

Final Study Guide

The final exam will be cumulative and any may include any material from lectures/assignments/quizzes from the entire semester. The following list of topics outline all material after the midterm. For a list of topics from before the midterm, see the ‘Midterm Topics List’

- **Algorithms**

- Linear search/binary search
- Bubble sort/insertion sort
- Greedy algorithms
- \mathcal{O} , Ω , Θ notation
- Complexity of matrix operations
 - * Matrix-matrix addition
 - * Mat-vec multiplication
 - * Matrix-matrix multiplication

- **Number theory**

- divisibility ($a \mid b$)
- The division algorithm
- Congruence modulo m
- Fast modular exponentiation (using binary representation of exponent)
- prime vs composite
- Fundamental theorem of arithmetic
- trial division
- prime sieve of Eratosthenes
- gcd
- Euclidean algorithm
- Solving linear congruences
- inverse of $a \bmod m$
- Bezout’s theorem
- Solving systems of linear congruences
 - * Back substitution
 - * Chinese remainder theorem
- Fermat’s little theorem
- Encryption/decryption
 - * Shift/Caesar cipher
 - * Affine cipher
 - * RSA

- **Recursion**

- recursive sequences
- recursive functions
- recursive sets

- recursive factorial algorithm

- **Combinatorics**

- The product rule/sum rule
- Pigeonhole principle (generalized)
- permutations/combinations
 - * w/ and w/out repetition
- Binomial theorem

- **Probability**

- experiment, sample space, event
- definition of discrete probability in terms of cardinalities
- probabilities of complements and unions of events
- probability distributions
- uniform distribution
- conditional probabilities
- Bayes' theorem
- Law of total probability

- **Recurrences**

- Solving counting problems with recurrences
- linear homogeneous recurrence relations
- characteristic polynomial
- Nonhomogeneous recurrences

- **Relations**

- relations as graphs
- reflexive, symmetric, transitive
- equivalence relations
- equivalence classes

- **Graph theory**

- directed/undirected graphs
- adjacency list/adjacency matrix
- degree sequence
- the handshake theorem
- in/out degrees
- walks/paths/Eulerian tours
- disconnectedness/connectedness
- connected components
- strongly/weakly connected
- graph coloring
- bipartite graphs
- chromatic number of a graph
- greedy coloring theorem
- 4 color theorem