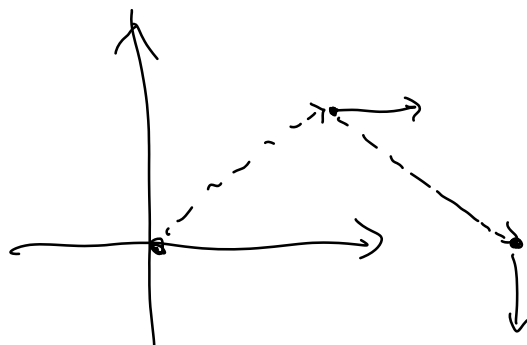


$$V = (0, +1)$$



Proof:

Let $\vec{v} = (x, y)$ be the displacement

and $\text{dir} = \text{north or south or west or east}$ be the final direction

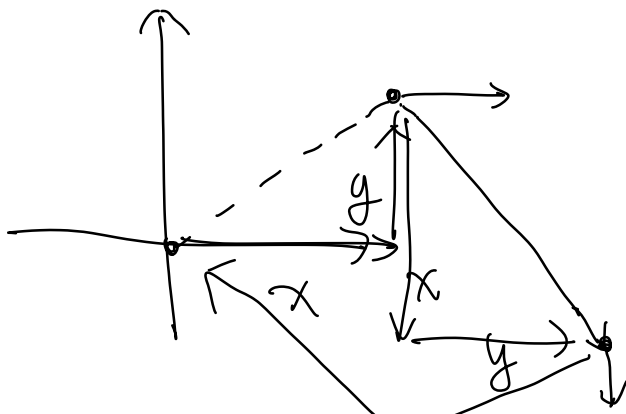
Claim:

if $\vec{v} = 0$ OR $\text{dir} \neq \text{north}$

\Leftrightarrow in a circle

① if $\vec{v} = 0 \Rightarrow$ trivial, it will stay at $(0,0)$

$(\Rightarrow) ②$



Assume $\vec{v} = \text{east}$

First time $(0, 0) \rightarrow (x, y)$

second time $(x, y) \xrightarrow{(y, -x)} (x+y, y-x)$

third time $(x+y, y-x) \xrightarrow{(-x, -y)} (y, -x)$

fourth time $(y, -x) \xrightarrow{(-y, +x)} (0, 0)$
#

(\Leftarrow) $\vec{v} = 0$ or $\text{dir} \neq \text{north} \Leftarrow$ in a circle

$\equiv v \neq 0$ and $\text{dir} = \text{north} \Rightarrow$ diverge

if $v \neq 0$ and $\text{dir} = \text{north}$

\Rightarrow trivially, it will keep going
north!, #