

LTL Translations

BNFs for LTL formulae in Isabelle are as follows:

```
L ::= (alw (L)) | (ev (L)) | (nxt (L)) | ((L) until (L)) | (L C L) | ((L) C (L)) | not (L) | (not (L) | Pred

C ::= aand | or | impl

Pred ::= LabelEq 'string' | checkInx IOR nat Fun (Value Option) | StateEq (nat Option) | InputEq [Value list] | OutputEq [Value Option list] | InputLength nat | OutputLength nat

IOR ::= ip | op | rg

Value ::= Num nat | Str 'String'

'a Option ::= None | Some a

Fun = ValueEq | ValueGt | ValueLt | ValueGe | ValueLe
```

Normally, Isabelle is pretty lax with bracketing but the LTL package is really strict about it. We can always add more brackets (e.g. we could have $((\text{alw } (L)))$) but obviously this is silly and we wouldn't do it) but we can't have less brackets unless specified (such as $(L \text{ C } L)$ and $((L) \text{ C } (L))$ are both allowed).

Translations to SAL are as follows:

```
L_t ::= G(Lt) | F(Lt) | X(Lt) | U(Lt, Lt) | Lt Ct Lt | NOT(Lt) | Pred_t

C_t ::= AND | OR | NOT

Value_t ::= NUM nat | STR 'String_t'

Fun_t = value_eq | value_gt | value_lt | value_ge | value_le

String_t = String_String
```

Translating the Preds is a little more complicated as there are a couple of special cases so I'll explain these manually rather than with straight BNFs:

LabelEq 'string' goes to `label = String`

checkInx IOR nat Fun (Value Option) depends on the value of IOR. If it's ip then the translation is `gval(Fun_t(I(nat), (Value_t Option)))`. For op, the translation is similar but with 0 instead of I. If the value of IOR is rg then we need to index a register so we have `r_nat` in place of `I(nat)` or `0(nat)`.

StateEq (nat Option) depends on whether `nat Option` is None or Some `n`. If it's None, we get `cfstate = NULL_STATE`. If it's Some `n` then we get `cfstate = State_n`.

InputEq [Value list] involves recursively building a sequence from the `Value list`. The final translation will be `I = translateValueList`. Translating value lists proceeds as follows:

```
translateValueList([]) = InputSequence ! empty
translateValueList((Num n)#t) = InputSequence ! insert(NUM n, translateValueList(t))
translateValueList((Str s)#t) = InputSequence ! insert(STR String_t, translateValueList(t))
```

OutputEq [Value Option list] is similar to InputEq. The final translation will be `O = translateValueOptionList` where the translation of the argument proceeds as follows:

```
translateValueOptionList([]) = OutputSequence ! empty
translateValueList((Some (Num n))#t) = OutputSequence ! insert(Some(NUM n), translateValueList(t))
translateValueList((Some (Str s))#t) = OutputSequence ! insert(Some(STR String_t), translateValueList(t))
translateValueList(None#t) = OutputSequence ! insert(None, translateValueList(t))
```

InputLength nat goes to `InputSequence ! size?(I)`

OutputLength nat goes to `OutputSequence ! size?(O)`