```
In[ • ]:= (* Initialisation *)
     (* Evaluate before start writing "real code" *)
     (* Usage e.g.: "ld [Spacekey]" becomes "⊨",
     so writing "a ld 5" turns into "a ⊨ 5" *)
     SetOptions [EvaluationNotebook [],
                    InputAutoReplacements → {(* special AceGen assignment operators: *)
         "ld" → "=", "ls" → "+", "rd" → "=", "rs" → "-",
                                                 (* brackets and symbols: *) "dbl" → "[",
         "dbr" \rightarrow "]", "lcb" \rightarrow "{", "rcb" \rightarrow "}", "lsb" \rightarrow "[", "rsb" \rightarrow "]", "->" \rightarrow "\rightarrow",
                                                 (* shortcuts for
          starting/ending a comment block: *) "co" → "(*", "cc" → "*)"
                                                }
                 1
     (* Output the current time,
     so we know when AceGen has been executed the last time *)
Out[ • ]= Wed 22 May 2024 11:25:37 GMT+2
In[ • ]:= (*initialization *)
     ClearAll["Global`*"](*all variables are initially cleared*)
     (* NAME OF SUBROUTINE YOU WANT TO PRODUCE *)
     NAME = "stabilisation_Q1LES";
In[ • ]:= << AceGen`; (*AceGen is started*)</pre>
```

```
ln[ \circ ] :=  shape_functions_Hex8 [\xi 1_, \xi 2_, \xi 3_] :=
             1/8 * \{(1 - \xi 1) * (1 - \xi 2) * (1 - \xi 3), (*N1*)
                      (1 + \xi 1) \times (1 - \xi 2) \times (1 - \xi 3), (*N2*)
                      (1 + \xi 1) \times (1 + \xi 2) \times (1 - \xi 3), (*N3*)
                      (1 - \xi 1) \times (1 + \xi 2) \times (1 - \xi 3), (*N4*)
                      (1 - \xi 1) \times (1 - \xi 2) \times (1 + \xi 3), (*N5*)
                      (1 + \xi 1) \times (1 - \xi 2) \times (1 + \xi 3), (*N6*)
                      (1 + \xi 1) \times (1 + \xi 2) \times (1 + \xi 3), (*N7*)
                      (1 - \xi 1) \times (1 + \xi 2) \times (1 + \xi 3) (*N8*)
                    }
        );
     quadrature_rule_full :=
     (
                s1by3 = Sqrt[1/3];
                QP\_coords = Transpose[{{-s1by3, -s1by3, -s1by3}, (*Q1*)}
                                             +s1by3, -s1by3, -s1by3, (*Q2*)
                                             +s1by3, +s1by3, -s1by3, (*Q3*)
                                             \{-s1by3, +s1by3, -s1by3\}, (*Q4*)
                                             \{-s1by3, -s1by3, +s1by3\}, (*Q5*)
                                             +s1by3, -s1by3, +s1by3, (*Q6*)
                                             +s1by3, +s1by3, +s1by3, (*Q7*)
                                             \{-s1by3, +s1by3, +s1by3\} (*Q8*)
                                            }];
                QP_{weights} = \{1, 1, 1, 1, 1, 1, 1, 1\};
                Return[{QP_coords , QP_weights }];
        );
     quadrature_rule_reduced :=
     (
                 QP\_coords = \{\{0\}, \{0\}, \{0\}\}; (*Q9*)
                 QP_weights ⊨ {8};
                 Return[{QP_coords , QP_weights }];
     );
In[ • ]:= dofs_per_node = 3;
     n_nodes = 8;
     ndtot = n_nodes * dofs_per_node;
```

```
Inf = ):= (* Programming language, Mode: Debug/Prototype/Optimal *)
    SMSInitialize [NAME, "Language" → "Fortran", "Mode" → "Optimal"];
    (* Create the module named NAME with all inputs and outputs *)
    (* Inputs:
     - X: (8,3) array with undeformed nodal
       coordinates of the 8 nodes of this 3D hexahedral element
      - u: (24) array with displacement values (degrees of freedom) listed as
            { u_N1_x, u_N1_y, u_N1_z, u_N2_x, u_N2_y, ..., u_N8_z } for each Node N1...
          N8 with components \{x,y,z\}
        - bulkModkappa: bulk modulus of the base material
        - shearModmu: shear modulus of the base material
           - HGscale: hourglass control coefficient,
    e.g. 1e-4 (higher values cause stronger stabilisation)
     - istif: integer/boolean to request the stiffness matrix,
    istif=1: stiffness matrix is requested thus computed therein,
    istif=0: stiffness matrix is not requested and not computed herein
       Outputs:
      - forceHG: (24) array of internal force components for hourglass
           stabilisation for each degree of freedom of the current element
          - stiffHG: (24x24) array with component of the stiffness
            matrix for the stabilisation 'for the current element
    SMSModule[NAME, Real[X$$[n nodes, dofs per node],
       u$$[n_nodes, dofs_per_node], bulkModkappa$$, shearModmu$$, HGscale$$],
      Integer[istif$$], Real[forceHG$$[ndtot], stiffHG$$[ndtot, ndtot]],
      "Input" → {X$$, u$$, bulkModkappa$$, shearModmu$$, HGscale$$, istif$$},
      "Output" → {forceHG$$, stiffHG$$}];
_{ln[\; \circ \; ]:=} (* Input declaration / copy Acegen variables to Mathematica variables *)
     XIO = SMSReal[Table[X$$[iNode, jdof], {iNode, n_nodes}, {jdof, dofs per_node}]];
     uIO = SMSReal[Table[u$$[iNode, jdof], {iNode, n_nodes}, {jdof, dofs_per_node}]];
     pe ⊨ Flatten[uI0];
     \kappa \models SMSReal[bulkModkappa$$];
     \mu \models SMSReal[shearModmu$$];
     \lambda \models \kappa - 2/3 * \mu;
     HGscaleValue ⊨ SMSReal[HGscale$$];
     istif ⊨ SMSInteger[istif$$];
```

```
Inf • ]:= (* Initialise output variables to zero
     (can be included optionally, if not done by the caller subroutine) *)
     (* SMSExport[Table[0,{idof,ndtot}],forceHG$$];
      SMSExport[Table[0,{idof,ndtot},{jdof,ndtot}],stiffHG$$];*)
<code>In[ • ]:= (* Standard QP coordinates and weights</code>
      for full integration (FuI) of stabilisation *)
     {QP_coords_FuI , QP_weights_FuI } = quadrature_rule_full ;
    (* Reduced integration (RI) for energy compensation *)
     { QP coords RI , QP weights RI } ⊨ quadrature rule reduced ;
    (* Merge the two lists, with first FuI followed by RI *)
     QP_coords = Join[QP_coords_FuI , QP_coords_RI , 2];
     QP_weights = Join[QP_weights_FuI , QP_weights_RI];
In[ • ]:= (* Loop over combined list of QPs *)
     SMSDo[qpoint, 1, 9];
        (* Using SMSPart to access qpoint's entry: *)
         ξ1 ⊢ SMSReal[SMSPart[QP_coords [1], qpoint]];
         ξ2 ⊢ SMSReal[SMSPart[QP coords [2], qpoint]];

ξ3 ⊢ SMSReal[SMSPart[QP_coords[3], qpoint]];

        \Xi = \{\xi 1, \, \xi 2, \, \xi 3\};
        weight_qpoint + SMSPart[QP_weights , qpoint];
        Nh = shape_functions_Hex8 [\xi1, \xi2, \xi3];
        X ⊢ SMSFreeze [Nh . XIO];
        u = Nh . uI0;
        Je = SMSD[X, \Xi];
        Jed ⊨ Det[Je];
        \mathbb{H} \models SMSD[u, X, "Dependency" \rightarrow \{\Xi, X, SMSInverse[Je]\}];
        \epsilon \models 1/2 * (H^T + H);
        (* For the fully integrated QPs we add the
      stabilising energy with a positive HG scaling factor *)
         SMSIf[qpoint ≤ 8];
           HGscale ≠ HGscaleValue *1;
        (* and for the reduced integrated centre QP (qpoint==9),
    we remove the "same" energy (1 QP with weight=8)
      leaving "only" the hourglass stabilising energy *)
         SMSElse[];
           HGscale → HGscaleValue *(-1);
         SMSEndIf[HGscale];
        (* Linear elastic energy *)
```

```
W = HGscale * \left(\frac{\lambda}{2} * (Tr[\epsilon])^2 + \mu * Tr[\epsilon \cdot \epsilon]\right);
       (* Compute the residual/force and the stiffness matrix *)
        SMSDo[m, 1, ndtot];
         Rgm = Jed * SMSD[W, pe, m];
         SMSExport[weight_qpoint *Rgm, forceHG$$[m], "AddIn" → True];
         SMSDo[n, 1, ndtot];
           Kgmn ⊨ SMSIf[istif == 1, SMSD[Rgm, pe, n], 0.0];
           SMSExport[weight qpoint * Kgmn, stiffHG$$[m, n], "AddIn" → True];
         SMSEndDo[];
        SMSEndDo[];
      SMSEndDo[]; (*End Gauss Quadrature Loop*)
In[ • ]:= (* write output file *)
    SMSWrite[NAME, "LocalAuxiliaryVariables " → True];
    (* print file on screen *)
    NAME_FileExtension = Which[SMSLanguage == "Fortran",
        ".f", SMSLanguage == "Matlab", ".m", SMSLanguage == "C++", ".cpp"];
    FilePrint[StringJoin[NAME, NAME_FileExtension]]
    File: stabilisation_Q1LES .f Size: 15895
                 stabilisation_Q1LES
     Method
                 235
     No.Formulae
    No.Leafs
                 4136
    !* AceGen 7.505 Linux (16 Aug 22)
                                             22 May 24 11:25:46 *
               Co. J. Korelc 2020
    !***************
    ! User : Full professional version
    ! Notebook : stabilisation_Q1LES
    ! Evaluation time
                                    : 7 s
                                               Mode : Optimal
    ! Number of formulae
                                     : 235
                                               Method: Automatic
    ! Subroutine
                                     : stabilisation Q1LES size: 4136
    ! Total size of Mathematica code : 4136 subexpressions
    ! Total size of Fortran code : 15274 bytes
    !******* S U B R O U T I N E ***********
          SUBROUTINE stabilisation_Q1LES(X,u,bulkModkappa,shearModmu
         &, HGscale, istif, forceHG, stiffHG)
          IMPLICIT NONE
          include 'sms.h'
          INTEGER istif, i55, i191, i203
          LOGICAL b188,b204,b205,b270
```

```
DOUBLE PRECISION v(734), X(8,3), u(8,3), bulkModkappa
&, shearModmu, HGscale, forceHG(24), stiffHG(24,24)
 v(348)=1d0
 v(349)=1d0
 v(350)=1d0
 v(351)=1d0
 v(352)=1d0
 v(353)=1d0
 v(354)=1d0
 v(355)=1d0
 v(356)=8d0
 v(339)=(-0.5773502691896257d0)
 v(340)=(-0.5773502691896257d0)
 v(341)=(-0.5773502691896257d0)
 v(342)=(-0.5773502691896257d0)
 v(343)=0.5773502691896257d0
 v(344)=0.5773502691896257d0
 v(345)=0.5773502691896257d0
 v(346)=0.5773502691896257d0
 v(347)=0d0
 v(330)=(-0.5773502691896257d0)
 v(331)=(-0.5773502691896257d0)
 v(332)=0.5773502691896257d0
 v(333)=0.5773502691896257d0
 v(334)=(-0.5773502691896257d0)
 v(335)=(-0.5773502691896257d0)
 v(336)=0.5773502691896257d0
 v(337)=0.5773502691896257d0
 v(338)=0d0
 v(321)=(-0.5773502691896257d0)
 v(322)=0.5773502691896257d0
 v(323)=0.5773502691896257d0
 v(324)=(-0.5773502691896257d0)
 v(325)=(-0.5773502691896257d0)
 v(326)=0.5773502691896257d0
 v(327)=0.5773502691896257d0
 v(328)=(-0.5773502691896257d0)
 v(329)=0d0
 V(1)=X(1,1)
 V(2)=X(1,2)
 v(3)=X(1,3)
 v(4)=X(2,1)
 v(263)=-v(1)+v(4)
 v(5)=X(2,2)
 v(259)=-v(2)+v(5)
 v(6)=X(2,3)
 v(255)=-v(3)+v(6)
 v(7)=X(3,1)
 v(252)=v(4)-v(7)
 v(8)=X(3,2)
 v(248)=v(5)-v(8)
 v(9)=X(3,3)
 v(244)=v(6)-v(9)
 V(10)=X(4,1)
```

v(264)=-v(10)+v(7)

- v(251)=v(1)-v(10)
- v(11)=X(4,2)
- V(260)=-V(11)+V(8)
- v(247)=-v(11)+v(2)
- v(12)=X(4,3)
- v(256)=-v(12)+v(9)
- v(243)=-v(12)+v(3)
- v(13)=X(5,1)
- v(238)=v(1)-v(13)
- v(14)=X(5,2)
- v(234)=-v(14)+v(2)
- v(15)=X(5,3)
- v(230)=-v(15)+v(3)
- v(16)=X(6,1)
- v(265)=-v(13)+v(16)
- v(239)=-v(16)+v(4)
- v(17)=X(6,2)
- v(261)=-v(14)+v(17)
- v(235)=-v(17)+v(5)
- v(18)=X(6,3)
- v(257)=-v(15)+v(18)
- v(231)=-v(18)+v(6)
- v(19)=X(7,1)
- v(254)=v(16)-v(19)
- v(240)=-v(19)+v(7)
- v(20)=X(7,2)
- v(250)=v(17)-v(20)
- v(236)=-v(20)+v(8)
- v(21)=X(7,3)
- v(246)=v(18)-v(21)
- v(232)=-v(21)+v(9)
- v(22)=X(8,1)
- v(266)=v(19)-v(22)
- v(253)=v(13)-v(22)
- v(241)=v(10)-v(22)
- v(23)=X(8,2)
- v(262)=v(20)-v(23)
- v(249)=v(14)-v(23)
- v(237)=v(11)-v(23)
- v(24)=X(8,3)
- v(258)=v(21)-v(24)
- v(245)=v(15)-v(24)
- v(233)=v(12)-v(24)
- v(25)=u(1,1)
- v(26)=u(1,2)
- v(27)=u(1,3)
- v(28)=u(2,1)
- v(29)=u(2,2)
- v(30)=u(2,3)
- v(31)=u(3,1)
- v(32)=u(3,2)
- v(33)=u(3,3)
- v(34)=u(4,1)
- v(35)=u(4,2)v(36)=u(4,3)

```
v(37)=u(5,1)
v(38)=u(5,2)
v(39)=u(5,3)
v(40)=u(6,1)
v(41)=u(6,2)
v(42)=u(6,3)
v(43)=u(7,1)
v(44)=u(7,2)
v(45)=u(7,3)
v(46)=u(8,1)
v(47)=u(8,2)
v(48)=u(8,3)
v(50)=shearModmu
v(227)=2d0*v(50)
v(51)=bulkModkappa+(-2d0/3d0)*v(50)
v(52)=HGscale
b204=istif.eq.1
DO i55=1,9
 v(56)=v(320+i55)
 v(67)=1d0-v(56)
 v(63)=1d0+v(56)
 v(57)=v(329+i55)
 v(73)=1d0+v(57)
 v(85)=v(73)/8d0
 v(93)=-(v(67)*v(85))
 v(92)=-(v(63)*v(85))
 v(69)=1d0-v(57)
 v(86)=v(69)/8d0
 v(91)=-(v(63)*v(86))
 v(89) = -(v(67) * v(86))
 v(104)=v(230)*v(89)+v(231)*v(91)+v(232)*v(92)+v(233)*v(93)
 V(101)=V(234)*V(89)+V(235)*V(91)+V(236)*V(92)+V(237)*V(93)
 v(98) = v(238) * v(89) + v(239) * v(91) + v(240) * v(92) + v(241) * v(93)
 v(58)=v(338+i55)
 v(84)=(1d0+v(58))/8d0
 v(95)=-(v(63)*v(84))
 v(94)=-(v(67)*v(84))
 v(76)=v(73)*v(84)
 v(71)=v(69)*v(84)
 v(87)=(1d0-v(58))/8d0
 v(90)=-(v(63)*v(87))
 v(88)=-(v(67)*v(87))
 v(103)=v(243)*v(88)+v(244)*v(90)+v(245)*v(94)+v(246)*v(95)
 v(100)=v(247)*v(88)+v(248)*v(90)+v(249)*v(94)+v(250)*v(95)
 V(224)=-(V(101)*V(103))+V(100)*V(104)
 v(97) = v(251) * v(88) + v(252) * v(90) + v(253) * v(94) + v(254) * v(95)
 v(66)=v(73)*v(87)
 v(61)=v(69)*v(87)
 v(102)=v(255)*v(61)+v(256)*v(66)+v(257)*v(71)+v(258)*v(76)
 v(99)=v(259)*v(61)+v(260)*v(66)+v(261)*v(71)+v(262)*v(76)
 V(226)=-(V(100)*V(102))+V(103)*V(99)
 v(225)=v(101)*v(102)-v(104)*v(99)
 v(96)=v(263)*v(61)+v(264)*v(66)+v(265)*v(71)+v(266)*v(76)
 v(59)=v(347+i55)
 v(105)=v(224)*v(96)+v(225)*v(97)+v(226)*v(98)
```

```
v(106)=-(v(224)/v(105))
v(169)=-(v(106)*v(76))
\vee(160)=\vee(106)*\vee(71)
v(151)=-(v(106)*v(66))
v(142)=v(106)*v(61)
v(107)=(v(104)*v(97)-v(103)*v(98))/v(105)
v(171)=-(v(107)*v(76))
v(162)=v(107)*v(71)
v(153)=-(v(107)*v(66))
V(144)=V(107)*V(61)
V(108)=(-(V(101)*V(97))+V(100)*V(98))/V(105)
v(173)=-(v(108)*v(76))
v(164)=v(108)*v(71)
v(155)=-(v(108)*v(66))
v(146)=v(108)*v(61)
v(109)=v(225)/v(105)
V(130)=V(109)*V(87)
V(118)=V(109)*V(84)
v(110)=(v(104)*v(96)-v(102)*v(98))/v(105)
V(133)=V(110)*V(87)
V(120)=V(110)*V(84)
V(111)=(-(V(101)*V(96))+V(98)*V(99))/V(105)
v(136)=v(111)*v(87)
V(122)=V(111)*V(84)
v(112)=v(226)/v(105)
v(131)=v(112)*v(86)
v(124)=v(112)*v(85)
v(113)=(-(v(103)*v(96))+v(102)*v(97))/v(105)
v(134)=v(113)*v(86)
v(126)=v(113)*v(85)
v(114)=(v(100)*v(96)-v(97)*v(99))/v(105)
v(137)=v(114)*v(86)
V(128)=V(114)*V(85)
v(115)=v(118)+v(124)
v(116)=v(120)+v(126)
v(117)=v(122)+v(128)
v(119)=-v(118)+v(131)
v(121)=-v(120)+v(134)
v(123)=-v(122)+v(137)
v(125)=-v(124)+v(130)
v(127)=-v(126)+v(133)
v(129)=-v(128)+v(136)
v(132)=-v(130)-v(131)
v(135)=-v(133)-v(134)
v(138)=-v(136)-v(137)
V(139)=V(142)+V(132)*V(67)
V(140)=V(144)+V(135)*V(67)
v(141)=v(146)+v(138)*v(67)
v(143)=-v(142)+v(132)*v(63)
v(145)=-v(144)+v(135)*v(63)
v(147)=-v(146)+v(138)*v(63)
v(148)=v(151)+v(125)*v(63)
V(149)=V(153)+V(127)*V(63)
V(150)=V(155)+V(129)*V(63)
```

v(152)=-v(151)+v(125)*v(67)

```
v(154)=-v(153)+v(127)*v(67)
              V(156)=-V(155)+V(129)*V(67)
              V(157)=V(160)+V(119)*V(67)
              v(158)=v(162)+v(121)*v(67)
              V(159)=V(164)+V(123)*V(67)
              v(161)=-v(160)+v(119)*v(63)
              v(163)=-v(162)+v(121)*v(63)
              v(165)=-v(164)+v(123)*v(63)
              V(166)=V(169)+V(115)*V(63)
              V(167)=V(171)+V(116)*V(63)
              v(168)=v(173)+v(117)*v(63)
              V(170)=-V(169)+V(115)*V(67)
              v(172)=-v(171)+v(116)*v(67)
              v(174)=-v(173)+v(117)*v(67)
              V(175)=V(139)*V(25)+V(143)*V(28)+V(148)*V(31)+V(152)*V(34)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)+V(31)
& (157)* \lor (37)+\lor (161)* \lor (40)+\lor (166)* \lor (43)+\lor (170)* \lor (46)
              v(198)=v(140)*v(25)+v(139)*v(26)+v(145)*v(28)+v(143)*v(29)+v(198)
& (149)* v(31)+v(148)* v(32)+v(154)* v(34)+v(152)* v(35)+v(158)* v(37
& )+v(157)*v(38)+v(163)*v(40)+v(161)*v(41)+v(167)*v(43)+v(166)*v
& (44)+v(172)*v(46)+v(170)*v(47)
              v(179)=v(140)*v(26)+v(145)*v(29)+v(149)*v(32)+v(154)*v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)+v(35)
& (158)* \lor (38)+\lor (163)* \lor (41)+\lor (167)* \lor (44)+\lor (172)* \lor (47)
              v(199)=v(141)*v(25)+v(139)*v(27)+v(147)*v(28)+v(143)*v(30)+v(199)=v(141)*v(25)+v(139)*v(27)+v(147)*v(28)+v(143)*v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+
& (150)*v(31)+v(148)*v(33)+v(156)*v(34)+v(152)*v(36)+v(159)*v(37)
& )+v(157)*v(39)+v(165)*v(40)+v(161)*v(42)+v(168)*v(43)+v(166)*v
& (45)+v(174)*v(46)+v(170)*v(48)
              v(200)=v(141)*v(26)+v(140)*v(27)+v(147)*v(29)+v(145)*v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)+v(30)
& (150)*v(32)+v(149)*v(33)+v(156)*v(35)+v(154)*v(36)+v(159)*v(38)
& )+v(158)*v(39)+v(165)*v(41)+v(163)*v(42)+v(168)*v(44)+v(167)*v
& (45)+v(174)*v(47)+v(172)*v(48)
              V(436)=V(140)*V(198)+V(141)*V(199)
              V(437)=V(139)*V(198)+V(141)*V(200)
              V(438)=V(139)*V(199)+V(140)*V(200)
              V(439)=V(145)*V(198)+V(147)*V(199)
              V(440)=V(143)*V(198)+V(147)*V(200)
              V(441)=V(143)*V(199)+V(145)*V(200)
              V(442)=V(149)*V(198)+V(150)*V(199)
              V(443)=V(148)*V(198)+V(150)*V(200)
              v(444)=v(148)*v(199)+v(149)*v(200)
              V(445)=V(154)*V(198)+V(156)*V(199)
              V(446)=V(152)*V(198)+V(156)*V(200)
              V(447)=V(152)*V(199)+V(154)*V(200)
              V(448)=V(158)*V(198)+V(159)*V(199)
              v(449)=v(157)*v(198)+v(159)*v(200)
              v(450)=v(157)*v(199)+v(158)*v(200)
              V(451)=V(163)*V(198)+V(165)*V(199)
              V(452)=V(161)*V(198)+V(165)*V(200)
              v(453)=v(161)*v(199)+v(163)*v(200)
              V(454)=V(167)*V(198)+V(168)*V(199)
              v(455)=v(166)*v(198)+v(168)*v(200)
              v(456)=v(166)*v(199)+v(167)*v(200)
              V(457)=V(172)*V(198)+V(174)*V(199)
              V(458)=V(170)*V(198)+V(174)*V(200)
              v(459)=v(170)*v(199)+v(172)*v(200)
              v(183) = v(141) * v(27) + v(147) * v(30) + v(150) * v(33) + v(156) * v(36) + v(36) +
```

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& (159)* \lor (39)+\lor (165)* \lor (42)+\lor (168)* \lor (45)+\lor (174)* \lor (48)
  v(195)=(v(175)+v(179)+v(183))*v(51)
  IF(i55.le.8) THEN
   v(189)=v(52)
  ELSE
   v(189) = -v(52)
  ENDIF
  v(217)=v(189)*v(227)
  v(212)=(v(105)*v(217))/2d0
  v(194)=v(189)*(v(195)+v(183)*v(227))
  v(196)=v(189)*(v(195)+v(179)*v(227))
  v(197)=v(189)*(v(195)+v(175)*v(227))
  v(388)=v(139)*v(197)
  v(389)=v(140)*v(196)
  V(390)=V(141)*V(194)
  V(391)=V(143)*V(197)
  V(392)=V(145)*V(196)
  v(393)=v(147)*v(194)
  v(394)=v(148)*v(197)
  v(395)=v(149)*v(196)
  v(396)=v(150)*v(194)
  v(397)=v(152)*v(197)
  v(398)=v(154)*v(196)
  v(399)=v(156)*v(194)
  v(400)=v(157)*v(197)
  v(401)=v(158)*v(196)
  v(402)=v(159)*v(194)
  v(403)=v(161)*v(197)
  v(404)=v(163)*v(196)
  v(405)=v(165)*v(194)
  V(406)=V(166)*V(197)
  v(407)=v(167)*v(196)
  v(408)=v(168)*v(194)
  \vee(409)=\vee(170)*\vee(197)
  v(410)=v(172)*v(196)
  \vee(411)=\vee(174)*\vee(194)
  IF(b204) THEN
   v(587)=v(140)
   v(588)=v(139)
   v(589)=0d0
    v(590)=v(145)
   v(591)=v(143)
   v(592)=0d0
    v(593)=v(149)
    v(594)=v(148)
   v(595)=0d0
    v(596)=v(154)
    v(597)=v(152)
    v(598)=0d0
    v(599)=v(158)
    v(600)=v(157)
   v(601)=0d0
    v(602)=v(163)
```

v(603)=v(161)v(604)=0d0

- v(605)=v(167)
- v(606)=v(166)
- v(607)=0d0
- v(608)=v(172)
- v(609)=v(170)
- v(610)=0d0
- v(563)=v(141)
- v(564)=0d0
- v(565)=v(139)
- v(566)=v(147)
- v(567)=0d0
- v(568)=v(143)
- v(569)=v(150)
- v(570)=0d0
- v(571)=v(148)
- v(572)=v(156)
- v(573)=0d0
- v(574)=v(152)
- v(575)=v(159)
- v(576)=0d0
- v(577)=v(157)
- v(578)=v(165)
- v(579)=0d0
- v(580)=v(161)
- v(581)=v(168)
- v(582)=0d0
- v(583)=v(166)
- v(584)=v(174)
- v(585)=0d0
- v(586)=v(170)
- v(539)=0d0
- v(540)=v(141)
- v(541)=v(140)
- v(542)=0d0
- v(543)=v(147)
- v(544)=v(145)
- v(545)=0d0
- v(546)=v(150)
- v(547)=v(149)
- v(548)=0d0
- v(549)=v(156)
- v(550)=v(154)
- v(551)=0d0
- v(552)=v(159)
- v(553)=v(158)
- v(554)=0d0
- v(555)=v(165)
- v(556)=v(163)
- v(557)=0d0
- v(558)=v(168)
- v(559)=v(167)
- v(560)=0d0
- v(561)=v(174)v(562)=v(172)
- v(515)=0d0

- v(516)=0d0
- v(517)=v(141)
- v(518)=0d0
- v(519)=0d0
- v(520)=v(147)
- v(521)=0d0
- v(522)=0d0
- v(523)=v(150)
- v(524)=0d0
- v(525)=0d0
- v(526)=v(156)
- v(527)=0d0
- v(528)=0d0
- v(529)=v(159)
- v(530)=0d0
- v(531)=0d0
- v(532)=v(165)
- v(533)=0d0
- v(534)=0d0
- v(535)=v(168)
- v(536)=0d0
- v(537)=0d0
- v(538)=v(174)
- v(491)=0d0
- v(492)=v(140)
- v(493)=0d0
- v(494)=0d0
- v(495)=v(145)
- v(496)=0d0
- v(497)=0d0
- v(498)=v(149)
- v(499)=0d0
- v(500)=0d0
- v(501)=v(154)
- v(502)=0d0
- v(503)=0d0
- v(504)=v(158)
- v(505)=0d0
- v(506)=0d0
- v(507)=v(163)
- v(508)=0d0
- v(509)=0d0
- v(510)=v(167)
- v(511)=0d0
- v(512)=0d0
- v(513)=v(172)
- v(514)=0d0
- v(467)=v(139)
- v(468)=0d0
- v(469)=0d0
- v(470)=v(143)
- v(471)=0d0
- v(472)=0d0
- v(473)=v(148)
- v(474)=0d0

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v(475)=0d0
   v(476)=v(152)
   v(477)=0d0
   v(478)=0d0
   v(479)=v(157)
   v(480) = 0d0
   v(481)=0d0
   v(482)=v(161)
   v(483)=0d0
   v(484) = 0d0
   v(485)=v(166)
   v(486)=0d0
   v(487)=0d0
   v(488)=v(170)
   v(489) = 0d0
   v(490)=0d0
  ELSE
  FNDTF
  DO i191=1,24
   forceHG(i191)=forceHG(i191)+v(105)*v(59)*(v(387+i191)+v(189
& )* v(50)* v(435+i191))
   DO i203=1,24
    IF(b204) THEN
      v(208)=v(105)*v(466+i191)
      v(209)=v(105)*v(490+i191)
      v(210)=v(105)*v(514+i191)
      v(211)=v(212)*v(538+i191)
      v(213)=v(212)*v(562+i191)
      v(214)=v(212)*v(586+i191)
      v(218)=v(189)*(v(208)+v(209)+v(210))*v(51)
      V(216)=V(210)*V(217)+V(218)
      V(219)=V(209)*V(217)+V(218)
      V(220)=V(208)*V(217)+V(218)
      V(611)=V(141)*V(213)+V(140)*V(214)+V(139)*V(220)
      v(612)=v(141)*v(211)+v(139)*v(214)+v(140)*v(219)
      V(613)=V(140)*V(211)+V(139)*V(213)+V(141)*V(216)
      V(614)=V(147)*V(213)+V(145)*V(214)+V(143)*V(220)
      v(615)=v(147)*v(211)+v(143)*v(214)+v(145)*v(219)
      V(616)=V(145)*V(211)+V(143)*V(213)+V(147)*V(216)
      V(617)=V(150)*V(213)+V(149)*V(214)+V(148)*V(220)
      V(618)=V(150)*V(211)+V(148)*V(214)+V(149)*V(219)
      v(619)=v(149)*v(211)+v(148)*v(213)+v(150)*v(216)
      V(620)=V(156)*V(213)+V(154)*V(214)+V(152)*V(220)
      v(621)=v(156)*v(211)+v(152)*v(214)+v(154)*v(219)
      V(622)=V(154)*V(211)+V(152)*V(213)+V(156)*V(216)
      V(623)=V(159)*V(213)+V(158)*V(214)+V(157)*V(220)
      V(624)=V(159)*V(211)+V(157)*V(214)+V(158)*V(219)
      v(625)=v(158)*v(211)+v(157)*v(213)+v(159)*v(216)
      v(626)=v(165)*v(213)+v(163)*v(214)+v(161)*v(220)
      V(627)=V(165)*V(211)+V(161)*V(214)+V(163)*V(219)
      V(628)=V(163)*V(211)+V(161)*V(213)+V(165)*V(216)
      v(629)=v(168)*v(213)+v(167)*v(214)+v(166)*v(220)
      V(630)=V(168)*V(211)+V(166)*V(214)+V(167)*V(219)
      V(631)=V(167)*V(211)+V(166)*V(213)+V(168)*V(216)
      v(632)=v(174)*v(213)+v(172)*v(214)+v(170)*v(220)
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v(633)=v(174)*v(211)+v(170)*v(214)+v(172)*v(219)
      \vee (\,634) {=} \vee (\,172) {*}\, \vee (\,211) {+} \vee (\,170) {*}\, \vee (\,213) {+} \vee (\,174) {*}\, \vee (\,216)
      v(222)=v(610+i203)
    ELSE
     v(222)=0d0
    ENDIF
    stiffHG(i191,i203)=stiffHG(i191,i203)+v(222)*v(59)
 ENDDO
ENDDO
END
```