and next course begin
29	min days between 10 days after current course end and next course end
30	min days between current course end and next visit
31	number of active days between last visit and course end
32	number of active days in 10 days after course end
33	number of courses ended after current course end



**Table A3: List of single models.**

ID	Stage	Algorithm	Feature	Note	5-CV	Public Leaderboard
S1	Single	GBM	F2 + F3 + F6 + F7	Feature selection with RF	0.906721	0.907765
S2	Single	GBM	F2 + F1 + F6 + F7	-	0.906729	0.907525
S3	Single	GBM	F2 + F1 + F3	Feature selection with RF	0.905875	0.906361
S4	Single	GBM	F2 + F3 + F6	Feature selection with RF	0.905543	0.905516
S5	Single	GBM	F2 + F1 + F3 + F5	Feature selection with RF	0.905356	-
S6	Single	GBM	F2 + F1	-	0.905312	-
S7	Single	GBM	F2 + F3	Feature selection with RF	0.904935	0.905480
S8	Single	GBM	F2 + F1	-	0.904914	-
S9	Single	NN	F2 + F1 + F3 + F4	DAE features added	0.904235	-
S10	Single	NN	F2 + F1 + F3 + F4	-	0.903736	-
S11	Single	NN	F2 + F1 + F3	DAE features added	0.903669	-
S12	Single	FM	F1 + F2	-	0.903560	0.904411
S13	Single	NN	F2 + F1 + F3	-	0.903428	-
S14	Single	GBM	F2 + F6	-	0.903385	-
S15	Single	GBM	F1	-	0.902918	-
S16	Single	GBM	F2	-	0.902287	-
S17	Single	FM	F2	-	0.901983	-
S18	Single	NN	F2	DAE features added	0.901846	0.902614
S19	Single	KRR	F2 + F1 + F3 + F4	DAE features added	0.901522	-
S20	Single	NN	F2 + F1 + F3	-	0.900982	-
S21	Single	GBM	F1	-	0.900906	-
S22	Single	GBM	F3	Feature selection with RF	0.899239	-
S23	Single	GBM	F3	Feature selection with RF	0.899167	-
S24	Single	GBM	F3	Feature selection with RF	0.898969	-
S25	Single	GBM	F3	Feature selection with RF	0.898890	-
S26	Single	GBM	F3	-	0.898749	-
S27	Single	FM	F2 + F6	-	0.898308	-
S28	Single	GBM	F2 + F6	-	0.897968	-
S29	Single	GBM	F3	-	0.897912	-
S30	Single	NN	F2 + F6	-	0.897143	-
S31	Single	NN	F2 + F5	-	0.896748	-
S32	Single	LR	F2 + F1 + F3	-	0.896435	-
S33	Single	FM	F2 + F6	-	0.896160	-
S34	Single	GBM	F3	-	0.895754	-
S35	Single	KRR	F4	-	0.894524	-
S36	Single	GBM	F3	-	0.893507	-
S37	Single	GBM	F6	-	0.892364	-
S38	Single	GBM	F6	-	0.892253	-
S39	Single	NN	F4	-	0.891217	-
S40	Single	LR	F3	-	0.890580	-
S41	Single	NN	F4	-	0.890565	-
S42	Single	FM	F3	-	0.888418	-
S43	Single	FM	F3	-	0.888381	-
S44	Single	RF	F3	-	0.887583	-
S45	Single	ET	F3	-	0.887768	-
S46	Single	FM	F6	-	0.887116	-
S47	Single	FM	F6	-	0.886866	-
S48	Single	NN	F4	-	0.886705	-
S49	Single	NN	F6	-	0.886109	-
S50	Single	GBM	F6	-	0.885184	-
S51	Single	GBM	F6	-	0.885124	-
S52	Single	FM	F6	-	0.885037	-
S53	Single	FM	F6	-	0.884697	-
S54	Single	GBM	F4	-	0.882441	-
S55	Single	ET	F2 + F6	-	0.881539	-
S56	Single	FM	F6	-	0.880878	-
S57	Single	FM	F6	-	0.880366	-
S58	Single	NN	F6	-	0.880219	-
S59	Single	KNN	F4	-	0.877652	-
S60	Single	NN	F6	-	0.876905	-
S61	Single	LR	F4	-	0.821332	-
S62	Single	LR	F6	-	0.804150	-
S63	Single	LR	F6	-	0.802138	-
S64	Single	LR	F6	-	0.800225	-

**Table A4: List of ensemble models.**

ID	Stage	Algorithm	Note	5-CV	Public Leaderboard
E1	3	LR	Stepwise greedy forward selection	0.908194	0.909181
E2	2	LR	Stepwise greedy forward selection	0.907968	-
E3	2	GBM	-	0.907379	0.908187
E4	1	GBM	-	0.907878	-
E5	1	GBM	-	0.907734	-
E6	1	LR	Stepwise greedy forward selection	0.907716	-
E7	1	GBM	-	0.907668	0.908796
E8	1	NN	DAE features added	0.907567	-
E9	1	GBM	-	0.907353	0.908060
E10	1	GBM	-	0.907283	0.908043
E11	1	NN	-	0.907076	-
E12	1	GBM	-	0.907036	0.907977
E13	1	NN	DAE features added	0.906956	-
E14	1	LR	-	0.906746	-
E15	1	NN	-	0.906714	-
E16	1	GBM	RF feature selection	0.906689	-
E17	1	FM	-	0.906537	-
E18	1	ET	-	0.906200	-