

Annotated bibliography on complex networks

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1 Network models

The first attempt to model real-complex networks was the Erdős-Rényi (ER) model of random networks. That model does not represent adequately real-world networks.

As an explanation of real-world network being more clustered than random networks, Watts and Strogatz [WS98] defined the small-world property of complex networks: networks having this property have an average path length similar to random networks, but a much higher clustering coefficient. Later, Latora and colleagues [LM01] reformulated the small-world property in terms of global and local efficiency.

Barabási and colleagues introduced the BA scale-free model of complex networks, where the mechanisms of growth and preferential attachment lead to a degree distribution following a power law [BA99]. Arguably, the behavior of the world-wide-web can be explained with this model [BAJ00]. The BA model has a low clustering coefficient, contrarily to random networks, then in [KE02] is defined a KE generative model of highly-clustered scale-free networks. In Refs. [HK02a] and [RB03] can be found other network models with power-law degree distribution, short average path length and high clustering coefficient.

Empirical research identified three structural classes of small-world networks: scale-free networks, with a degree distribution with a tail that decays as a power law, broad-scale or truncated scale-free, with a power-law regime followed by a sharper cutoff and single-scale networks, with a fast-decaying tail [ASBS00]. The emergence of the first two networks can be explained by optimization mechanisms, complementary to growth and preferential attachment [CS03].

2 Airport networks

The first analysis of the world airport network (WAN) were reported by [GMTA05, GA04] as unweighted network and by [BBPSV04] as weighted network.

The first analysis of the Chinese airport network were carried out by [LC04]. Later, [Lin12] makes a complex network and spatial analysis of the Chinese air transport network. Other regional studies of airport networks are:

- India: [Bag08]
- Brazil: [Roc09]

[ZL13] is a review of studies of air transport networks. The section of dynamic models of air transport is of special interest, especially for the referenced studies of connectivity [BW05] and [MPR08].

3 Air route networks

Analysis of air route networks: [CZDC12, SW14, SWL15, DLY⁺17].

4 Static robustness

Introduction of the problem of static robustness: [AJB00].

Analysis of static robustness in terms of network efficiency: [CLMR03] for BA and KE graphs, [CLMR04] for BA graphs. Scale-free tend to be robust to errors, but sensitive to attacks. In Ref. [HKYH02] is performed an analysis of the effect of edge and node removal for several real-world and models of complex networks.

In [PTHS05] is obtained the network that optimizes robustness for the sum of critical threshold for random deletion [CEBAH00] and for deletion of central nodes [CEBAH01].

Measures of network robustness: algebraic connectivity [Fie73], effective graph resistance [ESV⁺11] and mutiscale vulnerability [BBC⁺07].

Schneider and colleagues [SMA⁺11] define a unique network robustness measure (in [HHL⁺17] is described a procedure to compute an approximate value). They optimize this measure rewiring network nodes, maintaining the degree of each node. Refinements of this strategy can be found in [LDHT13, YLC⁺15, ZL14].

In [DBBV06] is introduced a method to evaluate robustness with weighted networks.

5 Cascading failures

In Ref. [ML02] is defined a global load-based model of cascading failures. Node load is equal to number of shortest paths passing through it. Nodes with load above capacity are removed from the network. Evolution is tracked through size of connected component. In Ref. [CLM04] is defined an similar model, and track evolution of damage through network efficiency.

In Ref. [WC08] is defined a local weighted flow redistribution rule model for cascading failures. In this model, the load of congested edges is redistributed locally, among the adjacent edges.

In Ref. [MGP02] is defined a fiber-bundle model of cascading failures, and in [HYY06] a sandpile model for a geographical network.

Holme and colleagues analyze the cascading failures for node [HK02b] and edge [Hol02] overload in growing networks. As the network grows, values of node or edge betweenness increase, so when they reach a critical point a cascading failure may arise.

6 Spatial networks

In [BGB19] is presented a good introduction to spatial analysis, using historical data from the French rail network.

References

- [AJB00] ALBERT, R.; JEONG, H. AND BARABÁSI, A.-L., 2000. Error and attack tolerance of complex networks. *Nature*, 406(6794):378–382. doi:10.1038/35019019.

KEY: Albert2000

ANNOTATION: Complex networks are divided in two major classes. Exponential networks, with a degree distribution that peaks around average and decays exponentially. These networks are homogeneous, and high-degree nodes are statistically non-significant. Theoretical models of exponential networks are the Erdős-Rényi (ER) or Watts-Strogatz (WS) models. Scale-free networks have a degree distribution that decays with a power-law. These networks are non-homogeneous and high-degree nodes are statistically significant. These networks have a different behaviour facing errors (removal of nodes at random) and attacks (removal of nodes of high degree). ER networks are fragmented when a fraction f_c of nodes is reached when exposed to errors and attacks. Scale-free networks are very resilient to errors, but vulnerable to attacks. When attacked, scale-free networks are fragmented with a fraction of removed nodes smaller than the f_c of random graphs.

- [AN07] ASH, J. AND NEWTH, D., 2007. Optimizing complex networks for resilience against cascading failure. *Physica A: Statistical Mechanics and its Applications*, 380(1-2):673–683. doi:10.1016/j.physa.2006.12.058.

KEY: Ash2007

ANNOTATION: As authors adopt the Crucitti model of cascading failures to justify that maximizing network efficiency leads to reduction of cascading failures. Efficiency is optimized with two constraints: that the network have a single connected component, and that network connectivity (number of edges) is below a critical level. Optimization is made using a local search method with three moves: creating edges at random, deleting edges at random and rewiring existing connections. The resulting optimized network is of broad scale, and with a characteristic path length larger than scale-free networks.

- [ASBS00] AMARAL, L. a. N.; SCALA, A.; BARTHELEMY, M. AND STANLEY, H. E., 2000. Classes of small-world networks. *Proceedings of the National Academy of Sciences*, 97(21):11149–11152. doi:10.1073/pnas.200327197.

KEY: Amaral2000

ANNOTATION: After empirical examination of real-world networks, authors identify three structural classes of small-world networks: a) scale-free networks, with a degree distribution with a tail that decays as a power law, b) broad-scale or truncated scale-free, with a degree distribution that has a power-law regime followed by a cutoff, like an exponential or Gaussian decay, c) single-scale networks, with a degree distribution with a fast-decaying tail, like

exponential or Gaussian. The last two regimes can be reached modifying the preferential attachment mechanism introducing aging of vertices or introducing cost of adding links and limited capacity of highly connected nodes.

- [BA99] BARABASI, A.-L. AND ALBERT, R., 1999. Emergence of scaling in random networks. *Science*, 286(5439):509–512. doi:10.1126/science.286.5439.509.

KEY: BarabasiA.-L;Albert1999

ANNOTATION: Networks that grow through simultaneous growth and preferential attachment have a degree distribution decaying following a power law $k^{-\lambda}$ with $\lambda = 3$. Exponents of different value may appear caused by additional mechanisms, like connection of old nodes or existence of directed connections. As the same degree distribution is observed with different evolutions of size / time, this type of networks are known as scale-free.

- [Bag08] BAGLER, G., 2008. Analysis of the airport network of India as a complex weighted network. *Physica A: Statistical Mechanics and its Applications*, 387(12):2972–2980. doi:10.1016/j.physa.2008.01.077.

KEY: Bagler2008

ANNOTATION: In this paper we are learned about the properties of the Airport Network of India (ANI). Similarly to other airport networks, the ANI has the small-world property and a power-law degree distribution. Clustering coefficient decays as node degree increases, showing evidence of a hierarchical organization of this network. ANI is also analyzed as a weighted network, being weights the number of flights between each pair of connected airports. Node strength is correlated with node degree similarly to the WAN, as found in [BBPSV04].

- [BAJ00] BARABÁSI, A.-L.; ALBERT, R. AND JEONG, H., 2000. Scale-free characteristics of random networks: the topology of the world-wide web. *Physica A: Statistical Mechanics and its Applications*, 281(1-4):69–77. doi: 10.1016/S0378-4371(00)00018-2.

KEY: Barabasi2000

ANNOTATION: The Barabasi-Albert model of scale-free networks is applied to the www network. According to this model, the mechanisms of growth and preferential attachment lead to a network with a degree distribution following a power law. This mechanism does not describe the www faithfully, but according to authors captures the main ingredients that structure the www. The actual structure of the www may depend of other characteristics, like nonlinear preferential attachment, rewiring of existing links or the appearance of new links.

- [BBC⁺07] BOCCALETTI, S.; BULDÚ, J.; CRIADO, R.; FLORES, J.; LATORA, V.; PELLO, J. AND ROMANCE, M., 2007. Multiscale vulnerability of complex networks. *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 17(4):043110. doi:10.1063/1.2801687.

KEY: Boccaletti2007

ANNOTATION: To analyze the impact of the deletion of one of several edges (without deleting any node) on graph connectivity, authors propose multiscale measures equal to the average edge betweenness. Graphs with an unequal distribution of loads will have higher values of edge betweenness and then will be more vulnerable. As the average betweenness is proportional to average path length, a complete exam of the scales $p > 0$ must be considered. In some cases might happen that two graphs may have equal values of vulnerability for $p = 1$ and $p = \infty$, so all scales must be considered. The formula for $p = -1$ yields a parameter similar to efficiency, but with edge betweenness instead of distances.

- [BBPSV04] BARRAT, A.; BARTHÉLEMY, M.; PASTOR-SATORRAS, R. AND VESPIGNANI, A., 2004. The architecture of complex weighted networks. *Proceedings of the National Academy of Sciences of the United States of America*, 101(11):3747–52. doi:10.1073/pnas.0400087101.

KEY: Barrat2004

ANNOTATION: The article analyzes complex networks whose edges have assigned weights representing the intensity of relationship between the nodes connecting them. Authors introduce metrics specific for complex weighted networks: node strength, weighted clustering coefficient and weighted average nearest-neighbors degree. Using two samples of the scientific citation network and the world airport network, they define a methodology for analyzing the architecture of complex weighted networks. They analyze the relationship between strength and degree and strength and betweenness, the distribution of weighted clustering coefficient as a function of node degree, and node strength correlation.

- [BC18] BROIDO, A. D. AND CLAUSET, A., 2018. Scale-free networks are rare. pp. 26–28.

KEY: Broido2018

ANNOTATION: A central claim of modern network science is that real-world networks are typically scale-free, meaning that degree distribution follows a power law k^γ with $2 < \gamma < 3$. Authors test this claim with 927 data sets from the Index of Complex Networks (ICON), comparing its plausibility via a likelihood test to alternative models, e.g., log-normal. Results show that only a few fraction of these networks show strong evidence of being scale-free. Authors claim that there is likely no single universal mechanism (e.g., preferential attachment) that can explain the wide diversity of degree structure found in real-world networks.

- [BCPZ16] BELKOURA, S.; COOK, A.; PEÑA, J. M. AND ZANIN, M., 2016. On the multi-dimensionality and sampling of air transport networks. *Transportation Research Part E: Logistics and Transportation Review*, 94:95–109. doi:10.1016/j.tre.2016.07.013.

KEY: Belkoura2016

ANNOTATION: This article reports how topological metrics depend on how the airport network is reconstructed, that is, the rules used to sample nodes and connections. They have used several sources of route data: the ALL-FT+ data set provided by the EUROCONTROL PRISME group, the On-Time Performance dataset provided by the Research and Innovative Technology Administration (RITA) of the US and OpenFlights. They find that using connections from a subset of airlines yields a more accurate representation than using a subset of airports, even when small airports are omitted.

- [BGB19] BOTTINELLI, A.; GHERARDI, M. AND BARTHELEMY, M., 2019. Efficiency and shrinking in evolving networks. pp. 1–12.

KEY: Bottinelli2019

ANNOTATION: This paper analyzes the evolution of the French railway network between 1840 and 2000, in correlation with evolution of French communes' population. Using elements of spatial networks theory, authors analyze the temporal evolution of network components; the evolution of measures of cost, efficiency and robustness; the evolution of population and coverage properties, including accessibility analysis.

- [BW05] BURGHOUWT, G. AND DE WIT, J., 2005. Temporal configurations of European airline networks. *Journal of Air Transport Management*, 11(3):185–198. doi:10.1016/j.jairtraman.2004.08.003.

KEY: Burghouwt2005

ANNOTATION: Spatial and temporal concentration are the two main features of the hub-and-spoke network. Airlines using an hub-and-spoke configuration organize their flights in a wave-system structure, that helps them to offer many indirect connections around a hub. In this paper, authors define a methodology to detect wave-system structures, and define a metric of indirect connectivity based on the number and quality of indirect connections generated by a flight schedule. The later metric is based on previous work reporting passengers' preferences with indirect connections. They use these concepts to analyze the effects of a wave-system structure on indirect connectivity.

- [CEBAH00] COHEN, R.; EREZ, K.; BEN-AVRAHAM, D. AND HAVLIN, S., 2000. Resilience of the Internet to Random Breakdowns. *Physical Review Letters*, 85(21):4626–4628. doi:10.1103/PhysRevLett.85.4626.

KEY: Cohen2000a

ANNOTATION: The article uses infinite percolation theory to obtain the critical threshold for networks with nodes connected randomly (not necessarily random networks). This threshold is the fraction of removed nodes at random that disconnects the network. For networks with a scale-free degree distribution k^γ , it is

found that for $\gamma < 3$ the threshold diverges, so that the network keeps connected even for an arbitrarily large fraction of removed nodes.

- [CEBAH01] COHEN, R.; EREZ, K.; BEN-AVRAHAM, D. AND HAVLIN, S., 2001. Break-down of the Internet under Intentional Attack. *Physical Review Letters*, 86(16):3682–3685. doi:10.1103/PhysRevLett.86.3682.

KEY: Cohen2001a

ANNOTATION: This article uses infinite percolation theory to analyze the effect of the removal of nodes of highest degree in scale free networks, with degree distribution k^γ . Results show that these networks are disrupted with the removal of a small fraction of nodes of highest connectivity for all $\gamma > 2$. Network robustness increases as lower connectivity cutoff m (smallest nonzero degree) increases. It is also observed that average path length in the spanning cluster grows dramatically near criticality, making communication very inefficient even before disruption of the spanning cluster.

- [CLM04] CRUCITTI, P.; LATORA, V. AND MARCHIORI, M., 2004. Model for cascading failures in complex networks. *Physical Review E*, 69(4):045104. doi:10.1103/PhysRevE.69.045104.

KEY: Crucitti2004

ANNOTATION: The dysfunction of a few nodes in a network transporting flows can initiate a dynamic process of cascading failures, as other nodes may experience malfunction if their load exceeds their capacity. In this model of cascading failures, overloaded nodes are not removed from the network, and the damage caused by a cascade is quantified in terms of decrease of global efficiency. In this model, the load of a node is proportional to the total number of most efficient paths passing through it, and capacity is proportional to its initial load and a tolerance parameter α for the network. The overload of a node degrades the communication through edges incident to that node, so shortest paths will go through other nodes. Two triggering strategies are examined: random removals and load-based removals. ER and BA graphs react similarly to random removals, while BA graphs are more sensitive to load-based removals.

- [CLMR03] CRUCITTI, P.; LATORA, V.; MARCHIORI, M. AND RAPISARDA, A., 2003. Efficiency of scale-free networks: error and attack tolerance. *Physica A: Statistical Mechanics and its Applications*, 320:622–642. doi:10.1016/S0378-4371(02)01545-5.

KEY: Crucitti2003

ANNOTATION: This paper reports the evolution of global (average path length and global efficiency) and local (clustering coefficient and local efficiency) properties of two models of scale-free networks when suffering errors (removal of random nodes) and attacks (removal of nodes of highest degree). The scale-free networks analyzed are the BA model, with low clustering coefficient,

and the KE model, with high clustering coefficient. For these networks, global and local efficiencies are unaffected by the failure of random nodes, but extremely sensitive to the removal of high degree nodes. This paper defines the efficiency approach to static robustness in more detail than works from the same authors.

- [CLMR04] CRUCITTI, P.; LATORA, V.; MARCHIORI, M. AND RAPISARDA, A., 2004. Error and attack tolerance of complex networks. *Physica A: Statistical Mechanics and its Applications*, 340(1-3):388–394. doi:10.1016/j.physa.2004.04.031.

KEY: Crucitti2004b

ANNOTATION: The tolerance to errors (removal of random nodes) and attacks (removal of central nodes) on ER random networks and BA scale-free networks can be compared examining the impact on global efficiency of the removal of nodes chosen according to the following criteria: random, degree, betweenness and adaptive betweenness. As ER are homogeneous networks, they react similarly to all criteria, while BA networks are resilient to errors but vulnerable to attacks. The paper is complemented with the cascading failures model based on load redistribution.

- [CS03] CANCHO, R. F. i. AND SOLÉ, R. V., 2003. Optimization in Complex Networks. pp. 114–126. doi:10.1007/978-3-540-44943-0_7.

KEY: Cancho2003

ANNOTATION: Complex networks can be the outcome of preferential mechanisms and optimization mechanisms, plus additional constraints imposed by the available components to the evolving network. Optimization of networks is examined in this paper, where a energy objective function, combination of normalized vertex-vertex distance and normalized number of links. When normalized number of links has more weight, the resulting network has an exponential degree distribution, and when normalized vertex-vertex distance is predominant, the optimized network is a star network. For intermediate weights, the result of optimization is truncated scale-free networks.

- [CZDC12] CAI, K.-Q.; ZHANG, J.; DU, W.-B. AND CAO, X.-B., 2012. Analysis of the Chinese air route network as a complex network. *Chinese Physics B*, 21(2):028903. doi:10.1088/1674-1056/21/2/028903.

KEY: Cai2012a

ANNOTATION: This article analyzes an air route network, a spatial network where nodes are air route waypoints (ARW) and the edges air route segments (ARS), with weight equal to the number of flights passing on a time window. Nodes in this network cannot have hubs, which would lead to traffic congestion and flight conflicts. As a consequence, the air route network has an homogeneous degree distribution, together with an heterogeneous, exponential strength distribution. Instant values and evolution of node strength can be useful elements to assess the evolution of air traffic in a geographical region.

- [DBBV06] DALL’ASTA, L.; BARRAT, A.; BARTHÉLEMY, M. AND VESPIGNANI, A., 2006. Vulnerability of weighted networks. *Journal of Statistical Mechanics: Theory and Experiment*, 2006(04):P04006–P04006. doi:10.1088/1742-5468/2006/04/P04006.

KEY: DallAsta2006

ANNOTATION: This article analyzes the robustness of the world airport network considering not only topological indicators (the ones obtained with the unweighted network) but also geographical and traffic indicators, associating weights to edges such as distance and available seats. Authors use Tau’s Kendall to compare rankings of nodes obtained from local (degree and strength) and global (betweenness and unweighted betweenness) indices of centrality. They carry out robustness analysis using as performance indicators the size of largest connected component and giant’s component integrity, defined as the sum of strengths of nodes remaining in the largest connected component. The decline in integrity is sharper than in size, and similar for any strategy of removal of central nodes.

- [DDL18] DAI, L.; DERUDDER, B. AND LIU, X., 2018. The evolving structure of the Southeast Asian air transport network through the lens of complex networks, 1979–2012. *Journal of Transport Geography*, 68(October 2017):67–77. doi:10.1016/j.jtrangeo.2018.02.010.

KEY: Dai2018

ANNOTATION: The article explores the structural evolution of the Southeast Asian air transport network (SAAN) during 1979-2004 from a complex network perspective. First, authors study the evolution of network metrics (scale-free properties, dissortative mixing and small-world properties), and compare them with other major regional blocs. Second, they unveil the core-bridge-periphery structure of the SANN, and its temporal evolution. This multi-layer structure has experienced significant changes in the studied period, as the core of the network shifts towards the north. Additionally, the introduction contains an geographical and historical analysis of Southeast Asia, and discuss the opportunity of defining region boundaries to analyze transportation networks.

- [DLY⁺17] DU, W.; LIANG, B.; YAN, G.; LORDAN, O. AND CAO, X., 2017. Identifying vital edges in Chinese air route network via memetic algorithm. *Chinese Journal of Aeronautics*, 30(1):330–336. doi:10.1016/j.cja.2016.12.001.

KEY: Du2017b

ANNOTATION: The object of analysis of this paper is the Chinese air route network. Its nodes are waypoints and its edges air route segments connecting them. This is the network where real flight operations take place. This network is quite different from airport networks: it has low clustering coefficient, large average shortest path length and exponential degree distribution. This properties

come from the spatial properties of the network. Authors investigate the robustness of this network to edge isolation detecting vital edges with a memetic algorithm. They find that the most vital edges are not the ones with highest topological importance (defined by edge betweenness).

- [DSP18] DAS, K.; SAMANTA, S. AND PAL, M., 2018. Study on centrality measures in social networks: a survey. *Social Network Analysis and Mining*, 8(1):13. doi:10.1007/s13278-018-0493-2.

KEY: Das2018

ANNOTATION: An article with awful writing and structuring. Can be of interest to check some centralities for characterizing important nodes, not necessarily on complex networks, like the ones based on k-core decomposition (k-shell centrality) or in number of closed loops (subgraph centrality and functional centrality).

- [DWZ10] DOU, B.-L.; WANG, X.-G. AND ZHANG, S.-Y., 2010. Robustness of networks against cascading failures. *Physica A: Statistical Mechanics and its Applications*, 389(11):2310–2317. doi:10.1016/j.physa.2010.02.002.

KEY: Dou2010

ANNOTATION: This paper proposes a modification of the Motter and Lai (ML) model of cascading failures. The ML model proposes that node capacity is proportional to initial load $C_i = (1 + \alpha) L_{0i}$, and here authors suggest a load equal to $C_i = L_{0i} + \beta L_{0i}^\alpha$. This model is applied to BA and ER networks and to the power grid and the internet. The contribution is rather limited, as the justification for a nonlinear load is weak.

- [ESV⁺11] ELLENS, W.; SPIEKSMAN, F.; VAN MIEGHEM, P.; JAMAKOVIC, A. AND KOOLIJ, R., 2011. Effective graph resistance. *Linear Algebra and its Applications*, 435(10):2491–2506. doi:10.1016/j.laa.2011.02.024.

KEY: Ellens2011

ANNOTATION: In this context, a graph is treated as a electrical circuit, with resistance between vertices equal to edge weights. The effective resistance between two vertices is obtained applying Kirchhoff laws when a difference of potential is applied between these nodes, and effective graph resistance is equal to the sum of the effective resistances over all pair of vertices. Effective resistance is infinite for non-connected graphs, and will decrease as graph connectivity increases by adding edges or increasing edge weights. It can be used as a measure of robustness as takes the number of paths between any pair of vertices and their length into account. It can be calculated as the sum of reciprocals of the eigenvalues of the Laplacian, excluding the smallest eigenvalue. The paper provides computation procedures and defines graphs of optimal effective resistance.

- [Fie73] FIEDLER, M., 1973. Algebraic connectivity of graphs. *Czechoslovak Mathematical Journal*, 23(2398):298–305.

KEY: Fiedler1973

ANNOTATION: The algebraic connectivity of a graph is the second smallest eigenvalue of the Laplacian of a graph. Diagonal of the Laplacian is equal to node degree, and the off diagonal elements equal to -1 if edge (i, j) exists and zero otherwise. In this paper is denoted as $a(G)$, and as λ_2 elsewhere. It is related with two other concepts: edge connectivity $e(G)$, or the minimal number of edges whose removal results in losing connectivity, and vertex connectivity $v(G)$ is defined similarly for removal of vertices together with adjacent edges. Algebraic connectivity is greater than zero if and only if G is a connected graph. The magnitude of this value reflects how well connected the overall graph is, so that the larger is, the better connected the graph is. For non-complete graphs, $a(G) \leq v(G)$, and $v(G) \leq e(G)$.

- [Fie04] FIEDLER, K., 2004. Tools, Toys, Truisms, and Theories: Some Thoughts on the Creative Cycle of Theory Formation. *Personality and Social Psychology Review*, 8(2):123–131. doi:10.1207/s15327957pspr0802_5.

KEY: Fiedler2004

ANNOTATION: This article studies the creative process of theory formation, and how theoretical thinking can be instigated and trained. Drawing on Moscovici's approach to social influence of majorities and minorities, author sees theory formation as a dialectic interplay between conversion (break-up with existing theories by the minorities) and compliance (establishment of existing theories by the majority). Author also argues that theoretical thinking can be instigated and trained with game-like heuristics. Loosening games are pluralistic-competition, distal-import and paying around with tools and methods. Tightening games are falsification and challenge (as in peer review), method-development and uncovering of pseudo-theories (quasi tautological theoretical constructions).

- [GA04] GUIMERÀ, R. AND AMARAL, L. A. N., 2004. Modeling the world-wide airport network. *The European Physical Journal B - Condensed Matter*, 38(2):381–385. doi:10.1140/epjb/e2004-00131-0.

KEY: Guimera2004

ANNOTATION: In this first analysis of the worldwide airport network, it is found that its degree distribution has a truncated power-law decaying tail, and that it has the small-world property. The existence of nodes with small degree and high betweenness is a specific property of this network. These anomalies exist because they act as hubs between their communities and the rest of the network. Authors identify the communities with a simulated annealing algorithm, and define the role of each node using two parameters: within-module degree and participation coefficient. Based on these values, they identify up to seven universal roles, that account for the multi-community structure of the network.

- [GMTA05] GUIMERA, R.; MOSSA, S.; TURTSCHI, A. AND AMARAL, L. a. N., 2005. The worldwide air transportation network: Anomalous centrality, community structure, and cities' global roles. *Proceedings of the National Academy of Sciences of the United States of America*, 102(22):7794–9. doi: 10.1073/pnas.0407994102.

KEY: Guimera2005

ANNOTATION: In this first analysis of the worldwide airport network, it is found that its degree distribution has a truncated power-law decaying tail, and that it has the small-world property. The existence of nodes with small degree and high betweenness is a specific property of this network. These anomalies exist because they act as hubs between their communities and the rest of the network. Authors identify the communities with a simulated annealing algorithm, and define the role of each node using two parameters: within-module degree and participation coefficient. Based on these values, they identify up to seven universal roles, that account for the multi-community structure of the network.

- [HARA13] HOSSAIN, M.; ALAM, S.; REES, T. AND ABBASS, H., 2013. Australian Airport Network Robustness Analysis : A Complex Network Approach. In *Australasian Transport Research Forum 2013 Proceedings*, October, pp. 1–21.

KEY: Hossain2013

ANNOTATION: This paper uses the Australian Airport Network (AAN) as a case study to measure the performance and to estimate the resilience of an airport network. In the literature review section, authors make a classification of short-time outages and long-time outages in airports. The AAN is modelled as a weighted network, with number of flights as weights. They perform a quite complete robustness analysis, with giant component and efficiency as performance indicators, and an analysis of node importance deleting one node and defining a rerouting algorithm.

- [HHL⁺17] HONG, C.; HE, N.; LORDAN, O.; LIANG, B.-Y. AND YIN, N.-Y., 2017. Efficient calculation of the robustness measure R for complex networks. *Physica A: Statistical Mechanics and its Applications*, 478:63–68. doi: 10.1016/j.physa.2017.02.054.

KEY: Hong2017

ANNOTATION: The calculation of the Schneider's unique robustness measure R can be very costly, as the size of the largest connected component has to be assessed N times. In this article an approximation of R is suggested consisting in stopping the calculation once the largest connected component is below a given value.

- [HK02a] HOLME, P. AND KIM, B. J., 2002. Growing scale-free networks with tunable clustering. *Physical Review E*, 65(2):026107. doi:10.1103/PhysRevE.65.026107.

KEY: Holme2002d

ANNOTATION: This work proposes a network model which has both the perfect power-law degree distribution and the high clustering. Clustering coefficient is tunable by adjusting a parameter in the model. Clustering is added via a triad formation (TF) mechanism, which can be triggered after a preferential attachment (PA) with a probability P_t : If an edge between v and w was added in the previous PA step, then add one more edge from v to a randomly chosen neighbor of w . If there remains no pair to connect, i.e., if all neighbors of w were already connected to v , do a PA step instead. The clustering is tuned by fixing the parameter P_t .

- [HK02b] HOLME, P. AND KIM, B. J., 2002. Vertex overload breakdown in evolving networks. *Physical Review E*, 65(6):066109. doi:10.1103/PhysRevE.65.066109.

KEY: Holme2002b

ANNOTATION: This paper analyzes the possibility of breakdown of an evolving network by overload of nodes. Load is equal to node betweenness computed for a number of paths proportional to $(N - 1)(N - 2)$ for the extrinsic communication activity (ECA) case, and to $(N - 1)$ for the intrinsic communication activity (ICA) case. Capacity is equal for all nodes. For the ICA case, is constant and for ICA grows linearly with N . As the network grows, the load of nodes may increase beyond capacity, triggering a cascading failure process. Two evolving networks are examined: the original BA model with preferential attachment, and a variant of the BA with random attachment. Interestingly, preferential attachment increases the probability of a giant component to form compared to random connection. In Ref. [Hol02] can be found a similar study with edge overload.

- [HKYH02] HOLME, P.; KIM, B. J.; YOON, C. N. AND HAN, S. K., 2002. Attack vulnerability of complex networks. *IEEE Transactions on Circuits and Systems II: Express Briefs*, 55(1):65–69. doi:10.1103/PhysRevE.65.056109.

KEY: Holme2002a

ANNOTATION: This study measures attack vulnerability of various complex network models and real world networks. The attack strategies considered are removal of vertices and edges by initial degree (ID), initial betweenness (IB), recalculated degree (RD) and recalculated betweenness (RB). The measure of edge degree considered is the product of the degree of vertices connected by the edge. As network performance measures, authors consider the size of giant component and the average inverse geodesic length (labeled as network efficiency in [LM01]). The real world networks considered are the scientific collaboration network and a computer network for Internet traffic. The theoretical models considered are ER, WS, BA and a clustered scale-free network model (CSF). Results shows that none of the network models shows a behaviour very similar to real world networks, suggesting that there

are other structures contributing to network behaviour. The ER model, which lacks structural bias, is the most robust of the tested networks.

- [Hol02] HOLME, P., 2002. Edge overload breakdown in evolving networks. *Physical Review E*, 66(3):036119. doi:10.1103/PhysRevE.66.036119.

KEY: Holme2002c

ANNOTATION: This paper analyzes the possibility of breakdown of an evolving network by overload of edges. Load is equal to edge betweenness computed for a number of paths proportional to $N(N - 1)$. Capacity is constant and equal for all edges. As the network grows, the load of edges may increase beyond capacity, triggering a cascading failure process. Two evolving networks are examined: the original BA model with preferential attachment, and a variant of the BA with random attachment. The effects of edge overload have a lesser impact than node overload, studied in [HK02b].

- [HYY06] HUANG, L.; YANG, L. AND YANG, K., 2006. Geographical effects on cascading breakdowns of scale-free networks. *Physical Review E*, 73(3):036102. doi:10.1103/PhysRevE.73.036102.

KEY: Huang2006

ANNOTATION: To be reviewed later

- [JC13] JAHANPOUR, E. AND CHEN, X., 2013. Analysis of complex network performance and heuristic node removal strategies. *Communications in Nonlinear Science and Numerical Simulation*, 18(12):3458–3468. doi:10.1016/j.cnsns.2013.04.030.

KEY: Jahanpour2013

ANNOTATION: The paper analyzes the performance of node removal strategies on the Krebs network of relationships between hijackers that participated on the September 11, 2001 attacks. The strategies are one-time (non-adaptive) and multiple-time (adaptive) based on degree, betweenness, reciprocal closeness, complement-derived closeness and eigenvector, and additionally random removal of nodes. Network performance measures are focused on diffusion speed measures (network reciprocal distance and average node coverage), diffusion scale (largest coverage probability and expected scale) and structural properties (shortest distance homogeneity and network diameter). This work neglects most of previous developments (e.g., network reciprocal distance is quite similar to network efficiency, and impact of network topology on robustness is not discussed), and the analysis is carried out in a single, small network.

- [KE02] KLEMM, K. AND EGUÍLUZ, V. M., 2002. Growing scale-free networks with small-world behavior. *Physical Review E*, 65(5):057102. doi:10.1103/PhysRevE.65.057102.

KEY: Klemm2002

ANNOTATION: This is an attempt to explain the dynamic behaviour of complex networks by a model of network self-organization that creates networks with a degree distribution with a power law decay and the small world property. This model adds a node in each iteration with the following rules. The graph start with a complete graph of m active nodes, and in each iteration a new node is included following three steps. 1) the new node has m links. Each link is attaching the new node to an active node with probability $1 - \mu$ or to any node according with linear preferential attachment with probability μ . 2) The new node becomes active, 3) One of the active nodes is deactivated with a probability proportional to the reciprocal of the degree. With $\mu = 0$ we obtain the BA model, and with $\mu \gg 1$ a scale-free graph with the small-world property.

- [KW06] KOSSINETS, G. AND WATTS, D. J., 2006. Empirical analysis of an evolving social network. *Science*, 311(5757):88–90. doi:10.1126/science.1116869.

KEY: Kossinets2006

ANNOTATION: Authors analyze a social network of e-mail interactions in a population of 43,553 members of a university, retaining 14,584,423 messages exchanged during 355 days of observation. They approximate instantaneous strength of a relationship by the geometric rate of bilateral email exchange within a window of 60 days. The instantaneous network at any point of time includes all pairs of individuals that sent one or more messages in each direction in the last 60 days. Using the later representation, they calculate the shortest path length and the number of shared affiliations for all members during 210 days. Appearance of new ties is assessed with two measures. Cyclic closure bias is the empirical probability that two individuals initiate a new tie as a function of shortest path length. Focal closure bias is the probability that two individuals who share an interaction focus share a new tie. For this network, average network properties appear to approach an equilibrium state, while individual properties are unstable.

- [KWKB13] KOÇ, Y.; WARNIER, M.; KOOLIJ, R. E. AND BRAZIER, F. M., 2013. An entropy-based metric to quantify the robustness of power grids against cascading failures. *Safety Science*, 59:126–134. doi:10.1016/j.ssci.2013.05.006.

KEY: Koc2013

ANNOTATION: This paper proposes a metric that quantifies robustness of a power transmission grid with respect to cascading failures by targeted attacks. The measure is defined specifically for power grids, and takes into account network structure and the operative state of the network. The metric is the product of electrical nodal robustness and electrical node significance. Electrical nodal robustness is based on entropy, to take into account load heterogeneity and out-degree of each node. Electrical node significance is the power distributed by each node, normalized by the

sum of values for each node. This measure captures the robustness of power grids to targeted attacks of edges, measured empirically by demand, link and capacity survivability.

- [LC04] LI, W. AND CAI, X., 2004. Statistical analysis of airport network of China. *Physical Review E*, 69(4):046106. doi:10.1103/PhysRevE.69.046106.

KEY: Li2004b

ANNOTATION: This is an analysis of the airport network of China (ANC), considered as a weighted, undirected graph, and obtaining a sample of the network for each weekday. In- and out-degree and degree follow a truncated power law distribution, called double Pareto law. Edge weight is found to be proportional to the square root of degree of origin and destination nodes. ANC has the small world property (small L and high C). Degree-degree correlation is negative, so the ANC is dissortative. Authors also assess efficiency with a parameter similar to the local efficiency defined in [LM01].

- [LDHT13] LOUZADA, V. H. P.; DAOLIO, F.; HERRMANN, H. J. AND TOMASSINI, M., 2013. Smart rewiring for network robustness. *Journal of Complex Networks*, 1(2):150–159. doi:10.1093/comnet/cnt010.

KEY: Louzada2013

ANNOTATION: This article proposes an improvement of the mitigation method of [SMA⁺11] for increasing network robustness. In this method, five nodes previously connected are transformed into a triangle and a pair of nodes. This method increases robustness by adding links between nodes of average degree. They also define a onionlikeness parameter to evaluate the degree to which a network has a onion structure, associated with high values of robustness. They find that after the smart rewiring process, network modularity and assortativity increases, so the resulting network has a *modular onion* structure.

- [Lin12] LIN, J., 2012. Network analysis of China’s aviation system, statistical and spatial structure. *Journal of Transport Geography*, 22:109–117. doi:10.1016/j.jtrangeo.2011.12.002.

KEY: Lin2012a

ANNOTATION: This paper reports the analysis of the Chinese air transportation network. The study includes analysis of small-world and scale-free properties, distribution of node degree and strength (with edge weights equal to number of flights), correlational analysis (the network has dissortative mixing) and hierarchical structure. Hierarchical structure is measured through correlation of degree and strength with clustering coefficient. Contrary to theoretical expectations for distance-driven networks, the analyzed aviation network presents hierarchical structure. Finally, authors conduct a spatial analysis studying frequency of distances and flows versus distances, and use gravitational models to analyze distance decay in terms of weight, population and GDP. Results show that

traffic between cities is proportional to product of centrality and inversely proportional to distance.

- [LM01] LATORA, V. AND MARCHIORI, M., 2001. Efficient Behavior of Small-World Networks. *Physical Review Letters*, 87(19):198701. doi:10.1103/PhysRevLett.87.198701.

KEY: Latora2001

ANNOTATION: The small world property and complex networks can be expressed in terms of global and local efficiency, two measures of how efficiently information is exchanged over the network. As communication between nodes will take place along the shortest paths connecting them, efficiency of communication is defined as inversely proportional to shortest distance $\epsilon_{ij} = 1/d_{ij}$. Global efficiency E_{glob} is equal to the average value of ϵ_{ij} , and local efficiency E_{loc} to the average value of the efficiency of the local subgraphs of each node. Both measures are normalized, taking values between zero and one. As $1/L$ and C are first approximations of E_{glob} and E_{loc} , small-world graphs have high values of E_{glob} and E_{loc} , and therefore are efficient in transporting information globally and locally. Global and local efficiency are defined for weighted and/or unconnected graphs.

- [LMG15] LEE, K. M.; MIN, B. AND GOH, K. I., 2015. Towards real-world complexity: an introduction to multiplex networks. *European Physical Journal B*, 88(2):48. doi:10.1140/epjb/e2015-50742-1.

KEY: Lee2015

ANNOTATION: This is an organic review of statistical physics of multiplex networks. Multiplex networks is a type of network where the same set of nodes can be connected via than one more type of link. Each type of link is a network layer. The paper reports modelling of multiplex structure and multiplex network models. It includes also a review of problems of mutual percolation, robustness against attacks and complex contagion for multiplex networks with cooperative (interdependent) layer coupling and complementary layer coupling. The bibliography section contains up to 175 references, updated at 2015.

- [MBK11] MISHKOVSKI, I.; BIEY, M. AND KOCAREV, L., 2011. Vulnerability of complex networks. *Communications in Nonlinear Science and Numerical Simulation*, 16(1):341–349. doi:10.1016/j.cnsns.2010.03.018.

KEY: Mishkovski2011a

ANNOTATION: Drawing on previous research by [BBC⁺07] the value of average edge betweenness is considered as a measure of vulnerability: the lower the average edge betweenness, the less vulnerable the network is. To this value, authors add two more values: the change of average edge betweenness when some important nodes or edges have been removed, respectively, to create a vulnerability index. It is unclear (or undefined) the number of

nodes or edges to be removed, and how vulnerability indices can be compared.

- [MCW18] MADUAKO, I.; CAVALHERI, E. AND WACHOWICZ, M., 2018. Exploring the use of time-varying graphs for modelling transit networks. *arXiv Physics and Society*. doi:arXiv:1803.07610v1.

KEY: Maduako2018

ANNOTATION: The aim of this paper is to propose a time-varying graph (TVG) model for modelling and analyzing the dynamic relationship between topological structures and mobility patterns in a transit network. TVGs are presented as dynamic representations, in opposition to static graphs. There are two major approaches to TVGs: sequence of snapshots method and aggregated graph method. This paper uses the later method, defining spatial, temporal and spatio-temporal nodes and edges. They define network metrics based on these representation, and implement them in the Neo4j database for a transit network, and implement it to the transit feeds generated by the bus transit network of Moncton (New Brunswick, Canada).

- [MGP02] MORENO, Y.; GÓMEZ, J. B. AND PACHECO, A. F., 2002. Instability of scale-free networks under node-breaking avalanches. *Europhysics Letters*, 58(4):630–636. doi:10.1209/epl/i2002-00442-2.

KEY: Moreno2002

ANNOTATION: This article defines a fiber bundle model for cascading failures in complex networks. Each node has a security threshold, usually following a Weibull distribution. In the starting point, the networks is exposed to a external force F , so each node bears a load of $\sigma = F/N$. All nodes with a load higher than their threshold are disconnected, and then the load of the disconnected nodes is equally transferred to the non-failed nodes directly linked to it, which in turn may lead to these nodes to collapse. The process ends where there are no new collapsed nodes. This process is tested in a BA network. The cascading process has a critical point. This critical point is larger, and more abrupt, for more homogeneous Weibull distributions, and smaller for uniform distributions.

- [ML02] MOTTER, A. E. AND LAI, Y.-C., 2002. Cascade-based attacks on complex networks. *Physical Review E*, 66(6):065102. doi:10.1103/PhysRevE.66.065102.

KEY: Motter2002

ANNOTATION: Authors introduce a model for cascading failures in complex networks, suitable for networks that vehiculate flows of information, energy of physical quantities. In these networks, the load of a node is equal to the total number of shortest paths passing through it (sometimes approximated by node betweenness). The capacity of a node is proportional to its initial load. The failure of a node can lead to a redistribution of loads, that can conversely

lead to the failure of nodes in which capacity is exceeded. Authors find that cascading failures occur in networks with a highly heterogeneous distribution of loads (e.g., scale-free networks), when the removed nodes are among those of higher load.

- [MPR08] MALIGHETTI, P.; PALEARI, S. AND REDONDI, R., 2008. Connectivity of the European airport network: “Self-help hubbing” and business implications. *Journal of Air Transport Management*, 14(2):53–65. doi:10.1016/j.jairtraman.2007.10.003.

KEY: Malighetti2008

ANNOTATION: Most of the potential of indirect connectivity of air transport networks is exploited by alliance systems, but there may be also potential for additional connectivity from “self-hubbing” connections established by users of low-cost and conventional airlines. This paper explores these possibilities of connection finding the paths of minimum travel time for a time window, or for a specific time of a time window. Based on these shortest paths, they can compute the betweenness and essential betweenness of each airport, which is a metric of indirect connectivity, and study in detail airport connectivity. Authors analyze the European air transport network for a time window of 24 hours.

- [MPSVV03] MORENO, Y.; PASTOR-SATORRAS, R.; VÁZQUEZ, A. AND VESPIGNANI, A., 2003. Critical load and congestion instabilities in scale-free networks. *Europhysics Letters (EPL)*, 62(2):292–298. doi:10.1209/epl/i2003-00140-7.

KEY: Moreno2003

ANNOTATION: The appearance of cascading failures in communication networks is analyzed here with a threshold model, where each link has a load coming from a random distribution with mean equal to average load $\langle \uparrow \rangle$. Capacity of all links is set equal to one. Load of congested nodes is redistributed following two alternative rules: equally among neighbour nodes or randomly. If a link is congested and has no neighbours, the load can be assigned equally to other links (non-dissipative model) or considered lost (dissipative model). When this model is applied to scale-free networks, there is a range of values of $\langle \uparrow \rangle$ where there is a small but relevant probability that the system collapses. This can explain why communication networks like the Internet can suffer cascading failures as load increases.

- [New03] NEWMAN, M. E. J., 2003. Mixing patterns in networks. *Physical Review E*, 67(2):026126. doi:10.1103/PhysRevE.67.026126.

KEY: Newman2003

ANNOTATION: Assortative mixing is a property initially defined for social networks. A social network is said to be assortative or have an assortative mixing if nodes tend to be connected to similar nodes, and disassortative when nodes tend to be connected to different nodes. Assortative mixing can be defined for discrete qualities

(gender, race) or scalar properties such as age. A particularly important scalar property is node degree. Regarding node degree, social networks tend to be assortative, while technological tend to be disassortative. The paper includes the definition of an assortativity coefficient measure, and models that allow the generation of networks with diverse values of grades of disassortativity.

- [PTHS05] PAUL, G.; TANIZAWA, T.; HAVLIN, S. AND STANLEY, H. E., 2005. Optimization of robustness of complex networks. *The European Physical Journal B*, 48(1):149–149. doi:10.1140/epjb/e2005-00385-x.

KEY: Paul2005

ANNOTATION: The goal of this research is to maximize the robustness of a network of N nodes to random failures and targeted attacks with the constraint that the cost remains constant. Cost is supposed proportional to the number of edges. Robustness is measured as the sum of thresholds for random and targeted removal of nodes. The resulting network has a degree distribution with only two values, obtained connecting $k_2 \sim AN^{2/3}$ nodes to a single node. The rest of nodes are of degree k_1 .

- [RB03] RAVASZ, E. AND BARABÁSI, A.-L., 2003. Hierarchical organization in complex networks. *Physical Review E*, 67(2):026112. doi:10.1103/PhysRevE.67.026112.

KEY: Ravasz2003

ANNOTATION: The scale-free topology and the high average clustering present in many real-world networks can be modelled through a hierarchical network. In this network, degree distribution follows a power law with exponent γ , and clustering coefficient is related with node degree with a scaling law of exponent β . These networks are modular, in the sense that they have many small, densely interconnected clusters, that combine recursively forming larger, but less cohesive groups. The hubs, nodes with high degree and low clustering coefficient, bridge the many small communities into a single, integrated network. The examination of real-world networks shows evidence of hierarchical organization in many real-world networks (the actor and language networks), but not in networks with a geographic organization (the Internet at the autonomous system level or the power grid). The clustering coefficient of the later is independent of node degree.

- [Roc09] DA ROCHA, L. E. C., 2009. Structural evolution of the Brazilian airport network. *Journal of Statistical Mechanics: Theory and Experiment*, 2009(04):P04020. doi:10.1088/1742-5468/2009/04/P04020.

KEY: DaRocha2009

ANNOTATION: Authors investigate the structure and evolution of the Brazilian Airport Network (BAN) for several quantities: routes, connections, passengers and cargo. The analysis of the evolution of the BAN in the period 1995-2006 suggests that despite of

small fluctuations in some structural properties, the network has undergone a strong rewiring dynamics in the considered period. What in principle might appear as a slowdown of the aviation sector, in fact is a reorganization of the structure according to changing demand. Along the years, the BAN presents the small-world property, and an exponential degree distribution. Network shrinks in nodes and number of connections although passengers and cargo traffic has raised.

- [SMA⁺11] SCHNEIDER, C. M.; MOREIRA, A. A.; ANDRADE, J. S.; HAVLIN, S. AND HERRMANN, H. J., 2011. Mitigation of malicious attacks on networks. *Proceedings of the National Academy of Sciences*, 108(10):3838–3841. doi:10.1073/pnas.1009440108.

KEY: Schneider2011

ANNOTATION: Authors describe a mitigation method to increase network robustness that keeps invariant the total number of links and the degree of each node. They also define a unique robustness measure R that assesses the evolution of the size of the largest connected cluster as a function of the fraction of removed nodes. The method consists in selecting two edges at random e_{ij} and e_{kl} , and replace them by e_{ik} and e_{jl} if this change increases R . Depending on the type of network, additional constraints can be added. A small fraction of edge changes increases robustness significantly. The resulting networks have a onion-like structure, consisting of a core of highly connected nodes hierarchically surrounded by rings of nodes of decreasing degree.

- [Str01] STROGATZ, S. H., 2001. Exploring complex networks. *Nature*, 410(6825):268–276. doi:10.1038/35065725.

KEY: Strogatz2001

ANNOTATION: A review of the state of the art of complex networks around 2001. First, he explores dynamic processes in simple network architectures (e.g., synchronization and Kuramoto models) and then more complex architectures. Beyond the usual discussion of ER, BA and WS models, they introduce generalized random models, and analysis of bipartite graphs. The later can be of interest for interlocking directorates.

- [SW14] SUN, X. AND WANDEL, S., 2014. Network similarity analysis of air navigation route systems. *Transportation Research Part E: Logistics and Transportation Review*, 70:416–434. doi:10.1016/j.tre.2014.08.005.

KEY: Sun2014

ANNOTATION: The paper reports a structural similarity analysis of the air route networks of the 58 countries with largest air route networks. In air navigation route networks, nodes are air navigation points and links are route segments connecting air navigation points. Data is obtained from the European Aeronautical Information Service Database, EAD) provided by Eurocontrol. Contains a

useful review on air route networks analysis and network comparison. The methodology used to compare air route networks needs to be refined. For instance, authors first discard Pearson correlation coefficients because variables are not normally distributed. Then, use R^2 of pairs of regression analysis as a measure of association. Other techniques used are clustering analysis and principal component analysis.

- [SWL15] SUN, X.; WANDEL, S. AND LINKE, F., 2015. Temporal evolution analysis of the European air transportation system: air navigation route network and airport network. *Transportmetrica B: Transport Dynamics*, 3(2):153–168. doi:10.1080/21680566.2014.960504.

KEY: Sun2015

ANNOTATION: This is a comparison of the seasonal evolution of the European airport network and air route network. To do so, data is obtained from the first week of each Aeronautical Information Regulation and Control (AIRAC) cycles from 2011 to 2013, retaining weighted and unweighted values of degree, betweenness and closeness. Airport network happens to be affected by seasonal (summer/winter) patterns and air route networks by seasonal and weekly (peak/off peak) patterns.

- [VAH15] VERMA, T.; ARAÚJO, N. A. M. AND HERRMANN, H. J., 2015. Revealing the structure of the world airline network. *Scientific Reports*, 4(1):5638. doi:10.1038/srep05638.

KEY: Verma2014

ANNOTATION: The usual approach to network robustness is examining the effect of node deletion on size of largest connected component. In this article authors examine the effect of removal of links, instead of node isolation. To assess link importance, they define two measures, one based on passenger flux and other on degree of connectivity (local clustering coefficient multiplied by number flights). Results show that the most effective strategy of edge removal is to begin with nodes of low passenger flux and low degree of connectivity. They identify a core, bridge and periphery of the network with a t-core decomposition based on number of triangles of each node. This suggests that robustness of the world airport network relies in peripheral nodes, as the simultaneous isolation of core nodes affects little size of giant component.

- [WC08] WANG, W.-X. AND CHEN, G., 2008. Universal robustness characteristic of weighted networks against cascading failure. *Physical Review E*, 77(2):026101. doi:10.1103/PhysRevE.77.026101.

KEY: Wang2008

ANNOTATION: The paper describes a local weighted flow redistribution rule (LWFRL) to model cascading failures. Each edge has a weight equal to $(k_i k_j)^\theta$, and a capacity proportional to its initial weight. Every time an edge is overloaded, its weight is redistributed among edges attached to node edges i and j . The rule

is tested in Barabási-Albert (BA) and Newman-Watts (NW) models, finding that maximum robustness is achieved for $\theta = 1$. This result is attained via computational experiments and analytic development.

- [WHO⁺13] WANG, S.; HONG, L.; OUYANG, M.; ZHANG, J. AND CHEN, X., 2013. Vulnerability analysis of interdependent infrastructure systems under edge attack strategies. *Safety Science*, 51(1):328–337. doi:10.1016/j.ssci.2012.07.003.

KEY: Wang2013

ANNOTATION: This paper analyzes the vulnerability of a two interdependent networked systems to cascading failures: a power grid and a gas network. The cascading failure model of the power grid is the defined in Wang et al. (2008), where edge load is proportional to the power of product of edge’s nodes. The model for the gas network is the generalized betweenness centrality model defined in Carvalho et al. (2009). Network interdependence is modeled through a specific interdependence function. Nodes that lead to interdependence are detected using spatial proximity criteria. Authors define three categories of network disturbance: random failures, deliberate attacks and natural disasters. Deliberate attacks are defined as suppression of edges of high load and nodes of high degree. The results of the vulnerability metrics are global vulnerability analysis and critical component analysis. Global vulnerability is measured with network efficiency and damaging rate. Critical component analysis reports the network components whose damage would lead to larger vulnerability.

- [WS98] WATTS, D. J. AND STROGATZ, S. H., 1998. Collective dynamics of ‘small-world’ networks. *Nature*, 393(6684):440–2. doi:10.1038/30918.

KEY: Watts1998a

ANNOTATION: Small-world networks can be obtain starting with a ring lattice with n nodes and k edges per node, and rewiring each edge at random with probability p . With $p = 0$ we have a regular high-clustered lattice whose characteristic path length L grows linearly with n , and with $p = 1$ a poorly-clustered random graph where L grows logarithmically with n . There is a broad range of values of p where L is similar to L_{random} and $C \gg C_{random}$, being C the average clustering coefficient. The small-world property, defined as the coexistence of a low L with a high C is present in a large number of real-world networks.

- [YLC⁺15] YANG, Y.; LI, Z.; CHEN, Y.; ZHANG, X. AND WANG, S., 2015. Improving the Robustness of Complex Networks with Preserving Community Structure. *PLOS ONE*, 10(2):e0116551. doi:10.1371/journal.pone.0116551.

KEY: Yang2015

ANNOTATION: This paper presents a method for increasing network robustness preserving the community structure. The method

has three steps: first, make each community tend to a onion-like structure; second, swap edges to make vertices with high importance (node degree) only connect with vertices of the same community; third, swap edges to increase the number of edges among communities. To design robust networks with community structure, authors suggest that each community is designed as an onion-like structure, and connect communities with edges between vertices of low degree. They also advance that structural diversity (the number of each possible 3-node and 4-node subgraphs) can play a role in network robustness, and that the best strategies to attack networks can be different for networks with strong and weak community structure.

- [ZL13] ZANIN, M. AND LILLO, F., 2013. Modelling the air transport with complex networks: A short review. *The European Physical Journal Special Topics*, 215(1):5–21. doi:10.1140/epjst/e2013-01711-9.

KEY: Zanin2013

ANNOTATION: This review covers the state of the art of analysis of air transport networks through complex network analysis in 2010. The most common representation of air transport networks is called here flight networks: nodes as airports connected with unweighted, undirected links if there is at least a direct flight between them. The review covers the following topics: network definition, topological analysis, dynamics on the air network (including indirect connectivity, air traffic jams and epidemic spreading) and resilience and vulnerability (very short, missing some contributions).

- [ZL14] ZHOU, M. AND LIU, J., 2014. A memetic algorithm for enhancing the robustness of scale-free networks against malicious attacks. *Physica A: Statistical Mechanics and its Applications*, 410:131–143. doi:10.1016/j.physa.2014.05.002.

KEY: Zhou2014

ANNOTATION: Networks with high robustness have a onion-like structure, where nodes of the same degree are connected. Here a memetic algorithm is defined to create this structure, optimizing Schneider’s unique robustness measure R . This memetic algorithm requires the definition of a crossover operator, and of a local search operator. In the later, a node swap is accepted if nodes are connected to others of similar degree. The bibliography includes other examples of metaheuristics to improve network robustness.

- [ZLC09] ZANIN, M.; LACASA, L. AND CEA, M., 2009. Dynamics in scheduled networks. *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 19(2):023111. doi:10.1063/1.3129785.

KEY: Zanin2009

ANNOTATION: To take into account the fact that air connections are planned with scheduled flights, here is presented a scheduled

network formalism. This formalism defines an adjacency matrix including a differential adjacency matrix which is constant and represents one time step, and an activation matrix holding the scheduling information. Authors deduce network properties and metrics of tolerance of errors and attacks from this formalism.