# PhenStat:

statistical analysis of phenotypic data using Linear Mixed Models and Fisher Exact Test **User's Guide** 

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## Contents

## 1 Introduction

High-throughput phenotyping generates large volumes of varied data including both categorical and continuous data. Operational and cost constraints can lead to a work-flow that precludes traditional analysis methods. Furthermore, for a high throughput environment, a robust automated statistical pipeline that alleviates manual intervention is required.

PhenStat is a package that provides statistical methods for the identification of abnormal phenotypes. The package contains dataset checks and cleaning in preparation for the analysis. For continuous data, an iterative fitting process is used to fit a regression model that is the most appropriate for the data (Mixed Model framework), whilst for categorical data; a Fisher Exact Test is implemented (Fisher Exact Test framework).

Both analysis frameworks output a statistical significance measure, an effect size measure, model diagnostics (when appropriate), and graphical visualisation of the genotype effect.

The Mixed Model (MM) framework is an iterative process to select the best model for the data which considers both the best modelling approach (mixed model or general linear regression) and which factors to include in the model. There is also user control functionality on whether to include body weight in the modelling process.

Depending on the user needs, the statistical analysis output can either be interactive where the user can view the graphical output and analysis summary or for a database implementation the output consists of a vector of output and saved graphical files.

This package has been tested and demonstrated with an application of 420 lines of historic mouse phenotyping data.

The package consists of three stages as shown in Figure ??:

- 1. Dataset processing: includes checking, cleaning and terminology unification procedures and is completed by function *PhenList* which creates a *PhenList* object.
- 2. Statistical analysis: is managed by function *testDataset* and consists of Mixed Model or Fisher Exact framework implementations. The results are stored in *PhenTestResult* object. Potentially this layer can be extended adding new statistical methods (dotted box in Figure ??).

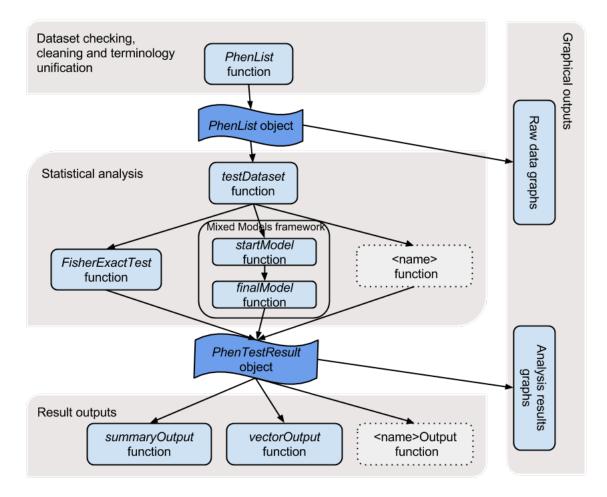


Figure 1: The PhenStat package's three stage structure: dataset processing, analysis, and result output. Dotted boxes show the place-holders for new functions that could implement other methods for data analysis and/or output of results.

3. Results Output: depending on user needs there are two functions for the test results output: summaryOutput and vectorOutput that present data from PhenTestResult object in a particular format. The output layer is also easily extendible (shown as dotted box in Figure ??).

The estimates of the package run time depends a lot on a size of a dataset used for analysis. In average the analysis **run time** regardless the method used and the size of the dataset is **1.34 seconds**.

## 2 Data Processing with PhenList Function

PhenList function performs data processing and creates a PhenList object. As input PhenList function requires dataset of phenotypic data that can be presented as data frame. For instance, it can be dataset stored in csv or txt file.

```
> dataset <- read.csv("myPhenotypicDataset.csv")
> dataset <- read.table("myPhenotypicDataset.txt",sep="\t")</pre>
```

Data is organised with a row for a sample and each column provides information such as meta data (strain, genotype, etc.) and the variable of interest.

In the Table ?? the example dataset is presented with numerical variables of interest. The Table ?? shows the example dataset with categorical data. Mandatory columns are "Genotype" and "Gender". "Assay.Date" column is used to model "Batch" effect if not specified differently. "Weight" column is used to model body weight effect.

The main tasks performed by the PhenStat package's function *PhenList* are:

- terminology unification (see section ?? for more details),
- filtering out undesirable records (when the argument dataset.clean is set to TRUE),
- and checking if the dataset can be used for the statistical analysis.

All tasks are accompanied by messages with errors, warnings and/or information: error messages explain why function stopped, warning messages require user's attention (for instance, user is notified that column was renamed in the dataset), information messages provide some details (for instance, Genotype levels). If messages are not desirable *PhenList* function's argument *outputMessages* can be set to FALSE meaning there will be no messages.

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Lean. Mass	17.29 15.99 17.73	14.84 17.34 15.84	15.38 18.31	19.64	21.91	24.25	20.25	19.54 20.07	18.93	19.71	18.66	21.71	19.41	18.33	17.92	19.12	18.17	19.46	19.12	17.67	:
Bone. Area	8.46 7.95 8.95	8.43 8.79 8.52	7.46 9.73	11	10.28	10.08	9.25	8.88	8.75	8.8	9.69 8 8	10.42	8.84	10.03	80.6	8.91	9.01	9.94	9.27	8.51	:
Bone Mineral. Density	0.0443 0.0427 0.0451	0.0443 0.047 0.0433	0.0419 0.0454	0.0471	0.0483	0.0483	0.0465	0.0465 $0.0444$	0.0461	0.0512	0.0519	0.0529	0.0474	0.0501	0.0477	0.0514	0.0496	0.0524	0.0503	0.0468	:
Weight	26.7 27.6 30.7	24.9 27.9 25.1	21.7 32.8	38 34.9	38.5 7.8 8.0	40.6	35.1	33.2 32.6	23.9	33.8	29 26 5	40.7	26.1	33.1	30.5	34	31.9	35.6	32.7	31.2	:
Age.In. Weeks	13.7 13.7 13.7	14.3 14	14 13.9	13.9 13.9	14.1	14.1	14	14 14	14.3	14	14.3	14.1	13.1	13.9	13.9	14	14	14	14	14.1	:
Assay. Date	07-Aug-09 07-Aug-09 07-Aug-09	07-Aug-09 23-Nov-09 23-Nov-09	23-Nov-09 23-Jun-09	23-Jun-09 23-Jun-09	06-Jan-10	06-Jan-10	01-Mar-10	01-Mar-10 01-Mar-10	05-May-09	07-May-09	07-May-09	08-May-09	08-May-09	08-May-09	14-May-09	14-May-09	14-May-09	14-May-09	15-May-09	18-May-09	:
Gender	Female Female Female	Female Female	Female Male	Male Male	Male Male	Male	Male Mêlê	Male Male	Female	Female	Female Female	Female	:								
Genotype	Sparc/Sparc Sparc/Sparc Sparc/Sparc	Sparc/Sparc Sparc/Sparc	Sparc/Sparc Sparc/Sparc	Sparc/Sparc Sparc/Sparc	Sparc/Sparc	Sparc/Sparc	Sparc/Sparc	Sparc/Sparc Sparc/Sparc	+/+	+/+	+ + + +	- +/-+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	:
Mouse	M00260466 M00260467 M00260468	M00260475 M00330799 M00330800		M00226963 M00226964	M00354835 M00354836			M00405766 M00405767	M00194360	M00191904	M00191913 M00191104	M00191105	M00195130	M00191134	M00197544	M00197565	M00197566	M00197567	M00197538	M00195664	:
Gene. Name	Sparc Sparc Sparc	Sparc Sparc Sparc	Sparc Sparc	Sparc Sparc	Sparc	Sparc	Spare	Sparc Sparc	Ccdc57	Yipf1	m Yipf1	Gatc	Gatc	Gatc	Mgst3	Mgst3	Mgst3	Mgst3	Myo5a	Setdb1	:
Colony. Prefix	MBAU MBAU MBAU	MBAU MBAU MBAU	MBAU MBAU	MBAU MBAU	MBAU	MBAU	MBAU	MBAU	MALA	MAOA	MAOA	MBFD	MBFD	MBFD	MBHU	MBHU	MBHU	MBHU	MBRR	MAIT	:

Table 1: The dataset example.

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Thoracic.	Processes	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Abnormal	Normal	Normal	Normal	Normal	Normal	Normal	Abnormal	Normal	Normal	Normal	Abnormal	Normal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnorma]	Abnormal	Abnormal	Abnormal	Abnorma	Abnormal	
Lumbar.	Processes	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	:
Cervical.	Processes	Abnormal	Normal	Abnormal	Normal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Normal	Abnormal	Abnormal	Abnormal	Abnormal	Normal	Normal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	Abnormal	:
Caudal.	Processes	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	Normal	:
Age.In.	Weeks	13.9	13.9	13.9	13.9	14	14	14	14	13.9	13.9	14	14	14	13.9	13.9	13.9	13.9	13.9	13.9	13.9	13.9	13.9	14	14	14.3	14.3	14.3	14.1	14.1	13.7	13.7	:
Assay.	Date	12-Mar- $12$	04-Jul-12	04-Jul-12	04-Jul-12	04-Sep-12	04 -Sep-12	04 egrid - Sep-12	04 -Sep-12	17-Jul-12	17-Jul-12	06-Aug- $12$	06-Aug- $12$	06-Aug- $12$	01-May-12	01-May-12	01-May-12	04-Jul-12	04-Jul-12	$20\text{-}\mathrm{Dec}$ - $12$	$20\text{-}\mathrm{Dec}$ - $12$	19-Sep-12	30-Apr-12	13-Jun-12	30-Apr-12	31-Jul-12	31-Jul-12	28-Mar-12	18-Dec-12	18-Dec-12	23-May- $12$	13-Jun-12	:
Gender		Male	Male	Female	Female	Male	Male	Male	Female	Female	Female	Male	Male	Male	Male	Male	Male	Male	Male	Female	Female	Female	Female	Male	Female	Female	Female	Male	Male	Male	Female	Female	:
Genotype		+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	+/+	Aff3/+	Aff3/+	Aff3/+	Aff3/+	Aff3/Aff3	Aff3/Aff3	:							
Mouse		M01005699	M01114643	M01108371	M01108373	M01167360	M01167394	M01167391	M01167363	M01128905	M01128906	M01140446	M01140447	M01140448	M01051596	M01049783	M01051598	M01114647	M01114649	M01268599	M01268600	M01176405	M01048233	M01087975	M01051403	M01127511	M01127512	M01024260	M01257342	M01257339	M01069212	M01087552	:
Gene.	Name	Smarcall	Egfr	Srrm4	Srrm4	Gpr107	Gpr107	Gpr107	Gpr107	Fam175b	Fam175b	Slitrk4	Slitrk4	Slitrk4	G3bp2	Map3k1	G3bp2	Egfr	Egfr	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	Aff3	:
Colony.	Prefix	MAPP	MCUB	MDYA	MDYA	MEFV	MEFV	MEFV	MEFV	MDYQ	MDYQ	MEGD	MEGD	MEGD	MDWN	MDDY	MDWN	MCUB	MCUB	MCND	MCND	MCND	MCND	MCND	MCND	MCND	MCND	MCND	MCND	MCND	MCND	MCND	:

Table 2: The dataset example with categorical data.

Here is an example when the user sets out-messages to FALSE:

```
> dataset1 <- read.csv("./PhenStat/extdata/test.csv")

# Default behaviour with messages
> test <- PhenList(dataset=dataset1,
    testGenotype="Sparc/Sparc")

Warning:
Dataset's column 'Assay.Date' has been renamed to 'Batch' and will be used for the batch effect modelling.

Information:
Dataset's 'Genotype' column has following values: '+/+', 'Sparc/Sparc'

Information:
Dataset's 'Gender' column has following value(s): 'Female', 'Male'

# Out-messages are switched off
> test <- PhenList(dataset=dataset1,
    testGenotype="Sparc/Sparc",
    outputMessages=FALSE)

# There are no messages!</pre>
```

## 2.1 Terminology Unification

Under the term "terminology unification" we mean the matching of the terminology for the data (variables) that are essential for the analysis. The PhenStat package uses the following nomenclature for the names of columns: "Gender", "Genotype", "Batch" or "Assay.Date" and "Weight". In addition expected gender values are "Male" and "Female" and missing value is NA. PhenList function creates a copy of the dataset and then uses internal arguments that help to map columns and values from user's naming system into the package's nomenclature. The original file with the dataset stays unchanged since all changes take place within PhenList object. Please note "Assay.Date" is renamed to "Batch" automatically.

The following *PhenList* function's arguments have to be specified to enable terminology unification to match expected columns to user names:

- dataset.colname.batch allows the user to define column name within dataset for the batch effect if this column name is other than "Batch" or "Assay.Date" (user's definition has a priority over "Assay.Date"),
- dataset.colname.qenotype allows the user to define column name within

dataset for the genotype info if this column name is other than "Genotype",

- dataset.colname.gender allows the user to define column name within dataset for the gender info if this column name is other than "Gender" in the dataset,
- dataset.colname.weight allows the user to specify column name within dataset for the weight info if this column name is other than "Weight" in the dataset,
- dataset.values.missing Value allows the user to specify value used as missing value in the dataset if other than NA,
- dataset.values.male allows the user to define value used to label "males" in the dataset if other than "Male",
- dataset.values.female allows the user to specify value used to label "females" in the dataset if other than "Female" value has been used.

In the example below dataset's values for females and males are 1 and 2 accordingly. Those values are changed to "Female" and "Male".

```
> dataset_test <- read.csv("./PhenStat/extdata/test3.csv")
> test <- PhenList(dataset=dataset_test,
    dataset.clean=TRUE,
    dataset.values.female=1,
    dataset.values.male=2,
    testGenotype="Mysm1/+")

Warning:
Dataset's column 'Assay.Date' has been renamed to 'Batch' and will be used for the batch effect modelling.

Information:
Dataset's 'Genotype' column has following values: '+/+', 'Mysm1/+'

Information:
Dataset's 'Gender' column has following value(s): 'Female', 'Male'</pre>
```

## 2.2 Filtering

Filtering is required, as the statistical analysis requires there to be only two genotype groups for comparison (e.g. wild-type versus knockout). Thus the function PhenList requires users to define the reference genotype (mandatory argument refGenotype with default value "+/+") and test genotype

(mandatory argument testGenotype). If the PhenList function argument dataset.clean is set to TRUE then all records with genotype values others than reference or test genotype are filtered out. The user may also specify hemizygotes genotype value (argument hemiGenotype) then hemizygotes are treated as test genotype. This is necessary to manage sex linked genes, where the genotype will be described differently depending on the sex but biologically then should be equivalent. Consider the following example of a knockout of a X-linked gene. In this situation, Table ?? describes the possible genotype labels and which should be compared biologically.

Sex	Reference genotype	Test genotype	Heterozygous genotype
Female	+/+	KO/KO	+/KO
Male	+/+	KO/Y	

Table 3: Example of the dataset with sex linked genes

With the dataset described in Table ?? when hemiGenotype argument of the PhenList function is defined as "KO/Y" the actions of the function are: "KO/Y" genotypes are relabelled to "KO/KO" for males; females "+/KO" heterozygous are filtered out.

```
> dataset1 <- read.csv("sex_linked_genes.csv")
> test <- PhenList(dataset=dataset1,
    testGenotype="KO/KO",
    refGenotype="KO/Y")

Warning:
Dataset's column 'Assay.Date' has been renamed to 'Batch' and will be used for the batch effect modelling.

Warning:
Hemizygotes 'KO/Y' have been relabeled to test genotype 'KO/KO'.
If you don't want this behaviour then don't define 'hemiGenotype' argument.

Information:
Dataset's 'Genotype' column has following values: '+/+', 'KO/KO'

Information:
Dataset's 'Gender' column has following value(s): 'Female', 'Male'</pre>
```

If a user would like to switch off filtering (s)he can set *PhenList* function's argument *dataset.clean* to FALSE (default value is TRUE). In the following example the same dataset is processed successfully passing the checks procedures (see section ??) when *dataset.clean* is set to TRUE and fails at checks otherwise.

```
> dataset <- read.csv("test_3genotypes.csv")</pre>
> test<-PhenList(dataset,
testGenotype="Mysm1/+")
Warning:
Dataset's column 'Assay.Date' has been renamed to 'Batch' and will be used for the batch effect modelling.
Dataset has been cleaned by filtering out records with genotype value
other than test genotype 'Mysm1/+' or reference genotype '+/+'.
Dataset's 'Genotype' column has following values: '+/+', 'Mysm1/+'
Information:
Dataset's 'Gender' column has following value(s): 'Female', 'Male'
# Filtering is switched off
> test<-PhenList(dataset,
testGenotype="Mysm1/+",
dataset.clean=FALSE)
Dataset's 'Batch' column is missed.
You can define 'dataset.colname.batch' argument to specify column
for the batch effect modelling. Otherwise you can only fit a glm.
Information:
Dataset's 'Genotype' column has following values: '+/+', 'HOM', 'Mysm1/+'
Information:
Dataset's 'Gender' column has following value(s): 'Female', 'Male'
****** Errors start ******
Check failed:
Dataset's 'Genotype' column has to have two values.
You can define 'testGenotype' and 'refGenotype' arguments to automatically
filter out records with genotype values other than specified.
Alternatively you can define 'hemiGenotype' and 'testGenotype' arguments to relabel hemizygotes to homozygotes.
****** Errors end *******
```

Filtering also takes place when there are records that do not have at least two records in the dataset with the same genotype and gender values.

Consider the following example of the genotype and gender values in the dataset:

Sex	Reference genotype	Test genotype
Female	+/+	Mysm1/+
Male	+/+	Mysm1/+
unsexed		Mysm1/+ (1 record only)

Table 4: Example of the dataset with 3 gender values

When *dataset.clean* argument's is set to TRUE all "unsexed" records are filtered out since there are no records for genotype "+/+" and only one record for "Mysm1/+".

#### 2.3 Dataset Checks

After terminology unification and filtering tasks, *PhenList* function checks the dataset availability for the statistical analysis:

- column names and gender values are there and described in the package's nomenclature,
- test and reference genotype records are in the dataset,
- there are at least two records for each genotype/gender values combination.

If one of the checks fails function stops and the PhenList object is not created. In the following example "Gender" column is missed in the dataset and checks fail. Note, a dataset can consist of one gender but a gender column is still required to ensure the appropriate model is fitted.

Next example shows the results of the dataset described in the previous section ??: three gender values and not enough records for the "unsexed" gender and both genotype values.

```
> dataset <- read.csv("test_3genders.csv")</pre>
> test<-PhenList(dataset,
testGenotype="Mysm1/+")
Warning:
Since dataset has to have at least two data points for each genotype/gender combination
and there are not enough records for the combination(s): '+/+'/'unsexed' (0),
 'Mysm1/+'/'unsexed' (1), appropriate gender records have been filtered out from the dataset.
# Filtering is switched off
> test<-PhenList(dataset.
testGenotype="Mysm1/+",
dataset.clean=FALSE)
****** Errors start ******
Check failed:
Dataset's 'Gender' column has to have one or two values and currently the data has more than two.
Dataset's 'Gender' column has 'Female', 'Male', 'unsexed' values
instead of 'Female' and/or 'Male' values only.
Please delete records with gender(s) 'unsexed' from the dataset.
Check failed:
Dataset should have at least two data points for each genotype/gender combination.
At the moment there are no enough data points for the following combination(s):
'+/+'/'unsexed' (0), 'Mysm1/+'/'unsexed' (1).
****** Errors end ******
```

Many checking failures will be avoided when *dataset.clean* argument of the *PhenList* function is set to TRUE (default value). See examples in this and in the previous section ??.

## 2.4 PhenList Object

The output of the *PhenList* function is *PhenList* object that contains cleaned dataset (*PhenList* object's section *dataset*), simple statistics about dataset columns and additional information.

The example below shows how to print out the whole cleaned dataset and how to view the statistics about it (output is shown in Table ??).

```
> dataset1 <- read.csv("./PhenStat/extdata/test.csv")
> test <- PhenList(dataset=dataset1,
    testGenotype="Sparc/Sparc", outputMessages=FALSE)
> test$dataset
...
> test$dataset.stat
```

Table ?? shows the content of the *PhenList* object's section *dataset.stat* and describes the data focusing on the columns of the dataset. Each column is a variable with summary description. The description includes: whether variable is numerical or not, whether variable's classed continuous (variability is more than 0.5%), number of levels, number of data points and for the numerical variables various summary measures (mean, standard deviation, minimal and maximal values).

PhenList object has stored many characteristics about the data: reference genotype, test genotype, hemizygotes genotype, original column names, etc.

An example is given below.

```
> dataset2 <- read.csv("./PhenStat/extdata/test2.csv")
> test2 <- PhenList(dataset=dataset2,
testGenotype="Arid4a/Arid4a",
dataset.colname.weight="Weight.Value")
> test2$testGenotype
[1] "Arid4a/Arid4a"
> test2$refGenotype
[1] "+/+"
> test2$dataset.colname.weight
[1] "Weight.Value"
```

## 3 Statistical Analysis

The PhenStat package provides two methods (frameworks) for statistical analysis: Linear Mixed Models for continuous data and Fisher Exact Test for categorical data. For both the MM and FE framework, the statistical

Variable	Num	Cont	Levels	#	Mean	StdDev	Min	Max
Age.In.Weeks	TRUE	FALSE	10	468	14	0.21	13.1	14.6
Batch	FALSE	FALSE	49	468	NA	NA	NA	NA
Birth.Date	FALSE	FALSE	111	468	NA	NA	NA	NA
Bone.Area	TRUE	TRUE	248	463	9.6	0.84	7.46	11.73
Bone.Mineral.Content	TRUE	TRUE	405	463	0.48	0.06	0.31	0.64
Bone.Mineral.Density	TRUE	TRUE	120	463	0.05	0	0.04	0.06
Cohort.Name	FALSE	FALSE	59	468	NA	NA	NA	NA
Colony.Name	FALSE	FALSE	76	468	NA	NA	NA	NA
Colony.Prefix	FALSE	FALSE	76	468	NA	NA	NA	NA
Core.Strain	FALSE	FALSE	1	468	NA	NA	NA	NA
Tissue.Mass	TRUE	TRUE	427	463	35.22	5.3	20.44	49.86
Fat.Mass	TRUE	TRUE	385	463	14.92	3.35	4.52	23.21
Fat.Percentage	TRUE	TRUE	403	463	42.01	5.16	19.26	55.21
Full.Strain	FALSE	FALSE	9	468	NA	NA	NA	NA
Gender	FALSE	FALSE	2	468	NA	NA	NA	NA
Gene.Name	FALSE	FALSE	76	468	NA	NA	NA	NA
Genotype	FALSE	FALSE	2	468	NA	NA	NA	NA
Lean.Mass	TRUE	TRUE	369	463	20.31	2.81	14.84	28.8
Mouse	FALSE	FALSE	468	468	NA	NA	NA	NA
Mouse.Name	FALSE	FALSE	468	468	NA	NA	NA	NA
Base.Length	TRUE	FALSE	17	468	10.19	0.32	9.3	10.9
Pipeline	FALSE	FALSE	1	468	NA	NA	NA	NA
Strain	FALSE	FALSE	2	468	NA	NA	NA	NA
Weight	TRUE	TRUE	183	468	34.95	5.09	20.4	48.4

Table 5: Simple statistics about dataset variables – dataset.stat content

significance is assessed, the biological significance measured through an effect size estimate and finally the genotype effect is classified e.g. "If phenotype is significant - both sexes equally".

PhenStat's function *testDataset* works as a manager for the different statistical analyses methods. It checks the dependent variable, runs the selected statistical analysis framework and returns modelling/testing results in the *PhenTestResult* object (see Figure ??).

# 3.1 Manager for Analysis Methods - testDataset function

The testDataset function's argument phenList defines the dataset stored in PhenList object.

Function's argument dep Variable defines the dependent variable.

Function's argument *method* defines which statistical analysis framework to use. The default value is "MM" which stands for mixed model framework. To perform Fisher Exact Test, the argument *method* is set to "FE".

The *testDataset* function performs basic checks which ensure the statistical analysis would be appropriate and successful:

- 1. dep Variable column is present in the dataset;
- 2. dep Variable is numeric for Mixed Model (MM) framework, otherwise Fisher Exact Test (FE) is performed;
- 3. dep Variable column values are variable enough (variability > 0.5%) for MM framework, otherwise FE framework is recommended;
- 4. Each one genotype level has more than one *depVariable* level for MM framework, otherwise FE framework is recommended;
- 5. Number of dep Variable levels is 10 or less for the FE framework.

If issues are identified, clear guidance is returned to the user. After the checking procedures, *testDataset* function runs the selected framework to analyse dependent variable.

To ensure flexibility and debugging, the framework can comprise of more than one stage. For instance, the more complex MM framework has the functionality to operate in two stages.

testDataset function's argument callAll instructs the package to run all stages of the framework one after another when set to TRUE (default behaviour).

However, when callAll flag is set to FALSE it instructs the testDataset function to run only the first stage of the selected framework. For instance, testDataset function runs startModel and after that finalModel functions of the MM framework if the argument callAll is set to TRUE. More information about this two stages process is provided in section ??.

If framework contains only one stage (such as the Fisher Exact Test case)

then testDataset function runs that single stage regardless of the callAll argument's value.

The example how to call MM and FE framework is given below.

```
> dataset1 <- read.csv("./PhenStat/extdata/test.csv")
> test <- PhenList(dataset=dataset1,
    testGenotype="Sparc/Sparc", outputMessages=FALSE)
> result_MM_Lean.Mass <- testDataset(test,depVariable="Lean.Mass", method="MM")
...
> result_FE_Length <- testDataset(test,depVariable="Nose.To.Tail.Base.Length", method="FE")</pre>
```

Further details about the MM and FE framework are in the next two subsections.

#### 3.2 Mixed Model Framework

First, we will describe the mixed model top-down methodology which starts with a fully loaded model and ends with final reduced model and genotype effect evaluation procedures as described in ?.

#### 3.2.1 Motivation

Through high throughput phenotyping programs, such as EUMODIC , where data was systematically collected on one genetic background, the significant sources of variation can be identified and it became obvious that batch (defined here as those readings collected on a particular day) can lead to large variation in phenotyping variables ?.

Figure ??, demonstrates variation seen in control data from a standardised phenotyping pipeline.

Figure ??, demonstrates using artificially constructed data how mathematically this can arise from batch variation adding variability to the data. With this batch to batch variation, data collected on the same day will be more similar than other days, hence the readings are correlated and the assumption, of many statistical tests, of independent readings cannot be made. Furthermore, the variation with batch, means that this has to be considered to be able to assign causality i.e. if there is a difference in readings is this due to batch or genotype difference. Therefore these observations have

significant implications for the data analysis of both high throughput and secondary phenotyping experiments where use of small batches of animals is common.

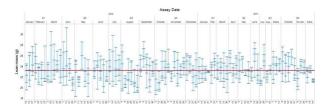


Figure 2: Representative time course plot showing the batch to batch variation in control data for male mice from a B6Brd;B6N- $Tyr^{c-Brd}$  genetic background from WTSI MGP program. Example shown is the variation seen in the lean mass variable measured in grams. For each day, data is collected a box plot is drawn as a five point summary indicating the minimum, 1<sup>st</sup> quartile, median, 3<sup>rd</sup> quartile and maximum. Shown in red is the global median fat mass value.

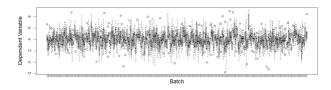


Figure 3: Artificially constructed data demonstrating how batch variation affects data distribution with time. In this artificial data, the variable of interest was assumed to be biologically randomly normally distributed variable with mean=7, standard deviation=1.5. To represent the batch effect, 300 assays days were generated with a randomly distributed batch effect (mean=0, standard deviation 0.5) which was added to the dependent variable biological mean before randomly sampling the dependent variable.

One option would be to ensure all animals for a line are processed in one day with concurrent controls. However, it is challenging and costly to produce sufficient animals of the right age within a narrow time point for an experiment. Consider the WTSI Sanger Mouse Genetics Project which requires 7 male and 7 female homozygote mice, generated by a heterozygote cross; a best case scenario would require 14 mating pairs being assembled at the same point in time? In order to generate these mating pairs, there would be a staged breeding process to generate the mice which involve several rounds of expansions depending on breeding success. This best case scenario is commonly hampered by fecundity, viability or other phenotypic problems within

a line and hence to achieve a one batch pipeline the pairing number needs increasing significantly. In contrast, by accepting smaller numbers of mice in multiple batches, lower breeding pair numbers can be established. The smaller scale allows the generation of mice to answer firstly developmental and breeding issues and secondly to feed the pipeline over time and subsequent litters. As soon as mice are produced at the right age, these are feed into the pipeline. This batch approach, allows the pipeline to utilise animals that would otherwise be discarded as the process had not generated the required experimental sample size which ensure meet the high throughput pipeline needs and also help reduce the breeding cost per line. Furthermore, the operational constraints arising in a high throughput environment make optimal experimental design impractical; typically mutant and control mice are not assayed on the same day, so any phenotypic differences could be due to genotype or to subtle changes in the environment (e.g. temperature fluctuations or pipetting errors).

An alternative method, linear mixed models (MM) are a class of statistical models suited to modelling multiple sources of variability on a phenotype, where some explanatory factors (such as sex, weight and mutant genotype) are assumed to take fixed values that affect the population mean, whilst others such as batch are treated as affecting the covariance structure; animals from the same batch will have correlated phenotypes. ? demonstrated the utility and benefits of a MM framework for high throughput phenotyping data. The methodology used there has been developed further and refined for this package.

### 3.2.2 Theory

There are two possible start models, depending on whether weight is included as a factor (see ?? for the model without weight and ?? for the model including weight).

$$depVariable \sim Genotype + Gender + Genotype * Gender$$
 (Eq1)

$$depVariable \sim Genotype + Gender + Genotype * Gender + Weight$$
(Eq2)

We reference to the ?? and ?? as to the models with "loaded" mean structure and random batch-specific intercepts or fully loaded model (see Figure ??).

The final model construct is influenced by a number of criteria. These criteria, such as fixed effects, batch effect and the structure of residual variances, can be either evaluated from the dataset or defined by user (see Figure ??). The following criteria (effects) are considered:

- Batch effect (batch variation). Considered only when batch column is present in the dataset.
- Residual variances homogeneity where homogeneous residual variances means the variance for all genotype levels is considered equivalent.
- Body weight effect. Considered only when Eq2 is used.
- Gender effect. Considered only when there are more than one gender in the dataset.
- Genotype by gender interaction effect. Considered only when there are more than one gender in the dataset.

The selection of model is influenced by the batch effect (random effects) — is batch in the dataset, and if so, is it significant in explaining variation in the dependent variable — and a covariance structure for the residuals that can be homogeneous or heterogeneous (see Figure ?? Step 1-3). The selected model is then modified by reducing non-significant effects (see Figure ?? Step 4 and Figure ??).

When the final model is selected and reduced, the genotype effect is assessed by comparing a genotype and null model fitted with maximum likelihood evaluation method (ML). Finally, the final genotype model is refitted using restricted maximum likelihood evaluation method (REML) to get unbiased estimates of the variance parameters (see Figure ?? Step 5,6 and Figure ??).

#### 3.2.3 Implementation

There are two functions in the PhenStat package that implements the mixed model framework:

- startModel function evaluates model's criteria and stores the result in the PhenTestResult object;
- finalModel function builds the final model using the model's criteria from PhenTestResult object and fits the model using restricted maximum likelihood method (REML).

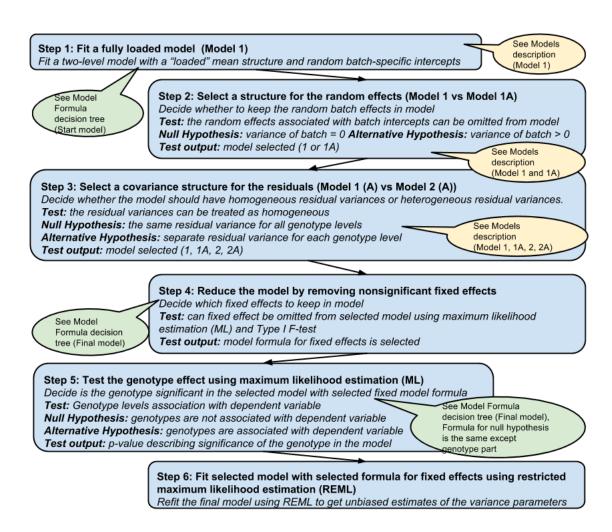


Figure 4: MM framework steps: model selection process and model reducing by using significance of fixed effects.

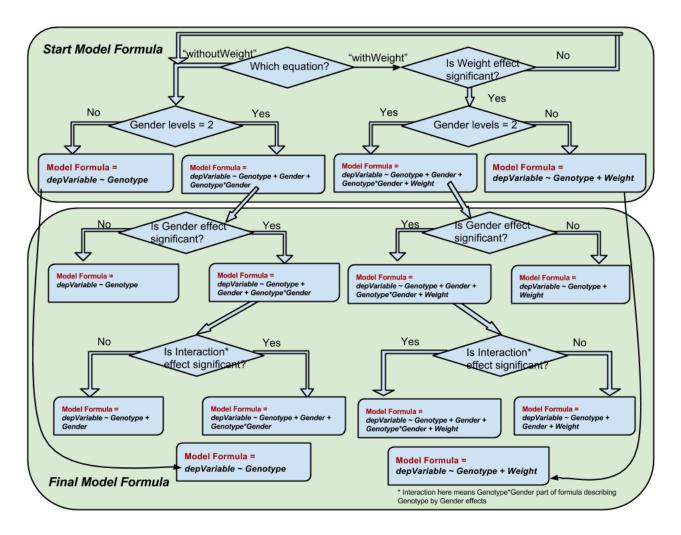


Figure 5: MM framework: start model formula and final model formula creation based on the dataset and significances of the effects (can be estimated or defined by user).

Model 1

fixed effects: Start or Final Model Formula

random effects: Batch

residual variance: the same residual variance for all Genotype levels

fitting method: linear mixed-effects model (Ime\* in R)

Model 1A

fixed effects: Start or Final Model Formula

random effects: none

residual variance: the same residual variance for all Genotype levels

fitting method: generalized least squares (gls in R)

Model 2

fixed effects: Start or Final Model Formula

random effects: Batch

residual variance: separate residual variance for each Genotype level

fitting method: linear mixed-effects model (Ime\* in R)

Model 2A

fixed effects: Start or Final Model Formula

random effects: none

residual variance: separate residual variance for each Genotype level

fitting method: generalized least squares (gls in R)

Figure 6: MM framework: different models that are considered.

<sup>\*</sup> Ime - fits a linear mixed-effects model in the formulation described in Laird and Ware (1982) but allowing for nested random effects.

By default, both functions will be called from *testDataset* manager sequentially, that is why *startModel* function's arguments and specific for MM method *testDataset* function's arguments concur. In the text above we mention *startModel* function's arguments only.

The equation type is defined by startModel function's argument equation that can take value "withWeight" which is default one and "withoutWeight". The argument defines the presence or absence of body weight effect in the model (see ?? and ??). In case when there are no body weight records in the dataset startModel sets equation argument to "withoutWeight" automatically.

startModel function creates start fully loaded model and modifies it after testing of different hypothesis. As was described in the previous theory section the model view is influenced by the number of criteria. Each criteria or effect (body weight effect, residual variances homogeneity, gender effect, genotype by gender interaction effect, batch effect) is evaluated individually and TRUE/FALSE values are assigned to the appropriate sections of *Phen-TestResult* object based on evaluation results. TRUE value means that effect is significant and will be modelled. FALSE value means deletion of the effect from the model.

The package allows to assign user defined values to the effects of the model. If user would like to assign TRUE/FALSE values to the effects of the model that differ from calculated ones then (s)he has to define *keepList* argument of *startModel* functions which is a list of TRUE/FALSE values for each one criterion in the following order: is batch effect significant, are residual variances homogeneous, is body weight effect significant, is gender effect significant, is gender by genotype interaction effect significant. For instance, keepList=c(TRUE, TRUE, TRUE, TRUE, TRUE) defines the fully loaded model will all possible fixed effects with homogeneous residual variances; in turn keepList=c(FALSE, FALSE, TRUE, TRUE, TRUE) defines the fully loaded model without random effects and with heterogeneous residual variances.

startModel function checks user defined effects for consistency (for instance, if there are no "Weight" column in the dataset then weight effect can't be assigned to TRUE, etc.) and prints out both calculated and user defined effects (only when outputMessages argument is set to TRUE) for the user's convenience. Note: user defined effects have a priority over calculated (evaluated) effects.

The result of the *startModel* function is MM start model with reduced non-significant effects stored in the *PhenTestResult* object together with the eval-

uated or user defined effects. It is important to mention here the convergency problem. If for some reason, the selected model is failing to converge we simplify it by selecting the similar but simplier model and try to fit again. For instance, if model with heterogeneous residuals is not converging then model with homogeneous residuals will be selected.

The next step of MM framework: evaluation of genotype effect and fitting of selected model using REML is implemented in package's function finalModel. The results are added into the PhenTestResult object. PhenTestResult object at the end of the MM framework contains model formula, significances of the effects, genotype evaluation results and model fitting results including effect sizes.

By default both functions (*startModel* and *finalModel*) will be called from *testDataset* manager one after another. We've made this logical separation of functionality in order to add more flexibility for the statisticians. Basically, it means that a user can check the evaluation of fixed effects and the selected model before final model fitting. This kind of "debugging" functionality allows the user to change some of the arguments of functions and start the model building process from scratch if needed.

We believe that the possibility to change mixed models framework behaviour as described above will help users to go deeper into details of the modelling process, as well as debug and compare the results from different models.

```
# Default behaviour
> result <- testDataset(test,depVariable="Bone.Area", equation="withoutWeight")
Information:
Dependent variable: 'Bone.Area'.

Information:
Method: Mixed Model framework.

Information:
Calculated values for model effects are: keepBatch=TRUE, keepVariance=TRUE, keepWeight=FALSE, keepGender=TRUE, keepInteraction=FALSE.

Information:
Equation: 'withoutWeight'.

Information:
Perform all MM framework stages: startModel and finalModel

# Perform each step of the MM framework separatly
> result <- testDataset(test,depVariable="Bone.Area", equation="withoutWeight",callAll=FALSE)</pre>
```

```
Information:
Dependent variable: 'Bone.Area'.
Information:
Method: Mixed Model framework.
Information:
{\tt Calculated\ values\ for\ model\ effects\ are:\ keepBatch=TRUE,\ keepVariance=TRUE,}
{\tt keepWeight=FALSE,\ keepGender=TRUE,\ keepInteraction=FALSE.}
Information:
Equation: 'withoutWeight'.
# Estimated model effects
> result$model.effect.batch
[1] TRUE
> result$model.effect.variance
[1] TRUE
> result$model.effect.weight
[1] FALSE
> result$model.effect.gender
> result$model.effect.interaction
[1] FALSE
> result$numberGenders
[1] 2
# Change the effect values: interaction effect will stay in the model
> result <- testDataset(test,depVariable="Bone.Area",</pre>
equation="withoutWeight",keepList=c(TRUE,TRUE,FALSE,TRUE,TRUE),callAll=FALSE)
Information:
Dependent variable: 'Bone.Area'.
Information:
Method: Mixed Model framework.
Information:
User's values for model effects are: keepBatch=TRUE, keepVariance=TRUE,
keepWeight=FALSE, keepGender=TRUE, keepInteraction=TRUE.
Information:
Calculated values for model effects are: keepBatch=TRUE, keepVariance=TRUE,
keepWeight=FALSE, keepGender=TRUE, keepInteraction=FALSE.
```

Calculated values differ from user defined values for model effects.

Warning:

```
Information:
Equation: 'withoutWeight'.
> result <- finalModel(result)
> summaryOutput(result)
```

## 3.2.4 Diagnostics

There are two functions we've implemented for the diagnostics and classification of MM framework results: testFinalModel and classificationTag.

The first one performs diagnostic tests to assess the MM quality of fit. This includes normality tests for the two genotype levels residuals, BLUPs (best linear unbiased prediction) and "rotated" residuals (?) (last two only if applicable). There is only one argument of the function which is *PhenTestResult* object. There are no arguments checks assuming that function is called internally from the *finalModel* function. Consequently if calling directly it should be used with precaution.

testFinalModel returns list of the following values:

- Reference genotype value.
- Normality test result (p-value) for the reference genotype's residuals.
- Test genotype value.
- Normality test result (p-value) for the test genotype's residuals.
- BLUPs normality test result (p-value); applicable only when there is batch random effects in the model, otherwise set to NA.
- "Rotated" residuals normality test result (p-value); applicable only when there is batch random effects in the model, otherwise set to NA.

BLUP in statistics is best linear unbiased prediction and is used in linear mixed models for the estimation of random effects. See tutorial BLUPs for more details.

"Rotated" residuals are constructed by multiplying the estimated marginal residual vector by the Cholesky decomposition of the inverse of the estimated marginal variance matrix. The resulting "rotated" residuals are used to construct an empirical cumulative distribution function and pointwise standard

errors. See Cholesky Residuals for Assessing Normal Errors in a Linear Model with Correlated Outcomes: Technical Report for more details about "rotated" residuals.

#### 3.2.5 Classification Tag

classification Tag function returns a classification tag to assign a sexual dimorphism assessment of the phenotypic change from the results of MM framework.

When the function is called through *vectorOutput* function, the tag shown in Figure ?? will be proceeded by the phrase "If phenotype is significant", meaning that globally the test has not assessed whether there was a statistical significant difference just that if there was this would be the classification if it was statistically significant. When the function is called through *summaryOutput* function or directly there is an argument *phenotypeThreshold* (default value is 0.01), which sets the significance threshold of whether there is a phenotype of interest. If globally, the analysis indicates there is a statistically significant phenotype then the classification tag is appended to the phrase "With phenotype threshold value XXX".

The Mammalian Phenotype Ontology is under development as a community effort to provide standard terms for annotating mammalian phenotypic data and is housed and managed by the JAXS laboratory (see MP ontology). With the mixed model implementation, the output is very rich and a classification tag can be appended to the MP term to give richer information on the observed phenotype (e.g. abnormal circulating sodium levels – both genders equally). Figure ??, details the decision tree that can be used with the MM output to interpret the results such a ontology term can be discerned and an annotation tag added when appropriate.

#### 3.3 Fisher Exact Test Framework

The Fisher Exact Test is implemented with basic R functions from the stats package after the construction of count matrices (also called chi squared tables) from the dataset.

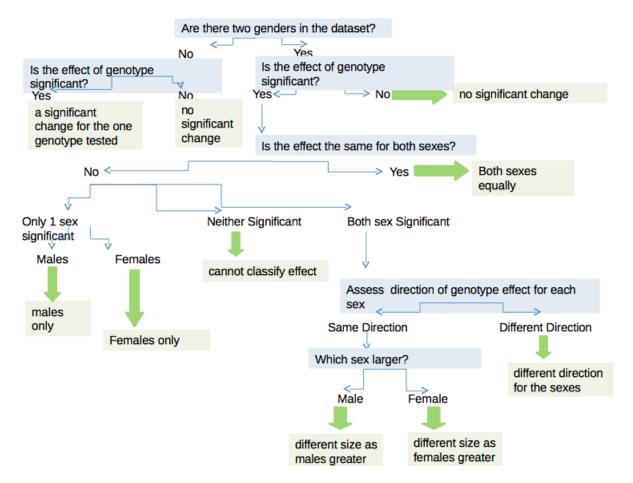


Figure 7: Assigning a classification tag. The output of the mixed model framework is queried to assign a classification tag of how the observed phenotype was observed across the two sexes. Within the decision tree, the question "Is the effect the same for both sexes? " is asking whether mathematically was there an interaction between the genotype and gender. Occasionally the procedure will find that there was a significant interaction but when it comes to identifying how this occurred and quantifying the effect for each gender, there is insufficient power. In this scenario the classification returned states that it "cannot classify the effect".

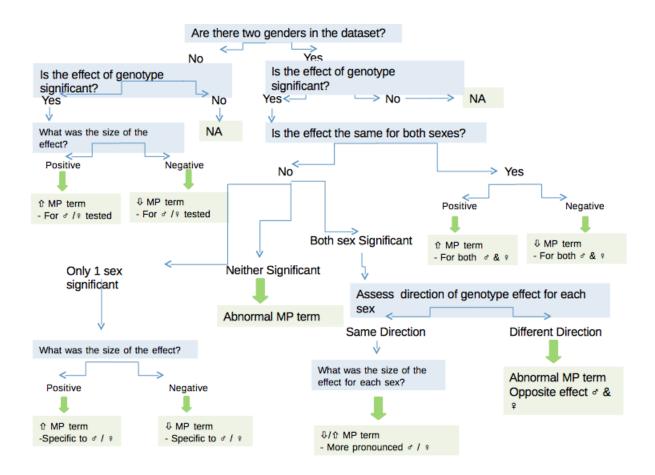


Figure 8: Assigning a Mammalian Phenotype (MP) ontology term in the presence of sexual dimorphism.

Together with count matrices we also calculate percentage matrices and statistics for the chi squared tables (using "vcd" R package "Visualizing Categorical Data"). As a measure of change we calculate the maximum effect sizes.

From the chi squared table statistical significance is assessed using a Fisher Exact Test whilst the biological significance is estimated by an effect size (see section ?? for more details).

This is calculated separately for 3 subsets (if there are multiple gender values in the dataset):

- combined dataset (regardless the gender values),
- males only subset,
- females only subset.

A Fisher Exact Test was chosen as most abnormal phenotype traits are rare event thus the signal is low. Batch is not considered significant because day to day variation does not effect abnormality call for these types of variables.

All results are stored in *PhenTestResult* object:

```
> dataset_cat <- read.csv("./PhenStat/extdata/test_categorical.csv")</pre>
> test_cat <- PhenList(dataset_cat,testGenotype="Aff3/Aff3")
Warning:
Dataset's column 'Assay.Date' has been renamed to 'Batch' and will be used for the batch effect modeling.
Dataset has been cleaned by filtering out records with genotype value
other than test genotype 'Aff3/Aff3' or reference genotype '+/+'.
Warning:
Dataset's 'Weight' column is missed.
You can define 'dataset.colname.weight' argument to specify column
for the weight effect modeling. Otherwise you can only use mixed model equation 'withoutWeight'.
Information:
Dataset's 'Genotype' column has following values: '+/+', 'Aff3/Aff3'
Dataset's 'Gender' column has following value(s): 'Female', 'Male'
> result_cat <- testDataset(test_cat,
 depVariable="Thoracic.Processes",
 method="FE")
```

#### Information:

Dependent variable: 'Thoracic.Processes'.

#### Information:

Method: Fisher Exact Test framework.

- > result\_cat\$depVariable
- [1] "Thoracic.Processes"
- > result\_cat\$method
- [1] "FE"
- > result\_cat\$numberGenders
- [1] 2
- # Chi squared table for all data
- > result\_cat\$model.output\$count\_matrix\_all

+/+ Aff3/Aff3

Abnormal 144 1: Normal 755

- # Chi squared table for males only records
- > result\_cat\$model.output\$count\_matrix\_male

+/+ Aff3/Aff3

Abnormal 61 5 Normal 392 1

- # Percentage matrix for all data
- > result\_cat\$model.output\$percentage\_matrix\_all

+/+ Aff3/Aff3 ES change

Abnormal 16 92 76 Normal 84 8 76

- # Percentage matrix for females only records
- > result\_cat\$model.output\$percentage\_matrix\_female

+/+ Aff3/Aff3 ES change

Abnormal 19 100 81 Normal 81 0 81

- # Matrix statistics for all data
- > result\_cat\$model.output\$stat\_all

X^2 df P(> X^2)

Likelihood Ratio 36.466 1 1.5536e-09 Pearson 52.600 1 4.0890e-13

```
Phi-Coefficient : 0.24
Contingency Coeff.: 0.234
Cramer's V
              : 0.24
# Matrix statistics for males only records
> result_cat$model.output$stat_male
                   X^2 df P(> X^2)
Likelihood Ratio 14.610 1 1.322e-04
               23.479 1 1.263e-06
Pearson
Phi-Coefficient : 0.226
Contingency Coeff.: 0.221
              : 0.226
Cramer's V
# Effect size for all data
> result_cat$model.output$ES
[1] 76
# Effect size for females only records
> result_cat$model.output$ES_female
[1] 81
# Fisher Exact Test results for all data
> result_cat$model.output$all
Fisher's Exact Test for Count Data
data: count_matrix_all
p-value = 4.844e-09
alternative hypothesis: true odds ratio is not equal to 1
95 percent confidence interval:
0.0003770171 0.1096287774
sample estimates:
odds ratio
0.0159923
# p-value for all data
> result_cat$model.output$all$p.value
```

[1] 4.844291e-09

The same data as shown in examples can be obtained by using output functions of the package: summaryOutput, vectorOutput and vectorOutputMatrices. See section ?? for more details.

If there is only one level for the dependent variable in the dataset e.g. "Nor-

mal" then the package will add level "Other" into the count matrices for consistency. All values for this level will be set to 0. The following is an example of such case:

```
> test2 <- PhenList(dataset=read.csv("test_categorical_normal.csv"),</pre>
> result2 <- testDataset(test2,depVariable="Thoracic.Processes", method="FE")
> levels(result2$model.dataset$Thoracic.Processes)
[1] "Normal"
> summaryOutput(result2)
Test for dependent variable: Thoracic.Processes
Method: Fisher Exact Test framework
Model output:
All data p-val: 1
All data effect size: 0%
Males only p-val: 1
Males only effect size: 0%
Females only p-val: 1
Females only effect size: 0%
Matrix 'all':
      +/+ Aff3/Aff3
Normal 895 13
Other 0
                 0
Percentage matrix 'all' statistics:
      +/+ Aff3/Aff3 ES change
Normal 100 100 0
Other 0
               0
```

### 3.3.1 Classification Tag

We've implemented the function *classificationTag* also for the FE framework. However, in the case of Fisher Exact Test it is not sexual dimorphism classification, but rather the overall estimation of the signals significance.

In the Table ?? classification tags and observed p-values classification is based on are presented.

Males only	Females only	All	Classification Tag
< 0.05	< 0.05	< 0.05	Significant in males, females and in combined
			dataset
< 0.05	$\geq 0.05$	< 0.05	Significant in males and in combined dataset
< 0.05	< 0.05	$\geq 0.05$	Significant in males and in females datasets
< 0.05	$\geq 0.05$	$\geq 0.05$	Significant in males dataset only
$\geq 0.05$	< 0.05	< 0.05	Significant in females and in combined
			dataset
$\geq 0.05$	< 0.05	$\geq 0.05$	Significant in females dataset only
$\geq 0.05$	$\geq 0.05$	< 0.05	Significant in combined dataset only
$\geq 0.05$	$\geq 0.05$	$\geq 0.05$	Not significant
< 0.05	NA	< 0.05	Significant for the sex tested
NA	< 0.05	< 0.05	Significant for the sex tested

Table 6: p-values from Fisher Exact Tests and classification tag

## 4 Output of Results

The PhenStat package stores the results of statistical analyses in the *Phen-TestResult* object. For numeric summary of the analysis, there are two functions to present *PhenTestResult* object data to the user: *summaryOutput* that provides a printed summary output and *vectorOutput* that creates a vector form output. These output forms were generated for differing users needs.

## 4.1 Summary Output

The *summaryOutput* function supports interactive analysis of the data and prints results on the screen.

The following is an example of summary output of MM framework:

```
# Mixed Model framework
```

depVariable="Lean.Mass",outputMessages=FALSE)

Test for dependent variable: Lean.Mass

Method: Mixed Model framework

<sup>&</sup>gt; result <- testDataset(test,

<sup>&</sup>gt; summaryOutput(result)

```
Was batch significant? TRUE

Was variance equal? FALSE

Was there evidence of sexual dimorphism? no (p-value 0.102)

Final fitted model: Lean.Mass ~ Genotype + Gender + Weight

Model output:

Genotype effect: 0.371508943

Classification tag: With phenotype threshold value 0.01 - no significant change

Value Std.Error DF t-value p-value

(Intercept) 7.6111388 0.58862654 411 12.9303357 2.512303e-32

GenotypeSparc/Sparc -0.2914357 0.33047985 411 -0.8818562 3.783700e-01

GenderMale 1.6407343 0.18080930 411 9.0743913 4.791912e-18

Weight 0.3430502 0.01808121 411 18.9727422 4.147891e-58
```

The summary output for MM framework contains metrics indicating the quality of the fit:

- Intercept is the reference level after all other factors are accounted for. For example, for equation with weight (??) in fully loaded model intercept is reference genotype's female with zero weight.
- Value stands for the estimated coefficient. This number will obviously vary based on the magnitude of the variable your are inputting into the regression, but it's always good to spot check this number to make sure it seems reasonable.
- **Std.Error** is a standard error of the coefficient estimate measure of the variability in the estimate for the coefficient. Lower is better but this number is relative to the value for the coefficient.
- **DF** stands for the "Degrees of Freedom" which is the difference between the number of observations included in training sample and the number of variables used in model (intercept counts as a variable).
- **t-value** of the coefficient estimate is a score that measures whether or not the coefficient for this variable is meaningful for the model. It is used to calculate the p-value.
- **p-value** is variable p-value that represents the probability the variable is NOT relevant. The smaller is number the more important is variable (model part). If the number is really small, R will display it in scientific notation.

For the "FE" framework results *summaryOutput* function's output includes count matrices, statistics and effect size measures.

```
result2 <- testDataset(test2,</pre>
           depVariable="Thoracic.Processes",
           method="FE",outputMessages=FALSE)
summaryOutput(result2)
Test for dependent variable: Thoracic.Processes
Method: Fisher Exact Test framework
Model output:
All data p-val: 4.84429148175386e-09
All data effect size: 76%
Males only p-val: 0.000286667802768362
Males only effect size: 70%
Females only p-val: 1.00779809539594e-05
Females only effect size: 81%
Matrix 'all':
       +/+ Aff3/Aff3
Abnormal 144 12
Normal 755
Percentage matrix 'all' statistics:
       +/+ Aff3/Aff3 ES change
Abnormal 16 92 76
       84
                  8
                            76
Normal
Matrix 'all' statistics:
                 X^2 df P(> X^2)
Likelihood Ratio 36.466 1 1.5536e-09
Pearson
              52.600 1 4.0890e-13
Phi-Coefficient : 0.24
Contingency Coeff.: 0.234
Cramer's V
           : 0.24
Matrix 'males only':
```

# 4.2 Vector Format

vectorOutput function was developed for large scale application where automatic implementation would be required. As such, each value within the output vector is strictly defined and depends only on the statistical analysis method that has been used. The main idea here is that vector format is specified and is the same regardless the analysis framework.

Genotype

```
> vectorOutput(result)
                                           Method
                                         "MM - Eq2"
                                Dependent variable
                                        "Lean.Mass"
                                     Batch included
                                             "TRUE"
                    Residual variances homogeneity
                                            "FALSE"
                             Genotype contribution
                               "0.371508943144266"
                                 Genotype estimate
                                "-0.29143571549456"
                           Genotype standard error
                               "0.330479850268177"
                                     Genotype p-val
                                "0.378369997588029"
                                   Gender estimate
                                 "1.64073430331594"
                             Gender standard error
                                "0.180809296427475"
                                      Gender p-val
                             "4.79191190571249e-18"
                                   Weight estimate
                               "0.343050209791982"
                             Weight standard error
                               "0.0180812139273457"
                                      Weight p-val
                             "4.1478905048872e-58"
```

In the Table ?? vector output values are described.

As was mentioned above *vectorOutput* format is the same for both frameworks. However, in case of "FE" many values are not defined. For example:

> vectorOutput(result\_cat)

Method

"Fisher Exact Test"

Dependent variable

"Thoracic.Processes"

Batch included

NA

Residual variances homogeneity

NA

Genotype contribution

dent variable String MM and FE included by Earling MM and FE included by Earling MM and FE included by Earling MM and FE included Numeric MM and FE included Earling Numeric MM and FE included Earling Numeric MM and FE is standard error Numeric MM increase it p-val Numeric MM increase it p-val String MM and FE increase it increase	7	Nomo	V. l	Dromomont	Dogomintion
Method  Dependent variable Batch included Residual variances homogeneity Genotype contribution Genotype estimate Genotype p-val Genotype p-val Gender estimate Gender standard error Gender standard error Weight estimate Weight standard error Weight standard error Weight standard error  Winneric  MM  And FE  Gp2 genotype  Gp2 genotype  Gp2 genotype  Gp2 Residuals normality test  Numeric  MM  And FE	#	INGILIC	v diuc	LIGHIEWOIR	Description
Dependent variable Batch included Residual variances homogeneity Genotype contribution Genotype estimate Genotype p-val Gender estimate Gender standard error Weight estimate Weight standard error Weight standard error Weight standard error  Winneric  MM  Mand FE  Gp2 genotype  Gp2 genotype  Gp2 genotype  Gp2 genotype  Gp2 genotype  Gp2 Residuals normality test  Numeric  MM  Am and FE  Gp2 Residuals normality test  Numeric  MM  Mand FE  Gp2 Residuals normality test  Numeric  MM  MM  MM  MM  MM  MM  MM  MM  MM	<del></del>	Method	String	MM and FE	Possible values: "FE", "MM - Eq1" (mixed model with-
Dependent variable Batch included Residual variances homogeneity Genotype contribution Genotype estimateString TRUE/FALSE MM Numeric MM Mand FEGenotype estimate Genotype p-val Gender estimateNumeric NumericMM MMGender estimate Gender standard errorNumeric NumericMMGender standard errorNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight standard errorNumericMMWeight standard errorNumericMMGp1 genotype Gp1 Residuals normality test Gp2 Residuals normality testString NumericMMBlups testNumericMMBlups testNumericMM					out body weight effect), "MM - Eq2" (mixed model with
Dependent variable Batch included Residual variances homogeneity Genotype contribution Genotype estimate Genotype p-val Genotype p-val Gender standard error Weight estimate Weight standard error Weight standard error Weight p-val Weight p-val  Gpl genotype Gpl genotype Gpl genotype Gpl genotype Gpl genotype Gpl Residuals normality test Gp2 genotype Gp2 Residuals normality test Blups test  Numeric  Numeric  Numeric  MM  Mand FE  MM  MM  MM  MA  Gpl genotype Gp2 genotype Gp2 genotype Gp2 Residuals normality test Numeric MM  Gp2 Residuals normality test Numeric MM  Blups test MM  Mineric MM					body weight effect).
Batch included Residual variances homogeneity Genotype estimateTRUE/FALSE NumericMM M	2	Dependent variable	String	MM and FE	Name of the dependent variable.
Residual variances homogeneity Genotype contribution Genotype estimateTRUE/FALSE NumericMM MM MM MMGenotype estimate Genotype p-val Genotype p-valNumeric NumericMMGender estimate Gender standard errorNumeric NumericMMWeight estimate Weight standard errorNumeric NumericMMWeight p-valNumeric NumericMMGp1 genotype Gp1 genotype Gp2 genotype Gp2 Residuals normality test Gp2 Residuals normality testString String NumericMM MM MM MM MMBlups testNumeric NumericMM	ಣ	Batch included	TRUE/FALSE	$\overline{\mathrm{MM}}$	Was batch significant in MM?
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Genotype estimateNumericMM and FEGenotype standard errorNumericMMGender estimateNumericMMGender standard errorNumericMMGender p-valNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM	ಬ	Genotype contribution	Numeric	MM and FE	p-value indicating genotype contribution.
Genotype standard errorNumericMMGenotype p-valNumericMMGender estimateNumericMMGender standard errorNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 genotypeStringMMGp2 Residuals normality testNumericMMBlups testNumericMM	9	Genotype estimate	Numeric	MM and FE	Estimated coefficient that describes genotype value cal-
Genotype standard errorNumericMMGenotype p-valNumericMMGender estimateNumericMMGender p-valNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 genotypeStringMMGp2 Residuals normality testNumericMMBlups testNumericMM					culated by MM or effect size estimates in FE.
Genotype p-valNumericMMGender estimateNumericMMGender standard errorNumericMMWeight estimateNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMMGp2 genotypeStringMMGp2 Residuals normality testStringMMBlups testNumericMM		Genotype standard error	Numeric	MM	Standard error of the coefficient estimate for genotype
Genotype p-valNumericMMGender estimateNumericMMGender standard errorNumericMMWeight estimateNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM					in MM.
Gender estimateNumericMMGender standard errorNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMMGp2 genotypeStringMMGp2 genotypeStringMMGp2 genotypeStringMMBlups testNumericMM	$\infty$	Genotype p-val	Numeric	MM	Genotype p-value that represents the probability the
Gender estimateNumericMMGender standard errorNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM					genotype is NOT relevant in MM.
Gender standard errorNumericMMGender p-valNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM	6	Gender estimate	Numeric	$\overline{\mathrm{MM}}$	Estimated coefficient that describes gender value calcu-
Gender standard errorNumericMMGender p-valNumericMMWeight estimateNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMMGp2 Residuals normality testStringMMGp2 Residuals normality testNumericMMBlups testNumericMM					lated by the MM.
Gender p-valNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 Residuals normality testStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM	10	Gender standard error	Numeric	MM	Standard error of the coefficient estimate for gender in
Gender p-valNumericMMWeight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMMGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM					MM.
Weight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMMGp2 genotypeStringMMGp2 Residuals normality testNumericMMBlups testNumericMM	1	Gender p-val	Numeric	MM	Gender p-value that represents the probability the gen-
Weight estimateNumericMMWeight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMMGp2 genotypeStringMMGp2 Residuals normality testNumericMMBlups testNumericMM					der is NOT relevant in MM.
Weight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMMGp2 genotypeStringMMGp2 Residuals normality testStringMMBlups testNumericMM	12	Weight estimate	Numeric	$\overline{\mathrm{MM}}$	Estimated coefficient that describes weight value calcu-
Weight standard errorNumericMMWeight p-valNumericMMGp1 genotypeStringMMGp2 genotypeStringMMGp2 Residuals normality testStringMMBlups testNumericMM					lated by the MM.
Weight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM	13	Weight standard error	Numeric	MM	Standard error of the coefficient estimate for weight in
Weight p-valNumericMMGp1 genotypeStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM					IVINI.
Gp1 genotypeStringMM and FEGp1 Residuals normality testStringMM and FEGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM	14	Weight p-val	Numeric	$\overline{\mathrm{MM}}$	Weight p-value that represents the probability the
Gp1 genotypeStringMM and FEGp1 Residuals normality testNumericMMGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM					weight is NOT relevant in MM.
Gp1 Residuals normality testNumericMMGp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM	15	Gp1 genotype	String	MM and FE	Value of reference genotype.
Gp2 genotype Gp2 Residuals normality test Numeric MM And FE MM Blups test Numeric MM	16	Gp1 Residuals normality test	Numeric	MM	p-value that represents the probability the residuals in
Gp2 genotypeStringMM and FEGp2 Residuals normality testNumericMMBlups testNumericMM					reference genotype subset are normally distributed.
Gp2 Residuals normality test Numeric MM  Blups test Numeric MM	17	Gp2 genotype	String	MM and FE	Value of test genotype.
Blups test Numeric MM	$\frac{18}{8}$	Gp2 Residuals normality test	Numeric	MM	p-value that represents the probability the residuals in
Blups test MM					test genotype subset are normally distrbuted.
mally distrbuted.	19	Blups test	Numeric	$\overline{\mathrm{MM}}$	p-value that represents the probability the blups are nor-
					mally distributed.

#	Name	Value	Framework	Description
20	Rotated residuals normality test	Numeric	MM	p-value that represents the probability the rotated resid-
				uals are normally distrbuted.
21	Intercept estimate	Numeric	MM	Estimated coefficient that describes intercept value cal-
				culated by the MM.
22	Intercept standard error	Numeric	MM	Standard error of the coefficient estimate for intercept
				in MM.
23	Interaction included	TRUE/FALSE	MM	Indicates the inclusion of genotype by gender interaction
				effect into MM.
24	Interaction p-val	Numeric	MM	Interaction p-value that represents the probability the
				interaction is NOT relevant in MM.
25	Gender FvKO estimate	Numeric	MM and FE	Estimated coefficient that describes value calculated by
				the MM for females in test genotype subset or effect
				size estimate calculated from chi table for females only
				subset in FE.
26	Gender FvKO standard error	Numeric	MM	Standard error of the "Gender FvKO estimate" in MM.
27	Gender FvKO p-val	Numeric	MM	p-value that represents the probability that females
				group from test genotype subset contribution into MM
				is NOT relevant.
28	Gender MvKO estimate	Numeric	MM and FE	Estimated coefficient that describes value calculated by
				the MM for males in test genotype subset or effect size
				estimate calculated from chi table for males only subset
				in FE.
29	Gender MvKO standard error	Numeric	MM	Standard error of the "Gender MvKO estimate" in MM.
30	Gender MvKO p-val	Numeric	MM	p-value that represents the probability that males group
				from test genotype subset contribution into MM is NOT
				relevant.
31	Classification tag	String	MM and FE	A sexual dimorphism assessment of the phenotypic
				change from the results of MM or the overall estima-
				tion of the signals significance in FE.

Table 7: Vector output description.

Genotype estimate

Genotype standard error

Genotype p-val

"4.84429148175386e-09"

Gender estimate

Gender standard error

NA

Gender p-val

Weight estimate

Weight standard error

Weight p-val

Gp1 genotype

"+/+"

Gp1 Residuals normality test

Gp2 genotype

"Aff3/Aff3"

Gp2 Residuals normality test

Blups test

Rotated residuals normality test

Intercept estimate

Intercept standard error

Interaction included

Interaction p-val

Gender FvKO estimate

Gender FvKO standard error

Gender FvKO p-val

"1.00779809539594e-05"

Gender MvKO estimate

Gender MvKO standard error

Gender MvKO p-val

## 4.3 Count Matrices in Vector Format

There is an additional function to support the FE framework: vectorOut-putMatrices. This function returns values from count matrices in the vector format. We've limited the number of levels for dependent variable to 10. In the vector, the first three positions represent: dependent variable, genotype level 1 (reference genotype) and genotype level 2 (test genotype). The next 10 positions are used to define the dependent variable levels. When there are less than 10 levels, "NA" value is used. The next 20 positions represent combined count matrix values. Thereafter the vector contains the males only count matrix values and females only count matrix values. Again "NA" is used when the values are not present. The positions are labelled with the group and level.

For the chi squared tables from example described in "Fisher Exact Test framework" subsection (see ??) results of *vectorOutputMatrices* function look like this:

> vcctoroacpathatrices(resure_cat)	
Dependent variable	Gp1 Genotype (g1)
"Thoracic.Processes"	"+/+"
Gp2 Genotype (g2)	Dependent variable level1 (11)
"Aff3/Aff3"	"Abnormal"
Dependent variable level2 (12)	Dependent variable level3 (13)
"Normal"	NA
Dependent variable level4 (14)	Dependent variable level5 (15)
NA	NA
Dependent variable level6 (16)	Dependent variable level7 (17)
NA	NA
Dependent variable level18 (18)	Dependent variable level9
NA	NA
Dependent variable level10 (110)	Value g1_11
NA	"144"
Value g2_11	Value g1_12
"12"	"755"
Value g2_12	Value g1_13
"1"	NA
Value g2_13	Value g1_14
NA	NA
Value g2_14	Value g1_15
NA	NA
Value g2_15	Value g1_16

> vectorOutputMatrices(result\_cat)

NA	NA
Value g2_16	Value g1_17
NA	Value gi_i/ NA
Value g2_17	Value g1_18
NA	NA
Value g2_18	Value g1_19
Value g2_10	Value gi_i3
Value g2_19	Value g1_110
Value gz_19	Value gr_110 NA
Value g2_110	
Value gz_110 NA	Male Value g1_l1 "61"
	Male Value g1_12
Male Value g2_11	"392"
_	
Male Value g2_12	Male Value g1_13
_	NA Mala Valua et 14
Male Value g2_13	Male Value g1_14
NA	NA
Male Value g2_14	Male Value g1_15
NA Nalua en la	NA Mala Valua et 16
Male Value g2_15 NA	Male Value g1_16
	NA Mala Valua et 17
Male Value g2_16	Male Value g1_17
NA	NA
Male Value g2_17	Male Value g1_18
NA Nalue en 19	NA Mala Valua et 10
Male Value g2_18 NA	Male Value g1_19
	NA
Male Value g2_19 NA	Male Value g1_110 NA
Male Value g2_110	
NA	Female Value g1_11 "83"
	Female Value g1_12
Female Value g2_11	"363"
•	Female Value g1_13
Female Value g2_12	remaie value gi_i3
_	Female Value g1_14
Female Value g2_13 NA	NA
Female Value g2_14	Female Value g1_15
NA	NA
Female Value g2_15	Female Value g1_16
NA	NA
Female Value g2_16	Female Value g1_17
NA	NA
Female Value g2_17	Female Value g1_18
NA	NA
Female Value g2_18	Female Value g1_19
NA	NA
Female Value g2_19	Female Value g1_110
NA	NA
IVA	NA

# 5 Graphics

For graphical output of the analysis, multiple graphical functions have been generated and these can be called by a user individually or alternatively, generateGraphs generates all relevant graphs for an analysis and stores the graphs in the defined directory.

```
> generateGraphs(phenTestResult=result,dir="./graphs",graphingName="Lean Mass",type="windows")
```

# 5.1 Graphics for Categorical Data

There is only one graphical output for FE framework: categorical bar plots. This graph allows a visual representation of the count data, comparing observed proportions between reference and test genotypes.

```
> categoricalBarplot(result_cat)
```

The example of bar plot is shown in Figure ??. This graph allows a visual representation of the genotype effect for the variable of interest.

# 5.2 Graphics for Continuous Data

There are many graphic functions for the MM framework results. They can be divided into two types: dataset based graphs and results based graphs. There are three functions in the dataset based graphs category:

- boxplotGenderGenotype creates a box plot split by gender and genotype.
- boxplotGenderGenotypeBatch creates a box plot split by gender, genotype and batch if batch data present in the dataset. Please note the batches are not ordered with time but allow assessment of how the treatment groups lie relative to the normal control variation.

<sup>&</sup>gt; generateGraphs(phenTestResult=result\_cat,dir="./graphs\_categorical",type="windows")

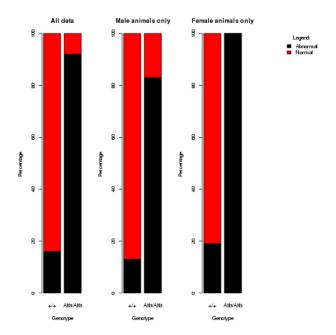


Figure 9: The PhenStat package's graphical output: categorical bar plot.

- scatterplotGenotypeWeight creates a scatter plot body weight versus dependent variable. Both a regression line and a loess line (locally weighted line) is fitted for each genotype.
- > boxplotGenderGenotype(test,depVariable="Lean.Mass",graphingName="Lean Mass")
- > boxplotGenderGenotypeBatch(test,depVariable="Lean.Mass",graphingName="Lean Mass")
- > scatterplotGenotypeWeight(test,depVariable="Bone.Mineral.Content",graphingName="BMC")

An example of box plot split by gender and genotype is shown in Figure ??. Outliers are shown as independent data points beyond the fences ("whiskers") of the boxplot. An outlier is defined as a data point that is 1.5 times the interquartile range above the upper quartile and bellow the lower quartile.

The example of box plot split by gender, genotype and batch is shown in Figure ??. This allows a visualisation of variation of dependent variable with time. The MM framework assumes this variation is random and conforms the normal distribution. Then the genotype distribution can be compared relative to natural variation.

The example of scatter plot of body weight versus dependent variable is shown in Figure ??. When weight is included in the model MM framework, it assumes a linear relationship between dependent variable and body weight.

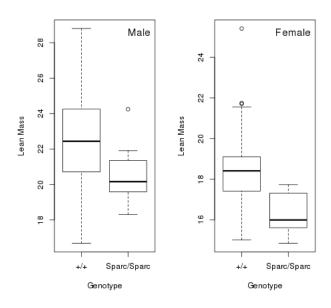


Figure 10: The PhenStat package's graphical output: box plot split by gender and genotype.

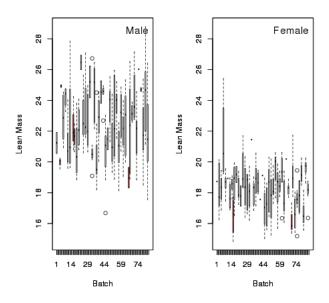


Figure 11: The PhenStat package's graphical output: box plot split by gender, genotype and batch.

This graph allows an assessment of this assumption.

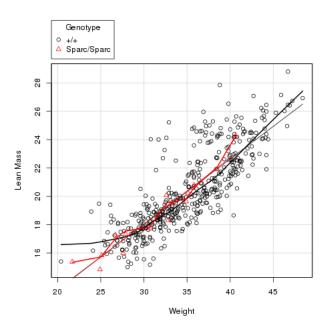


Figure 12: The PhenStat package's graphical output: scatter plot of body weight versus dependent variable.

There are five functions in the results based graphs category:

- qqplotGenotype creates a Q-Q plot of residuals for each genotype.
- qqplotRandomEffects creates a Q-Q plot of blups (best linear unbiased predictions).
- qqplotRotatedResiduals creates a Q-Q plot of "rotated" residuals.
- plotResidualPredicted creates predicted versus residual values plots split by genotype.
- boxplotResidualBatch creates a box plot with residue versus batch split by genotype.
- > qqplotGenotype(result)
- > qqplotRandomEffects(result)
- > qqplotRotatedResiduals(result)
- > plotResidualPredicted(result)
- > boxplotResidualBatch(result)

The example of Q-Q plot of residuals for each genotype is shown in Figure ??. The MM framework assumes residuals are normally distributed. Residuals

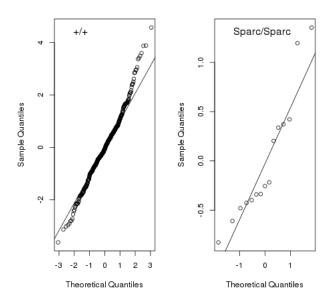


Figure 13: The PhenStat package's graphical output: Q-Q plot of residuals for each genotype.

are the differences between the real values observed for a dependent variable and the fitted values from the model. A Q-Q plot assesses this assumption (residuals will be randomly arranged around the line if normally distributed).

The example of Q-Q plot of BLUPs (best linear unbiased predictions) is shown in Figure ??. The MM framework assumes the BLUPs are normally distributed. This graph assesses this assumption by plotting BLUPs and the ideal normal line (large deviations from the line can be an indicator of problems with the model fit). BLUPs are best linear unbiased predictions and are used for the estimation of batch effects. See tutorial BLUPs for more details.

Another method to assess the model fit is to consider the normality of the "rotated" and "unrotated" residuals. The example of Q-Q plot of "rotated" residuals is shown in Figure ??. See section ?? for the details about "rotated" residuals.

The example of residual-by-predicted plot is shown in Figure ??. Residuals, differences between fitted and real values, are plotted against the predicted (fitted) values of dependent variable. A residual-by-predicted plot can be

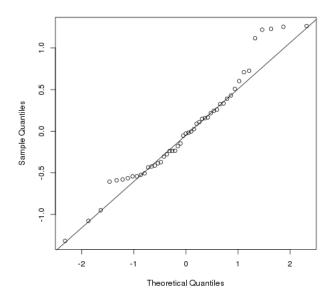


Figure 14: The PhenStat package's graphical output: Q-Q plot of BLUPs (best linear unbiased predictions).

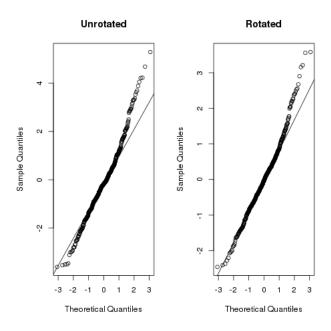


Figure 15: The PhenStat package's graphical output: Q-Q plot of "rotated" residuals.

used to diagnose nonlinearity or nonconstant error variance. It is also can be used to find outliers.

Here are the characteristics of a residual-by-predicted plot when model fitness is close to the ideal and what they suggest about the appropriateness of the model:

- The residuals are arranged randomly around the 0 line. This suggests that the assumption that the relationship is linear is reasonable.
- The residuals roughly form a "horizontal band" around the 0 line. This suggests that the variances of the error terms are equal.
- No one residual outstands from the basic random pattern of residuals. This suggests that there are no outliers. See Regression Methods for more details.

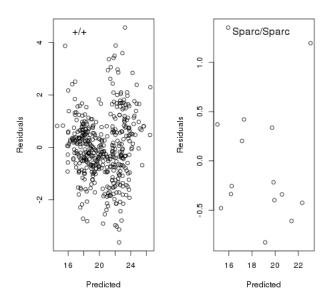


Figure 16: The PhenStat package's graphical output: residual-by-predicted plot split by genotype.

The example of box plot with residue versus batch split by genotype is shown in Figure ??. This allows assessment that the residual behaviour for all batches is within natural deviation and the model is fitting the data well.

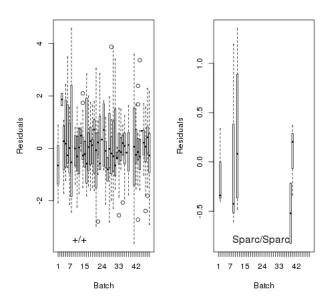


Figure 17: The PhenStat package's graphical output: box plot with residual versus batch split by genotype.

# 6 Case Studies

# 6.1 PhenStat Usage Example Continuous Data

The following dataset, provided by Wellcome Trust Sanger Institute (WTSI) Mouse Genetics Project (MGP) is Dual-energy X-ray absorptiometry data obtained for a study on gene knockout mice carrying the Akt2 < tm1Wcs > targeted allele which were created by blastocyst injection of targeted ES cells, and bred on the 129S5SvEvBrd genetic background. Data was collected doing a standardized high throughput phenotyping pipeline following a multibatch workflow, where regular control animals are collected and knockout animals of the correct age are issued to the pipeline as they arise.

## 6.1.1 Loading the data and initial steps of analysis

Initial steps focus on loading the data, using the PhenStat tools to generate the PhenList object, and then the result object. We can then explore the data and fitted results using the visualisation and output functions.

<sup>&</sup>gt; DEXAdata=read.csv("WTSI\_AKt2\_data.csv")

Genotype	Gender	Number Animals	Number Batches
Akt2/Akt2	Female	12	3
ANUZ / ANUZ	Male	14	3
1 / 1	Female	574	96
+/+	Male	572	97

Table 8: Number of animals and number of batches in the Akt2 dataset

```
> test <- PhenList(dataset=DEXAdata,testGenotype="Akt2/Akt2",
    refGenotype="WT",
    dataset.colname.batch="dateOfExperiment",
    dataset.values.female="female",
    dataset.values.male="male" )
> result <- testDataset(test,depVariable="Lean.Mass",method="MM",equation="withoutWeight")</pre>
```

### 6.1.2 Exploring and understanding the output

The first two lines of the *summaryOutput* confirm the statistical framework used and the dependent variable studied. The next section of the output clarifies the final fitted model details. As the MM framework is an optimisation process exploring the data to fit the best model to the data, the final fitted model details will vary. We can see that batch variation, the variation in readings between different assay dates, were found to be statistical significant and hence a mixed model will have been fitted where batch is treated as a random effect. If it was not significant, then the model would have reverted to a simpler linear model. The next line of output, "was variance equal?", indicating whether the model assumes equal variance between genotype groups or unequal. In this case, the variance was not found to be equal and therefore the final model estimated the variance for each group separately.

The next stage of the output, indicates whether there was evidence of sexual dimorphism (i.e. the genotype effect was found to be dependent on sexes). In this case, the statistical test of sexual dimorphism was non-significant (p-value = 0.899) hence the final model assessed a genotype effect rather than the genotypes for each sex separately. The following line indicate which main effects were included in the final model; for this variable and dataset we can see that gender was significant in explaining variation in the data and hence is included in the final model.

The final stage of the output gives information on the final model details. The "Genotype effect" reports the statistical significance for the genotype effect and is assessed by comparing a treatment model (final fitted model) with a null model where a null model has no genotype effects in the model but all other significant main effects. In this example the null model would thus be Lean.Mass  $\sim$  Gender. Looking at the output the "Genotype effect" is highly statistical significant as a 0 value is reported. We can then look at the model fitting details in the final output of the function by examining the table to see how the main effects contributed to the variation in the dependent variables.

```
> summaryOutput(result)

Test for dependent variable: Lean.Mass

Method: Mixed Model framework

Was batch significant? TRUE

Was variance equal? FALSE

Was there evidence of sexual dimorphism? no (p-value 0.906)

Final fitted model: Lean.Mass ~ Genotype + Gender

Model output:

Genotype effect: 0

Classification tag: With phenotype threshold value 0.01 - both sexes equally

Value Std.Error DF t-value p-value

(Intercept) 18.525264 0.1936360 1048 95.670550 0.000000e+00

GenotypeAkt2/Akt2 -3.527111 0.4866433 1048 -7.247836 8.204401e-13

GenderMale 4.620361 0.1581236 1048 29.219943 8.940893e-138
```

A regression model estimates each component of the model, by isolating how that effect influences the dependent variable (i.e. lean mass) as though all other parts of the model had been fixed and isolated. From the table of output, we can see that the intercept (the expected reading for lean mass for female reference genotype (aka female wild type animals) is 18.5. Then we can see the effect of the genotype is -3.5 in that knockout animals are predicted to have 3.5 grams less lean mass relative to the control animals. Finally we can see that being a male animals leads to an increase of 4.6 grams. As there was no evidence for sexual dimorphism, and thus the genotype effect was estimated independently of gender, then a classification tag "both sexes equally" has been assigned. These estimates are in agreement with the visualisation of the data (see section ??).

#### 6.1.3 Assessment of raw data and distribution characteristics

To assess model fit, graphical tools are ideal. They focus on two areas:

- 1. Assessment of raw data and distribution characteristics
- 2. Assessment of model fit

The function, boxplotGenderGenotype, allows the genotype effect to be visualised for each gender group. For the Akt2 example, we can suggest that there looks to be a significant genotype effect that is seen in both genders.

> boxplotGenderGenotype(result, "Lean.Mass", "Lean Mass (g)")

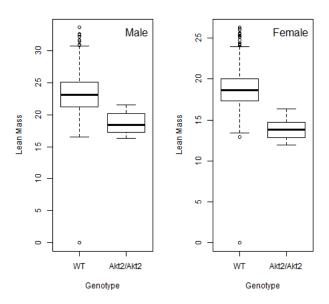


Figure 18: boxplotGenderGenotype function for Akt2 example.

A second function, boxplotGenderGenotypeBatch, allows the comparison between genotype as a function of batch and gender. This plot allows the user to visualise the batch variation and assess how the treatment measures look relative to the batch variation. It is important to note that as dates can be entered in many forms, the batches are not ordered with time. For the Akt2 lean mass example, we can see that there is significant batch variation, which explains why a mixed model was fitted.

<sup>&</sup>gt; boxplotGenderGenotypeBatch(test, "Lean.Mass", "Lean Mass (g)")

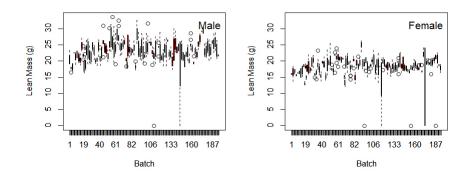


Figure 19: boxplotGenderGenotypeBatch function for Akt2 example.

#### 6.1.4 Assessment of model fit

Five functions are available and they focus on looking at residual behaviour. A residual, is the difference between the estimated dependent variable from the final model estimates and the actual measured dependent variable response. A model is a good fit, when the residuals are normally distributed and there is no systematic pattern in the distribution of the residuals relative to the dependent variable.

The vectorOutput function includes statistical tests for normality on the residuals for the wild type, residuals for the knockout, the blups and "rotated" residuals (see section ??). These normality tests are provide to assist in the building automated tools for assessing model fit, however when there is a lot of data (e.g. in a dataset where the wild type arises from a high throughput program with a running baseline), the statistical test can be overall sensitive to departures from normality and when the number of data points is low (e.g. in many knockout groups), the test can lack ability to detect deviations from normality.

#### • qqplotGenotype

This function assesses the normality of the residuals are assessed for each genotype through plotting a normal Q-Q plot. Q-Q plots are a means of comparing two distributions. To test normality, we plot the residuals against a normal distribution and see if they match. If the two distributions are similar the points on a QQ plot will fall along the y=x line (unity). Thus we are looking for a random distribution of points along the lines.

Looking at the Akt2 lean mass example, the residuals on the homozygous knockout group are near perfect showing the model is fitting this data well. The residuals on the WT group are deviating in a way (systematic below at one end and systematic above at the other) which indicates that we have long tails to our distribution. This is not concerning as we have a very large control dataset and we do have outliers in the data.

#### > qqplotGenotype(result)

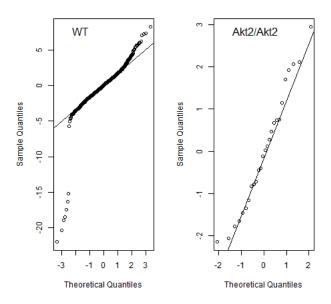


Figure 20: qqplotGenotype function for Akt2 example.

### • boxplotResidualBatch

This function allows visualisation to assist the user to assess whether the deviation in the residual is consistent across all the batches and similar in size between the wild type and knockout line. For the Akt2 example, we can see that the variation in residual is consistent across all the batches and similar in size between the knockout and wildtype group.

A few of the wildtype (control) dataset points have large residuals and it would be worth looking at these data points further to see why these are outliers. They do not suggest the model should be discarded because

as a proportion of the dataset they are few and scattered through the dataset.

#### > boxplotResidualBatch(result)

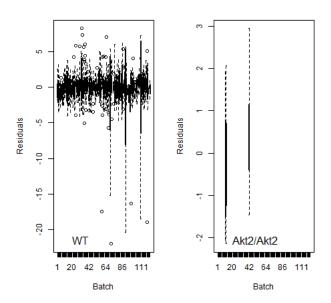


Figure 21: boxplotResidualBatch function for Akt2 example.

## $\bullet$ plotResidualPredicted

This function plots the residuals against the predicted readings for both genotypes. The predicted readings are the values the model would estimate for the dependent variable. As a user, you are looking to see that the model is fitting the data well over the entire data range. Looking at the Akt2 data, we can see that there spread of the residuals is fairly consistent, however there are some data points that are not being fit well by the model, the good news is that they are in the control set but they should be considered further to see if a reason for their poor fit can be ascertained.

> plotResidualPredicted(result)

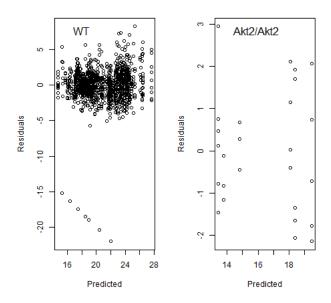


Figure 22: plotResidualPredicted function for Akt2 example.

## • qqplotRandomEffects

This function is assessing the assumption that the batch effects are normally distributed. The estimates of the random effects, aka the estimates of the batch effects in this scenario, are called best linear unbiased prediction BLUPs. Here a normal Q-Q plot is used to plot the estimated BLUPs against a normal distribution. So looking at the Akt2 lean mass example, the majority of the data points are distributed along the line. There is some systematic deviation at the tails but it is a small percentage of the points and as it is above and below the line it indicates long tails (ie outliers) and so we can conclude the distribution is not too far from the ideal and the model is a good representation of the data.

> qqplotRandomEffects(result)

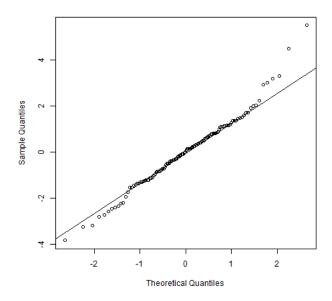


Figure 23: qqplotRandomEffects function for Akt2 example.

## • qqplotRotatedResiduals

This function, allows the user to consider the normality of the "rotated" and "unrotated" residuals and have been recommended to assess model fit success with mixed models (?). See section ?? for more details. So looking at the Akt2 lean mass example, the majority of the data points are distributed along the line. There is some systematic deviation at the tails but it is a small percentage of the points and as it is above and below the line it indicates long tails (i.e. outliers) and so we can conclude the distribution is not too far from the ideal and the model is a good representation of the data.

> qqplotRotatedResiduals(result)

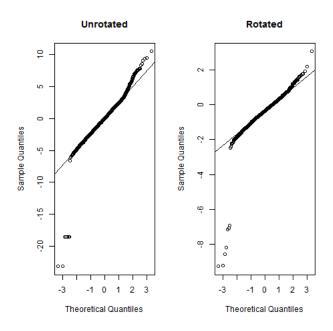


Figure 24: qqplotRotatedResiduals function for Akt2 example.

# 6.1.5 Including weight as a covariate in the model fitting process

Weight is included in the initial model via the *testDataset* function equation argument being set to either "withWeight" or "withoutWeight". When weight is included as a covariate, the model is assuming that the dependent variable (e.g. lean mass) has a linear relationship with body weight. If weight is not found to be statistical significant in explaining the variation in the dependent variable, then weight as a covariate will drop out of the final model and the equation will automatically revert to an equation type "withoutWeight".

There are two advantages to including weight:

- 1. **Increase in sensitivity.** If differences in animal weight lead to greater variability in the dependent variable, then by adding weight and accounting for this variability then the statistical model will be more sensitive to a genotype effect.
- 2. Adjusting for weight differences between the knockout and control group. When there is a weight difference between the knockout and wild type animals, the genotype effect is confounded by the

weight effect in that there is a difference in the dependent variable but you cannot assess whether it is due to the differences in body weight of the knockout and control animals or genotype differences between the knockout and control animals. When weight is included in the equation, the genotype effect is then testing for a genotype difference after adjusting for the weight difference.

We have found that the majority of continuous phenotypic variables monitored in the WTSI Mouse Genetics Project (MGP) have a relationship with body weight. Looking at the Akt2 dataset we can see that there is a difference in body weight between the wild type and knockout group and thus body weight can be a confounding factor to isolating the genotype effect.

> boxplotGenderGenotype(test, "Weight", "Body Weight (g)")

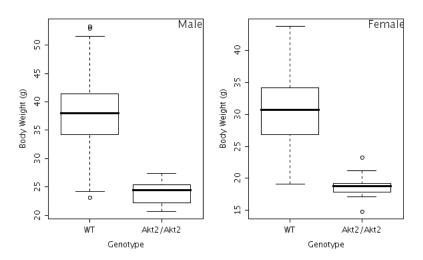


Figure 25: boxplotGenderGenotype function for Akt2 example to show the body weight impact.

When body weight is included, the inclusion can be seen in the final fitted model as weight is listed as a covariate and then in the final model output table, where the influence of weight on the fitted model is shown. With weight included the genotype effect is estimating the impact of genotype after adjusting for weight differences in the animals.

Looking at the summaryOutput for the Akt2 example, the table shows that for each gram of body weight the lean mass increased by 0.32g. When weight is included in the equation it changes the definition of the intercept from the

lean mass value of a wild type female animal to the lean mass value of a wild type female animal of zero body weight. This happens as the model is estimating each of these terms influences in isolation of the other terms. In contrast to the earlier fitted results (section ??), when weight is included in the model, the classification tag identifies the change as "no significant change" as the global genotype test is now not significant with a p-value of 0.64. This means the statistically difference observed with the fitted model "withoutWeight" was entirely due to a body weight differences between the knockout and control animals. So whilst there is a fundamental differences in lean mass between the knockout and control this is due to the knockout animals being smaller than the control animals.

```
> summaryOutput(result)
Test for dependent variable: Lean.Mass
Method: Mixed Model framework
Was batch significant? TRUE
Was variance equal? FALSE
Was there evidence of sexual dimorphism? no (p-value 0.105)
Final fitted model: Lean.Mass ~ Genotype + Gender + Weight
Model output:
Genotype effect: 0.639989841
Classification tag: With phenotype threshold value 0.01 - no significant change
                       Value Std.Error DF t-value
                                                            p-value
                 7.6201046 0.52150631 1047 14.6117207 3.827390e-44
(Intercept)
GenotypeAkt2/Akt2 -0.1924952 0.41201772 1047 -0.4672012 6.404531e-01
                  2.1550868 0.17386173 1047 12.3954067 5.056608e-33
GenderMale
                  0.3541522 0.01623164 1047 21.8186332 2.718321e-87
Weight
```

#### 6.1.6 Additional model diagnostics when weight is included

In addition to the diagnostic discussed in previous section, when weight is included in the model, it is important to consider whether the linear relationship between body weight and the dependent variable is a valid assumption. This can be assessed with the scatterplotGenotypeWeight function. In this plot, for each genotype a regression line is fitted to assess the relationship between the dependent variable and body weight. Then a locally weight line (loess line) is plotted. The loess line allows assessment that the regression line fits all the data well. Note the loess line can be distorted by a few data points so if it deviates strongly but for only a few data points, this is not concerning. This graph is used to assess whether a linear relationship exists

and whether it is the same for both genotypes.

In the Akt2 example, it can be clearly seen that a common linear relationship exists between lean mass and body weight, such that as the weight increases so does the lean mass. It can also be seen that the knockout animals have a lower body weight and subsequently lower lean mass but the drop in lean mass is entirely in accordance with the drop in body weight.

> scatterplotGenotypeWeight(test, depVariable="Lean.Mass")

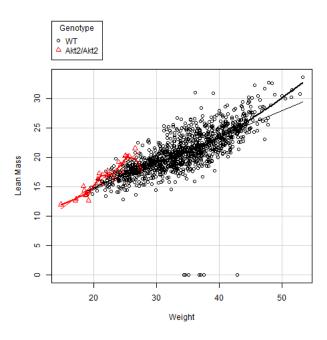


Figure 26: scatterplotGenotypeWeight function for Akt2 example.

# 6.2 PhenStat Usage Example Categorical Data

The following dataset, provided by Wellcome Trust Sanger Institute (WTSI) Mouse Genetics Project (MGP) of high resolution X-ray data obtained from a study on gene knockout mice carrying the Aff3tm1a(EUCOMM)Wtsi targeted allele which were created by blastocyst injection of targeted ES cells, and bred on the B6N genetic background. Data was collected on a standardized high throughput phenotyping pipeline following a multi-batch workflow, where regular control animals are collected and knockout animals of the correct age are then issued to the pipeline as they arise. At WTSI, batch to batch variation has not been found to be significant for these rare event cat-

egorical variables. Consequently, we ignore batch and combine data for the same genetic background when collected with the same protocol and housing and husbandry conditions. This increases the sensitivity of the analysis as we have more accuracy on the estimate of the prevalence of the condition in the wild type population.

Genotype	Gender	Number Animals	Number Batches
1 ff 0 / 1 ff 0	Female	7	4
Aff3/Aff3	Male	6	4
Wild type	Female	446	70
Wild type	Male	451	70

Table 9: Number of animals and number of batches in the Aff3 dataset

### 6.2.1 Loading the data and initial steps of analysis

Initial steps focus on loading the data, using the PhenStat tools to generate the PhenList object, and then the result object. We can then explore the data and fitted results using the visualisation and output functions.

```
> aff3data=read.csv("categorical_example 1_aff3_Xray.csv")
> test <- PhenList(dataset=aff3data,testGenotype="Aff3/Aff3",
    refGenotype="+/+", dataset.colname.batch="Assay.Date")
> result <- testDataset(test, depVariable="Thoracic.Processes", method="FE")</pre>
```

#### 6.2.2 Visualisation of data

The function categoricalBarplot has been provided to visualise the categorical data as summary percentage data. It reports the percentage of each classification observed for up to three datasets: all data, male only and female only. It is important to note that percentage accuracy is very dependent on the number of readings so it is important to consider the dataset size when interpreting these graphs. Therefore tables showing both the percentage and count values are included in the summaryOutput.

```
> categoricalBarplot(result)
```

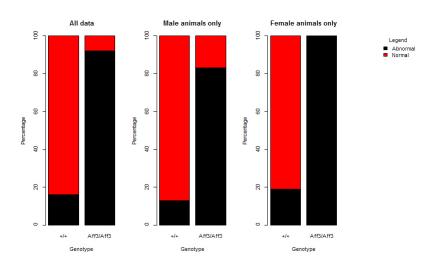


Figure 27: categoricalBarplot function for Aff3 example.

## 6.2.3 Understanding the summaryOutput

The first two lines of the *summaryOutput* confirm the statistical framework used and the dependent variable studied. The next section of the output reports the summary of statistical assessment. Two measures are provided for each dataset considered. First a test of statistical significance assessed using a Fisher Exact Test and then a measure of biological significance, the maximum effect size. The final section of the output provides tables showing the counts and percentage calculated for each group and possible level.

The following is reported for dependent variable thoracic processes for the *Aff3* dataset and we can see that for all datasets, there is a statistically significant change with a large effect size.

The *summaryOutput* function shows the model fitted and the model output for the analysis of the thoracic processes for the *Aff3* dataset. The example is showing the summary tables provided for the composite (male and female data) for the thoracic processes for the *Aff3* dataset.

```
> summaryOutput(result)
```

. . .

Model output:

All data p-val: 4.35745946092922e-09

All data effect size: 76%

Males only p-val: 0.00025633944344021

Males only effect size: 70%

```
Females only p-val: 1.00779809539594e-05
Females only effect size: 81%
Matrix 'all':
       +/+ Aff3/Aff3
Abnormal 142 12
Normal 753
Percentage matrix 'all' statistics:
       +/+ Aff3/Aff3 ES change
Abnormal 16 92 76
Normal
                  8
                           76
Matrix 'all' statistics:
                 X^2 df P(> X^2)
Likelihood Ratio 36.678 1 1.3931e-09
Pearson
              53.164 1 3.0675e-13
Phi-Coefficient : 0.242
Contingency Coeff.: 0.235
Cramer's V
           : 0.242
```

### 6.2.4 Understanding the maximum effect size reported

The maximum effect size is the maximum percentage change seen for an observation type. Below is a table showing an artificial example where the majority of the wild type are normal but the abnormality is spread across multiple levels in the knockout. For each trait level (i.e. the observed phenotype), the change in percentage effect size is seen by subtracting the percentage observed in the knockout from the wild type. Then across all the observed levels, the maximum percentage change is selected after ignoring the direction of the change. Thus in the example below, the maximum effect size would be 86.5% which indicates that there has been 86.5% change in how often a level is observed.

## 6.2.5 A dependent variable with little variation

Within the IMPC pipeline, there are a number of dependent variables which have little variation but are numeric. For example, no of digits, or number of caudal vertebrae etc. If you try to process these variables through a mixed

Trait level	wildty	ype	knock	kout	Effect size calculation	Effect size
Trait level	count	%	count	%	Effect Size calculation	Effect size
Normal	198	99	1	12.5	99-12.5	86.5
Abnormal left eye	0	0	0	0	0	0
Abnormal right eye	1	0.5	4	50	0.5 - 50	49.5
Abnormal both eye	1	0.5	3	37.5	0.5 - 37.5	37

Table 10: Number of animals and number of batches in the Aff3 dataset

model framework the analysis will stop and an error will report that there is insufficient variability in the data.

For our example dataset, the number of ribs is a dependent variable with little variation as shown by plotting the data with the *categoricalBarplot* function.

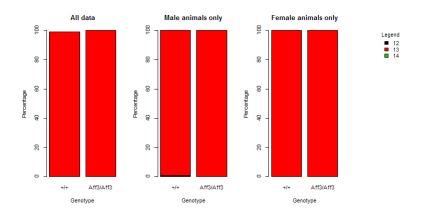


Figure 28: categoricalBarplot function for Aff3 example with number of ribs as dependent variable.

If we try and process this variable through a mixed model framework the following output is obtained:

> result<-testDataset(test,depVariable="Number.Of.Ribs.Left",method="MM")

#### Error

Insufficient variability in the dependent variable 'Number.Of.Ribs.Left' for MM framework. Fisher Exact Test can be better way to do the analysis.

#### Error

Insufficient variability in the dependent variable 'Number.Of.Ribs.Left' for genotype/gender combinations to allow the application of Mixed Model.

Instead the dependent variable should be treated as a categorical variable which each numeric output possible treated as a level allowing a statistical comparison of how the levels are distributed between the knockout and wild-type groups. Thus for our example the following summary output and count table is obtained:

```
> summaryOutput(result)
Test for dependent variable: Number.Of.Ribs.Left
Method: Fisher Exact Test framework
Model output:
All data p-val: 1
All data effect size: 0%
Males only p-val: 1
Males only effect size: 0%
Females only p-val: 1
Females only effect size: 0%
Matrix 'all':
  +/+ Aff3/Aff3
12 1 0
13 893
           13
Percentage matrix 'all' statistics:
  +/+ Aff3/Aff3 ES change
12 0 0
                      0
13 100 100
14 0 0
                      0
```

# 6.3 PhenStat Example Using Cluster

If someone would like to analyse all variables in the dataset and has a cluster available for such kind of job then here is an example of PhenStat package usage.

First, the function that runs on each cluster's node and stores the results in particular directory is created. This function is based on the section dataset.stat of the PhenList object.

```
PhenStatCluster<-function(phenList,i){
    # reads variable names from dataset.stat table
    variable <- as.character(phenList$dataset.stat$Variables[i])

# checks if variable is continuous again by using dataset.stat table</pre>
```

```
isContinuous <- phenList$dataset.stat$Continuous[i]</pre>
    # skip the analysis for Batch and Genotype variables
    if (!(variable %in% c("Batch", "Genotype"))){
      if (isContinuous && !(variable %in% c("Weight")))
  # performs MM framework for continuous data
  result <- testDataset(phenList, variable, method="MM",outputMessages=FALSE)</pre>
     else
  if (!isContinuous){
     # performs FET framework for categorical data
     result <- testDataset(phenList, variable, method="FE",outputMessages=FALSE)</pre>
   }
  else
     # performs MM framework for weight variable
     result <- testDataset(phenList, variable, method="MM",equation="withoutWeight",outputMessages=FALSE)
     write(vectorOutput(result),paste("./",variable,".txt",sep="")) # stores the results
    }
}
We are planning to analyse every individual variable of the dataset using a
cluster. Each one cluster node has to have sourced function PhenStatCluster
and loaded PhenStat library. PhenList object with dataset to analyse should
also be available for every cluster node.
# cluster preparation
# set the folder
setwd("/yourWorkingDirectory")
# create logs folder in it
dir.create(paste(getwd(), "/logs", sep=""))
# define tasks
tasks <- c(1:length(test$dataset.stat$Variables))</pre>
# load snow
# snow creates and manages clusters
library(snow)
# create cluster
cluster = makeCluster(length(tasks), type="...") # type values: MPI, RCLOUD, etc.
# Setup cluster nodes
# set current folder on each node
clusterEvalQ(cluster, setwd("/yourWorkingDirectory"))
# create logs and forward output to the log files
clusterEvalQ(cluster, try({ fn = paste(getwd(), "./", Sys.info()[4], "-", Sys.getpid(), ".log", sep="");
```

o <- file(fn, open = "w"); sink(o); sink(o, type = "message"); }))</pre>

```
# test output is routed to the logs
clusterEvalQ(cluster, message("message - OK"))
clusterEvalQ(cluster, cat("cat - OK"))

# load package and source function for each node
clusterEvalQ(cluster, library(PhenStat))
clusterEvalQ(cluster, source("/pathToTheSource/PhenStatCluster.R"))

# export PhenList object to make it available for every node
clusterExport(cluster, "test")

# finally apply function for each one variable within the dataset
clusterApplyLB(cluster, tasks, function(x){ message("------ processing ",
test$dataset.stat$Variables[x], " ------"); try(PhenStatCluster(test,x)); })

# clean up
stopCluster(cluster)
rm(cluster)
clusterCleanup()
```

The output is available in the specified directory: "/yourWorkingDirectory". For each variable from the dataset the output file with results in vector format is created.

## References

Gentleman, R., Carey, V., Huber, W., Irizarry, R., Dudoit, S. (2008) Bioinformatics and Computational Biology Solutions Using R and Bioconductor. Springer. ISBN 978-0-387-25146-2.

Gentleman, R. (2008) R Programming for Bioinformatics. Chapman & Hall\CRC. ISBN 978-1-4200-6367-7.

Hahne, F., Huber, W., Gentleman, R., Falcon, S. (2008). Bioconductor Case Studies. Springer. ISBN 978-0-387-77239-4.

Karp,N., Melvin,D., Sanger Mouse Genetics Project, Mott,R. (2012) Robust and Sensitive Analysis of Mouse Knockout Phenotypes, PLoS ONE, 7(12), e52410, doi:10.1371/journal.pone.0052410.

West,B., Welch,K., Galecki,A. (2007) Linear Mixed Models: A practical guide using statistical software. Chapman & Hall\CRC. ISBN 978-1-584-88480-4.

E. Andrés Houseman, Louise M. Ryan and Brent A. Coull (2004) Cholesky Residuals for Assessing Normal Errors in a Linear Model with Correlated Outcomes, Journal of the American Statistical Association, 99 (466), 383-394

C.A. Pinkert, Transgenic Animal Technology. A laboratory Handbook (2002), Academic Press Inc., USA