

Max-Margin Structured Output Regression for Spatio-Temporal Action Localization

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Abstract

Structured output learning has been successfully applied to object localization, where the mapping between an image and an object bounding box can be well captured. Its extension to action localization in videos, however, is much more challenging, because one needs to predict the locations of the action patterns both spatially and temporally, i.e., identifying a sequence of bounding boxes that track the action in video. The problem becomes intractable due to the exponentially large size of the structured video space where actions could occur. We propose a novel structured learning approach for spatio-temporal action localization. The mapping between a video and a spatio-temporal action trajectory is learned. The intractable inference and learning problems are addressed by leveraging an efficient Max-Path search method, thus makes it feasible to optimize the model over the whole structured space. Experiments on two challenging benchmark datasets show that our proposed method outperforms the state-of-the-art methods.

1 Paper Body

Blaschko and Lampert have recently shown that object localization can be approached as structured regression problem [2]. Instead of modeling object localization as a binary classification and treating every bounding box independently, their method trains a discriminant function directly for predicting the bounding boxes of objects located in images. Compared with conventional sliding-window based approach, it considers the correlations among the output variables and avoids an exhaustive search of the subwindows for object detection. Motivated by the successful application of structured regression in object localization [2], it is natural to ask if we can perform structured regression for action localization in videos. Although this idea looks plausible, the extension from object localization to action localization is non-trivial. Different from object localization, where a visual object can be well localized by a 2-dimensional (2D) subwindow, human actions cannot be tightly bounded in such a similar way, i.e., using a

3dimensional (3D) subvolume. Although many current methods for action detection are based on this 3D subvolume assumption [6, 9, 20, 29], and search for video subvolumes to detect actions, such an assumption is only reasonable for ?static? actions, where the subjects do not move globally e.g., pick-up or kiss. For ?dynamic? actions, where the subjects can move globally e.g., walk, run, or dive, the subvolume constraint is no longer suitable. Thus, a more accurate localization scheme that can track the actions is required for localizing dynamic actions in videos. For example, one can localize an action by a 2D bounding box in each frame, and track it as the action moves across different frames. This localization structured output generates a smooth spatio-temporal path of connected 2-D bounding boxes. Such a spatio-temporal path can tightly bound the actions in the video space and provides a more accurate spatio-temporal localization of actions. 1

right
left top object bottom
a)
b)
c)

Figure 1: Complexities of object and action localization: a) Object localization is of $O(n^4)$. b) Action localization by subvolume search is of $O(n^6)$. c) Spatio-temporal action localization in a much larger search space. However, as the video space is much larger than the image space, spatio-temporal action localization has a much larger structured space compared with object localization. For a video with size $w \times h \times n$, the search space for 3D subvolumes and 2D subwindows is only $O(w^2 h^2 n^2)$ and $O(w^2 h^2)$, respectively (Figure 1). However, the search space for possible spatio-temporal paths in the video space is exponential $O(whnk \times n)$ [23] if we do not know the start and end points of the path (k is the number of incoming edges per node). Any one of these paths can be the candidates for spatiotemporal action localization, thus an exhaustive search is infeasible. This huge structured space keeps structured learning approaches from being practical to spatio-temporal action localization due to intractable inferences. This paper proposes a new approach for spatio-temporal action localization which mainly addresses the above mentioned problems. Instead of using the 3D subvolume localization scheme, we precisely locate and track the action by finding an optimal spatio-temporal path to detect and localize actions. The mapping between a video and a spatio-temporal action trajectory is learned. By leveraging an efficient Max-Path search method [23], the intractable inference and learning problems can be addressed, thus makes our approach practical and effective although the structured space is very large. Being solved as structured learning problem, our method can well exploit the correlations between local dependent video features, and therefore optimizes the structured output. Experiments on two challenging benchmark datasets show that our method significantly outperforms the state-of-the-art methods. 1.1

Related work

Human action detection is traditionally approached by spatio-temporal video volume matching using different features: space-time orientation [6], volumetric

[9], action MACH [20], HOG3D [10]. The sliding window scheme is then applied to locate actions which is ineffective and time-consuming. Different matching, learning models have also been introduced. Boiman and Irani proposed ensembles of patches to detect irregularities in images and videos [3]. Hu et al used multiple-instance learning to detect actions [8]. Mahadevan et al used mixtures of dynamic textures to detect anomaly events [15]. Le et al used deep learning to learn unsupervised features for recognizing human activities [14]. Niebles et al used a probabilistic latent semantic analysis model for recognizing actions [17]. Yao et al trained probabilistic non-linear latent variable models to track complex activities [28]. Yuan et al extended the branch-and-bound subwindow search [11] to subvolume search for action detection [29]. Recently, Tran and Yuan relaxed the 3D bounding box constraint for detecting and localizing medium and long video events [23]. Despite the improvements over 3D subvolume based approaches, this method did not fully utilize the correlations between local part detectors as they were independently trained. Max-margin structured output learning [19, 21, 24] was recently proposed and demonstrated its success in many applications. One of its attractive features is that although the structured space can be very large, whenever inference is tractable, learning is also tractable. Finley and Joachims further showed that overgenerating (e.g. relaxations) algorithms have theoretic advantages over undergenerating (e.g. greedy) methods when exact inference is intractable [7]. Various structured learning based approaches were proposed to solve computer vision problems including pedestrian detection [22], object detection [2, 25], object segmentation [1], facial action unit detection [16], human interaction recognition [18], group activity recognition [13], and human pose parsing [27]. More recently, Lan et al used a latent SVM to jointly detect and recognize actions in videos [12]. 2

Among these work, Lan et al is most similar to ours. However, this method requires a reliable human detector in both inference and learning, thus it is not applicable to ?dynamic? actions where the human poses are significantly varied. Moreover, because of its using HOG3D [26], it only detects actions in a sparse subset of frames where the interest points present.

2

Spatio-Temporal Action Localization as Structured Output Regression

Given a video x with the size of $w \times h \times m$ where $w \times h$ is the frame size and m is its length, to localize actions, one needs to predict a structured object y which is a smooth spatio-temporal path in the video space. We denote a path $y = \{(l, t, r, b)_i\}_{i=1..m}$ where $(l, t, r, b)_i$ are respectively the left, top, right, bottom of the rectangle that bounds the action in the i -th frame. These values of (l, t, r, b) are all set to zeros when there is no action in this frame. Because of the spatio-temporal smoothness constraint, the boxes in y are necessarily smoothed over the spatio-temporal video space. Let us denote $X \subset [0, 255]^3 \times [0, 255]^3 \times [0, 255]^3 \times [0, 255]^3 \times [0, 255]^3$ as the set of color videos, and $Y \subset \mathbb{R}^{4m}$ as the set of all smooth spatiotemporal paths in the video space. The problem of spatio-temporal action localization becomes to learn a structured prediction function of $f: X \rightarrow Y$. 2.1

Structured Output Learning

Let $\{x_1, \dots, x_n\} \subset X$ be the training videos, and $\{y_1, \dots, y_n\} \subset Y$

$y_n \} \subseteq Y$ be their corresponding annotated ground truths. We formulate the action localization problem using the structured learning as presented in [24]. Instead of searching for f , we learn a discriminant function $F : X \times Y \rightarrow \mathbb{R}$. F is a compatibility function which measures how compatible the localization y will be suited to the given input video x . If the model utilizes a parameter set of w , then we denote $F(x, y; w) = \langle w, \phi(x, y) \rangle$, which is a family of functions parameterized by w , and $\phi(x, y)$ is a joint kernel feature map which represents spatio-temporal features of y given x . Once F is trained, meaning the optimal parameter w^* is determined, the final prediction y^* can be obtained by maximizing F over Y for a specific input x . $y^* = f(x; w^*) = \arg\max_{y \in Y} F(x, y; w^*) = \arg\max_{y \in Y} \langle w^*, \phi(x, y) \rangle$

The optimal parameter set w^* is selected by solving the convex optimization problem in Eq. 2: $\min_w \sum_{i=1}^n \|w\|_k + C \sum_{i=1}^n \xi_i(w)$ s.t.

$$\begin{aligned} (1) \quad & y^* \in Y \\ & \langle w, \phi(x_i, y_i) \rangle - \langle w, \phi(x_i, y) \rangle - \langle w, \phi(y_i, y) \rangle \geq \xi_i, \forall y \in Y, \xi_i \geq 0, \forall i. \end{aligned}$$

(2)

Eq. 2 optimizes w such that the score of the true structure y_i of x_i will be larger than any other structure y by a margin which is rescaled by the loss of $\phi(y_i, y)$. The loss function will be defined in Section 2.3. This optimization is similar to the traditional support vector machine (SVM) formulation except for two differences. First, the number of constraints is much larger due to the huge size of the structure space Y . Second, the margins are rescaled differently by the constraint's loss $\phi(y_i, y)$. Because of the large number of constraints, the problem in Eq. 2 cannot be solved directly although it is a convex problem. Alternatively, one can solve the above problem by the cutting plane algorithm [24] or subgradient methods [19, 21]. We use the cutting plane algorithm to solve this learning problem. The algorithm starts with a random parameter w and an empty constraint set. At each round, it searches for the most violated constraint and add it to the constraint set. This step is to search for y that maximizes the violation value ξ_i (Eq. 3). When a new constraint is found, the optimization is applied to update w . The process is repeated until no more constraint is added. This algorithm is proven to converge [24] and normally within a small number of constraints due to the sparsity of the structured space. $\xi_i = \langle w, \phi(y_i, y) \rangle + \langle w, \phi(x_i, y) \rangle - \langle w, \phi(x_i, y_i) \rangle, \forall y \in Y, \xi_i \geq 0$ (3)

The Joint Kernel Feature Map for Action Localization

Let us denote $x \dashv y$ as the video portion cut out from x by the path y , namely the stack of images cropped by the bounding boxes $b_1 \dots b_m$ of y . We also denote $\phi(b_i) \in \mathbb{R}^k$ as a feature map for a 2D

box b_i . It is worth noting that $\phi(b_i)$ can be represented by either local features (e.g. local interest points) or global features (e.g. HOG, HOF) of the whole box b_i . We thus have a feature map for $x \dashv y$ as $\phi(x, y)$ which is also a vector in \mathbb{R}^k : $\phi(x, y) = \sum_{i=1}^m \phi(b_i)$ (4) Finally, the decision function of our structured prediction is now formed as in Eq. 5. $\phi(x, y) = \sum_{i=1}^m \phi(b_i)$ (5)

(5)

Loss Function

We define a Hinge loss function $\ell : \mathcal{Y} \times \mathcal{Y} \rightarrow [0, 1]$ for evaluating the loss induced by a predicted structure y compared with a true structure label y . We denote $y = \{b_i = 1..m\}$, where $b_i = (l, t, r, b)_i$ is the ground truth box of the i -th frame. Similarly, we denote $y = \{\hat{b}_i = 1..m\}$ the predicted structure. The loss function is defined as follow: $m \times \sum_{i=1}^m \ell(y_i, \hat{y}_i) = \sum_{i=1}^m (|b_i - \hat{b}_i| + 1)$, otherwise.

?1 if $\mathbf{b} = (0, 0, 0, 0)$ lb = (8) 1, otherwise.

3

Inference and Learning

We need a feasible way to perform the inference in Eq. 1 during testing which can be rewritten as in Eq. 9. $\max_{y \in Y} \sum_{i=1}^m h(w_i, y_i) = \arg\max_{y \in Y} \sum_{i=1}^m h(w_i, y_i)$. During training, we need to search for the most violated constraints by maximizing the right hand side of Eq. 3 which is equivalent to Eq. 10. From now on, we denote y_i for y_i in Eq. 2 because the example index i is no longer important. $\max_{y \in Y} \sum_{i=1}^m h(w_i, y_i) = \arg\max_{y \in Y} \sum_{i=1}^m h(w_i, y_i)$ (10). To solve Eq. 9 and Eq. 12, one needs to search for a smooth path y in the spatio-temporal video space Y which gives the maximum total score. Both of the above equations are difficult due to the large size of Y , e.g. the exponential number of possible spatio-temporal paths in Y (see supplemental material). We now show that both problems in Eq. 9 and Eq. 12 can be reduced to Max-Path search problem and solved by [23] efficiently. Max-Path algorithm [23] was proposed to detect dynamic video events. It is guaranteed to obtain the best spatio-temporal path in the video space provided that the local windows' scores can be precomputed. The algorithm takes a 3D trellis of local windows' scores as input, and outputs the best path which the maximum total score. In testing, the trellis's local scores are $h(w_i, y_i)$ where w_i is the local window. These values are easily evaluated given a w and a feature map f . In training, those values of the trellis are $h(b_i, y_i) + h(w_i, y_i)$ which are also computable given parameter w , feature map f , and ground truth b_i . After the trellis is constructed, the Max-Path algorithm is employed to find the best path, therefore we can identify the smoothed spatio-temporal path y that maximizes Eq. 9 and Eq. 12. 4

3.1

Constraint Enforcement

Let us consider one constraint in Eq. 2, here we ignore the index i of the example for simplicity and use $y^?$ as the ground truth for example x . We also denote $y = b1..m$ and $y^? = ?b1..m$.

[illegible]

quality of detections, e.g. how accurate are the predicted spatio-temporal paths compared with ground truth. More specific, detection is to answer the question "Is there any action of interest in this video?" while localization is to answer to "Provided that there is one action instance that appears in this video, where is it?". 5

Horse-ride; Subset test
0.6 0.4 0.2 0
0
0.2
0.4
0.6 Recall Horse-ride; All test
0.8
0.6
0.4
0
1
0.6 0.4 0.2
0
0.2
0.4
Recall
0.6
0.8
0
1
Run; All test
1
Tran&Yuan Our method
0.6
Precision
0.6
Precision
0.6
0.2
0.4
0.2
0.2
0.4
Recall
0.6
0.8
1
0
0.4
0.6 Recall Dive; All test
0.8

1
 0.8
 1
 Tran&Yuan Our method 0.8
 0.4
 0.2
 1
 0.8
 0
 0
 Tran&Yuan Our method
 0.8
 0
 Lan et al Tran&Yuan Our method
 0.8
 0.2
 1
 Precision
 1
 Lan et al Tran&Yuan Our method
 0.8
 Precision
 Precision
 0.8
 Dive; Subset test
 Run; Subset test
 1
 Lan et al Tran&Yuan Our method
 Precision
 1
 0.4
 0.2
 0
 0.2
 0.4
 Recall
 0.6
 0.8
 1
 0
 0
 0.2
 0.4
 Recall
 0.6

Figure 2: Action detection results on UCF-Sport: detection curves of our proposed method compared with [12] and [23]. Upper plots are detection results evaluated on subset frames given by [12], while lower plots are the results of all-frame evaluations. Except for diving, our proposed method significantly improves the other methods. Eval. Set Subset

Method H-Ride Run Dive Average [12] 21.75 19.60 42.67 28.01 [23] 62.19 50.20 16.41 42.93 Our 68.06 61.41 36.54 55.34 All [12] N/A N/A N/A N/A [23] 63.06 48.09 22.64 44.60 Our 64.01 61.86 37.03 54.30 Table 1: Action localization results on UCF-Sport: comparisons among our proposed method, [12], and [23]. The upper section presents results evaluated on a subset of frames given by [12], while the lower section reports results from evaluating on all frames. Our method improves 27.33% from [12] and 12.41% from [23] on subset evaluations and improves 9.7% from [23] on all-frame evaluations. N/A indicates not applicable.

5

Experimental Results

UCF-Sport: we compare our method with two current approaches: Lan et al [12], Tran and Yuan [23]. The output predictions of Lan et al are directly obtained from [12]. For [23], we train a linear SVM detector for each action class using the same features as ours. The Max-Path algorithm is then applied to detect the actions of interest. According to [12], its method used HOG3D [26], so that it is only able to detect and localize actions at a sparse set of frames where the HOG3D interest points present. To provide a fair comparison with [12], we report two different sets of evaluations. The first set is applied only to the subset of frames where [12] reports detections and the second set is to take all frames into consideration. Table 1 reports the results of action localization of different methods and action classes. On average, our method improves 27.33% from [12] and 12.41% from [23] on subset evaluations and improves 9.7% from [23] on all-frame evaluations. Figure 2 shows detection results of different methods on UCF-Sport dataset. Our method significantly improves over [23] for all three action classes on both subset and all-frame evaluations. Compared with [12] on subset evaluations, our method significantly improve over [12] on horse-riding and running detection. However, [12] provides better detection results than ours on diving detection. This better detection is because their interest-pointbased sparse features are more suitable to deformable actions as diving. For a complete presentation, we visualize localization results of our method compared with those of [12] and [23] on a diving sequence (Figure 3). All predicted boxes are plotted together with ground truth boxes for comparisons. It is worth noting that [12] has only predictions at a sparse set of frames, therefore blue 6

7

Localization score

0.8

20

45

28

51

0.6 0.4 Lan et al Tran&Yuan Our method
0.2 0
0
10
20
30 Frame number
40
50
60

Figure 3: Visualization of diving localization: the plots of localization scores of different methods on a diving video sequence. Lan et al’s [12] results are visualized in blue, Tran and Yuan’s [23] are green, ours are red, and ground truth are black boxes. Best view in color.

Figure 4: Action detection and localization on UCF-Sport: Lan et al’s [12] results are visualized in blue, Tran and Yuan’s [23] are green, ours are read, and ground truth are black. Our method and [23] can detect multiple instances of actions (two bottom left images). squares are visualized as discrete dots while the other methods are visualized by continuous curves. Our method (red curve) localizes diving action much more accurately than [23] (green curve). [12] localizes diving action fairly good, however it is not applicable when more accurate localizations (e.g. all frame predictions) are required. Oxford-TV: we compare our method with [23] on both detection and localization tasks. For detection, we report two different quantitative evaluations: the equal precision-recall (EPR) and the area under ROC curve (AUC). For localization, besides the spatial localization (SL) metric as used in UCF dataset experiments, we also evaluate different methods by temporal localization (TL) metric. This metric is not applicable to UCF dataset because most action instances in UCF dataset start and end at the first and last frame, respectively. Temporal localization is computed as the length Method EPR(%) AUC SL(%) TL(%) [18] 32.50* N/A N/A N/A [23] 24.14 0.27 18.46 40.09 Our 38.89 0.42 39.52 45.30 Table 2: Kiss detection and localization results. We improve 14.74% in equal precision/recall detection rate, 0.15 in area under ROC curve, 21.06% in spatial localization, and 5.21% in temporal localization over [23]. *Result of [18] is not directly comparable. N/A indicates not applicable. 7

Figure 5: Visualizaiton of kiss detection: our results are visualized in red; ground truths are in green. The upper two rows are some of correct detections while the last row shows false or missed detections.

1
0.5
0.8 Tran&Yuan: 8.82/10.34 Our method: 29.03/31.03
0.4
0.6
0.3
0.4
0.2
Tran&Yuan: 0.27 Our method: 0.42

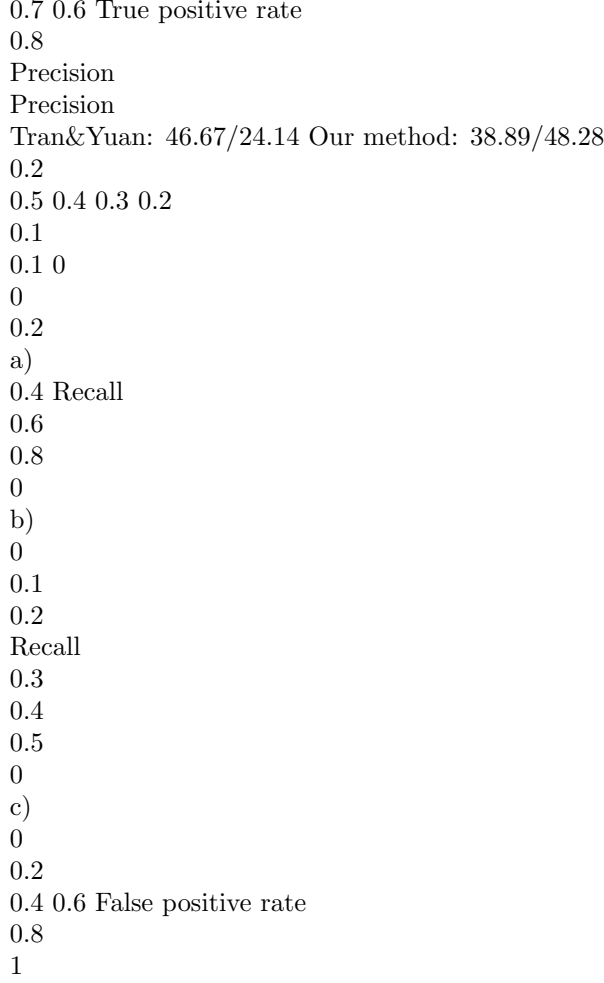


Figure 6: Kiss detection results: a) Precision-recall curves with $\tau = 0.2$. b) Precision-recall curves with $\tau = 0.4$. c) ROC curves with $\tau = 0.2$. Numbers inside the legends are best precision-recall values(a and b) and the area under ROC curve(c).

(measured in frames) of the intersection divided by the union of detection and ground truth. Table 2 presents detection and localization results of our proposed method compared with [23]. On localization task, our method improves 21.06% in spatial localization, and 5.21% in temporal localization over [23]. On detection task, by using the cut-off threshold $\tau = 0.2$, our method improves 14.74% in equal precision-recall rate and 0.15 in area under ROC curve over [23] (Figure 6a and 6c). One may further ask ?what if we need more accurate detections??. Interestingly, when we increase the cut-off threshold τ to 0.4, [23] significantly drops from 24.11% to 8.82% while our method remains 29.03% (Figure 6b) which demonstrates that our method can simultaneously detect and localize actions with high accuracy.

We have proposed a novel structured learning approach for spatio-temporal action localization in videos. While most of current approaches detect actions as 3D subvolumes [6, 9, 20, 29] or a sparse subset of frames [12], our method can precisely detect and track actions in both spatial and temporal spaces. Although [23] is also applicable to spatio-temporal action detection, this method cannot be optimized over the large video space due to its independently trained detectors. Our approach significantly outperforms [23] thanks to the structured optimization. This improvement gap is also consistent with the theoretic analysis in [7]. Moreover, being free from people detection and background subtraction, our approach can efficiently handle unconstrained videos and be easily extended to detect other spatio-temporal video patterns. Strong experimental results on two challenging benchmark datasets demonstrate that our proposed method significantly outperforms the state-of-the-arts. 8

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