User Documentation for KINSOL v2.6.0

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Chapter 1

Introduction

KINSOL is part of a software family called SUNDIALS: SUite of Nonlinear and DIfferential/ALgebraic equation Solvers. This suite consists of CVODE, KINSOL, and IDA, and variants of these. KINSOL is a general-purpose nonlinear system solver based on Newton-Krylov solver technology.

1.1 Historical Background

The first nonlinear solver packages based on Newton-Krylov methods were written in FORTRAN. In particular, the NKSOL package, written at LLNL, was the first Newton-Krylov solver package written for solution of systems arising in the solution of partial differential equations [2]. This FORTRAN code made use of Newton's method to solve the discrete nonlinear systems and applied a preconditioned Krylov linear solver for solution of the Jacobian system at each nonlinear iteration. The key to the Newton-Krylov method was that the matrix-vector multiplies required by the Krylov method could effectively be approximated by a finite difference of the nonlinear system-defining function, avoiding a requirement for the formation of the actual Jacobian matrix. Significantly less memory was required for the solver as a result.

In the late 1990's, there was a push at LLNL to rewrite the nonlinear solver in C and port it to distributed memory parallel machines. Both Newton and Krylov methods are easily implemented in parallel, and this effort gave rise to the KINSOL package. KINSOL is similar to NKSOL in functionality, except that it provides for more options in the choice of linear system methods and tolerances, and has a more modular design to provide flexibility for future enhancements.

At present, KINSOL contains three Krylov methods: the GMRES (Generalized Minimal RESidual) [9], Bi-CGStab (Bi-Conjugate Gradient Stabilized) [10], and TFQMR (Transpose-Free Quasi-Minimal Residual) [7] linear iterative methods. As Krylov methods, these require almost no matrix storage as compared to direct methods. However, the algorithms allow for a user-supplied preconditioner matrix, and for most problems preconditioning is essential for an efficient solution. For very large nonlinear algebraic systems, the Krylov methods are preferable over direct linear solver methods, and are often the only feasible choice. Among the three Krylov methods in KINSOL, we recommend GMRES as the best overall choice. However, users are encouraged to compare all three, especially if encountering convergence failures with GMRES. Bi-CGStab and TFQMR have an advantage in storage requirements, in that the number of workspace vectors they require is fixed, while that number for GMRES depends on the desired Krylov subspace size.

For the sake of completeness in functionality, direct linear systems are now included in KINSOL. These include methods for both dense and banded linear systems, with Jacobians that are either user-supplied or generated internally by difference quotients.

In the process of translating NKSOL into C, the overall KINSOL organization has been changed considerably. One key feature of the KINSOL organization is that a separate module devoted to vector operations has been created. This module facilitated extension to multiprosessor environments with minimal impact on the rest of the solver. The new vector module design is shared across the SUNDIALS suite. This NVECTOR module is written in terms of abstract vector operations with the actual routines

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attached by a particular implementation (such as serial or parallel) of NVECTOR. This allows writing the SUNDIALS solvers in a manner independent of the actual NVECTOR implementation (which can be user-supplied), as well as allowing more than one NVECTOR module linked into an executable file.

There are several motivations for choosing the C language for KINSOL. First, a general movement away from FORTRAN and toward C in scientific computing is apparent. Second, the pointer, structure, and dynamic memory allocation features in C are extremely useful in software of this complexity, with the great variety of method options offered. Finally, we prefer C over C++ for KINSOL because of the wider availability of C compilers, the potentially greater efficiency of C, and the greater ease of interfacing the solver to applications written in FORTRAN.

1.2 Changes from previous versions

Changes in v2.6.0

This release introduces a new linear solver module, based on Blas and Lapack for both dense and banded matrices.

The user interface has been further refined. Some of the API changes involve: (a) a reorganization of all linear solver modules into two families (besides the already present family of scaled preconditioned iterative linear solvers, the direct solvers, including the new Lapack-based ones, were also organized into a *direct* family); (b) maintaining a single pointer to user data, optionally specified through a Set-type function; (c) a general streamlining of the band-block-diagonal preconditioner module distributed with the solver.

Changes in v2.5.0

The main changes in this release involve a rearrangement of the entire SUNDIALS source tree (see §3.1). At the user interface level, the main impact is in the mechanism of including SUNDIALS header files which must now include the relative path (e.g. #include <cvode/cvode.h>). Additional changes were made to the build system: all exported header files are now installed in separate subdirectories of the installation *include* directory.

The functions in the generic dense linear solver (sundials_dense and sundials_smalldense) were modified to work for rectangular $m \times n$ matrices ($m \le n$), while the factorization and solution functions were renamed to DenseGETRF/denGETRF and DenseGETRS/denGETRS, respectively. The factorization and solution functions in the generic band linear solver were renamed BandGBTRF and BandGBTRS, respectively.

Changes in v2.4.0

KINSPBCG, KINSPTFQMR, KINDENSE, and KINBAND modules have been added to interface with the Scaled Preconditioned Bi-CGStab (SPBCG), Scaled Preconditioned Transpose-Free Quasi-Minimal Residual (SPTFQMR), DENSE, and BAND linear solver modules, respectively. (For details see Chapter 4.) Corresponding additions were made to the FORTRAN interface module FKINSOL. At the same time, function type names for Scaled Preconditioned Iterative Linear Solvers were added for the user-supplied Jacobian-times-vector and preconditioner setup and solve functions.

Regarding the FORTRAN interface module FKINSOL, optional inputs are now set using FKINSETIIN (integer inputs), FKINSETRIN (real inputs), and FKINSETVIN (vector inputs). Optional outputs are still obtained from the IOUT and ROUT arrays which are owned by the user and passed as arguments to FKINMALLOC.

The KINDENSE and KINBAND linear solver modules include support for nonlinear residual monitoring which can be used to control Jacobian updating.

To reduce the possibility of conflicts, the names of all header files have been changed by adding unique prefixes (kinsol_ and sundials_). When using the default installation procedure, the header files are exported under various subdirectories of the target include directory. For more details see Appendix A.

Changes in v2.3.0

The user interface has been further refined. Several functions used for setting optional inputs were combined into a single one. Additionally, to resolve potential variable scope issues, all SUNDIALS solvers release user data right after its use. The build system has been further improved to make it more robust.

Changes in v2.2.1

The changes in this minor SUNDIALS release affect only the build system.

Changes in v2.2.0

The major changes from the previous version involve a redesign of the user interface across the entire SUNDIALS suite. We have eliminated the mechanism of providing optional inputs and extracting optional statistics from the solver through the iopt and ropt arrays. Instead, KINSOL now provides a set of routines (with prefix KINSet) to change the default values for various quantities controlling the solver and a set of extraction routines (with prefix KINGet) to extract statistics after return from the main solver routine. Similarly, each linear solver module provides its own set of Set- and Get-type routines. For more details see Chapter 4.

Additionally, the interfaces to several user-supplied routines (such as those providing Jacobian-vector products and preconditioner information) were simplified by reducing the number of arguments. The same information that was previously accessible through such arguments can now be obtained through Get-type functions.

Installation of KINSOL (and all of SUNDIALS) has been completely redesigned and is now based on configure scripts.

1.3 Reading this User Guide

This user guide is a combination of general usage instructions and specific examples. We expect that some readers will want to concentrate on the general instructions, while others will refer mostly to the examples, and the organization is intended to accommodate both styles.

There are different possible levels of usage of KINSOL. The most casual user, with a small nonlinear system, can get by with reading all of Chapter 2, then Chapter 4 through §4.5.3 only, and looking at examples in [3]. In a different direction, a more expert user with a nonlinear system may want to (a) use a package preconditioner (§4.7), (b) supply his/her own Jacobian or preconditioner routines (§4.6), (c) supply a new NVECTOR module (Chapter 6), or even (d) supply a different linear solver module (§3.2 and Chapter 7).

The structure of this document is as follows:

- In Chapter 2, we provide short descriptions of the numerical methods implemented by KINSOL for the solution of nonlinear systems.
- The following chapter describes the structure of the SUNDIALS suite of solvers (§3.1) and the software organization of the KINSOL solver (§3.2).
- Chapter 4 is the main usage document for KINSOL for C applications. It includes a complete description of the user interface for the solution of nonlinear algebraic systems.
- In Chapter 5, we describe FKINSOL, an interface module for the use of KINSOL with FORTRAN applications.
- Chapter 6 gives a brief overview of the generic NVECTOR module shared among the various components of SUNDIALS, and details on the two NVECTOR implementations provided with SUNDIALS: a serial implementation (§6.1) and a parallel implementation based on MPI (§6.2).

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• Chapter 7 describes the interfaces to the linear solver modules, so that a user can provide his/her own such module.

- Chapter 8 describes in detail the generic linear solvers shared by all SUNDIALS solvers.
- Finally, in the appendices, we provide detailed instructions for the installation of KINSOL, within the structure of SUNDIALS (Appendix A), as well as a list of all the constants used for input to and output from KINSOL functions (Appendix B).

Finally, the reader should be aware of the following notational conventions in this user guide: program listings and identifiers (such as KINInit) within textual explanations appear in typewriter type style; fields in C structures (such as *content*) appear in italics; and packages or modules are written in all capitals. Usage and installation instructions that constitute important warnings are marked with a triangular symbol in the margin.



Acknowledgments. We wish to acknowledge the contributions to previous versions of the KINSOL code and user guide by Allan G. Taylor.

Chapter 2

Mathematical Considerations

KINSOL solves nonlinear algebraic systems in real N-space,

$$F(u) = 0, \quad F: \mathbf{R}^N \to \mathbf{R}^N,$$
 (2.1)

given an initial guess u_0 .

Basic Newton iteration

Depending on the linear solver used, KINSOL can employ either an Inexact Newton method [1, 2, 4, 5, 8], or a Modified Newton method. At the highest level, KINSOL implements the following iteration scheme:

- 1. Set $u_0 = \text{an initial guess}$
- 2. For $n = 0, 1, 2, \dots$ until convergence do:
 - (a) Solve $J(u_n)\delta_n = -F(u_n)$
 - (b) Set $u_{n+1} = u_n + \lambda \delta_n$, $0 < \lambda \le 1$
 - (c) Test for convergence

Here, u_n is the *n*th iterate to u, and J(u) = F'(u) is the system Jacobian. At each stage in the iteration process, a scalar multiple of the step δ_n , is added to u_n to produce a new iterate, u_{n+1} . A test for convergence is made before the iteration continues.

Newton method variants

For solving the linear system given in step 2(a), KINSOL provides several choices, including the option of a user-supplied linear solver module. The linear solver modules distributed with SUNDIALS are organized in two families, a *direct* family comprising direct linear solvers for dense or banded matrices and a *spils* family comprising scaled preconditioned iterative (Krylov) linear solvers. The methods offered through these modules are as follows:

- dense direct solvers, using either an internal implementation or a Blas/Lapack implementation (serial version only),
- band direct solvers, using either an internal implementation or a Blas/Lapack implementation (serial version only),
- SPGMR, a scaled preconditioned GMRES (Generalized Minimal Residual method) solver without restarts,
- SPBCG, a scaled preconditioned Bi-CGStab (Bi-Conjugate Gradient Stable method) solver, or

• SPTFQMR, a scaled preconditioned TFQMR (Transpose-Free Quasi-Minimal Residual method) solver.

When using one of the direct linear solvers, the linear system in 2(a) is solved exactly, thus resulting in a Modified Newton method (the Jacobian matrix is normally out of date; see below¹). Note that the direct linear solvers (dense and band) can only be used with serial vector representations.

On the other hand, when using any of the iterative linear solvers (GMRES, Bi-CGStab, or TFQMR), the linear system in 2(a) is solved only approximately, thus resulting in an Inexact Newton method. Here right preconditioning is available by way of the preconditioning setup and solve routines supplied by the user, in which case the iterative method is applied to the linear systems $(JP^{-1})(P\delta) = -F$, where P denotes the right preconditioning matrix.

Jacobian information update strategy

In general, unless specified otherwise by the user, KINSOL strives to update Jacobian information (the actual system Jacobian J in the case of direct linear solvers, or the preconditioner matrix P in the case of iterative linear solvers) as infrequently as possible to balance the high costs of matrix operations against other costs. Specifically, these updates occur when:

- the problem is initialized,
- $\|\lambda \delta_{n-1}\|_{D_u,\infty} > 1.5$ (Inexact Newton only),
- mbset= 10 nonlinear iterations have passed since the last update,
- the linear solver failed recoverably with outdated Jacobian information,
- the global strategy failed with outdated Jacobian information, or
- $\|\lambda \delta_n\|_{D_{n,\infty}} < \text{STEPTOL}$ with outdated Jacobian information.

KINSOL allows, through optional solver inputs, changes to the above strategy. Indeed, the user can disable the initial Jacobian information evaluation or change the default value of mbset, the number of nonlinear iterations after which a Jacobian information update is enforced.

Scaling

To address the case of ill-conditioned nonlinear systems, KINSOL allows prescribing scaling factors both for the solution vector and for the residual vector. For scaling to be used, the user should supply values D_u , which are diagonal elements of the scaling matrix such that $D_u u_n$ has all components roughly the same magnitude when u_n is close to a solution, and D_F , which are diagonal scaling matrix elements such that $D_F F$ has all components roughly the same magnitude when u_n is not too close to a solution. In the text below, we use the following scaled norms:

$$||z||_{D_u} = ||D_u z||_2, \quad ||z||_{D_F} = ||D_F z||_2, \quad ||z||_{D_u,\infty} = ||D_u z||_\infty, \quad \text{and} \quad ||z||_{D_F,\infty} = ||D_F z||_\infty$$
 (2.2)

where $\|\cdot\|_{\infty}$ is the max norm. When scaling values are provided for the solution vector, these values are automatically incorporated into the calculation of the perturbations used for the default difference quotient approximations for Jacobian information; see (2.6) and (2.8) below.

Globalization strategy

Two methods of applying a computed step δ_n to the previously computed solution vector are implemented. The first and simplest is the standard Newton strategy which applies step 2(b) as above with λ always set to 1. The other method is a global strategy, which attempts to use the direction implied by δ_n in the most efficient way for furthering convergence of the nonlinear problem. This technique is implemented in the second strategy, called Linesearch. This option employs both the

 $^{^{1}}$ KINSOL allows the user to enforce a Jacobian evaluation at each iteration thus allowing for an Exact Newton iteration.

 α and β conditions of the Goldstein-Armijo linesearch given in [5] for step 2(b), where λ is chosen to guarantee a sufficient decrease in F relative to the step length as well as a minimum step length relative to the initial rate of decrease of F. One property of the algorithm is that the full Newton step tends to be taken close to the solution.

KINSOL implements a backtracking algorithm to first find the value λ such that $u_n + \lambda \delta_n$ satisfies the sufficient decrease condition (or α -condition)

$$F(u_n + \lambda \delta_n) \leq F(u_n) + \alpha \nabla F(u_n) \lambda \delta_n$$

where $\alpha = 10^{-4}$. Although backtracking in itself guarantees that the step is not too small, KINSOL secondly relaxes λ to satisfy the so-called β -condition (equivalent to Wolfe's curvature condition):

$$F(u_n + \lambda \delta_n) \ge F(u_n) + \beta \nabla F(u_n) \lambda \delta_n$$

where $\beta = 0.9$. During this second phase, λ is allowed to vary in the interval $[\lambda_{min}, \lambda_{max}]$ where

$$\lambda_{min} = \frac{\text{STEPTOL}}{\|\bar{\delta}_n\|_{\infty}}, \quad \bar{\delta}_n^j = \frac{\delta_n^j}{1/D_n^j + |u^j|},$$

and λ_{max} corresponds to the maximum feasible step size at the current iteration (typically $\lambda_{max} = \text{STEPMAX}/\|\delta_n\|_{D_u}$). In the above expressions, v^j denotes the jth component of a vector v.

For more details, the reader is referred to [5].

Nonlinear iteration stopping criteria

Stopping criteria for the Newton method are applied to both of the nonlinear residual and the step length. For the former, the Newton iteration must pass a stopping test

$$||F(u_n)||_{D_{F,\infty}} < \text{FTOL}$$
,

where FTOL is an input scalar tolerance with a default value of $U^{1/3}$. Here U is the machine unit roundoff. For the latter, the Newton method will terminate when the maximum scaled step is below a given tolerance

$$\|\lambda \delta_n\|_{D_n,\infty} < \text{STEPTOL},$$

where STEPTOL is an input scalar tolerance with a default value of $U^{2/3}$. Only the first condition (small residual) is considered a successful completion of KINSOL. The second condition (small step) may indicate that the iteration is stalled near a point for which the residual is still unacceptable.

Additional constraints

As a user option, KINSOL permits the application of inequality constraints, $u^i > 0$ and $u^i < 0$, as well as $u^i \geq 0$ and $u^i \leq 0$, where u^i is the *i*th component of u. Any such constraint, or no constraint, may be imposed on each component. KINSOL will reduce step lengths in order to ensure that no constraint is violated. Specifically, if a new Newton iterate will violate a constraint, the maximum step length along the Newton direction that will satisfy all constraints is found, and δ_n in Step 2(b) is scaled to take a step of that length.

Residual monitoring for Modified Newton method

When using a Modified Newton method (i.e. when a direct linear solver is used), in addition to the strategy described above for the update of the Jacobian matrix, KINSOL also provides an optional nonlinear residual monitoring scheme to control when the system Jacobian is updated. Specifically, a Jacobian update will also occur when mbsetsub= 5 nonlinear iterations have passed since the last update and

$$||F(u_n)||_{D_F} > \omega ||F(u_m)||_{D_F}$$
,

where u_n is the current iterate and u_m is the iterate at the last Jacobian update. The scalar ω is given by

$$\omega = \min \left(\omega_{min} \, e^{\max(0, \rho - 1)}, \omega_{max} \right) \,, \tag{2.3}$$

with ρ defined as

$$\rho = \frac{\|F(u_n)\|_{D_F}}{\text{FTOL}},\tag{2.4}$$

where FTOL is the input scalar tolerance discussed before. Optionally, a constant value ω_{const} can be used for the parameter ω .

The constants controlling the nonlinear residual monitoring algorithm can be changed from their default values through optional inputs to KINSOL. These include the parameters ω_{min} and ω_{max} , the constant value ω_{const} , and the threshold mbsetsub.

Stopping criteria for iterative linear solvers

When using an Inexact Newton method (i.e. when an iterative linear solver is used), the convergence of the overall nonlinear solver is intimately coupled with the accuracy with which the linear solver in 2(a) above is solved. KINSOL provides three options for stopping criteria for the linear system solver, including the two algorithms of Eisenstat and Walker [6]. More precisely, the Krylov iteration must pass a stopping test

$$||J\delta_n + F||_{D_F} < (\eta_n + U)||F||_{D_F}$$

where η_n is one of:

Eisenstat and Walker Choice 1

$$\eta_n = \frac{| \|F(u_n)\|_{D_F} - \|F(u_{n-1}) + J(u_{n-1})\delta_n\|_{D_F} |}{\|F(u_{n-1})\|_{D_F}},$$

Eisenstat and Walker Choice 2

$$\eta_n = \gamma \left(\frac{\|F(u_n)\|_{D_F}}{\|F(u_{n-1})\|_{D_F}} \right)^{\alpha},$$

where default values of γ and α are 0.9 and 2, respectively.

Constant η

$$\eta_n = constant,$$

with 0.1 as the default.

The default strategy is "Eisenstat and Walker Choice 1". For both options 1 and 2, appropriate safeguards are incorporated to ensure that η does not decrease too quickly [6].

Difference quotient Jacobian approximations

With the direct dense and band methods, the Jacobian may be supplied by a user routine, or approximated by difference quotients, at the user's option. In the latter case, we use the usual approximation

$$J^{ij} = [F^{i}(u + \sigma_{j}e^{j}) - F^{i}(u)]/\sigma_{j}.$$
(2.5)

The increments σ_j are given by

$$\sigma_j = \sqrt{U} \max\left\{|u^j|, 1/D_u^j\right\}. \tag{2.6}$$

In the dense case, this scheme requires N evaluations of F, one for each column of J. In the band case, the columns of J are computed in groups, by the Curtis-Powell-Reid algorithm, with the number of F evaluations equal to the bandwidth.

In the case of a Krylov method, Jacobian information is needed only as matrix-vector products Jv. If a routine for Jv is not supplied, these products are approximated by directional difference quotients as

$$J(u)v \approx [F(u+\sigma v) - F(u)]/\sigma, \qquad (2.7)$$

where u is the current approximation to a root of (2.1), and σ is a scalar. The choice of σ is taken from [2] and is given by

$$\sigma = \frac{\max\{|u^T v|, u_{typ}^T | v|\}}{\|v\|_2} \operatorname{sign}(u^T v) \sqrt{U}, \qquad (2.8)$$

where u_{typ} is a vector of typical values for the absolute values of the solution (and can be taken to be inverses of the scale factors given for u as described below). Convergence of the Newton method is maintained as long as the value of σ remains appropriately small, as shown in [1].

Chapter 3

Code Organization

3.1 SUNDIALS organization

The family of solvers referred to as SUNDIALS consists of the solvers CVODE (for ODE systems), KINSOL (for nonlinear algebraic systems), and IDA (for differential-algebraic systems). In addition, SUNDIALS also includes variants of CVODE and IDA with sensitivity analysis capabilities (using either forward or adjoint methods): CVODES and IDAS, respectively.

The various solvers of this family share many subordinate modules. For this reason, it is organized as a family, with a directory structure that exploits that sharing (see Fig. 3.1). The following is a list of the solver packages presently available:

- CVODE, a solver for stiff and nonstiff ODEs dy/dt = f(t, y);
- CVODES, a solver for stiff and nonstiff ODEs with sensitivity analysis capabilities;
- IDA, a solver for differential-algebraic systems $F(t, y, \dot{y}) = 0$;
- IDAS, a solver for differential-algebraic systems with sensitivity analysis capabilities;
- KINSOL, a solver for nonlinear algebraic systems F(u) = 0.

3.2 KINSOL organization

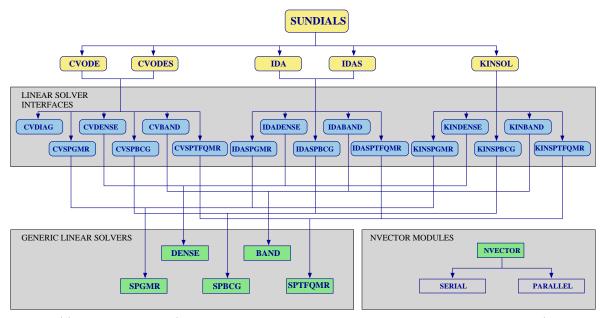
The KINSOL package is written in the ANSI C language. This section summarizes the basic structure of the package, although knowledge of this structure is not necessary for its use.

The overall organization of the KINSOL package is shown in Figure 3.2. The central solver module, implemented in the files kinsol.h, kinsol_impl.h and kinsol.c, deals with the solution of a nonlinear algebraic system using either an Inexact Newton method or a line search method for the global strategy. Although this module contains logic for the Newton iteration, it has no knowledge of the method used to solve the linear systems that arise. For any given user problem, one of the linear system modules is specified, and is then invoked as needed.

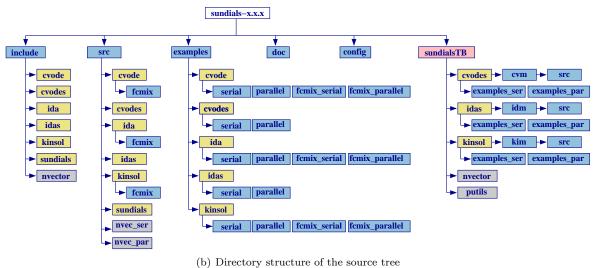
At present, the package includes the following seven KINSOL linear algebra modules, organized into two families. The *direct* families of linear solvers provides solvers for the direct solution of linear systems with dense or banded matrices and includes:

- KINDENSE: LU factorization and backsolving with dense matrices (using either an internal implementation or Blas/Lapack);
- KINBAND: LU factorization and backsolving with banded matrices (using either an internal implementation or Blas/Lapack);

The spils family of linear solvers providess scaled preconditioned iterative linear solvers and includes:



 $\hbox{(a) High-level diagram (note that none of the Lapack-based linear solver modules are represented.)}\\$



(s) Bricerelly structure of the source tree

Figure 3.1: Organization of the SUNDIALS suite

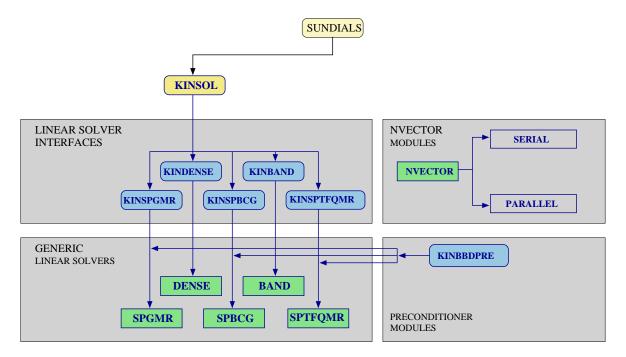


Figure 3.2: Overall structure diagram of the KINSOL package. Modules specific to KINSOL are distinguished by rounded boxes, while generic solver and auxiliary modules are in rectangular boxes. Grayed boxes refer to the encompassing SUNDIALS structure. Note that the direct linear solvers using Lapack implementations are not explicitly represented.

- KINSPGMR: scaled preconditioned GMRES method;
- KINSPBCG: scaled preconditioned Bi-CGStab method;
- KINSPTFQMR: scaled preconditioned TFQMR method.

The set of linear solver modules distributed with KINSOL is intended to be expanded in the future as new algorithms are developed.

In the case of the direct methods KINDENSE and KINBAND the package includes an algorithm for the approximation of the Jacobian by difference quotients, but the user also has the option of supplying the Jacobian (or an approximation to it) directly. In the case of the Krylov methods KINSPGMR, KINSPBCG and KINSPTFQMR, the package includes an algorithm for the approximation by difference quotients of the product between the Jacobian matrix and a vector of appropriate length. Again, the user has the option of providing a routine for this operation. For the Krylov methods, the preconditioning must be supplied by the user, in two phases: setup (preprocessing of Jacobian data) and solve.

Each KINSOL linear solver module consists of four routines, devoted to (1) memory allocation and initialization, (2) setup of the matrix data involved, (3) solution of the system, and (4) freeing of memory. The setup and solution phases are separate because the evaluation of Jacobians and preconditioners is done only periodically during the integration, as required to achieve convergence. The call list within the central KINSOL module to each of the associated functions is fixed, thus allowing the central module to be completely independent of the linear system method.

These modules are also decomposed in another way. With the exception of the modules interfacing to Lapack linear solvers, each of the modules KINDENSE, KINBAND, KINSPGMR, KINSPBCG, and KINSPTFQMR is a set of interface routines built on top of a generic solver module, name DENSE, BAND, SPGMR, SPBCG, and SPTFQMR, respectively. The interface deals with the use of these methods in the KINSOL context, whereas the generic solver is independent of the context. While the generic solvers here were generated with SUNDIALS in mind, our intention is that they be usable in other applications

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as general-purpose solvers. This separation also allows for any generic solver to be replaced by an improved version, with no necessity to revise the KINSOL package elsewhere.

KINSOL also provides a preconditioner module called KINBBDPRE for use with any of the Krylov iterative liear solvers. It works in conjunction with NVECTOR_PARALLEL and generates a preconditioner that is a block-diagonal matrix with each block being a band matrix, as further described in §4.7.

All state information used by KINSOL to solve a given problem is saved in a structure, and a pointer to that structure is returned to the user. There is no global data in the KINSOL package, and so in this respect it is reentrant. State information specific to the linear solver is saved in a separate structure, a pointer to which resides in the KINSOL memory structure. The reentrancy of KINSOL was motivated by the anticipated multi-computer extension.

Chapter 4

Using KINSOL for C Applications

This chapter is concerned with the use of KINSOL for the solution of nonlinear systems. The following subsections treat the header files, the layout of the user's main program, description of the KINSOL user-callable routines, and user-supplied functions. The listings of the sample programs in the companion document [3] may also be helpful. Those codes may be used as templates (with the removal of some lines involved in testing), and are included in the KINSOL package.

Users with applications written in FORTRAN77 should see Chapter 5, which describes the FORTRAN/C interface module.

The user should be aware that not all linear solver modules are compatible with all NVECTOR implementations. For example, NVECTOR_PARALLEL is not compatible with the direct dense or direct band linear solvers since these linear solver modules need to form the complete system Jacobian. The following KINSOL modules can only be used with NVECTOR_SERIAL: KINDENSE and KINBAND. The preconditioner module KINBBDPRE can only be used with NVECTOR_PARALLEL.

KINSOL uses various constants for both input and output. These are defined as needed in this chapter, but for convenience are also listed separately in Appendix B.

4.1 Access to library and header files

At this point, it is assumed that the installation of KINSOL, following the procedure described in Appendix A, has been completed successfully.

Regardless of where the user's application program resides, its associated compilation and load commands must make reference to the appropriate locations for the library and header files required by KINSOL. The relevant library files are

- *libdir*/libsundials_kinsol. *lib*,
- libdir/libsundials_nvec*.lib (one or two files),

where the file extension .lib is typically .so for shared libraries and .a for static libraries. The relevant header files are located in the subdirectories

- incdir/include
- incdir/include/kinsol
- incdir/include/sundials

The directories *libdir* and *incdir* are the install library and include directories, respectively. For a default installation, these are *builddir*/lib and *builddir*/include, respectively, where *builddir* was defined in Appendix A.

4.2 Data types

The sundials_types.h file contains the definition of the type realtype, which is used by the SUNDIALS solvers for all floating-point data. The type realtype can be float, double, or long double, with the default being double. The user can change the precision of the SUNDIALS solvers arithmetic at the configuration stage (see $\S A.1.1$).

Additionally, based on the current precision, sundials_types.h defines BIG_REAL to be the largest value representable as a realtype, SMALL_REAL to be the smallest value representable as a realtype, and UNIT_ROUNDOFF to be the difference between 1.0 and the minimum realtype greater than 1.0.

Within SUNDIALS, real constants are set by way of a macro called RCONST. It is this macro that needs the ability to branch on the definition realtype. In ANSI C, a floating-point constant with no suffix is stored as a double. Placing the suffix "F" at the end of a floating point constant makes it a float, whereas using the suffix "L" makes it a long double. For example,

```
#define A 1.0
#define B 1.0F
#define C 1.0L
```

defines A to be a double constant equal to 1.0, B to be a float constant equal to 1.0, and C to be a long double constant equal to 1.0. The macro call RCONST(1.0) automatically expands to 1.0 if realtype is double, to 1.0F if realtype is float, or to 1.0L if realtype is long double. SUNDIALS uses the RCONST macro internally to declare all of its floating-point constants.

A user program which uses the type realtype and the RCONST macro to handle floating-point constants is precision-independent except for any calls to precision-specific standard math library functions. (Our example programs use both realtype and RCONST.) Users can, however, use the type double, float, or long double in their code (assuming that this usage is consistent with the typedef for realtype). Thus, a previously existing piece of ANSI C code can use SUNDIALS without modifying the code to use realtype, so long as the SUNDIALS libraries use the correct precision (for details see $\S A.1.1$).

4.3 Header files

The calling program must include several header files so that various macros and data types can be used. The header file that is always required is:

• kinsol.h, the header file for KINSOL, which defines several types and various constants, and includes function prototypes.

kinsol.h also includes sundials_types.h, which defines the types realtype and booleantype and constants FALSE and TRUE.

The calling program must also include an NVECTOR implementation header file (see Chapter 6 for details). For the two NVECTOR implementations that are included in the KINSOL package, the corresponding header files are:

- nvector_serial.h, which defines the serial implementation, NVECTOR_SERIAL;
- nvector_parallel.h, which defines the parallel MPI implementation, NVECTOR_PARALLEL.

Note that both of these files include in turn the header file sundials_nvector.h, which defines the abstract N_Vector type.

Finally, a linear solver module header file is required. The header files corresponding to the various linear solver options in KINSOL are:

- kinsol_dense.h, which is used with the dense direct linear solver;
- kinsol_band.h, which is used with the band direct linear solver;

- kinsol_lapack.h, which is used with Lapack implementations of dense or band direct linear solvers;
- kinsol_spgmr.h, which is used with the Krylov solver SPGMR;
- kinsol_spbcgs.h, which is used with the Krylov solver SPBCG;
- kinsol_sptfqmr.h, which is used with the Krylov solver SPTFQMR;

The header files for the dense and banded linear solvers (both internal and Lapack) include the file kinsol_direct.h which defines common functions. This in turn includes a file (sundials_direct.h) which defines the matrix type for these direct linear solvers (DlsMat), as well as various functions and macros acting on such matrices.

The header files for the Krylov iterative solvers include kinsol_spils.h which defined common functions and which in turn includes a header file (sundials_iterative.h) which enumerates the kind of preconditioning and for the choices for the Gram-Schmidt process for SPGMR.

Other headers may be needed, according to the choice of preconditioner, etc. For example, in the kinFoodWeb_kry_p example (see [3]), preconditioning is done with a block-diagonal matrix. For this, even though the KINSPGMR linear solver is used, the header sundials_dense.h is included for access to the underlying generic dense linear solver.

4.4 A skeleton of the user's main program

The following is a skeleton of the user's main program (or calling program) for the solution of a nonlinear problem. Some steps are independent of the NVECTOR implementation used; where this is not the case, usage specifications are given for the two implementations provided with KINSOL: Steps marked [P] correspond to NVECTOR_PARALLEL, while steps marked [S] correspond to NVECTOR_SERIAL.

1. [P] Initialize MPI

Call MPI_Init(&argc, &argv) to initialize MPI if used by the user's program, aside from the internal use in NVECTOR_PARALLEL. Here argc and argv are the command line argument counter and array received by main.

2. Set problem dimensions

- [S] Set N, the problem size N.
- [P] Set Nlocal, the local vector length (the sub-vector length for this process); N, the global vector length (the problem size N, and the sum of all the values of Nlocal); and the active set of processes.

3. Set vector with initial guess

To set the vector \mathbf{u} of initial values, use functions defined by a particular NVECTOR implementation. If a realtype array udata already exists, containing the initial guess of u_0 , make the call:

```
[S] u = N_VMake_Serial(N, udata);
[P] u = N_VMake_Parallel(comm, Nlocal, N, udata);
Otherwise, make the call:
[S] u = N_VNew_Serial(N);
[P] u = N_VNew_Parallel(comm, Nlocal, N);
and load initial values into the structure defined by:
[S] NV_DATA_S(u)
[P] NV_DATA_P(u)
```

Here comm is the MPI communicator, set in one of two ways: If a proper subset of active processes is to be used, comm must be set by suitable MPI calls. Otherwise, to specify that all processes are to be used, comm must be MPI_COMM_WORLD.

4. Create KINSOL object

Call kin_mem = KINCreate() to create the KINSOL memory block. KINCreate returns a pointer to the KINSOL memory structure. See §4.5.1 for details.

5. Set optional inputs

Call KINSet* routines to change from their default values any optional inputs that control the behavior of KINSOL. See §4.5.4 for details.

6. Allocate internal memory

Call KINInit(...) to specify the problem defining function F, allocate internal memory for KINSOL, and initialize KINSOL. KINInit returns a flag to indicate success or an illegal argument value. See §4.5.1 for details.

7. Attach linear solver module

Initialize the linear solver module with one of the following calls (for details see §4.5.2).

```
[S] ier = KINDense(...);
[S] ier = KINBand(...);
[S] flag = KINLapackDense(...);
[S] flag = KINLapackBand(...);
ier = KINSpgmr(...);
ier = KINSptcg(...);
ier = KINSptfqmr(...);
```

8. Set linear solver optional inputs

Call KIN*Set* functions from the selected linear solver module to change optional inputs specific to that linear solver. See §4.5.4 for details.

9. Solve problem

Call ier = KINSol(...) to solve the nonlinear problem for a given initial guess. See §4.5.3 for details.

10. Get optional outputs

Call KINGet* and KIN*Get* functions to obtain optional output. See §4.5.5 for details.

11. Deallocate memory for solution vector

Upon completion of the solution, deallocate memory for the vector **u** by calling the destructor function defined by the NVECTOR implementation:

```
[S] N_VDestroy_Serial(u);
[P] N_VDestroy_Parallel(u);
```

12. Free solver memory

Call KINFree (&kin_mem) to free the memory allocated for KINSOL.

13. [P] Finalize MPI

Call MPI_Finalize() to terminate MPI.

4.5 User-callable functions

This section describes the KINSOL functions that are called by the user to set up and solve a nonlinear problem. Some of these are required. However, starting with §4.5.4, the functions listed involve optional inputs/outputs or restarting, and those paragraphs can be skipped for a casual use of KINSOL. In any case, refer to §4.4 for the correct order of these calls.

The return flag (when present) for each of these routines is a negative integer if an error occurred, and non-negative otherwise.

4.5.1 KINSOL initialization and deallocation functions

The following three functions must be called in the order listed. The last one is to be called only after the problem solution is complete, as it frees the KINSOL memory block created and allocated by the first two calls.

KINCreate

Call kin_mem = KINCreate();

Description The function KINCreate instantiates a KINSOL solver object.

Arguments This function has no arguments.

Return value If successful, KINCreate returns a pointer to the newly created KINSOL memory block

(of type void *). If an error occurred, KINCreate prints an error message to stderr

and returns NULL.

KINInit

Call flag = KINInit(kin_mem, func, tmpl);

Description The function KINInit specifies the problem-defining function, allocates internal mem-

ory, and initializes KINSOL.

Arguments kin_mem (void *) pointer to the KINSOL memory block returned by KINCreate.

func (KINSysFn) is the C function which computes the system function F in the nonlinear problem. This function has the form func(u, fval, user_data).

(For full details see $\S4.6.1$.)

tmpl (N_Vector) is any N_Vector (e.g. the initial guess vector u) which is used as a

template to create (by cloning) necessary vectors in kin_mem.

Return value The return value flag (of type int) will be one of the following:

KIN_SUCCESS The call to KINInit was successful.

KIN_MEM_NULL The KINSOL memory block was not initialized through a previous call

 $to \ {\tt KINCreate}.$

KIN_MEM_FAIL A memory allocation request has failed.

KIN_ILL_INPUT An input argument to KINInit has an illegal value.

Notes If an error occurred, KINInit sends an error message to the error handler function.

KINFree

Call KINFree(&kin_mem);

Description The function KINFree frees the memory allocated by a previous call to KINCreate.

Arguments The argument is the address of the pointer to the KINSOL memory block returned by

KINCreate (of type void *).

Return value The function KINFree has no return value.

4.5.2Linear solver specification functions

As previously explained, Newton iteration requires the solution of linear systems of the form $J\delta = -F$. There are five KINSOL linear solvers currently available for this task: KINDENSE, KINBAND, KINSPGMR, KINSPBCG, and KINSPTFQMR.

The first two linear solvers are direct and derive their names from the type of approximation used for the Jacobian $J = \partial F/\partial u$; KINDENSE and KINBAND work with dense and banded approximations to J, respectively. The SUNDIALS suite includes both internal implementations of these two linear solvers and interfaces to Lapack implementations. Together, these linear solvers are referred to as KINDLS (from Direct Linear Solvers).

The remaining three KINSOL linear solvers — KINSPGMR, KINSPBCG, and KINSPTFQMR — are Krylov iterative solvers, which use scaled preconditioned GMRES, scaled preconditioned Bi-CGStab, and scaled preconditioned TFQMR, respectively. Together, they are referred to as KINSPILS (from Scaled Preconditioned Iterative Linear Solvers).

With any of the Krylov solvers, only right preconditioning is available. For specification of the preconditioner, see the Krylov solver sections within §4.5.4 and §4.6. If preconditioning is done, usersupplied functions define the right preconditioner matrix P, which should approximate the system Jacobian matrix J.

To specify a KINSOL linear solver, after the call to KINCreate but before any calls to KINSOL, the user's program must call one of the functions KINDense/KINLapackDense, KINBand/KINLapackBand, KINSpgmr, KINSpbcg, or KINSptfqmr, as documented below. The first argument passed to these functions is the KINSOL memory pointer returned by KINCreate. A call to one of these functions links the main KINSOL nonlinear solver to a linear solver and allows the user to specify parameters which are specific to a particular solver, such as the half-bandwidths in the KINBAND case. The use of each of the linear solvers involves certain constants and possibly some macros, that are likely to be needed in the user code. These are available in the corresponding header file associated with the linear solver, as specified below.

In each case, with the exception of the Lapack-based direct solvers, the linear solver module used by KINSOL is actually built on top of a generic linear system solver, which may be of interest in itself. These generic solvers, denoted DENSE, BAND, SPGMR, SPBCG, and SPTFQMR, are described separately in Chapter 8.

KINDense

Call flag = KINDense(kin_mem, N);

The function KINDense selects the KINDENSE linear solver and indicates the use of the Description internal direct dense linear algebra functions.

The user's main function must include the kinsol_dense.h header file.

kin_mem (void *) pointer to the KINSOL memory block. Arguments

(int) problem dimension.

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The KINDENSE initialization was successful.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_ILL_INPUT The KINDENSE solver is not compatible with the current NVECTOR module.

KINDLS_MEM_FAIL A memory allocation request failed.

Notes

The KINDENSE linear solver may not be compatible with a particular implementation of the NVECTOR module. Of the two NVECTOR modules provided by SUNDIALS, only NVECTOR_SERIAL is compatible, while NVECTOR_PARALLEL is not.

KINLapackDense

Call flag = KINLapackDense(kin_mem, N);

Description The function KINLapackDense selects the KINDENSE linear solver and indicates the use

of Lapack functions.

The user's main function must include the kinsol_lapack.h header file.

Arguments The input arguments are identical to those of KINDense.

Return value The values of the returned flag (of type int) are identical to those of KINDense.

KINBand

Call flag = KINBand(kin_mem, N, mupper, mlower);

Description The function KINBand selects the KINBAND linear solver and indicates the use of the

internal direct band linear algebra functions.

The user's main function must include the kinsol_band.h header file.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

N (int) problem dimension.

mupper (int) upper half-bandwidth of the problem Jacobian (or of the approximation

of it)

mlower (int) lower half-bandwidth of the problem Jacobian (or of the approximation

of it).

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The KINBAND initialization was successful.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_ILL_INPUT The KINBAND solver is not compatible with the current NVECTOR

module, or one of the Jacobian half-bandwidths is outside its valid

range $(0 \dots N-1)$.

KINDLS_MEM_FAIL A memory allocation request failed.

Notes The KINBAND linear solver may not be compatible with a particular implementation of the NVECTOR module. Of the two NVECTOR modules provided by SUNDIALS, only NVECTOR_SERIAL is compatible, while NVECTOR_PARALLEL is not. The half-bandwidths

NVECTOR_SERIAL is compatible, while NVECTOR_PARALLEL is not. The half-bandwidths are to be set so that the nonzero locations (i, j) in the banded (approximate) Jacobian

satisfy $-mlower \le j - i \le mupper$.

KINLapackBand

Call flag = KINLapackBand(kin_mem, N, mupper, mlower);

Description The function KINLapackBand selects the KINBAND linear solver and indicates the use of

Lapack functions.

The user's main function must include the kinsol_lapack.h header file.

Arguments The input arguments are identical to those of KINBand.

Return value The values of the returned flag (of type int) are identical to those of KINBand.

KINSpgmr

Call flag = KINSpgmr(kin_mem, maxl);

Description The function KINSpgmr selects the KINSPGMR linear solver.

The user's main function must include the kinsol_spgmr.h header file.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use the default value KINSPILS_MAXL= 5.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The KINSPGMR initialization was successful.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_ILL_INPUT The NVECTOR module used does not implement a required operation.

KINSPILS_MEM_FAIL A memory allocation request failed.

KINSpbcg

Call flag = KINSpbcg(kin_mem, maxl);

Description The function KINSpbcg selects the KINSPBCG linear solver.

The user's main function must include the kinsol_spbcgs.h header file.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use the default value KINSPILS_MAXL= 5.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The KINSPBCG initialization was successful.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_ILL_INPUT The NVECTOR module used does not implement a required operation

KINSPILS_MEM_FAIL A memory allocation request failed.

KINSptfqmr

Call flag = KINSptfqmr(kin_mem, maxl);

Description The function KINSptfqmr selects the KINSPTFQMR linear solver.

The user's main function must include the kinsol_sptfqmr.h header file.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

maxl (int) maximum dimension of the Krylov subspace to be used. Pass 0 to use the default value KINSPILS_MAXL= 5.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The KINSPTFQMR initialization was successful.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_ILL_INPUT The NVECTOR module used does not implement a required oper-

ation.

KINSPILS_MEM_FAIL A memory allocation request failed.

4.5.3 KINSOL solver function

This is the central step in the solution process, the call to solve the nonlinear algebraic system.

KINSol

Call flag = KINSol(kin_mem, u, strategy, u_scale, f_scale);

Description The function KINSol computes an approximate solution to the nonlinear system.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

u (N_Vector) vector set to initial guess by user before calling KINSol, but which upon return contains an approximate solution of the nonlinear system F(u) = 0.

strategy (int) globalization strategy applied to the Newton method. It must be one of KIN_NONE or KIN_LINESEARCH.

u_scale (N_Vector) vector containing diagonal elements of scaling matrix D_u for vector u chosen so that the components of D_u ·u (as a matrix multiplication) all have roughly the same magnitude when u is close to a root of F(u).

f_scale (N_Vector) vector containing diagonal elements of scaling matrix D_F for F(u) chosen so that the components of $D_F \cdot F(u)$ (as a matrix multiplication) all have roughly the same magnitude when u is not too near a root of F(u).

Return value On return, KINSol returns the approximate solution in the vector u if successful. The return value flag (of type int) will be one of the following:

KIN_SUCCESS

KINSol succeeded; the scaled norm of F(u) is less than fnormtol.

KIN_INITIAL_GUESS_OK

The guess $\mathbf{u} = u_0$ satisfied the system F(u) = 0 within the tolerances specified.

KIN_STEP_LT_STPTOL

KINSOL stopped based on scaled step length. This means that the current iterate may be an approximate solution of the given nonlinear system, but it is also quite possible that the algorithm is "stalled" (making insufficient progress) near an invalid solution, or that the scalar scsteptol is too large (see KINSetScaledStepTol in §4.5.4 to change scsteptol from its default value).

KIN_MEM_NULL

The KINSOL memory block pointer was NULL.

KIN_ILL_INPUT

An input parameter was invalid.

KIN_NO_MALLOC

The KINSOL memory was not allocated by a call to KINCreate.

KIN_LINESEARCH_NONCONV

The line search algorithm was unable to find an iterate sufficiently distinct from the current iterate, or could not find an iterate satisfying the sufficient decrease condition.

Failure to satisfy the sufficient decrease condition could mean the current iterate is "close" to an approximate solution of the given nonlinear system, the difference approximation of the matrix-vector product J(u)v is inaccurate, or the real scalar scsteptol is too large.

KIN_MAXITER_REACHED

The maximum number of nonlinear iterations has been reached.

KIN MXNEWT 5X EXCEEDED

Five consecutive steps have been taken that satisfy the inequality $||D_u p||_{L^2} > 0.99$ mxnewtstep, where p denotes the current step and mxnewtstep is a scalar upper bound on the scaled step length. Such a failure may mean that $||D_F F(u)||_{L^2}$ asymptotes from above to a positive value, or the real scalar mxnewtstep is too small.

KIN_LINESEARCH_BCFAIL

The line search algorithm was unable to satisfy the "beta-condition" for MXNBCF + 1 nonlinear iterations (not necessarily consecutive), which may indicate the algorithm is making poor progress.

KIN_LINSOLV_NO_RECOVERY

The user-supplied routine psolve encountered a recoverable error, but the preconditioner is already current.

KIN_LINIT_FAIL

The linear solver initialization routine (linit) encountered an error.

KIN LSETUP FAIL

The user-supplied routine pset (used to set up the preconditioner data) encountered an unrecoverable error.

KIN_LSOLVE_FAIL

Either the user-supplied routine psolve (used to to solve the preconditioned linear system) encountered an unrecoverable error, or the linear solver routine (lsolve) encountered an error condition.

KIN_SYSFUNC_FAIL

The system function failed in an unrecoverable manner.

KIN FIRST SYSFUNC ERR

The system function failed recoverably at the first call.

KIN_REPTD_SYSFUNC_ERR

The system function had repeated recoverable errors. No recovery is possible.

Notes

The components of vectors u_scale and f_scale should be strictly positive.

KIN_SUCCESS = 0, KIN_INITIAL_GUESS_OK = 1, and KIN_STEP_LT_STPTOL = 2. All remaining return values are negative and therefore a test flag < 0 will trap all KINSol failures.

4.5.4 Optional input functions

There are numerous optional input parameters that control the behavior of the KINSOL solver. KINSOL provides functions that can be used to change these from their default values. Table 4.1 lists all optional input functions in KINSOL which are then described in detail in the remainder of this section, beginning with those for the main KINSOL solver and continuing with those for the linear solver modules. For the most casual use of KINSOL, the reader can skip to §4.6.

We note that, on error return, all of these functions also send an error message to the error handler function. We also note that all error return values are negative, so a test flag < 0 will catch any error.

4.5.4.1 Main solver optional input functions

The calls listed here can be executed in any order. However, if either of the functions KINSetErrFile or KINSetErrHandlerFn is to be called, that call should be first, in order to take effect for any later error message.

KINSetErrFile

Call flag = KINSetErrFile(kin_mem, errfp);

Description The function KINSetErrFile specifies the pointer to the file where all KINSOL messages should be directed when the default KINSOL error handler function is used.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

errfp (FILE *) pointer to output file.

Table 4.1: Optional inputs for ${\tt KINSOL},$ ${\tt KINDENSE},$ and ${\tt KINSPILS}$

Optional input	Function name	Default		
KINSOL main solver				
Error handler function	KINSetErrHandlerFn	internal fn.		
Pointer to an error file	KINSetErrFile	stderr		
Info handler function	KINSetInfoHandlerFn	internal fn.		
Pointer to an info file	KINSetInfoFile	stdout		
Data for problem-defining function	KINSetUserData	NULL		
Verbosity level of output	KINSetPrintLevel	0		
Max. number of nonlinear iterations	KINSetNumMaxIters	200		
No initial preconditioner setup	KINSetNoInitSetup	FALSE		
No residual monitoring*	KINSetNoResMon	FALSE		
Max. iterations without prec. setup	KINSetMaxSetupCalls	10		
Max. iterations without residual check*	KINSetMaxSubSetupCalls	5		
Form of η coefficient	KINSetEtaForm	KIN_ETACHOICE1		
Constant value of η	KINSetEtaConstValue	0.1		
Values of γ and α	KINSetEtaParams	0.9 and 2.0		
Values of ω_{min} and ω_{max}^*	KINSetResMonParams	0.00001 and 0.9		
Constant value of ω^*	KINSetResMonConstValue	0.9		
Lower bound on ϵ	KINSetNoMinEps	FALSE		
Max. scaled length of Newton step	KINSetMaxNewtonStep	$ 1000 D_uu_0 _2$		
Max. number of β -condition failures	KINSetMaxBetaFails	10		
Rel. error for D.Q. Jv	KINSetRelErrFunc	$\sqrt{\text{uround}}$		
Function-norm stopping tolerance	KINSetFuncNormTol	$uround^{1/3}$		
Scaled-step stopping tolerance	KINSetScaledSteptol	$uround^{2/3}$		
Inequality constraints on solution	KINSetConstraints	NULL		
Nonlinear system function	KINSetSysFunc	none		
KINDI	S linear solvers	I		
Dense Jacobian function	KINDlsSetDenseJacFn	DQ		
Band Jacobian function	KINDlsSetBandJacFn	$\mid \mathrm{DQ} \mid$		
KINSPILS linear solvers				
Max. number of restarts**	KINSpilsSetMaxRestarts	0		
Preconditioner functions and data	KINSpilsSetPreconditioner	NULL, NULL, NULL		
Jacobian-times-vector function and data	KINSpilsSetJacTimesVecFn	internal DQ,		
		NULL		

^{*} Only for the KINDLS linear solvers ** Only for KINSPGMR

Return value The return value flag (of type int) is one of

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default value for errfp is stderr.

Passing a value of NULL disables all future error message output (except for the case in which the KINSOL memory pointer is NULL). This use of KINSetErrFile is strongly

discouraged.

If KINSetErrFile is to be called, it should be called before any other optional input functions, in order to take effect for any later error message.

KINSetErrHandlerFn

Call flag = KINSetErrHandlerFn(kin_mem, ehfun, eh_data);

Description The function KINSetErrHandlerFn specifies the optional user-defined function to be

used in handling error messages.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

ehfun (KINErrHandlerFn) is the user's C error handler function (see $\S4.6.2$).

eh_data (void *) pointer to user data passed to ehfun every time it is called.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The function ehfun and data pointer eh_data have been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default internal error handler function directs error messages to the file specified

by the file pointer errfp (see KINSetErrFile above).

Error messages indicating that the KINSOL solver memory is NULL will always be directed

to stderr.

KINSetInfoFile

Call flag = KINSetInfoFile(kin_mem, infofp);

Description The function KINSetInfoFile specifies the pointer to the file where all informative

(non-error) messages should be directed.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

infofp (FILE *) pointer to output file.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default value for infofp is stdout.

KINSetInfoHandlerFn

Call flag = KINSetInfoHandlerFn(kin_mem, ihfun, ih_data);

Description The function KINSetInfoHandlerFn specifies the optional user-defined function to be

used in handling informative (non-error) messages.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

ihfun (KINInfoHandlerFn) is the user's C information handler function (see §4.6.3).

ih_data (void *) pointer to user data passed to ihfun every time it is called.

Return value The return value flag (of type int) is one of:



KIN_SUCCESS The function infun and data pointer ih_data have been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default internal information handler function directs informative (non-error) messages to the file specified by the file pointer infofp (see KINSetInfoFile above).

KINSetPrintLevel

Call flag = KINSetPrintLevel(kin_mem, printfl);

Description The function KINSetPrintLevel specifies the level of verbosity of the output.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

printfl (int) flag indicating the level of verbosity. Must be one of:

0 no information displayed.

- 1 for each nonlinear iteration display the following information: the scaled Euclidean ℓ_2 norm of the system function evaluated at the current iterate, the scaled norm of the Newton step (only if using KIN_NONE), and the number of function evaluations performed so far.
- $2\,$ display level 1 output and the following values for each iteration:

 $||F(u)||_{D_F}$ (only for KIN_NONE).

 $||F(u)||_{D_F,\infty}$ (for KIN_NONE and KIN_LINESEARCH).

3 display level 2 output plus additional values used by the global strategy (only if using KIN_LINESEARCH), and statistical information for the linear solver.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The argument printfl had an illegal value.

Notes The default value for printfl is 0.

KINSetUserData

Call flag = KINSetUserData(kin_mem, user_data);

Description The function KINSetUserData specifies the pointer to user-defined memory that is to

be passed to all user-supplied functions.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

user_data (void *) pointer to the user-defined memory.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default value for user_data is NULL.

KINSetNumMaxIters

Call flag = KINSetNumMaxIters(kin_mem, mxiter);

Description The function KINSetNumMaxIters specifies the maximum number of nonlinear iterations

allowed.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

mxiter (long int) maximum number of nonlinear iterations.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The maximum number of iterations was non-positive.

Notes The default value for mxiter is MXITER_DEFAULT = 200.

KINSetNoInitSetup

Call flag = KINSetNoInitSetup(kin_mem, noInitSetup);

Description The function KINSetNoInitSetup specifies whether an initial call to the preconditioner

setup function should be made or not.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

noInitSetup (booleantype) flag controlling whether an initial call to the precondi-

tioner setup function is made (pass FALSE) or not made (pass TRUE).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default value for noInitSetup is FALSE, meaning that an initial call to the precon-

ditioner setup function will be made.

A call to this function is useful when solving a sequence of problems, in which the final preconditioner value from problem is to be used initially for the next problem.

KINSetNoResMon

Call flag = KINSetNoResMon(kin_mem, noNNIResMon);

Description The function KINSetNoResMon specifies whether or not the nonlinear residual monitoring

scheme is used to control Jacobian updating

Arguments kin_mem (void *) pointer to the KINSOL memory block.

noNNIResMon (booleantype) flag controlling whether residual monitoring is used (pass

FALSE) or not used (pass TRUE).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes When using a direct solver, the default value for nonniresmon is FALSE, meaning that

the nonlinear residual will be monitored.

Residual monitoring is only available for use with the direct linear solver modules (mean-

ing KINDENSE and KINBAND).

KINSetMaxSetupCalls

Call flag = KINSetMaxSetupCalls(kin_mem, msbset);

Description The function KINSetMaxSetupCalls specifies the maximum number of nonlinear itera-

tions that can be performed between calls to the preconditioner setup function.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

msbset (long int) maximum number of nonlinear iterations without a call to the

preconditioner setup function. Pass 0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.



KIN_ILL_INPUT The argument msbset was negative.

Notes The default value for msbset is MSBSET_DEFAULT = 10.

KINSetMaxSubSetupCalls

Call flag = KINSetMaxSubSetupCalls(kin_mem, msbsetsub);

Description The function KINSetMaxSubSetupCalls specifies the maximum number of nonlinear

iterations between checks by the residual monitoring algorithm.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

msbsetsub (long int) maximum number of nonlinear iterations without checking the nonlinear residual. Pass 0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The argument msbsetsub was negative.

Notes The default value for msbsetsub is MSBSET_SUB_DEFAULT = 5.

Residual monitoring is only available for use with the direct linear solver modules (meaning KINDENSE and KINBAND).

!

KINSetEtaForm

Call flag = KINSetEtaForm(kin_mem, etachoice);

Description The function KINSetEtaForm specifies the method for computing the value of the η coefficient used in the calculation of the linear solver convergence tolerance.

coefficient used in the calculation of the linear solver convergence

Arguments kin_mem (void *) pointer to the KINSOL memory block.

etachoice (int) flag indicating the method for computing η . The value must be one of KIN_ETACHOICE1, KIN_ETACHOICE2, or KIN_ETACONSTANT (see Chapter 2

for details).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The argument etachoice had an illegal value.

Notes The default value for etachoice is KIN_ETACHOICE1.

KINSetEtaConstValue

Call flag = KINSetEtaConstValue(kin_mem, eta);

Description The function KINSetEtaConstValue specifies the constant value for η in the case

etachoice = KIN_ETACONSTANT.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

eta (realtype) constant value for η . Pass 0.0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The argument eta had an illegal value

Notes The default value for eta is 0.1. The legal values are $0.0 < \text{eta} \le 1.0$.

KINSetEtaParams

Call flag = KINSetEtaParams(kin_mem, egamma, ealpha);

Description The function KINSetEtaParams specifies the parameters γ and α in the formula for η ,

in the case etachoice = KIN_ETACHOICE2.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

egamma (realtype) value of the γ parameter. Pass 0.0 to indicate the default. ealpha (realtype) value of the α parameter. Pass 0.0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional values have been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT One of the arguments egamma or ealpha had an illegal value.

Notes The default values for egamma and ealpha are 0.9 and 2.0, respectively.

The legal values are $0.0 < \text{egamma} \le 1.0$ and $1.0 < \text{ealpha} \le 2.0$.

KINSetResMonConstValue

Call flag = KINSetResMonConstValue(kin_mem, omegaconst);

Description The function KINSetResMonConstValue specifies the constant value for ω when using

residual monitoring.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

omegaconst (realtype) constant value for ω . Passing 0.0 results in using Eqn. (2.3).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The argument omegaconst had an illegal value

Notes The default value for omegaconst is 0.9. The legal values are 0.0 < omegaconst < 1.0.

KINSetResMonParams

Call flag = KINSetResMonParams(kin_mem, omegamin, omegamax);

Description The function KINSetResMonParams specifies the parameters ω_{min} and ω_{max} in the for-

mula (2.3) for ω .

Arguments kin_mem (void *) pointer to the KINSOL memory block.

omegamin (realtype) value of the ω_{min} parameter. Pass 0.0 to indicate the default. omegamax (realtype) value of the ω_{max} parameter. Pass 0.0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional values have been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT One of the arguments omegamin or omegamax had an illegal value.

Notes The default values for omegamin and omegamax are 0.00001 and 0.9, respectively.

The legal values are 0.0 < omegamin < omegamax < 1.0.

KINSetNoMinEps

Call flag = KINSetNoMinEps(kin_mem, noMinEps);

Description The function KINSetNoMinEps specifies a flag that controls whether or not the value of

 ϵ , the scaled linear residual tolerance, is bounded from below.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

noMinEps (booleantype) flag controlling the bound on ϵ .

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

Notes The default value for noMinEps is FALSE, meaning that a positive minimum value, equal

to 0.01*fnormtol, is applied to ϵ . (See KINSetFuncNormTol below.)

KINSetMaxNewtonStep

Call flag = KINSetMaxNewtonStep(kin_mem, mxnewtstep);

Description The function KINSetMaxNewtonStep specifies the maximum allowable scaled length of

the Newton step.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

mxnewtstep (realtype) maximum scaled step length (≥ 0.0). Pass 0.0 to indicate the

default

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The input value was negative.

Notes The default value of mxnewtstep is $1000 \|u_0\|_{D_u}$, where u_0 is the initial guess.

KINSetMaxBetaFails

Call flag = KINSetMaxBetaFails(kin_mem, mxnbcf);

Description The function KINSetMaxBetaFails specifies the maximum number of β -condition fail-

ures in the linesearch algorithm.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

mxnbcf (realtype) maximum number of β -condition failures. Pass 0.0 to indicate the

default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT mxnbcf was negative.

Notes The default value of mxnbcf is MXNBCF_DEFAULT = 10.

KINSetRelErrFunc

Call flag = KINSetRelErrFunc(kin_mem, relfunc);

Description The function KINSetRelErrFunc specifies the relative error in computing F(u), which

is used in the difference quotient approximation of the Jacobian-vector product.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

relfunc (realtype) relative error in F(u) (relfunc ≥ 0.0). Pass 0.0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The relative error was negative.

Notes The default value for relfunc is $\sqrt{\text{unit roundoff}}$.

KINSetFuncNormTol

Call flag = KINSetFuncNormTol(kin_mem, fnormtol);

the scaled maximum norm of the system function F(u).

Arguments kin_mem (void *) pointer to the KINSOL memory block.

fnormtol (realtype) tolerance for stopping based on scaled function norm (≥ 0.0).

Pass 0.0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

 ${\tt KIN_ILL_INPUT}$ The tolerance was negative.

Notes The default value for fnormtol is (unit roundoff) $^{1/3}$.

KINSetScaledStepTol

Call flag = KINSetScaledStepTol(kin_mem, scsteptol);

Description The function KINSetScaledStepTol specifies the scalar used as a stopping tolerance on

the minimum scaled step length.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

scsteptol (realtype) tolerance for stopping based on scaled step length (≥ 0.0). Pass

0.0 to indicate the default.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The tolerance was non-positive.

Notes The default value for scsteptol is (unit roundoff) $^{2/3}$.

KINSetConstraints

Call flag = KINSetConstraints(kin_mem, constraints);

Description The function KINSetConstraints specifies a vector that defines inequality constraints

for each component of the solution vector u.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

constraints (N_Vector) vector of constraint flags. If constraints[i] is

0.0 then no constraint is imposed on u_i .

1.0 then u_i will be constrained to be $u_i \geq 0.0$.

-1.0 then u_i will be constrained to be $u_i \leq 0.0$.

2.0 then u_i will be constrained to be $u_i > 0.0$.

-2.0 then u_i will be constrained to be $u_i < 0.0$.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

cause constraint checking to be performed.

KIN_ILL_INPUT The constraint vector contains illegal values.

Notes The presence of a non-NULL constraints vector that is not 0.0 in all components will

The function creates a private copy of the constraints vector. Consequently, the user-supplied vector can be freed after the function call, and the constraints can only be changed by calling this function.

KINSetSysFunc

Call flag = KINSetSysFunc(kin_mem, func);

Description The function KINSetSysFunc specifies the user-provided function that evaluates the

nonlinear system function F(u).

Arguments kin_mem (void *) pointer to the KINSOL memory block.

func (KINSysFn) user-supplied function that evaluates F(u).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KIN_ILL_INPUT The argument func was NULL.

Notes The nonlinear system function is initially specified through KINInit. The option of

changing the system function is provided for a user who wishes to solve several problems

of the same size but with different functions.

4.5.4.2 Direct linear solvers optional input functions

The KINDENSE solver needs a function to compute a dense approximation to the Jacobian matrix J(u). This function must be of type KINDlsDenseJacFn. The user can supply his/her own dense Jacobian function, or use the default internal difference quotient approximation that comes with the KINDENSE solver. To specify a user-supplied Jacobian function djac, KINDENSE provides the function KINDlsSetDenseJacFn. The KINDENSE solver passes the pointer user_data to the dense Jacobian function. This allows the user to create an arbitrary structure with relevant problem data and access it during the execution of the user-supplied Jacobian function, without using global data in the program. The pointer use_data may be specified through KINSetUserData.

KINDlsSetDenseJacFn

Call flag = KINDlsSetDenseJacFn(kin_mem, djac);

Description The function KINDlsSetDenseJacFn specifies the dense Jacobian approximation func-

tion to be used.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

djac (KINDlsDenseJacFn) user-defined dense Jacobian approximation function.

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The optional value has been successfully set.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_LMEM_NULL The KINDENSE linear solver has not been initialized.

Notes

By default, KINDENSE uses an internal difference quotient function. If NULL is passed to djac, this default function is used.

The function type KINDlsDenseJacFn is described in §4.6.4.

The KINDENSE solver needs a function to compute a banded approximation to the Jacobian matrix J(u). This function must be of type KINDlsBandJacFn. The user can supply his/her own banded Jacobian approximation function, or use the default internal difference quotient approximation that comes with the KINBAND solver. To specify a user-supplied Jacobian function bjac KINBAND provides the function KINDlsSetBandJacFn. The KINBAND solver passes the pointer user_data to the banded Jacobian approximation function. This allows the user to create an arbitrary structure with relevant problem data and access it during the execution of the user-supplied Jacobian function, without using global data in the program. The pointer user_data may be specified through KINSetUserData.

KINDlsSetBandJacFn

Call flag = KINDlsSetBandJacFn(kin_mem, bjac);

Description The function KINBandSetJacFn specifies the banded Jacobian approximation function

to be used.

kin_mem (void *) pointer to the KINSOL memory block. Arguments

(KINDlsBandJacFn) user-defined banded Jacobian approximation function.

Return value The return value flag (of type int) is one of

KINDLS SUCCESS The optional value has been successfully set.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_LMEM_NULL The KINBAND linear solver has not been initialized.

Notes

By default, KINBAND uses an internal difference quotient approximation. If NULL is passed to bjac, this default function is used.

The function type KINDlsBandJacFn is described in §4.6.5.

Iterative linear solvers optional input functions

If any preconditioning is to be done with one of the KINSPILS linear solvers, then the user must supply a preconditioner solve function psolve and specify its name in a call to KINSpilsSetPreconditioner.

The evaluation and preprocessing of any Jacobian-related data needed by the user's preconditioner solve function is done in the optional user-supplied function psetup. Both of these functions are fully specified in §4.6. If used, the psetup function should also be specified in the call to KINSpilsSetPreconditioner. A KINSPILS solver passes the pointer user_data received through KINSetUserData to the preconditioner psetup and psolve functions. This allows the user to create an arbitrary structure with relevant problem data and access it during the execution of the user-supplied preconditioner functions without using global data in the program.

Ther KINSPILS solvers require a function to compute an approximation to the product between the Jacobian matrix J(u) and a vector v. The user can supply his/her own Jacobian-times-vector approximation function, or use the internal difference quotient approximation that comes with the KINSPILS solvers. A user-defined Jacobian-vector function must be of type KINSpilsJacTimesVecFn and can be specified through a call to KINSpilsSetJacTimesVecFn (see §4.6.6 for specification details). A KINSPILS solver passes the pointer user_data received through KINSetUserData to the Jacobiantimes-vector function jtimes each time it is called.

KINSpilsSetPreconditioner

Call flag = KINSpilsSetPreconditioner(kin_mem, psetup, psolve);

Description The function KINSpilsSetPreconditioner specifies the preconditioner setup and solve

functions.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

 ${\tt psetup} \quad ({\tt KINSpilsPrecSetupFn}) \ user-defined \ preconditioner \ setup \ function. \ Pass \ {\tt NULL}$

if no setup operation is to be done.

psolve (KINSpilsPrecSolveFn) user-defined preconditioner solve function.

Return value The return value flag (of type int) is one of

KINSPILS_SUCCESS The optional values have been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The KINSPILS linear solver has not been initialized.

Notes The function type KINSpilsPrecSolveFn is described in §4.6.7. The function type

KINSpilsPrecSetupFn is described in $\S4.6.8$.

KINSpilsSetJacTimesVecFn

Call flag = KINSpilsSetJacTimesVecFn(kin_mem, jtimes);

Description The function KINSpilsSetJacTimesFn specifies the Jacobian-vector function to be used.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

jtimes (KINSpilsJacTimesVecFn) user-defined Jacobian-vector product function.

Return value The return value flag (of type int) is one of

KINSPILS_SUCCESS The optional value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The KINSPILS linear solver has not been initialized.

Notes By default, the KINSPILS linear solvers use an internal difference quotient function

KINSpilsDQJtimes. If NULL is passed as jtimes, this default function is used.

The function type KINSpilsJacTimesVecFn is described in §4.6.6.

KINSpilsSetMaxRestarts

Call flag = KINSpilsSetMaxRestarts(kin_mem, maxrs);

Description The function KINSpilsSetMaxRestarts specifies the maximum number of times the

iterative linear solver can be restarted.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

maxrs (int) maximum number of restarts (≥ 0).

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional value has been successfully set.

KINSPILS_ILL_INPUT The maximum number of restarts specified is negative.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver has not been initialized.

Notes The default value is 0 (meaning no restarts).

This option is available only for the KINSPGMR linear solver.

4.5.5 Optional output functions

KINSOL provides an extensive list of functions that can be used to obtain solver performance information. Table 4.2 lists all optional output functions in KINSOL, which are then described in detail in the remainder of this section, beginning with those for the main KINSOL solver and continuing with those for the linear solver modules. Where the name of an output from a linear solver module would otherwise conflict with the name of an optional output from the main solver, a suffix LS (for Linear Solver) has been added here (e.g., lenrwLS).



Optional output	Function name			
KINSOL main solver				
Size of kinsol real and integer workspaces	KINGetWorkSpace			
Number of function evaluations	KINGetNumFuncEvals			
Number of nonlinear iterations	KINGetNumNolinSolvIters			
Number of β -condition failures	KINGetNumBetaCondFails			
Number of backtrack operations	KINGetNumBacktrackOps			
Scaled norm of F	KINGetFuncNorm			
Scaled norm of the step	KINGetStepLength			
KINDLS linear s	solvers			
Size of real and integer workspaces	KINDlsGetWorkSpace			
No. of Jacobian evaluations	KINDlsGetNumJacEvals			
No. of F calls for D.Q. Jacobian evals.	KINDlsGetNumFuncEvals			
Last return from a kindle function	KINDlsGetLastFlag			
KINSPILS linear	solvers			
Size of real and integer workspaces	KINSpilsGetWorkSpace			
No. of linear iterations	KINSpilsGetNumLinIters			
No. of linear convergence failures	KINSpilsGetNumConvFails			
No. of preconditioner evaluations	KINSpilsGetNumPrecEvals			
No. of preconditioner solves	KINSpilsGetNumPrecSolves			
No. of Jacobian-vector product evaluations	KINSpilsGetNumJtimesEvals			
No. of F calls for D.Q. Jacobian-vector evals.	KINSpilsGetNumFuncEvals			
Last return from a linear solver function	KINSpilsGetLastFlag			

Table 4.2: Optional outputs from KINSOL, KINDLS, and KINSPILS

4.5.5.1 Main solver optional output functions

KINSOL provides several user-callable functions that can be used to obtain different quantities that may be of interest to the user, such as solver workspace requirements and solver performance statistics. These optional output functions are described next.

KINGetWorkSpace Call flag = KINGetWorkSpace(kin_mem, &lenrw, &leniw); Description The function KINGetWorkSpace returns the KINSOL integer and real workspace sizes. Arguments kin_mem (void *) pointer to the KINSOL memory block. (long int) the number of realtype values in the KINSOL workspace. (long int) the number of integer values in the KINSOL workspace. leniw Return value The return value flag (of type int) is one of: KIN_SUCCESS The optional output values have been successfully set. KIN_MEM_NULL The kin_mem pointer is NULL. Notes In terms of the problem size N, the actual size of the real workspace is 17+5N realtype words. The real workspace is increased by an additional N words if constraint checking is enabled (see KINSetConstraints). The actual size of the integer workspace (without distinction between int and long int) is 22 + 5N (increased by N if constraint checking is enabled).

KINGetNumFuncEvals

Call flag = KINGetNumFuncEvals(kin_mem, &nfevals);

Description The function KINGetNumFuncEvals returns the number of evaluations of the system

function.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nfevals (long int) number of calls to the user-supplied function that evaluates F(u).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional output value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KINGetNumNonlinSolvIters

Call flag = KINGetNumNonlinSolvIters(kin_mem, &nniters);

Description The function KINGetNumNonlinSolvIters returns the number of nonlinear iterations.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nniters (long int) number of nonlinear iterations.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional output value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KINGetNumBetaCondFails

Call flag = KINGetNumBetaCondFails(kin_mem, &nbcfails);

Description The function KINGetNumBetaCondFails returns the number of β -condition failures.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nbcfails (long int) number of β -condition failures.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional output value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KINGetNumBacktrackOps

Call flag = KINGetNumBacktrackOps(kin_mem, &nbacktr);

Description The function KINGetNumBacktrackOps returns the number of backtrack operations (step

length adjustments) performed by the line search algorithm.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nbacktr (long int) number of backtrack operations.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional output value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KINGetFuncNorm

Call flag = KINGetFuncNorm(kin_mem, &fnorm);

Description The function KINGetFuncNorm returns the scaled Euclidean ℓ_2 norm of the nonlinear

system function F(u) evaluated at the current iterate.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

fnorm (realtype) current scaled norm of F(u).

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional output value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

KINGetStepLength

Call flag = KINGetStepLength(kin_mem, &steplength);

Description The function KINGetStepLength returns the scaled Euclidean ℓ_2 norm of the step used

during the previous iteration.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

steplength (realtype) scaled norm of the Newton step.

Return value The return value flag (of type int) is one of:

KIN_SUCCESS The optional output value has been successfully set.

KIN_MEM_NULL The kin_mem pointer is NULL.

4.5.5.2 Direct linear solvers optional output functions

The following optional outputs are available from the KINDLS module: workspace requirements, number of calls to the Jacobian routine, number of calls to the system function routine for difference quotient Jacobian approximation, and last return value from a KINDLS function.

KINDlsGetWorkSpace

Call flag = KINDlsGetWorkSpace(kin_mem, &lenrwLS, &leniwLS);

Description The function KINDlsGetWorkSpace returns the KINDENSE real and integer workspace

sizes.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

lenrwLS (long int) the number of realtype values in the KINDLS workspace.

leniwLS (long int) the number of integer values in the KINDLS workspace.

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The optional output value has been successfully set.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_LMEM_NULL The KINDENSE linear solver has not been initialized.

Notes For the KINDENSE linear soler, in terms of the problem size N, the actual size of the

real workspace is N^2 realtype words, and the actual size of the integer workspace is

N integer words.

For the KINBAND linear solver, in terms of the problem size N and Jacobian half-bandwidths, the actual size of the real workspace, in realtype words, is approximately (2 mupper + 3 mlower + 2) N, and the actual size of the integer workspace is N integer

words.

KINDlsGetNumJacEvals

Call flag = KINDlsGetNumJacEvals(kin_mem, &njevals);

Description The function KINDlsGetNumJacEvals returns the number of calls to the dense Jacobian

approximation function.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

njevals (long int) the number of calls to the Jacobian function.

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The optional output value has been successfully set.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_LMEM_NULL The KINDENSE linear solver has not been initialized.

KINDlsGetNumFuncEvals

Call flag = KINDlsGetNumFuncEvals(kin_mem, &nfevalsLS);

Description The function KINDlsGetNumFuncEvals returns the number of calls to the user system

function used to compute the difference quotient approximation to the dense or banded

Jacobian.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nfevalsLS (long int) the number of calls to the user system function.

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The optional output value has been successfully set.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_LMEM_NULL The KINDENSE or KINBAND linear solver has not been initialized.

Notes The value nfevalsLS is incremented only if the internal difference quotient function is

used.

KINDlsGetLastFlag

Call flag = KINDlsGetLastFlag(kin_mem, &lsflag);

Description The function KINDlsGetLastFlag returns the last return value from a KINDENSE rou-

tine.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

lsflag (int) the value of the last return flag from a KINDENSE function.

Return value The return value flag (of type int) is one of

KINDLS_SUCCESS The optional output value has been successfully set.

KINDLS_MEM_NULL The kin_mem pointer is NULL.

KINDLS_LMEM_NULL The KINDENSE linear solver has not been initialized.

Notes If the KINDLS setup function failed (KINSol returned KIN_LSETUP_FAIL), then lsflag is

equal to the column index (numbered from one) at which a zero diagonal element was encountered during the LU factorization of the dense Jacobian matrix. For all other

failures, lsflag is negative.

4.5.5.3 Iterative linear solvers optional output functions

The following optional outputs are available from the KINSPILS modules: workspace requirements, number of linear iterations, number of linear convergence failures, number of calls to the preconditioner setup and solve routines, number of calls to the Jacobian-vector product routine, number of calls to the system function routine for difference quotient Jacobian-vector product approximation, and last return value from a linear solver function.

KINSpilsGetWorkSpace

Call flag = KINSpilsGetWorkSpace(kin_mem, &lenrwLS, &leniwLS);

Description The function KINSpilsGetWorkSpace returns the global sizes of the linear solver real

and integer workspaces.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

lenrwLS (long int) the number of realtype values in the linear solver workspace.

leniwLS (long int) the number of integer values in the linear solver workspace.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output values have been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The KINSPGMR linear solver has not been initialized.

Notes

In terms of the problem size N and maximum subspace size max1, the actual size of the real workspace, inrealtype words, is roughly:

 $(\max 1+3) * N + \max 1 * (\max 1+4) + 1$ for KINSPGMR,

7*N for KINSPBCG, and 11*N for KINSPTFQMR.

In a parallel setting, this value is global, summed over all processes.

KINSpilsGetNumLinIters

Call flag = KINSpilsGetNumLinIters(kin_mem, &nliters);

Description The function KINSpilsGetNumLinIters returns the cumulative number of linear itera-

tions.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nliters (long int) the current number of linear iterations.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPLIS_LMEM_NULL The linear solver module has not been initialized.

KINSpilsGetNumConvFails

Call flag = KINSpilsGetNumConvFails(kin_mem, &nlcfails);

Description The function KINSpilsGetNumConvFails returns the cumulative number of linear con-

vergence failures.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nlcfails (long int) the current number of linear convergence failures.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver module has not been initialized.

KINSpilsGetNumPrecEvals

Call flag = KINSpilsGetNumPrecEvals(kin_mem, &npevals);

Description The function KINSpilsGetNumPrecEvals returns the number of preconditioner evalua-

tions, i.e., the number of calls made to psetup.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

npevals (long int) the current number of calls to psetup.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver module has not been initialized.

KINSpilsGetNumPrecSolves

Call flag = KINSpilsGetNumPrecSolves(kin_mem, &npsolves);

Description The function KINSpilsGetNumPrecSolves returns the cumulative number of calls made

to the preconditioner solve function, psolve.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

npsolves (long int) the current number of calls to psolve.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver module has not been initialized.

KINSpilsGetNumJtimesEvals

Call flag = KINSpilsGetNumJtimesEvals(kin_mem, &njvevals);

Description The function KINSpilsGetNumJtimesEvals returns the cumulative number made to the

Jacobian-vector product function, jtimes.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

njvevals (long int) the current number of calls to jtimes.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver module has not been initialized.

KINSpilsGetNumFuncEvals

Call flag = KINSpilsGetNumFuncEvals(kin_mem, &nfevalsLS);

Description The function KINSpilsGetNumFuncEvals returns the number of calls to the user system

function for difference quotient Jacobian-vector product approximations.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

nfevalsLS (long int) the number of calls to the user system function.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver module has not been initialized.

Notes The value nfevalsLS is incremented only if the default KINSpilsDQJtimes difference

quotient function is used.

KINSpilsGetLastFlag

Call flag = KINSpilsGetLastFlag(kin_mem, &lsflag);

Description The function KINSpilsGetLastFlag returns the last return value from a KINSPILS rou-

tine.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

lsflag (int) the value of the last return flag from a KINSPILS function.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer is NULL.

KINSPILS_LMEM_NULL The linear solver module has not been initialized.

Notes

If the KINSPILS setup function failed (KINSOL returned KIN_LSETUP_FAIL), lsflag will be SPGMR_PSET_FAIL_UNREC, SPBCG_PSET_FAIL_UNREC, or SPTFQMR_PSET_FAIL_UNREC.

If the KINSPGMR solve function failed (KINSol returned KIN_LSOLVE_FAIL), lsflag contains the error return flag from SpgmrSolve and will be one of: SPGMR_MEM_NULL, indicating that the SPGMR memory is NULL; SPGMR_ATIMES_FAIL_UNREC, indicating an unrecoverable failure in the Jacobian-times-vector function; SPGMR_PSOLVE_FAIL_UNREC, indicating that the preconditioner solve function psolve failed unrecoverably; SPGMR_GS_FAIL, indicating a failure in the Gram-Schmidt procedure; or SPGMR_QRSOL_FAIL, indicating that the matrix R was found to be singular during the QR solve phase.

If the KINSPBCG solve function failed (KINSol returned KIN_LSOLVE_FAIL), lsflag contains the error return flag from SpbcgSolve and will be one of: SPBCG_MEM_NULL, indicating that the SPBCG memory is NULL; SPBCG_ATIMES_FAIL_UNREC, indicating an unrecoverable failure in the Jacobian-times-vector function; or SPBCG_PSOLVE_FAIL_UNREC, indicating that the preconditioner solve function psolve failed unrecoverably.

If the KINSPTFQMR solve function failed (KINSol returned KIN_LSOLVE_FAIL), lsflag contains the error return flag from SptfqmrSolve and will be one of: SPTFQMR_MEM_NULL, indicating that the SPTFQMR memory is NULL; SPTFQMR_ATIMES_FAIL_UNREC, indicating an unrecoverable failure in the J*v function; or SPTFQMR_PSOLVE_FAIL_UNREC, indicating that the preconditioner solve function psolve failed unrecoverably.

4.6 User-supplied functions

The user-supplied functions consist of one function defining the nonlinear system, (optionally) a function that handles error and warning messages, (optionally) a function that handles informational messages, (optionally) a function that provides Jacobian-related information for the linear solver, and (optionally) one or two functions that define the preconditioner for use in any of the Krylov iterative algorithms.

4.6.1 Problem-defining function

The user must provide a function of type KINSysFn defined as follows:

KINSysFn

Definition typedef void (*KINSysFn)(N_Vector u, N_Vector fval, void *user_data);

Purpose This function computes F(u) for a given value of the vector u.

Arguments u is the current value of the variable vector, u.

fval is the output vector F(u).

user_data is a pointer to user data, the pointer user_data passed to KINSetUserData.

Return value A KINSysFn function should return 0 if successful, a positive value if a recoverable error

occurred (in which case KINSOL will attempt to correct), or a negative value if it failed unrecoverably (in which case the solution process is halted and KIN_SYSFUNC_FAIL is

returned).

Notes Allocation of memory for fval is handled within KINSOL.

4.6.2 Error message handler function

As an alternative to the default behavior of directing error and warning messages to the file pointed to by errfp (see KINSetErrFile), the user may provide a function of type KINErrHandlerFn to process any such messages. The function type KINErrHandlerFn is defined as follows:

KINErrHandlerFn

Definition typedef void (*KINErrHandlerFn)(int error_code, const char *module, const char *function, char *msg, void *eh_data);

Purpose This function processes error and warning messages from KINSOL and its sub-modules.

Arguments error_code is the error code.

module is the name of the KINSOL module reporting the error.

function is the name of the function in which the error occurred.

msg is the error message.

eh_data is a pointer to user data, the same as the eh_data parameter passed to

KINSetErrHandlerFn.

Return value A KINErrHandlerFn function has no return value.

Notes error_code is negative for errors and positive (KIN_WARNING) for warnings. If a function that returns a pointer to memory encounters an error, it sets error_code to 0.

4.6.3 Informational message handler function

As an alternative to the default behavior of directing informational (meaning non-error) messages to the file pointed to by infofp (see KINSetInfoFile), the user may provide a function of type KINInfoHandlerFn to process any such messages. The function type KINInfoHandlerFn is defined as follows:

KINInfoHandlerFn

Definition typedef void (*KINInfoHandlerFn)(const char *module, const char *function, char *msg, void *ih_data);

Purpose This function processes informational messages from KINSOL and its sub-modules.

Arguments module is the name of the KINSOL module reporting the information.

function is the name of the function reporting the information.

msg is the message.

ih_data is a pointer to user data, the same as the ih_data parameter passed to

KINSetInfoHandlerFn.

Return value A KINInfoHandlerFn function has no return value.

4.6.4 Jacobian information (direct method with dense Jacobian)

If the direct linear solver with dense treatment of the Jacobian is used (KINDense or KINLapackDense is called in Step 7 of §4.4), the user may provide a function of type KINDlsDenseJacFn defined by

KINDlsDenseJacFn

Definition typedef int (*KINDlsDenseJacFn)(int N, N_Vector u, N_Vector fu, DlsMat J, void *user_data, N_Vector tmp1, N_Vector tmp2);

Purpose This function computes the dense Jacobian J(u) or an approximation to it.

Arguments N is the problem size.

u is the current (unscaled) iterate.

fu is the current value of the vector F(u).

J is the output approximate Jacobian matrix, $J = \partial F/\partial u$.

user_data is a pointer to user data, the same as the user_data parameter passed to KINSetUserData.

tmp1

tmp2 are pointers to memory allocated for variables of type N_Vector which can be used by KINDenseJacFn as temporary storage or work space.

Return value A function of type KINDlsDenseJacFn should return 0 if successful or a non-zero value otherwise.

Notes

A user-supplied dense Jacobian function must load the N by N dense matrix J with an approximation to the Jacobian matrix J(u) at u. Only nonzero elements need to be loaded into J because J is set to the zero matrix before the call to the Jacobian function. The type of J is DlsMat.

The accessor macros DENSE_ELEM and DENSE_COL allow the user to read and write dense matrix elements without making explicit references to the underlying representation of the DlsMat type. DENSE_ELEM(J, i, j) references the (i, j)-th element of the dense matrix J (i, j=0...N-1). This macro is for use in small problems in which efficiency of access is not a major concern. Thus, in terms of indices m and n running from 1 to N, the Jacobian element $J_{m,n}$ can be loaded with the statement DENSE_ELEM(J, m-1, n-1) = $J_{m,n}$. Alternatively, DENSE_COL(J, j) returns a pointer to the storage for the jth column of J (j=0...N-1), and the elements of the jth column are then accessed via ordinary array indexing. Thus $J_{m,n}$ can be loaded with the statements col_n = DENSE_COL(J, n-1); col_n[m-1] = $J_{m,n}$. For large problems, it is more efficient to use DENSE_COL than to use DENSE_ELEM. Note that both of these macros number rows and columns starting from 0, not 1.

The DlsMat type and the accessor macros DENSE_ELEM and DENSE_COL are documented in §8.1.3.

If the user's KINDlsDenseJacFn function uses difference quotient approximations, it may need to access quantities not in the call list. To obtain these, use the KINGet* functions described in §4.5.5.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

4.6.5 Jacobian information (direct method with banded Jacobian)

If the direct linear solver with banded treatment of the Jacobian is used (KINBand or KINLapackBand is called in Step 7 of §4.4), the user may provide a function of type KINDlsBandJacFn defined by:

KINDlsBandJacFn

Definition typedef int (*KINDlsBandJacFn)(int N, int mupper, int mlower, N_Vector u, N_Vector fu, DlsMat J, void *user_data, N_Vector tmp1, N_Vector tmp2);

Purpose This function computes the banded Jacobian J(u) or a banded approximation to it.

Arguments N is the problem size.

mlower

mupper are the lower and upper half-bandwidths of the Jacobian.

u is the current (unscaled) iterate.

fu is the current value of the vector F(u).

J is the output approximate Jacobian matrix, $J = \partial F/\partial u$.

user_data is a pointer to user data, the same as the user_data parameter passed to KINSetUserData.

tmp1

tmp2 are pointers to memory allocated for variables of type N_Vector which can be used by KINBandJacFn as temporary storage or work space.

Return value A function of type KINDlsBandJacFn should return 0 if successful or a non-zero value otherwise.

Notes

A user-supplied band Jacobian function must load the band matrix J of type DlsMat with the elements of the Jacobian J(u) at u. Only nonzero elements need to be loaded into J because J is preset to zero before the call to the Jacobian function.

The accessor macros BAND_ELEM, BAND_COL, and BAND_COL_ELEM allow the user to read and write band matrix elements without making specific references to the underlying representation of the DlsMat type. BAND_ELEM(J, i, j) references the (i, j)th element of the band matrix J, counting from 0. This macro is for use in small problems in which efficiency of access is not a major concern. Thus, in terms of indices m and n running from 1 to N with (m,n) within the band defined by mupper and mlower, the Jacobian element $J_{m,n}$ can be loaded with the statement BAND_ELEM(J, m-1, n-1) = $J_{m,n}$. The elements within the band are those with -mupper $\leq m-n \leq mlower$. Alternatively, BAND_COL(J, j) returns a pointer to the diagonal element of the jth column of J, and if we assign this address to realtype *col_j, then the ith element of the jth column is given by BAND_COL_ELEM(col_j, i, j), counting from 0. Thus for (m,n) within the band, $J_{m,n}$ can be loaded by setting col_n = BAND_COL(J, n-1); BAND_COL_ELEM(col_n, m-1, n-1) = $J_{m,n}$. The elements of the jth column can also be accessed via ordinary array indexing, but this approach requires knowledge of the underlying storage for a band matrix of type DlsMat. The array coln can be indexed from -mupper to mlower. For large problems, it is more efficient to use the combination of BAND_COL and BAND_COL_ELEM than to use the BAND_ELEM. As in the dense case, these macros all number rows and columns starting from 0, not 1.

The DlsMat type and the accessor macros BAND_ELEM, BAND_COL, and BAND_COL_ELEM are documented in §8.1.4.

If the user's KINDlsBandJacFn function uses difference quotient approximations, it may need to access quantities not in the call list. To obtain these, use the KINGet* functions described in §4.5.5.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

4.6.6 Jacobian information (matrix-vector product)

If one of the Krylov iterative linear solvers SPGMR, SPBCG, or SPTFQMR is selected (KINSp* is called in step 7 of $\S4.4$), the user may provide a jtimes function of type KINSpilsJacTimesVecFn to compute products Jv. If such a function is not supplied, the default is a difference quotient approximation of these products.

KINSpilsJacTimesVecFn

Definition typedef int (*KINSpilsJacTimesVecFn)(N_Vector v, N_Vector Jv, N_Vector u, booleantype new_u, void *user_data):

Purpose This jtimes function computes the product Jv (or an approximation to it).

Arguments v is the vector by which the Jacobian must be multiplied to the right.

Jv is the computed output vector.

u is the current value of the dependent variable vector.

new_u is a flag, input from KINSOL and possibly reset by the user's jtimes function, indicating whether the iterate vector u has been updated since the last call to jtimes. This is useful if the jtimes function computes and saves Jacobian data that depends on u for use in computing J(u)v. The input value of new_u is TRUE following an update by KINSOL, and in that case any saved Jacobian data depending on u should be recomputed. The jtimes routine should then

set new_u to FALSE, so that on subsequent calls to jtimes with the same u, the saved data can be reused.

user_data is a pointer to user data, the same as the user_data parameter passed to KINSetUserData.

Return value The value to be returned by the Jacobian-times-vector function should be 0 if successful. If a recoverable failure occured, the return value should be positive. In this case, KINSOL will attempt to correct by calling the preconditioner setup function if the preconditioner information. If this information is current, KINSOL halts. If the Jacobian-times-vector function encounters an unrecoverable error, it should return a negative value, prompting KINSOL to halt.

Notes

If a user-defined routine is not given, then an internal KINSPGMR function, using difference quotient approximations, is used.

If the user-provided KINSpilsJacTimesVecFn function needs the unit roundoff, this can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

Preconditioning (linear system solution) 4.6.7

If preconditioning is used, then the user must provide a C function to solve the linear system Pz = rwhere P is the preconditioner matrix, approximating (at least crudely) the system Jacobian J = $\partial F/\partial u$. This function must be of type KINSpilsPrecSolveFn, defined as follows:

KINSpilsPrecSolveFn

Definition typedef int (*KINSpilsPrecSolveFn)(N_Vector u, N_Vector uscale, N_Vector fval, N_Vector fscale, N_Vector v, void *user_data, N_Vector tmp);

Purpose

This function solves the preconditioning system Pz = r.

Arguments

is the current (unscaled) value of the iterate. u

uscale is a vector containing diagonal elements of the scaling matrix for u.

fval is the vector F(u) evaluated at **u**.

fscale is a vector containing diagonal elements of the scaling matrix for fval.

on input, v is set to the right-hand side vector of the linear system, r. On output, v must contain the solution z of the linear system Pz = r.

user_data is a pointer to user data, the same as the user_data parameter passed to the function KINSetUserData.

is a pointer to memory allocated for a variable of type N_Vector which can tmp be used for work space.

Return value The value to be returned by the preconditioner solve function is a flag indicating whether it was successful. This value should be 0 if successful, positive for a recoverable error, and negative for an unrecoverable error.

Notes

If the preconditioner solve function fails recoverably and if the preconditioner information (set by the preconditioner setup function) is out of date, KINSOL attempts to correct by calling the setup function. If the preconditioner data is current, KINSOL halts.

4.6.8 Preconditioning (Jacobian data)

If the user's preconditioner requires that any Jacobian-related data be evaluated or preprocessed, then this needs to be done in a user-supplied C function of type KINSpilsPrecSetupFn, defined as follows:

KINSpilsPrecSetupFn

Definition typedef int (*KINSpilsPrecSetupFn)(N_Vector u, N_Vector uscale,

N_Vector fval, N_Vector fscale,
void *user_data, N_Vector tmp1,
N_Vector tmp2);

Purpose This function evaluates and/or preprocesses Jacobian-related data needed by the pre-

conditioner solve function.

Arguments The arguments of a KINSpilsPrecSetupFn are as follows:

u is the current (unscaled) value of the iterate.

uscale is a vector containing diagonal elements of the scaling matrix for u.

fval is the vector F(u) evaluated at \mathbf{u} .

fscale is a vector containing diagonal elements of the scaling matrix for fval.

user_data is a pointer to user data, the same as the user_data parameter passed to

the function KINSetUserData.

tmp1

Notes

tmp2 are pointers to memory allocated for variables of type N_Vector which can

be used by ${\tt KINSpilsPrecSetupFn}$ as temporary storage or work space.

Return value The value to be returned by the preconditioner setup function is a flag indicating whether it was successful. This value should be 0 if successful, any other value re-

sulting in halting the KINSOL solver.

The user-supplied preconditioner setup subroutine should compute the right preconditioner matrix P (stored in the memory block referenced by the user_data pointer) used to form the scaled preconditioned linear system

$$(D_F J(u) P^{-1} D_u^{-1}) \cdot (D_u P x) = -D_F F(u),$$

where D_u and D_F denote the diagonal scaling matrices whose diagonal elements are stored in the vectors uscale and fscale, respectively.

The preconditioner setup routine will not be called prior to every call made to the preconditioner solve function, but will instead be called only as often as necessary to achieve convergence of the Newton iteration.

If the user's KINSpilsPrecSetupFn function uses difference quotient approximations, it may need to access quantities not in the call list. To obtain these, use the KINGet* functions described in §4.5.5.1. The unit roundoff can be accessed as UNIT_ROUNDOFF defined in sundials_types.h.

If the preconditioner solve routine requires no preparation, then a preconditioner setup function need not be given.

4.7 A parallel band-block-diagonal preconditioner module

The efficiency of Krylov iterative methods for the solution of linear systems can be greatly enhanced through preconditioning. For problems in which the user cannot define a more effective, problem-specific preconditioner, KINSOL provides a band-block-diagonal preconditioner module KINBBDPRE, to be used with the parallel N_Vector module described in §6.2.

This module provides a preconditioner matrix for KINSOL that is block-diagonal with banded blocks. The blocking corresponds to the distribution of the dependent variable vector u amongst the processes. Each preconditioner block is generated from the Jacobian of the local part (associated with the current process) of a given function G(u) approximating F(u) (G = F is allowed). The blocks are generated by each process via a difference quotient scheme, utilizing a specified band structure. This structure is given by upper and lower half-bandwidths, mudq and mldq, defined as the number

of non-zero diagonals above and below the main diagonal, respectively. However, from the resulting approximate Jacobain blocks, only a matrix of bandwidth $\mathtt{mukeep} + \mathtt{mlkeep} + 1$ is retained.

Neither pair of parameters need be the true half-bandwidths of the Jacobian of the local block of G, if smaller values provide a more efficient preconditioner. Such an efficiency gain may occur if the couplings in the system outside a certain bandwidth are considerably weaker than those within the band. Reducing mukeep and mlkeep while keeping mudq and mldq at their true values, discards the elements outside the narrower band. Reducing both pairs has the additional effect of lumping the outer Jacobian elements into the computed elements within the band, and requires more caution and experimentation to see whether the lower cost of narrower band matrices offsets the loss of accuracy in the blocks.

The KINBBDPRE module calls two user-provided functions to construct P: a required function Gloc (of type KINLocalFn) which approximates the nonlinear system function function $G(u) \approx F(u)$ and which is computed locally, and an optional function Gcomm (of type KINCommFn) which performs all interprocess communication necessary to evaluate the approximate function G. These are in addition to the user-supplied nonlinear system function that evaluates F(u). Both functions take as input the same pointer user-data as that passed by the user to KINSetUserData and passed to the user's function func, and neither function has a return value. The user is responsible for providing space (presumably within user-data) for components of u that are communicated by Gcomm from the other processes, and that are then used by Gloc, which should not do any communication.

KINLocalFn

Definition typedef void (*KINLocalFn)(int Nlocal, N_Vector u,

N_Vector gval, void *user_data);

Purpose This Gloc function computes G(u), and outputs the resulting vector as gval.

Arguments Nlocal is the local vector length.

u is the current value of the iterate.

gval is the output vector.

user_data is a pointer to user data, the same as the user_data parameter passed to KINSetUserData.

Return value A KINLocalFn function type does not have a return value.

Notes This function must assume that all interprocess communication of data needed to calculate gval has already been done, and this data is accessible within user_data.

Memory for u and gval is handled within the preconditioner module.

The case where G is mathematically identical to F is allowed.

KINCommFn

Definition typedef void (*KINCommFn)(int Nlocal, N_Vector u, void *user_data);

Purpose This Gcomm function performs all interprocess communications necessary for the execu-

tion of the Gloc function above, using the input vector u.

Arguments Nlocal is the local vector length.

u is the current value of the iterate.

user_data is a pointer to user data, the same as the user_data parameter passed to KINSetUserData.

Return value A KINCommFn function type does not have a return value.

Notes The Gcomm function is expected to save communicated data in space defined within the

structure user_data.

Each call to the Gcomm function is preceded by a call to the system function func with the same u argument. Thus Gcomm can omit any communications done by func if relevant to the evaluation of Gloc. If all necessary communication was done in func, then Gcomm = NULL can be passed in the call to KINBBDPrecInit (see below).

Besides the header files required for the solution of a nonlinear problem (see §4.3), to use the KINBBDPRE module, the main program must include the header file kinbbdpre.h which declares the needed function prototypes.

The following is a summary of the usage of this module and describes the sequence of calls in the user main program. Steps that are unchanged from the user main program presented in $\S4.4$ are graved out.

- 1. Initialize MPI
- 2. Set problem dimensions
- 3. Set vector with initial guess
- 4. Create KINSOL object
- 5. Set optional inputs
- 6. Allocate internal memory

7. Attach iterative linear solver, one of:

```
flag = KINSpgmr(kin.mem, maxl);
flag = KINSpbcg(kin.mem, maxl);
flag = KINSptfqmr(kin.mem, maxl);
```

8. Initialize the KINBBDPRE preconditioner module

Specify the upper and lower half-bandwidth pairs (mudq, mldq) and (mukeep, mlkeep), and call

to allocate memory for and initialize the internal preconditoner data. The last two arguments of KINBBDPrecInit are the two user-supplied functions described above.

9. Set linear solver optional inputs

Note that the user should not overwrite the preconditioner data, setup function, or solve function through calls to KINSPILS optional input functions.

10. Solve problem

11. Get optional output

Additional optional outputs associated with KINBBDPRE are available by way of two routines described below, KINBBDPrecGetWorkSpace and KINBBDPrecGetNumGfnEvals.

- 12. Deallocate memory for solution vector
- 13. Free solver memory
- 14. Finalize MPI

The user-callable function that initializes KINBBDPRE (step 8), is described in more detail below.

KINBBDPrecInit

```
Call flag = KINBBDPrecInit(kin_mem, Nlocal, mudq, mldq, mukeep, mlkeep, dq_rel_u, Gloc, Gcomm);
```

Description The function KINBBDPrecInit initializes and allocates memory for the KINBBDPRE preconditioner.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

Nlocal (int) local vector length.

mudq (int) upper half-bandwidth to be used in the difference-quotient Jacobian approximation.

mldq (int) lower half-bandwidth to be used in the difference-quotient Jacobian approximation.

mukeep (int) upper half-bandwidth of the retained banded approximate Jacobian block.

mlkeep (int) lower half-bandwidth of the retained banded approximate Jacobian block.

dq_rel_u (realtype) the relative increment in components of u used in the difference quotient approximations. The default is dq_rel_u= √unit roundoff, which can be specified by passing dq_rel_u= 0.0.

Gloc (KINLocalFn) the C function which computes the approximation $G(u) \approx F(u)$.

Gcomm (KINCommFn) the optional C function which performs all interprocess communication required for the computation of G(u).

Return value The return value flag (of type int) is one of

KINSPILS_SUCCESS The call to KINBBDPrecInit was successful.

KINSPILS_MEM_NULL The kin_mem pointer was NULL.

KINSPILS_MEM_FAIL A memory allocation request has failed.

 ${\tt KINSPILS_LMEM_NULL}$ A KINSPILS linear solver was not attached.

 $\begin{tabular}{ll} {\tt KINSPILS_ILL_INPUT} & {\tt The supplied vector implementation was not compatible with block band preconditioner.} \end{tabular}$

Notes

If one of the half-bandwidths mudq or mldq to be used in the difference-quotient calculation of the approximate Jacobian is negative or exceeds the value Nlocal-1, it is replaced with 0 or Nlocal-1 accordingly.

The half-bandwidths mudq and mldq need not be the true half-bandwidths of the Jacobian of the local block of G, when smaller values may provide greater efficiency.

Also, the half-bandwidths mukeep and mlkeep of the retained banded approximate Jacobian block may be even smaller, to reduce storage and computation costs further.

For all four half-bandwidths, the values need not be the same for every process.

The following two optional output functions are available for use with the KINBBDPRE module:

KINBBDPrecGetWorkSpace

Call flag = KINBBDPrecGetWorkSpace(kin_mem, &lenrwBBDP, &leniwBBDP);

Description The function KINBBDPrecGetWorkSpace returns the local KINBBDPRE real and integer workspace sizes.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

 ${\tt lenrwBBDP} \ ({\tt long\ int}) \ {\tt local\ number\ of\ realtype\ values\ in\ the\ KINBBDPRE\ workspace}.$

leniwBBDP (long int) local number of integer values in the KINBBDPRE workspace.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer was NULL.

KINSPILS_PMEM_NULL The KINBBDPRE preconditioner has not been initialized.

Notes

In terms of the local vector dimension Nlocal and $smu = min(N_l - 1, mukeep + mlkeep)$, the actual size of the real workspace is $(2 \, mlkeep + mukeep + smu + 2)$ Nlocal realtype words, and the actual size of the integer workspace is Nlocal integer words. These values are local to the current processor.

The workspaces referred to here exist in addition to those given by the corresponding KINSp*GetWorkSpace function.

KINBBDPrecGetNumGfnEvals

Call flag = KINBBDPrecGetNumGfnEvals(kin_mem, &ngevalsBBDP);

Description The function KINBBDPrecGetNumGfnEvals returns the number of calls to the user Gloc

function due to the difference quotient approximation of the Jacobian blocks used within

KINBBDPRE's preconditioner setup function.

Arguments kin_mem (void *) pointer to the KINSOL memory block.

ngevalsBBDP (long int) the number of calls to the user Gloc function.

Return value The return value flag (of type int) is one of:

KINSPILS_SUCCESS The optional output value has been successfully set.

KINSPILS_MEM_NULL The kin_mem pointer was NULL.

KINSPILS_PMEM_NULL The KINBBDPRE preconditioner has not been initialized.

In addition to the ngevalsBBDP Gloc evaluations, the costs associated with KINBBDPRE also include nlinsetups LU factorizations, nlinsetups calls to Gcomm, npsolves banded backsolve calls, and nfevalsLS right-hand side function evaluations, where nlinsetups is an optional KINSOL output and npsolves and nfevalsLS are linear solver optional outputs (see §4.5.5).

Chapter 5

FKINSOL, an Interface Module for FORTRAN Applications

The FKINSOL interface module is a package of C functions which support the use of the KINSOL solver, for the solution nonlinear systems F(u) = 0, in a mixed FORTRAN/C setting. While KINSOL is written in C, it is assumed here that the user's calling program and user-supplied problem-defining routines are written in FORTRAN. This package provides the necessary interface to KINSOL for both the serial and the parallel NVECTOR implementations.

5.1 FKINSOL routines

The user-callable functions, with the corresponding KINSOL functions, are as follows:

- Interface to the NVECTOR modules
 - FNVINITS (defined by NVECTOR_SERIAL) interfaces to N_VNewEmpty_Serial.
 - FNVINITP (defined by NVECTOR_PARALLEL) interfaces to N_VNewEmpty_Parallel.
- Interface to the main kinsol module
 - FKINMALLOC interfaces to KINCreate, KINSetUserData, and KINInit.
 - FKINSETIIN and FKINSETRIN interface to KINSet* functions.
 - FKINSETVIN interfaces to KINSetConstraints.
 - FKINSOL interfaces to KINSol, KINGet* functions, and to the optional output functions for the selected linear solver module.
 - FKINFREE interfaces to KINFree.
- Interface to the linear solver modules
 - FKINDENSE interfaces to KINDense.
 - FKINDENSESETJAC interfaces to KINDlsSetDenseJacFn.
 - FKINLAPACKDENSE interfaces to KINLapackDense.
 - FKINLAPACKDENSESETJAC interfaces to KINDlsSetDenseJacFn.
 - FKINBAND interfaces to KINBand.
 - FKINBANDSETJAC interfaces to KINDlsSetBandJacFn.
 - FKINLAPACKBAND interfaces to KINLapackBand.
 - FKINLAPACKBANDSETJAC interfaces to KINDlsSetBandJacFn.

- FKINSPGMR interfaces to KINSpgmr and SPGMR optional input functions.
- FKINSPBCG interfaces to KINSpbcg and SPBCG optional input functions.
- FKINSPTFQMR interfaces to KINSptfqmr and SPTFQMR optional input functions.
- FKINSPILSSETJAC interfaces to KINSpilsSetJacTimesVecFn.
- FKINSPILSSETPREC interfaces to KINSpilsSetPreconditioner.

The user-supplied functions, each listed with the corresponding internal interface function which calls it (and its type within KINSOL), are as follows:

FKINSOL routine	KINSOL function	KINSOL type of
(FORTRAN, user-supplied)	(C, interface)	interface function
FKFUN	FKINfunc	KINSysFn
FKDJAC	FKINDenseJac	KINDlsDenseJacFn
	FKINLapackDenseJac	KINDlsDenseJacFn
FKBJAC	FKINBandJac	KINDlsBandJacFn
	FKINLapackBandJac	KINDlsBandJacFn
FKPSET	FKINPSet	KINSpilsPrecSetupFn
FKPSOL	FKINPSol	KINSpilsPrecSolveFn
FKJTIMES	FKINJtimes	KINSpilsJacTimesVecFn

In contrast to the case of direct use of KINSOL, the names of all user-supplied routines here are fixed, in order to maximize portability for the resulting mixed-language program.

5.2 Important note on portability

In this package, the names of the interface functions, and the names of the FORTRAN user routines called by them, appear as dummy names which are mapped to actual values by a series of definitions in the header files fkinsol.h and fkinbbd.h. By default, those mapping definitions depend in turn on the C macro F77_FUNC defined in the header file sundials_config.h and decided upon at configuration time (see Appendix A).

The user must also ensure that variables in the user FORTRAN code are declared in a manner consistent with their counterparts in KINSOL. All real variables must be declared as REAL, DOUBLE PRECISION, or perhaps as REAL*n, where n denotes the number of bytes, depending on whether KINSOL was built in single, double or extended precision (see Appendix A). Moreover, some of the FORTRAN integer variables must be declared as INTEGER*4 or INTEGER*8 according to the C type long int. These integer variables include: the array of integer optional inputs and outputs (IOUT), problem dimensions (NEQ, NLOCAL, NGLOBAL), and Jacobian half-bandwidths (MU and ML). This is particularly important when using KINSOL and the FKINSOL package on 64-bit architectures.

5.3 Usage of the FKINSOL interface module

The usage of FKINSOL requires calls to a few different interface functions, depending on the method options selected, and one or more user-supplied routines which define the problem to be solved. These function calls and user routines are summarized separately below. Some details are omitted, and the user is referred to the description of the corresponding KINSOL functions for information on the arguments of any given user-callable interface routine, or of a given user-supplied function called by an interface function.

Steps marked [S] in the instructions below apply to the serial NVECTOR implementation (NVECTOR_SERIAL) only, while those marked [P] apply to NVECTOR_PARALLEL.

1. Nonlinear system function specification

The user must in all cases supply the following FORTRAN routine

SUBROUTINE FKFUN (U, FVAL, IER)
DIMENSION U(*), FVAL(*)

It must set the FVAL array to F(u), the system function, as a function of U = u. IER is an error return flag which should be set to 0 if successful, a positive value if a recoverable error occurred (in which case KINSOL will attempt to correct), or a negative value if it failed unrecoverably (in which case the solution process is halted).

2. NVECTOR module initialization

[S] To initialize the serial NVECTOR module, the user must make the following call:

```
CALL FNVINITS (KEY, NEQ, IER)
```

where KEY is the solver id (KEY = 3 for KINSOL), NEQ is the size of vectors, and IER is a return completion flag which is 0 on success and -1 if a failure occurred.

[P] To initialize the parallel vector module, the user must make the following call:

```
CALL FNVINITP (COMM, KEY, NLOCAL, NGLOBAL, IER)
```

in which the arguments are: COMM = MPI communicator, KEY = 3, NLOCAL = the local size of vectors on this processor, and NGLOBAL = the system size (and the global size of all vectors, equal to the sum of all values of NLOCAL). The return flag IER is set to 0 on a successful return and to -1 otherwise.

If the header file sundials_config.h defines SUNDIALS_MPI_COMM_F2C to be 1 (meaning the MPI implementation used to build SUNDIALS includes the MPI_Comm_f2c function), then COMM can be any valid MPI communicator. Otherwise, MPI_COMM_WORLD will be used, so just pass an integer value as a placeholder.

3. Problem specification

To set various problem and solution parameters and allocate internal memory, make the following call:

FKINMALLOC

Call CALL FKINMALLOC (IOUT, ROUT, IER)

Description This function specifies the optional output arrays, allocates internal memory, and

initializes KINSOL.

Arguments IOUT is an integer array for integer optional outputs.

ROUT is a real array for real optional outputs.

Return value IER is the return completion flag. Values are 0 for successful return and -1 other-

wise. See printed message for details in case of failure.

Notes The user integer data array IOUT must be declared as INTEGER*4 or INTEGER*8

according to the C type long int.

The optional outputs associated with the main KINSOL integrator are listed in Ta-

ble 5.2.

4. Set optional inputs

Call FKINSETIIN and/or FKINSETRIN to set desired optional inputs, if any. See §5.4 for details.

5. Linear solver specification

The solution method in KINSOL involves the solution of linear systems related to the Jacobian of the nonlinear system. KINSOL presently includes five choices for the treatment of these systems, and the user of FKINSOL must call a routine with a specific name to make the desired choice.



[S] Dense treatment of the linear system

To use the direct dense linear solver based on the internal KINSOL implementation, the user must make the call:

```
CALL FKINDENSE (NEQ, IER)
```

where NEQ is the size of the nonlinear system. The argument IER is an error return flag which is 0 for success, -1 if a memory allocation failure occurred, or -2 for illegal input.

Alternatively, to use the Lapack-based direct dense linear solver, the user must make the call:

```
CALL FKINLAPACKDENSE(NEQ, IER)
```

where the arguments have the exact same meanings as for FKINDENSE.

As an option when using the DENSE linear solver, the user may supply a routine that computes a dense approximation of the system Jacobian $J = \partial F/\partial u$. If supplied, it must have the following form:

```
SUBROUTINE FKDJAC (NEQ, U, FVAL, DJAC, WK1, WK2, IER)
DIMENSION U(*), FVAL(*), DJAC(NEQ,*), WK1(*), WK2(*)
```

Typically this routine will use only NEQ, U, and DJAC. It must compute the Jacobian and store it columnwise in DJAC. The input arguments U and FVAL contain the current values of u and F(u), respectively. The vectors WK1 and WK2 of length NEQ are provided as work space for use in FKDJAC. IER is an error return flag which should be set to 0 if successful, a positive value if a recoverable error occurred (in which case KINSOL will attempt to correct), or a negative value if FKDJAC failed unrecoverably (in which case the solution process is halted).

If the FKDJAC routine is provided, then, following the call to FKINDENSE, the user must make the call:

```
CALL FKINDENSESETJAC (FLAG, IER)
```

with ${\tt FLAG} \neq 0$ to specify use of the user-supplied Jacobian approximation. The argument ${\tt IER}$ is an error return flag which is 0 for success or non-zero if an error occurred. If using the Lapack-based direct dense linear solver, the use of a Jacobian approximation supplied by the user is indicated through the call

```
CALL FKINLAPACKDENSESETJAC (FLAG. IER)
```

Optional outputs specific to the DENSE case are listed in Table 5.2.

[S] Band treatment of the linear system

To use the direct band linear solver based on the internal KINSOL implementation, the user must make the call:

```
CALL FKINBAND (NEQ, MU, ML, IER)
```

The arguments are: MU, the upper half-bandwidth; ML, the lower half-bandwidth; and IER, an error return flag which is 0 for success, -1 if a memory allocation failure occurred, or -2 in case an input has an illegal value.

Alternatively, to use the Lapack-based direct band linear solver, the user must make the call:

```
CALL FKINLAPACKBAND (NEQ, MU, ML, IER)
```

where the arguments have the exact same meanings as for FKINBAND.

As an option when using the BAND linear solver, the user may supply a routine that computes a band approximation of the system Jacobian $J = \partial F/\partial u$. If supplied, it must have the following form:

```
SUBROUTINE FKBJAC (NEQ, MU, ML, MDIM, U, FVAL, BJAC, WK1, WK2, IER) DIMENSION U(*), FVAL(*), BJAC(MDIM,*), WK1(*), WK2(*)
```

Typically this routine will use only NEQ, MU, ML, U, and BJAC. It must load the MDIM by N array BJAC with the Jacobian matrix at the current u in band form. Store in BJAC(k,j) the Jacobian element $J_{i,j}$ with k=i-j+ MU +1 ($k=1\cdots$ ML + MU + 1) and $j=1\cdots N$. The input arguments U and FVAL contain the current values of u, and F(u), respectively. The vectors WK1 and WK2 of length NEQ are provided as work space for use in FKBJAC. IER is an error return flag, which should be set to 0 if successful, a positive value if a recoverable error occurred (in which case KINSOL will attempt to correct), or a negative value if FKBJAC failed unrecoverably (in which case the solution process is halted).

If the FKBJAC routine is provided, then, following the call to FKINBAND, the user must make the call:

```
CALL FKINBANDSETJAC (FLAG, IER)
```

with ${\tt FLAG} \neq 0$ to specify use of the user-supplied Jacobian approximation. The argument IER is an error return flag which is 0 for success or non-zero if an error occurred. If using the Lapack-based direct band linear solver, the use of a Jacobian approximation supplied by the user is indicated through the call

```
CALL FKINLAPACKNBANDSETJAC (FLAG, IER)
```

Optional outputs specific to the BAND case are listed in Table 5.2.

[S][P] SPGMR treatment of the linear systems

For the Scaled Preconditioned GMRES solution of the linear systems, the user must make the call

```
CALL FKINSPGMR (MAXL, MAXLRST, IER)
```

The arguments are as follows. MAXL is the maximum Krylov subspace dimension. MAXLRST is the maximum number of restarts. IER is an error return flag which is 0 to indicate success, -1 if a memory allocation failure occurred, or -2 to indicate an illegal input.

Optional outputs specific to the SPGMR case are listed in Table 5.2.

For descriptions of the relevant optional user-supplied routines, see User-supplied routines for SPGMR/SPBCG/SPTFQMR below.

[S][P] SPBCG treatment of the linear systems

For the Scaled Preconditioned Bi-CGStab solution of the linear systems, the user must make the call

```
CALL FKINSPBCG (MAXL, IER)
```

Its arguments are the same as those with the same names for FKINSPGMR.

Optional outputs specific to the SPBCG case are listed in Table 5.2.

For descriptions of the relevant optional user-supplied routines, see **User-supplied routines for SPGMR/SPBCG/SPTFQMR** below.

[S][P] SPTFQMR treatment of the linear systems

For the Scaled Preconditioned Transpose-Free Quasi-Minimal Residual solution of the linear systems, the user must make the call

```
CALL FKINSPTFQMR (MAXL, IER)
```

Its arguments are the same as those with the same names for FKINSPGMR.

Optional outputs specific to the SPTFQMR case are listed in Table 5.2.

For descriptions of the relevant optional user-supplied routines, see below.

[S][P] Functions used by SPGMR/SPBCG/SPTFQMR

An optional user-supplied routine, FKINJTIMES (see below), can be provided for Jacobian-vector products. If it is, then, following the call to FKINSPGMR, FKINSPBCG, or FKINSPTFQMR, the user must make the call:

```
CALL FKINSPILSSETJAC (FLAG, IER)
```

with $\mathtt{FLAG} \neq 0$ to specify use of the user-supplied Jacobian-times-vector approximation. The argument IER is an error return flag which is 0 for success or non-zero if an error occurred.

If preconditioning is to be done, then the user must call

```
CALL FKINSPILSSETPREC (FLAG, IER)
```

with FLAG $\neq 0$. The return flag IER is 0 if successful, or negative if a memory error occurred. In addition, the user program must include preconditioner routines FKPSOL and FKPSET (see below).

[S][P] User-supplied routines for SPGMR/SPBCG/SPTFQMR

With treatment of the linear systems by any of the Krylov iterative solvers, there are three optional user-supplied routines — FKINJTIMES, FKPSOL, and FKPSET. The specifications for these routines are given below.

As an option when using the SPGMR, SPBCG, or SPTFQMR linear solvers, the user may supply a routine that computes the product of the system Jacobian $J = \partial F/\partial u$ and a given vector v. If supplied, it must have the following form:

```
SUBROUTINE FKINJTIMES (V, FJV, NEWU, U, IER) DIMENSION V(*), FJV(*), U(*)
```

Typically this routine will use only U, V, and FJV. It must compute the product vector Jv, where the vector v is stored in V, and store the product in FJV. The input argument U contains the current value of u. On return, set IER = 0 if FKINJTIMES was successful, and nonzero otherwise. NEWU is a flag to indicate if U has been changed since the last call; if it has, then NEWU = 1, and FKINJTIMES should recompute any saved Jacobian data it uses and reset NEWU to 0. (See §4.6.6.)

If preconditioning is to be included, the following routine must be supplied, for solution of the preconditioner linear system:

```
SUBROUTINE FKPSOL (U, USCALE, FVAL, FSCALE, VTEM, FTEM, IER)
DIMENSION U(*), USCALE(*), FVAL(*), FSCALE(*), VTEM(*), FTEM(*)
```

Typically this routine will use only U, FVAL, VTEM and FTEM. It must solve the preconditioned linear system Pz = r, where r = VTEM is input, and store the solution z in VTEM as well. Here P is the

right preconditioner. If scaling is being used, the routine supplied must also account for scaling on either coordinate or function value, as given in the arrays USCALE and FSCALE, respectively.

If the user's preconditioner requires that any Jacobian-related data be evaluated or preprocessed, then the following routine can be used for the evaluation and preprocessing of the preconditioner:

```
SUBROUTINE FKPSET (U, USCALE, FVAL, FSCALE, VTEMP1, VTEMP2, IER)
DIMENSION U(*), USCALE(*), FVAL(*), FSCALE(*), VTEMP1(*), VTEMP2(*)
```

It must perform any evaluation of Jacobian-related data and preprocessing needed for the solution of the preconditioned linear systems by FKPSOL. The variables U through FSCALE are for use in the preconditioning setup process. Typically, the system function FKFUN is called before any calls to FKPSET, so that FVAL will have been updated. U is the current solution iterate. The arrays VTEMP1 and VTEMP2 are available for work space. If scaling is being used, USCALE and FSCALE are available for those operations requiring scaling.

On return, set IER = 0 if FKPSET was successful, or set IER = 1 if an error occurred.

If the user calls FKINSPILSSETPREC, the routine FKPSET must be provided, even if it is not needed, and then it should return IER = 0.



6. Problem solution

Solving the nonlinear system is accomplished by making the following call:

```
CALL FKINSOL (U, GLOBALSTRAT, USCALE, FSCALE, IER)
```

The arguments are as follows. U is an array containing the initial guess on input, and the solution on return. GLOBALSTRAT is an integer (type INTEGER) defining the global strategy choice (1 specifies Inexact Newton, while 2 indicates line search). USCALE is an array of scaling factors for the U vector. FSCALE is an array of scaling factors for the FVAL vector. IER is an integer completion flag and will have one of the following values: 0 to indicate success, 1 to indicate that the initial guess satisfies F(u) = 0 within tolerances, 2 to indicate apparent stalling (small step), or a negative value to indicate an error or failure. These values correspond to the KINSo1 returns (see §4.5.3 and §B.2). The values of the optional outputs are available in IOPT and ROPT (see Table 5.2).

7. Memory deallocation

To free the internal memory created by the call to FKINMALLOC, make the call

CALL FKINFREE

5.4 FKINSOL optional input and output

In order to keep the number of user-callable FKINSOL interface routines to a minimum, optional inputs to the KINSOL solver are passed through only two routines: FKINSETIIN for integer optional inputs and FKINSETRIN for real optional inputs. These functions should be called as follows:

```
CALL FKINSETIIN (KEY, IVAL, IER)
CALL FKINSETRIN (KEY, RVAL, IER)
```

where KEY is a quoted string indicating which optional input is set (see Table 5.1), IVAL is the integer input value to the used, RVAL is the real input value to be used, and IER is an integer return flag which is set to 0 on success and a negative value if a failure occurred.

The optional outputs from the KINSOL solver are accessed not through individual functions, but rather through a pair of arrays, IOUT (integer type) of dimension at least 15, and ROUT (real type) of

Integer optional inputs FKINSETIIN			
Key Optional input		Default value	
PRNT_LEVEL	Verbosity level of output	0	
MAX_NITER	Maximum no. of nonlinear iterations	200	
ETA_FORM	Form of η coefficient	1 (KIN_ETACHOICE1)	
MAX_SETUPS	Maximum no. of iterations without prec. setup	10	
MAX_SP_SETUPS	Maximum no. of iterations without residual check	5	
NO_INIT_SETUP	No initial preconditioner setup	FALSE	
NO_MIN_EPS	Lower bound on ϵ	FALSE	
NO_RES_MON	No residual monitoring	FALSE	

Table 5.1: Keys for setting FKINSOL optional inputs

Real optional inputs (FKINSETRIN)

Key	Optional input	Default value
FNORM_TOL	Function-norm stopping tolerance	$uround^{1/3}$
SSTEP_TOL	Scaled-step stopping tolerance	$uround^{2/3}$
MAX_STEP	Max. scaled length of Newton step	$ 1000 D_uu_0 _2$
RERR_FUNC	Relative error for F.D. Jv	$\sqrt{\text{uround}}$
ETA_CONST	Constant value of η	0.1
ETA_PARAMS	Values of γ and α	0.9 and 2.0
RMON_CONST	Constant value of ω	0.9
RMON_PARAMS	Values of ω_{min} and ω_{max}	0.00001 and 0.9

dimension at least 2. These arrays are owned (and allocated) by the user and are passed as arguments to FKINMALLOC. Table 5.2 lists the entries in these two arrays and specifies the optional variable as well as the KINSOL function which is actually called to extract the optional output.

For more details on the optional inputs and outputs, see §4.5.4 and §4.5.5.

5.5 Usage of the FKINBBD interface to KINBBDPRE

The FKINBBD interface sub-module is a package of C functions which, as part of the FKINSOL interface module, support the use of the KINSOL solver with the parallel NVECTOR_PARALLEL module and the KINBBDPRE preconditioner module (see §4.7), for the solution of nonlinear problems in a mixed FORTRAN/C setting.

The user-callable functions in this package, with the corresponding KINSOL and KINBBDPRE functions, are as follows:

- FKINBBDINIT interfaces to KINBBDPrecInit.
- FKINBBDOPT interfaces to KINBBDPRE optional output functions.

In addition to the FORTRAN right-hand side function FKFUN, the user-supplied functions used by this package, are listed below, each with the corresponding interface function which calls it (and its type within KINBBDPRE or KINSOL):

	FKINBBD routine	CVODE function	CVODE type of
(FORTRAN, user-supplied)		(C, interface)	interface function
-	FKLOCFN	FKINgloc	KINLocalFn
	FKCOMMF	FKINgcomm	KINCommFn
	FKJTIMES	FKINJtimes	KINSpilsJacTimesVecFn

As with the rest of the FKINSOL routines, the names of all user-supplied routines here are fixed, in order to maximize portability for the resulting mixed-language program. Additionally, based on flags

Table 5.2: Description of the FKINSOL optional output arrays IOUT and ROUT

Integer output array IOUT

Integer output array IOUT				
		KINSOL function		
KINSOL main solver				
1	LENRW	KINGetWorkSpace		
2	LENIW	KINGetWorkSpace		
3	NNI	KINGetNumNonlinSolvIters		
4	NFE	KINGetNumFuncEvals		
5	NBCF	KINGetNumBetaCondFails		
6	NBKTRK	KINGetNumBacktrackOps		
	KINDENSE, KINB	AND linear solver		
7	LENRWLS	KINDlsGetWorkSpace		
8	LENIWLS	KINDlsGetWorkSpace		
9 LS_FLAG KINDlsGet		KINDlsGetLastFlag		
10 NFELS KINDlsGetNumFuncEval		KINDlsGetNumFuncEvals		
11 NJE KINDlsGetNu		KINDlsGetNumJacEvals		
KIN	SPGMR, KINSPBCG, K	INSPTFQMR linear solvers		
7	LENRWLS	KINSpilsGetWorkSpace		
8	LENIWLS	KINSpilsGetWorkSpace		
9	LS_FLAG	KINSpilsGetLastFlag		
10	NFELS	KINSpilsGetNumFuncEvals		
11	NJTV	KINSpilsGetNumJacEvals		
12	NPE	KINSpilsGetNumPrecEvals		
13	NPS	KINSpilsGetNumPrecSolves		
14	NLI	KINSpilsGetNumLinIters		
15 NCFL KINSpilsGetNumConvFa		KINSpilsGetNumConvFails		

Real output array ${\tt ROUT}$

Index	Optional output	KINSOL function
1	FNORM	KINGetFuncNorm
2	SSTEP	KINGetStepLength

discussed above in §5.1, the names of the user-supplied routines are mapped to actual values through a series of definitions in the header file fkinbbd.h.

The following is a summary of the usage of this module. Steps that are unchanged from the main program described in §5.3 are grayed-out.

- 1. Nonlinear system function specification
- 2. NVECTOR module initialization
- 3. Problem specification
- 4. Set optional inputs

5. Linear solver specification

First, specify one of the KINSPILS iterative linear solvers, by calling one of FKINSPGMR, FKINSPBCG, or FKINSPTFQMR.

To initialize the KINBBDPRE preconditioner, make the following call:

```
CALL FKINBBDINIT (NLOCAL, MUDQ, MLDQ, MU, ML, IER)
```

The arguments are as follows. NLOCAL is the local size of vectors for this process. MUDQ and MLDQ are the upper and lower half-bandwidths to be used in the computation of the local Jacobian blocks by difference quotients; these may be smaller than the true half-bandwidths of the Jacobian of the local block of G, when smaller values may provide greater efficiency. MU and ML are the upper and lower half-bandwidths of the band matrix that is retained as an approximation of the local Jacobian block; these may be smaller than MUDQ and MLDQ. IER is a return completion flag. A value of 0 indicates success, while a value of -1 indicates that a memory failure occurred or that an input had an illegal value.

Optionally, to specify that SPGMR, SPBCG, or SPTFQMR should use the supplied FKJTIMES, make the call

```
CALL FKINSPILSSETJAC (FLAG, IER)
```

with FLAG $\neq 0$. (See step 5 in §5.3).

6. Problem solution

7. KINBBDPRE Optional outputs

Optional outputs specific to the SPGMR, SPBCG, or SPTFQMR solver are listed in Table 5.2. To obtain the optional outputs associated with the KINBBDPRE module, make the following call:

```
CALL FKINBBDOPT (LENRBBD, LENIBBD, NGEBBD)
```

The arguments returned are as follows. LENRBBD is the length of real preconditioner work space, in realtype words. LENIBBD is the length of integer preconditioner work space, in integer words. These sizes are local to the current process. NGEBBD is the cumulative number of G(u) evaluations (calls to FKLOCFN) so far.

8. Memory deallocation

(The memory allocated for the FKINBBD module is deallocated automatically by FKINFREE.)

9. User-supplied routines

The following two routines must be supplied for use with the KINBBDPRE module:

SUBROUTINE FKLOCFN (NLOC, ULOC, GLOC, IER)
DIMENSION ULOC(*), GLOC(*)

This routine is to evaluate the function G(u) approximating F (possibly identical to F), in terms of the array ULOC (of length NLOC), which is the sub-vector of u local to this processor. The resulting (local) sub-vector is to be stored in the array GLOC. IER is an error return flag which should be set to 0 if successful, a positive value if a recoverable error occurred (in which case KINSOL will attempt to correct), or a negative value if FKLOCFN failed unrecoverably (in which case the solution process is halted).

SUBROUTINE FKCOMMFN (NLOC, ULOC, IER) DIMENSION ULOC(*)

This routine is to perform the inter-processor communication necessary for the FKLOCFN routine. Each call to FKCOMMFN is preceded by a call to the system function routine FKFUN with the same argument ULOC. IER is an error return flag which should be set to 0 if successful, a positive value if a recoverable error occurred (in which case KINSOL will attempt to correct), or a negative value if FKCOMMFN failed recoverably (in which case the solution process is halted).

The subroutine FKCOMMFN must be supplied even if it is not needed and must return IER = 0.

Optionally, the user can supply a routine FKINJTIMES for the evaluation of Jacobian-vector products, as described above in step 5 in §5.3.



Chapter 6

Description of the NVECTOR module

The SUNDIALS solvers are written in a data-independent manner. They all operate on generic vectors (of type N_Vector) through a set of operations defined by the particular NVECTOR implementation. Users can provide their own specific implementation of the NVECTOR module or use one of two provided within SUNDIALS, a serial and an MPI parallel implementations.

The generic N_Vector type is a pointer to a structure that has an implementation-dependent content field containing the description and actual data of the vector, and an ops field pointing to a structure with generic vector operations. The type N_Vector is defined as

```
typedef struct _generic_N_Vector *N_Vector;
struct _generic_N_Vector {
    void *content;
    struct _generic_N_Vector_Ops *ops;
};
```

The _generic_N_Vector_Ops structure is essentially a list of pointers to the various actual vector operations, and is defined as

```
struct _generic_N_Vector_Ops {
  N_Vector
              (*nvclone)(N_Vector);
              (*nvcloneempty)(N_Vector);
  N_Vector
  void
              (*nvdestroy)(N_Vector);
              (*nvspace)(N_Vector, long int *, long int *);
  void
              (*nvgetarraypointer)(N_Vector);
  realtype*
              (*nvsetarraypointer)(realtype *, N_Vector);
  void
  void
              (*nvlinearsum)(realtype, N_Vector, realtype, N_Vector, N_Vector);
              (*nvconst)(realtype, N_Vector);
  void
              (*nvprod)(N_Vector, N_Vector, N_Vector);
  void
              (*nvdiv)(N_Vector, N_Vector, N_Vector);
  void
  void
              (*nvscale)(realtype, N_Vector, N_Vector);
              (*nvabs)(N_Vector, N_Vector);
  void
              (*nvinv)(N_Vector, N_Vector);
  void
  void
              (*nvaddconst)(N_Vector, realtype, N_Vector);
              (*nvdotprod)(N_Vector, N_Vector);
  realtype
  realtype
              (*nvmaxnorm)(N_Vector);
              (*nvwrmsnorm)(N_Vector, N_Vector);
  realtype
  realtype
              (*nvwrmsnormmask)(N_Vector, N_Vector, N_Vector);
  realtype
              (*nvmin)(N_Vector);
```

```
realtype (*nvwl2norm)(N_Vector, N_Vector);
realtype (*nvl1norm)(N_Vector);
void (*nvcompare)(realtype, N_Vector, N_Vector);
booleantype (*nvinvtest)(N_Vector, N_Vector);
booleantype (*nvconstrmask)(N_Vector, N_Vector, N_Vector);
realtype (*nvminquotient)(N_Vector, N_Vector);
};
```

The generic NVECTOR module defines and implements the vector operations acting on N_Vector. These routines are nothing but wrappers for the vector operations defined by a particular NVECTOR implementation, which are accessed through the *ops* field of the N_Vector structure. To illustrate this point we show below the implementation of a typical vector operation from the generic NVECTOR module, namely N_VScale, which performs the scaling of a vector x by a scalar c:

```
void N_VScale(realtype c, N_Vector x, N_Vector z)
{
   z->ops->nvscale(c, x, z);
}
```

Table 6.1 contains a complete list of all vector operations defined by the generic NVECTOR module.

Finally, note that the generic NVECTOR module defines the functions N_VCloneVectorArray and N_VCloneEmptyVectorArray. Both functions create (by cloning) an array of count variables of type N_Vector, each of the same type as an existing N_Vector. Their prototypes are

```
N_Vector *N_VCloneVectorArray(int count, N_Vector w);
N_Vector *N_VCloneEmptyVectorArray(int count, N_Vector w);
```

and their definitions are based on the implementation-specific N_VClone and $N_VCloneEmpty$ operations, respectively.

An array of variables of type N_Vector can be destroyed by calling N_VDestroyVectorArray, whose prototype is

```
void N_VDestroyVectorArray(N_Vector *vs, int count);
```

and whose definition is based on the implementation-specific N_VDestroy operation.

A particular implementation of the NVECTOR module must:

- Specify the *content* field of N_Vector.
- Define and implement the vector operations. Note that the names of these routines should be unique to that implementation in order to permit using more than one NVECTOR module (each with different N_Vector internal data representations) in the same code.
- Define and implement user-callable constructor and destructor routines to create and free an N_Vector with the new *content* field and with *ops* pointing to the new vector operations.
- Optionally, define and implement additional user-callable routines acting on the newly defined N_Vector (e.g., a routine to print the content for debugging purposes).
- Optionally, provide accessor macros as needed for that particular implementation to be used to access different parts in the *content* field of the newly defined N_Vector.

Table 6.1: Description of the NVECTOR operations

Name	Usage and Description
N_VClone	<pre>v = N_VClone(w); Creates a new N_Vector of the same type as an existing vector w and sets the ops field. It does not copy the vector, but rather allocates storage for the new vector.</pre>
N_VCloneEmpty	v = N_VCloneEmpty(w); Creates a new N_Vector of the same type as an existing vector w and sets the <i>ops</i> field. It does not allocate storage for the data array.
N_VDestroy	N_VDestroy(v); Destroys the N_Vector v and frees memory allocated for its internal data.
N_VSpace	N_VSpace(nvSpec, &lrw, &liw); Returns storage requirements for one N_Vector. lrw contains the number of realtype words and liw contains the number of integer words.
N_VGetArrayPointer	<pre>vdata = N_VGetArrayPointer(v); Returns a pointer to a realtype array from the N_Vector v. Note that this assumes that the internal data in N_Vector is a contiguous array of realtype. This routine is only used in the solver-specific interfaces to the dense and banded linear solvers, as well as the interfaces to the banded preconditioners provided with SUNDIALS.</pre>
N_VSetArrayPointer	N_VSetArrayPointer(vdata, v); Overwrites the data in an N_Vector with a given array of realtype. Note that this assumes that the internal data in N_Vector is a contiguous array of realtype. This routine is only used in the interfaces to the dense linear solver.
N_VLinearSum	N_VLinearSum(a, x, b, y, z); Performs the operation $z = ax + by$, where a and b are scalars and x and y are of type N_Vector: $z_i = ax_i + by_i$, $i = 0, \ldots, n-1$.
$N_{-}VConst$	N_VConst(c, z); Sets all components of the N_Vector z to c: $z_i=c,\ i=0,\dots,n-1.$
N_VProd	N_VProd(x, y, z); Sets the N_Vector z to be the component-wise product of the N_Vector inputs x and y: $z_i = x_i y_i$, $i = 0, \ldots, n-1$.
N_VDiv	N_VDiv(x, y, z); Sets the N_Vector z to be the component-wise ratio of the N_Vector inputs x and y: $z_i = x_i/y_i$, $i = 0, \ldots, n-1$. The y_i may not be tested for 0 values. It should only be called with a y that is guaranteed to have all nonzero components.
	continued on next page

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Name	Usage and Description
N_VScale	N_VScale(c, x, z); Scales the N_Vector x by the scalar c and returns the result in z: $z_i = cx_i$, $i = 0,, n-1$.
N_VAbs	N_VAbs(x, z); Sets the components of the N_Vector z to be the absolute values of the components of the N_Vector x: $y_i = x_i , i = 0, \ldots, n-1$.
N_VInv	N_VInv(x, z); Sets the components of the N_Vector z to be the inverses of the components of the N_Vector x: $z_i = 1.0/x_i$, $i = 0, \ldots, n-1$. This routine may not check for division by 0. It should be called only with an x which is guaranteed to have all nonzero components.
N_VAddConst	N_VAddConst(x, b, z); Adds the scalar b to all components of x and returns the result in the N_Vector z: $z_i = x_i + b, i = 0, \ldots, n-1$.
N_VDotProd	d = N_VDotProd(x, y); Returns the value of the ordinary dot product of x and y: $d = \sum_{i=0}^{n-1} x_i y_i$.
N_VMaxNorm	m = N_VMaxNorm(x); Returns the maximum norm of the N_Vector x: $m = \max_i x_i $.
N_VWrmsNorm	m = N_VWrmsNorm(x, w) Returns the weighted root-mean-square norm of the N_Vector x with weight vector w: $m = \sqrt{\left(\sum_{i=0}^{n-1} (x_i w_i)^2\right)/n}$.
N_VWrmsNormMask	m = N_VWrmsNormMask(x, w, id); Returns the weighted root mean square norm of the N_Vector x with weight vector w built using only the elements of x corresponding to nonzero elements of the N_Vector id:
N_VMin	$m = \sqrt{\left(\sum_{i=0}^{n-1} (x_i w_i \operatorname{sign}(id_i))^2\right)/n}.$ $m = \text{N_VMin(x)};$ Returns the smallest element of the N_Vector x: $m = \min_i x_i$.
N_VWL2Norm	m = N_VWL2Norm(x, w); Returns the weighted Euclidean ℓ_2 norm of the N_Vector x with weight vector w: $m = \sqrt{\sum_{i=0}^{n-1} (x_i w_i)^2}$.
N_VL1Norm	m = N_VL1Norm(x); Returns the ℓ_1 norm of the N_Vector x: $m = \sum_{i=0}^{n-1} x_i $.
N_VCompare	N_VCompare(c, x, z); Compares the components of the N_Vector x to the scalar c and returns an N_Vector z such that: $z_i = 1.0$ if $ x_i \ge c$ and $z_i = 0.0$ otherwise.
	continued on next page

continued from last page				
Name	Usage and Description			
N_VInvTest	t = N_VInvTest(x, z); Sets the components of the N_Vector z to be the inverses of the components of the N_Vector x, with prior testing for zero values: $z_i = 1.0/x_i, i = 0, \ldots, n-1$. This routine returns TRUE if all components of x are nonzero (successful inversion) and returns FALSE otherwise.			
N_VConstrMask	t = N_VConstrMask(c, x, m); Performs the following constraint tests: $x_i > 0$ if $c_i = 2$, $x_i \geq 0$ if $c_i = 1$, $x_i \leq 0$ if $c_i = -1$, $x_i < 0$ if $c_i = -2$. There is no constraint on x_i if $c_i = 0$. This routine returns FALSE if any element failed the constraint test, TRUE if all passed. It also sets a mask vector m, with elements equal to 1.0 where the constraint test failed, and 0.0 where the test passed. This routine is used only for constraint checking.			
${ t N_{ m L}VMinQuotient}$	minq = N_VMinQuotient(num, denom); This routine returns the minimum of the quotients obtained by termwise dividing num _i by denom _i . A zero element in denom will be skipped. If no such quotients are found, then the large value BIG_REAL (defined in the header file sundials_types.h) is returned.			

6.1 The NVECTOR_SERIAL implementation

The serial implementation of the NVECTOR module provided with SUNDIALS, NVECTOR_SERIAL, defines the *content* field of N_Vector to be a structure containing the length of the vector, a pointer to the beginning of a contiguous data array, and a boolean flag *own_data* which specifies the ownership of *data*.

```
struct _N_VectorContent_Serial {
  long int length;
  booleantype own_data;
  realtype *data;
};
```

The following five macros are provided to access the content of an NVECTOR_SERIAL vector. The suffix _S in the names denotes serial version.

• NV_CONTENT_S

This routine gives access to the contents of the serial vector N_Vector.

The assignment $v_cont = NV_CONTENT_S(v)$ sets v_cont to be a pointer to the serial N_Vector content structure.

Implementation:

```
#define NV_CONTENT_S(v) ( (N_VectorContent_Serial)(v->content) )
```

• NV_OWN_DATA_S, NV_DATA_S, NV_LENGTH_S

These macros give individual access to the parts of the content of a serial N_Vector.

The assignment $v_{data} = NV_DATA_S(v)$ sets v_{data} to be a pointer to the first component of the data for the $N_Vector v$. The assignment $NV_DATA_S(v) = v_{data}$ sets the component array of v to be v_{data} by storing the pointer v_{data} .

The assignment $v_len = NV_LENGTH_S(v)$ sets v_len to be the length of v. On the other hand, the call $NV_LENGTH_S(v) = len_v$ sets the length of v to be len_v .

Implementation:

```
#define NV_OWN_DATA_S(v) ( NV_CONTENT_S(v)->own_data )
#define NV_DATA_S(v) ( NV_CONTENT_S(v)->data )
#define NV_LENGTH_S(v) ( NV_CONTENT_S(v)->length )
```

• NV Ith S

This macro gives access to the individual components of the data array of an N_Vector.

The assignment $r = NV_{i,i}$ sets r to be the value of the i-th component of v. The assignment $NV_{i,i} = r$ sets the value of the i-th component of v to be r.

Here i ranges from 0 to n-1 for a vector of length n.

Implementation:

```
#define NV_Ith_S(v,i) ( NV_DATA_S(v)[i] )
```

The NVECTOR_SERIAL module defines serial implementations of all vector operations listed in Table 6.1. Their names are obtained from those in Table 6.1 by appending the suffix _Serial. The module NVECTOR_SERIAL provides the following additional user-callable routines:

• N_VNew_Serial

This function creates and allocates memory for a serial N_Vector . Its only argument is the vector length.

```
N_Vector N_VNew_Serial(long int vec_length);
```

• N_VNewEmpty_Serial

This function creates a new serial N_Vector with an empty (NULL) data array.

```
N_Vector N_VNewEmpty_Serial(long int vec_length);
```

• N_VMake_Serial

This function creates and allocates memory for a serial vector with user-provided data array.

```
N_Vector N_VMake_Serial(long int vec_length, realtype *v_data);
```

• N_VCloneVectorArray_Serial

This function creates (by cloning) an array of count serial vectors.

```
N_Vector *N_VCloneVectorArray_Serial(int count, N_Vector w);
```

• N_VCloneEmptyVectorArray_Serial

This function creates (by cloning) an array of count serial vectors, each with an empty (NULL) data array.

```
N_Vector *N_VCloneEmptyVectorArray_Serial(int count, N_Vector w);
```

• N_VDestroyVectorArray_Serial

This function frees memory allocated for the array of count variables of type N_Vector created with N_VCloneVectorArray_Serial or with N_VCloneEmptyVectorArray_Serial.

```
void N_VDestroyVectorArray_Serial(N_Vector *vs, int count);
```

• N_VPrint_Serial

This function prints the content of a serial vector to stdout.

```
void N_VPrint_Serial(N_Vector v);
```

Notes

- When looping over the components of an N_Vector v, it is more efficient to first obtain the component array via v_data = NV_DATA_S(v) and then access v_data[i] within the loop than it is to use NV_Ith_S(v,i) within the loop.
- N_VNewEmpty_Serial, N_VMake_Serial, and N_VCloneEmptyVectorArray_Serial set the field $own_data = FALSE$. N_VDestroy_Serial and N_VDestroyVectorArray_Serial will not attempt to free the pointer data for any N_Vector with own_data set to FALSE. In such a case, it is the user's responsibility to deallocate the data pointer.
- To maximize efficiency, vector operations in the NVECTOR_SERIAL implementation that have more than one N_Vector argument do not check for consistent internal representation of these vectors. It is the user's responsibility to ensure that such routines are called with N_Vector arguments that were all created with the same internal representations.





6.2 The NVECTOR_PARALLEL implementation

The parallel implementation of the NVECTOR module provided with SUNDIALS, NVECTOR_PARALLEL, defines the *content* field of N_Vector to be a structure containing the global and local lengths of the vector, a pointer to the beginning of a contiguous local data array, an MPI communicator, an a boolean flag own_data indicating ownership of the data array data.

```
struct _N_VectorContent_Parallel {
  long int local_length;
  long int global_length;
  booleantype own_data;
  realtype *data;
  MPI_Comm comm;
};
```

The following seven macros are provided to access the content of a NVECTOR_PARALLEL vector. The suffix _P in the names denotes parallel version.

• NV_CONTENT_P

This macro gives access to the contents of the parallel vector N_Vector.

The assignment $v_cont = NV_CONTENT_P(v)$ sets v_cont to be a pointer to the N_Vector content structure of type struct $_N_VectorParallelContent$.

Implementation:

```
#define NV_CONTENT_P(v) ( (N_VectorContent_Parallel)(v->content) )
```

• NV_OWN_DATA_P, NV_DATA_P, NV_LOCLENGTH_P, NV_GLOBLENGTH_P

These macros give individual access to the parts of the content of a parallel N_Vector.

The assignment $v_{data} = NV_DATA_P(v)$ sets v_{data} to be a pointer to the first component of the local data for the $N_Vector\ v$. The assignment $NV_DATA_P(v) = v_{data}$ sets the component array of v to be v_{data} by storing the pointer v_{data} .

The assignment v_llen = NV_LOCLENGTH_P(v) sets v_llen to be the length of the local part of v. The call NV_LENGTH_P(v) = llen_v sets the local length of v to be llen_v.

The assignment $v_glen = NV_GLOBLENGTH_P(v)$ sets v_glen to be the global length of the vector v. The call $NV_GLOBLENGTH_P(v) = glen_v$ sets the global length of v to be $glen_v$.

Implementation:

```
#define NV_OWN_DATA_P(v) ( NV_CONTENT_P(v)->own_data )
#define NV_DATA_P(v) ( NV_CONTENT_P(v)->data )
```

```
#define NV_LOCLENGTH_P(v) ( NV_CONTENT_P(v)->local_length )
#define NV_GLOBLENGTH_P(v) ( NV_CONTENT_P(v)->global_length )
```

• NV_COMM_P

This macro provides access to the MPI communicator used by the NVECTOR_PARALLEL vectors. Implementation:

```
#define NV_COMM_P(v) ( NV_CONTENT_P(v)->comm )
```

• NV_Ith_P

This macro gives access to the individual components of the local data array of an N-Vector.

The assignment $r = NV_i(v,i)$ sets r to be the value of the i-th component of the local part of v. The assignment $NV_i(v,i) = r$ sets the value of the i-th component of the local part of v to be r.

Here i ranges from 0 to n-1, where n is the local length.

Implementation:

```
#define NV_Ith_P(v,i) ( NV_DATA_P(v)[i] )
```

The NVECTOR_PARALLEL module defines parallel implementations of all vector operations listed in Table 6.1 Their names are obtained from those in Table 6.1 by appending the suffix _Parallel. The module NVECTOR_PARALLEL provides the following additional user-callable routines:

• N_VNew_Parallel

This function creates and allocates memory for a parallel vector.

• N_VNewEmpty_Parallel

This function creates a new parallel N_Vector with an empty (NULL) data array.

• N_VMake_Parallel

This function creates and allocates memory for a parallel vector with user-provided data array.

• N_VCloneVectorArray_Parallel

This function creates (by cloning) an array of count parallel vectors.

```
N_Vector *N_VCloneVectorArray_Parallel(int count, N_Vector w);
```

• N_VCloneEmptyVectorArray_Parallel

This function creates (by cloning) an array of count parallel vectors, each with an empty (NULL) data array.

N_Vector *N_VCloneEmptyVectorArray_Parallel(int count, N_Vector w);

• N_VDestroyVectorArray_Parallel

This function frees memory allocated for the array of count variables of type N_Vector created with N_VCloneVectorArray_Parallel or with N_VCloneEmptyVectorArray_Parallel.

void N_VDestroyVectorArray_Parallel(N_Vector *vs, int count);

• N_VPrint_Parallel

This function prints the content of a parallel vector to stdout. void N_VPrint_Parallel(N_Vector v);

Notes

- When looping over the components of an N_Vector v, it is more efficient to first obtain the local component array via v_data = NV_DATA_P(v) and then access v_data[i] within the loop than it is to use NV_Ith_P(v,i) within the loop.
- N_VNewEmpty_Parallel, N_VMake_Parallel, and N_VCloneEmptyVectorArray_Parallel set the field own_data = FALSE. N_VDestroy_Parallel and N_VDestroyVectorArray_Parallel will not attempt to free the pointer data for any N_Vector with own_data set to FALSE. In such a case, it is the user's responsibility to deallocate the data pointer.
- To maximize efficiency, vector operations in the NVECTOR_PARALLEL implementation that have more than one N_Vector argument do not check for consistent internal representation of these vectors. It is the user's responsibility to ensure that such routines are called with N_Vector arguments that were all created with the same internal representations.

6.3 NVECTOR functions used by KINSOL

In Table 6.2 below, we list the vector functions in the NVECTOR module within the KINSOL package. The table also shows, for each function, which of the code modules uses the function. The KINSOL column shows function usage within the main solver module, while the remaining five columns show function usage within each of the four KINSOL linear solvers (KINSPILS stands for any of KINSPGMR, KINSPBCG, or KINSPTFQMR), the KINBBDPRE preconditioner module, and the FKINSOL module.

There is one subtlety in the KINSPILS column hidden by the table, explained here for the case of the KINSPGMR module. The N_VDotProd function is called both within the interface file kinsol_spgmr.c and within the implementation files sundials_spgmr.c and sundials_iterative.c for the generic SPGMR solver upon which the KINSPGMR solver is built. Also, although N_VDiv and N_VProd are not called within the interface file kinsol_spgmr.c, they are called within the implementation file sundials_spgmr.c, and so are required by the KINSPGMR solver module. Analogous statements apply to the KINSPBCG and KINSPTFQMR modules, except that they do not use sundials_iterative.c. This issue does not arise for the direct KINSOL linear solvers because the generic DENSE and BAND solvers (used in the implementation of KINDENSE and KINBAND) do not make calls to any vector functions.

At this point, we should emphasize that the KINSOL user does not need to know anything about the usage of vector functions by the KINSOL code modules in order to use KINSOL. The information is presented as an implementation detail for the interested reader.

The vector functions listed in Table 6.1 that are *not* used by KINSOL are: N_VAddConst, N_VWrmsNorm, N_VWrmsNormMask, N_VCompare, and N_VInvTest. Therefore a user-supplied NVECTOR module for KINSOL could omit these five functions.





Table 6.2: List of vector functions usage by KINSOL code modules

	KINSOL	KINDENSE	KINBAND	KINSPILS	KINBBDPRE	FKINSOL
N_VClone	√			√	√	
$N_{VCloneEmpty}$						√
$N_{-}VDestroy$	√			√	√	√
N_VSpace	√					
N_VGetArrayPointer		√	√		√	√
N_VSetArrayPointer		√				√
$N_{-}VLinearSum$	√	√		√		
$N_{-}VConst$				✓		
N_VProd	√	√	√	√		
$N_{-}VDiv$	√			✓		
N_VScale	√	✓	✓	✓	√	
$N_{-}VAbs$	√					
$N_{-}VInv$	✓					
N_VDotProd		√	√	√		
N_VMaxNorm	√					
N_VMin	√					
N_VWL2Norm	√	√	√	√		
N_VL1Norm				√		
N_VConstrMask	√					
$N_VMinQuotient$	√					

Chapter 7

Providing Alternate Linear Solver Modules

The central KINSOL module interfaces with the linear solver module to be used by way of calls to four routines. These are denoted here by linit, lsetup, lsolve, and lfree. Briefly, their purposes are as follows:

- linit: initialize and allocate memory specific to the linear solver;
- lsetup: evaluate and preprocess the Jacobian or preconditioner;
- lsolve: solve the linear system;
- lfree: free the linear solver memory.

A linear solver module must also provide a user-callable specification routine (like that described in §4.5.2) which will attach the above four routines to the main KINSOL memory block. The KINSOL memory block is a structure defined in the header file kinsol_impl.h. A pointer to such a structure is defined as the type KINMem. The four fields in a KINMem structure that must point to the linear solver's functions are kin_linit, kin_lsetup, kin_lsolve, and kin_lfree, respectively. Note that of the four interface routines, only the lsolve routine is required. The lfree routine must be provided only if the solver specification routine makes any memory allocation. For consistency with the existing KINSOL linear solver modules, we recommend that the return value of the specification function be 0 for a successful return or a negative value if an error occurs (the pointer to the main KINSOL memory block is NULL, an input is illegal, the NVECTOR implementation is not compatible, a memory allocation fails, etc.)

To facilitate data exchange between the four interface functions, the field kin_lmem in the KINSOL memory block can be used to attach a linear solver-specific memory block.

These four routines, which interface between KINSOL and the linear solver module, necessarily have fixed call sequences. Thus, a user wishing to implement another linear solver within the KINSOL package must adhere to this set of interfaces. The following is a complete description of the call list for each of these routines. Note that the call list of each routine includes a pointer to the main KINSOL memory block, by which the routine can access various data related to the KINSOL solution. The contents of this memory block are given in the file kinsol_impl.h (but not reproduced here, for the sake of space).

7.1 Initialization function

linit

Definition int (*linit)(KINMem kin_mem);

Purpose The purpose of limit is to complete initializations for a specific linear solver, such as

counters and statistics.

Arguments kin_mem is the KINSOL memory pointer of type KINMem.

Return value An linit function should return 0 if it has successfully initialized the KINSOL linear

solver and -1 otherwise.

7.2 Setup function

The type definition of lsetup is

lsetup

Definition int (*lsetup)(KINMem kin_mem);

Purpose The job of 1setup is to prepare the linear solver for subsequent calls to 1solve. It may

recompute Jacobian-related data if it deems necessary.

Arguments kin_mem is the KINSOL memory pointer of type KINMem.

Return value The 1setup routine should return 0 if successful and a non-zero value otherwise.

7.3 Solve function

The type definition of lsolve is

lsolve

Definition int (*lsolve)(KINMem kin_mem, N_Vector x,

N_Vector b, realtype *res_norm);

Purpose The routine 1solve must solve the linear equation Jx = b, where $J = \partial F/\partial u$ is

evaluated at the current iterate and the right-hand side vector b is input.

Arguments kin_mem is the KINSOL memory pointer of type KINMem.

x is a vector set to an initial guess prior to calling lsolve. On return it should

contain the solution to Jx = b.

b is the right-hand side vector b, set to -F(u), evaluated at the current iterate.

res_norm holds the value of the L_2 norm of the residual vector upon return.

Return value lsolve should return 0 if successful. If an error occurs and recovery could be possible

by calling again the lsetup function, then it should return a positive value. Otherwise,

lsolve should return a negative value.

7.4 Memory deallocation function

The type definition of lfree is

lfree

Definition void (*lfree)(KINMem kin_mem);

Purpose The routine lfree should free any linear solver memory allocated by the linit routine.

Arguments kin_mem is the KINSOL memory pointer of type KINMem.

Return value This routine has no return value.

 ${\bf Notes}$

This routine is called once a problem has been completed and the linear solver is no longer needed.

Chapter 8

Generic Linear Solvers in SUNDIALS

In this chapter, we describe five generic linear solver code modules that are included in SUNDIALS, but which are of potential use as generic packages in themselves, either in conjunction with the use of KINSOL or separately.

These generic linear solver modules in SUNDIALS are organized in two families of solvers, the *dls* family, which includes direct linear solvers appropriate for sequential computations; and the *spils* family, which includes scaled preconditioned iterative (Krylov) linear solvers. The solvers in each family share common data structures and functions.

The dls family contains the following two generic linear solvers:

- The DENSE package, a linear solver for dense matrices either specified through a matrix type (defined below) or as simple arrays.
- The BAND package, a linear solver for banded matrices either specified through a matrix type (defined below) or as simple arrays.

Note that this family also includes the Blas/Lapack linear solvers (dense and band) available to the SUNDIALS solvers, but these are not discussed here.

The spils family contains the following three generic linear solvers:

- The SPGMR package, a solver for the scaled preconditioned GMRES method.
- The SPBCG package, a solver for the scaled preconditioned Bi-CGStab method.
- The SPTFQMR package, a solver for the scaled preconditioned TFQMR method.

For reasons related to installation, the names of the files involved in these generic solvers begin with the prefix sundials. But despite this, each of the solvers is in fact generic, in that it is usable completely independently of SUNDIALS.

For the sake of space, the functions for the dense and band modules that work with a matrix type and the functions in the SPGMR, SPBCG, and SPTFQMR modules are only summarized briefly, since they are less likely to be of direct use in connection with a SUNDIALS solver. However, the functions for dense matrices treated as simple arrays are fully described, because we expect that they will be useful in the implementation of preconditioners used with the combination of one of the SUNDIALS solvers and one of the spils linear solvers.

8.1 The DLS modules: DENSE and BAND

The files comprising the DENSE generic linear solver, and their locations in the SUNDIALS srcdir, are as follows:

- header files (located in srcdir/include/sundials) sundials_direct.h sundials_dense.h sundials_types.h sundials_math.h sundials_config.h
- source files (located in *srcdir*/src/sundials) sundials_direct.c sundials_dense.c sundials_math.c

The files comprising the BAND generic linear solver are as follows:

- header files (located in srcdir/include/sundials) sundials_direct.h sundials_band.h sundials_types.h sundials_math.h sundials_config.h
- source files (located in *srcdir*/src/sundials) sundials_direct.c sundials_band.c sundials_math.c

Only two of the preprocessing directives in the header file sundials_config.h are relevant to the DENSE and BAND packages by themselves (see §A.3 for details):

• (required) definition of the precision of the SUNDIALS type realtype. One of the following lines must be present:

```
#define SUNDIALS_DOUBLE_PRECISION 1
#define SUNDIALS_SINGLE_PRECISION 1
#define SUNDIALS_EXTENDED_PRECISION 1
```

• (optional) use of generic math functions: #define SUNDIALS_USE_GENERIC_MATH 1

The sundials_types.h header file defines the SUNDIALS realtype and booleantype types and the macro RCONST, while the sundials_math.h header file is needed for the MIN, MAX, and ABS macros and RAbs function.

The files listed above for either module can be extracted from the SUNDIALS *srcdir* and compiled by themselves into a separate library or into a larger user code.

8.1.1 Type DlsMat

The type DlsMat, defined in sundials_direct.h is a pointer to a structure defining a generic matrix, and is used with all linear solvers in the *dls* family:

```
typedef struct _DlsMat {
  int type;
  int M;
  int N;
  int ldim;
  int mu;
  int s_mu;
  realtype *data;
  int ldata;
  realtype **cols;
} *DlsMat;
```

For the DENSE module, the relevant fields of this structure are as follows. Note that a dense matrix of type DlsMat need not be square.

```
 \begin{aligned} \mathbf{type} &\text{ - SUNDIALS\_DENSE } (=1) \\ \mathbf{M} &\text{ - number of rows} \end{aligned}
```

N - number of columns

```
ldim - leading dimension (ldim \ge M)
```

data - pointer to a contiguous block of realtype variables

ldata - length of the data array (= ldim·N). The (i,j)-th element of a dense matrix A of type DlsMat (with $0 \le i < M$ and $0 \le j < N$) is given by the expression (A->data)[0][j*M+i]

cols - array of pointers. cols[j] points to the first element of the j-th column of the matrix in the array data. The (i,j)-th element of a dense matrix A of type DlsMat (with $0 \le i < M$ and $0 \le j < N$) is given by the expression (A->cols)[j][i]

For the BAND module, the relevant fields of this structure are as follows (see Figure 8.1 for a diagram of the underlying data representation in a banded matrix of type DlsMat). Note that only square band matrices are allowed.

```
\mathbf{type} - SUNDIALS_BAND (=2)
```

M - number of rows

N - number of columns (N = M)

 \mathbf{mu} - upper half-bandwidth, $0 \le \mathbf{mu} < \min(\mathbf{M}, \mathbf{N})$

 \mathbf{ml} - lower half-bandwidth, $0 \leq \mathtt{ml} < \min(\mathtt{M}, \mathtt{N})$

 s_mu - storage upper bandwidth, $mu \le s_mu < N$. The LU decomposition routine writes the LU factors into the storage for A. The upper triangular factor U, however, may have an upper bandwidth as big as min(N-1,mu+ml) because of partial pivoting. The s_mu field holds the upper half-bandwidth allocated for A.

```
ldim - leading dimension (ldim ≥ s_mu)
```

data - pointer to a contiguous block of realtype variables. The elements of a banded matrix of type DlsMat are stored columnwise (i.e. columns are stored one on top of the other in memory). Only elements within the specified half-bandwidths are stored. data is a pointer to ldata contiguous locations which hold the elements within the band of A.

```
ldata - length of the data array (= ldim·(s_mu+ml+1)
```

cols - array of pointers. cols[j] is a pointer to the uppermost element within the band in the j-th column. This pointer may be treated as an array indexed from s_mu-mu (to access the uppermost element within the band in the j-th column) to s_mu+ml (to access the lowest element within the band in the j-th column). Indices from 0 to $s_mu-mu-1$ give access to extra storage elements required by the LU decomposition function. Finally, $cols[j][i-j+s_mu]$ is the (i,j)-th element, $j-mu \le i \le j+ml$.

8.1.2 Accessor macros for the DLS modules

The macros below allow a user to efficiently access individual matrix elements without writing out explicit data structure references and without knowing too much about the underlying element storage. The only storage assumption needed is that elements are stored columnwise and that a pointer to the j-th column of elements can be obtained via the DENSE_COL or BAND_COL macros. Users should use these macros whenever possible.

The following two macros are defined by the DENSE module to provide access to data in the DlsMat type:

• DENSE_ELEM

```
Usage: DENSE_ELEM(A,i,j) = a_ij; or a_ij = DENSE_ELEM(A,i,j); DENSE_ELEM references the (i,j)-th element of the M \times N DlsMat A, 0 \le i < M, 0 \le j < N.
```

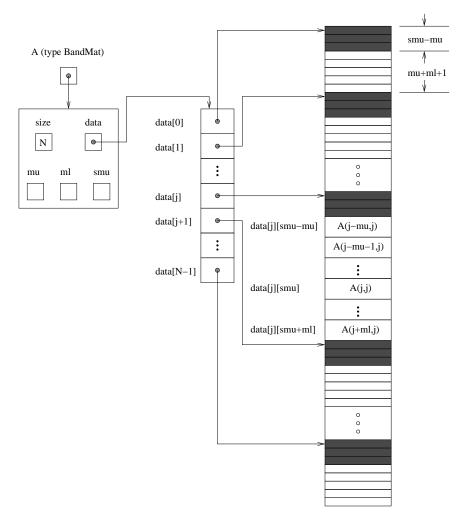


Figure 8.1: Diagram of the storage for a banded matrix of type DlsMat. Here A is an $N \times N$ band matrix of type DlsMat with upper and lower half-bandwidths mu and ml, respectively. The rows and columns of A are numbered from 0 to N-1 and the (i,j)-th element of A is denoted A(i,j). The greyed out areas of the underlying component storage are used by the BandGBTRF and BandGBTRS routines.

• DENSE_COL

```
Usage : col_j = DENSE_COL(A,j);
```

DENSE_COL references the j-th column of the $M \times N$ DlsMat A, $0 \le j < N$. The type of the expression DENSE_COL(A,j) is realtype * . After the assignment in the usage above, col_j may be treated as an array indexed from 0 to M-1. The (i, j)-th element of A is referenced by col_j[i].

The following three macros are defined by the BAND module to provide access to data in the DlsMat type:

• BAND_ELEM

```
Usage : BAND_ELEM(A,i,j) = a_ij; or a_ij = BAND_ELEM(A,i,j); 
BAND_ELEM references the (i,j)-th element of the N \times N band matrix A, where 0 \le i, j \le N-1. The location (i,j) should further satisfy j-(A->mu) \le i \le j+(A->m1).
```

• BAND_COL

```
Usage : col_j = BAND_COL(A,j);
```

BAND_COL references the diagonal element of the j-th column of the $N \times N$ band matrix A, $0 \le j \le N-1$. The type of the expression BAND_COL(A,j) is realtype *. The pointer returned by the call BAND_COL(A,j) can be treated as an array which is indexed from -(A-mu) to (A-ml).

• BAND_COL_ELEM

```
Usage : BAND_COL_ELEM(col_j,i,j) = a_ij; or a_ij = BAND_COL_ELEM(col_j,i,j);
```

This macro references the (i,j)-th entry of the band matrix A when used in conjunction with BAND_COL to reference the j-th column through col_j. The index (i,j) should satisfy $j-(A->mu) \le i \le j+(A->m1)$.

8.1.3 Functions in the DENSE module

The DENSE module defines two sets of functions with corresponding names. The first set contains functions (with names starting with a capital letter) that act on dense matrices of type DlsMat. The second set contains functions (with names starting with a lower case letter) that act on matrices represented as simple arrays.

The following functions for DlsMat dense matrices are available in the DENSE package. For full details, see the header files sundials_direct.h and sundials_dense.h.

- NewDenseMat: allocation of a DlsMat dense matrix:
- DestroyMatrix: free memory for a DlsMat matrix;
- PrintMat: print a DlsMat matrix to standard output.
- NewIntArray: allocation of an array of int for use as pivots with DenseGETRF/DenseGETRS;
- NewRealArray: allocation of an array of realtype for use as right-hand side with DenseGETRS;
- DestroyArray: free memory for an array;
- SetToZero: load a matrix with zeros;
- AddIdentity: increment a square matrix by the identity matrix;
- DenseCopy: copy one matrix to another;
- DenseScale: scale a matrix by a scalar;

- DenseGETRF: LU factorization with partial pivoting;
- DenseGETRS: solution of Ax = b using LU factorization (for square matrices A);
- DensePOTRF: Cholesky factorization of a real symmetric positive matrix;
- DensePOTRS: solution of Ax = b using the Cholesky factorization of A;
- DenseGEQRF: QR factorization of an $m \times n$ matrix, with $m \ge n$;
- DenseORMQR: compute the product w = Qv, with Q calculated using DenseGEQRF;

The following functions for small dense matrices are available in the DENSE package:

newDenseMat

newDenseMat(m,n) allocates storage for an m by n dense matrix. It returns a pointer to the newly allocated storage if successful. If the memory request cannot be satisfied, then newDenseMat returns NULL. The underlying type of the dense matrix returned is realtype**. If we allocate a dense matrix realtype** a by a = newDenseMat(m,n), then a[j][i] references the (i,j)-th element of the matrix a, $0 \le i < m$, $0 \le j < n$, and a[j] is a pointer to the first element in the j-th column of a. The location a[0] contains a pointer to m × n contiguous locations which contain the elements of a.

• destroyMat

destroyMat(a) frees the dense matrix a allocated by newDenseMat;

• newIntArray

newIntArray(n) allocates an array of n integers. It returns a pointer to the first element in the array if successful. It returns NULL if the memory request could not be satisfied.

• newRealArray

newRealArray(n) allocates an array of n realtype values. It returns a pointer to the first element in the array if successful. It returns NULL if the memory request could not be satisfied.

• destroyArray

destroyArray(p) frees the array p allocated by newIntArray or newRealArray;

• denseCopy

denseCopy(a,b,m,n) copies the m by n dense matrix a into the m by n dense matrix b;

• denseScale

denseScale(c,a,m,n) scales every element in the m by n dense matrix a by the scalar c;

• denseAddIdentity

denseAddIdentity(a,n) increments the square n by n dense matrix a by the identity matrix I_n ;

denseGETRF

denseGETRF(a,m,n,p) factors the m by n dense matrix a, using Gaussian elimination with row pivoting. It overwrites the elements of a with its LU factors and keeps track of the pivot rows chosen in the pivot array p.

A successful LU factorization leaves the matrix **a** and the pivot array **p** with the following information:

1. p[k] contains the row number of the pivot element chosen at the beginning of elimination step k, k = 0, 1, ..., n-1.

2. If the unique LU factorization of a is given by Pa = LU, where P is a permutation matrix, L is an m by n lower trapezoidal matrix with all diagonal elements equal to 1, and U is an n by n upper triangular matrix, then the upper triangular part of a (including its diagonal) contains U and the strictly lower trapezoidal part of a contains the multipliers, I - L. If a is square, L is a unit lower triangular matrix.

denseGETRF returns 0 if successful. Otherwise it encountered a zero diagonal element during the factorization, indicating that the matrix **a** does not have full column rank. In this case it returns the column index (numbered from one) at which it encountered the zero.

• denseGETRS

denseGETRS(a,n,p,b) solves the n by n linear system ax = b. It assumes that a (of size $n \times n$) has been LU-factored and the pivot array p has been set by a successful call to denseGETRF(a,n,n,p). The solution x is written into the b array.

• densePOTRF

densePOTRF(a,m) calculates the Cholesky decomposition of the m by m dense matrix a, assumed to be symmetric positive definite. Only the lower triangle of a is accessed and overwritten with the Cholesky factor.

• densePOTRS

densePOTRS(a,m,b) solves the m by m linear system ax = b. It assumes that the Cholesky factorization of a has been calculated in the lower triangular part of a by a successful call to densePOTRF(a,m).

• denseGEQRF

denseGEQRF(a,m,n,beta,wrk) calculates the QR decomposition of the m by n matrix a $(m \ge n)$ using Householder reflections. On exit, the elements on and above the diagonal of a contain the n by n upper triangular matrix R; the elements below the diagonal, with the array beta, represent the orthogonal matrix Q as a product of elementary reflectors. The real array wrk, of length m, must be provided as temporary workspace.

• denseORMQR

denseORMQR(a,m,n,beta,v,w,wrk) calculates the product w = Qv for a given vector v of length n, where the orthogonal matrix Q is encoded in the m by n matrix a and the vector beta of length n, after a successful call to denseGEQRF(a,m,n,beta,wrk). The real array wrk, of length m, must be provided as temporary workspace.

8.1.4 Functions in the BAND module

The BAND module defines two sets of functions with corresponding names. The first set contains functions (with names starting with a capital letter) that act on band matrices of type DlsMat. The second set contains functions (with names starting with a lower case letter) that act on matrices represented as simple arrays.

The following functions for DlsMat banded matrices are available in the BAND package. For full details, see the header files sundials_direct.h and sundials_band.h.

- NewBandMat: allocation of a DlsMat band matrix;
- DestroyMatrix: free memory for a DlsMat matrix;
- PrintMat: print a DlsMat matrix to standard output.
- NewIntArray: allocation of an array of int for use as pivots with BandGBRF/BandGBRS;
- NewRealArray: allocation of an array of realtype for use as right-hand side with BandGBRS;

- DestroyArray: free memory for an array;
- SetToZero: load a matrix with zeros;
- AddIdentity: increment a square matrix by the identity matrix;
- BandCopy: copy one matrix to another;
- BandScale: scale a matrix by a scalar;
- BandGBTRF: LU factorization with partial pivoting;
- BandGBTRS: solution of Ax = b using LU factorization;

The following functions for small band matrices are available in the BAND package:

• newBandMat

newBandMat(n, smu, ml) allocates storage for an n by n band matrix with lower half-bandwidth ml.

• destroyMat

destroyMat(a) frees the band matrix a allocated by newBandMat;

• newIntArray

newIntArray(n) allocates an array of n integers. It returns a pointer to the first element in the array if successful. It returns NULL if the memory request could not be satisfied.

• newRealArray

newRealArray(n) allocates an array of n realtype values. It returns a pointer to the first element in the array if successful. It returns NULL if the memory request could not be satisfied.

• destroyArray

destroyArray(p) frees the array p allocated by newIntArray or newRealArray;

bandCopy

bandCopy(a,b,n,a_smu, b_smu,copymu, copyml) copies the n by n band matrix a into the n by n band matrix b;

bandScale

bandScale(c,a,n,mu,ml,smu) scales every element in the n by n band matrix a by c;

• bandAddIdentity

bandAddIdentity(a,n,smu) increments the n by n band matrix a by the identity matrix;

• bandGETRF

bandGETRF(a,n,mu,ml,smu,p) factors the n by n band matrix a, using Gaussian elimination with row pivoting. It overwrites the elements of a with its LU factors and keeps track of the pivot rows chosen in the pivot array p.

• bandGETRS

bandGETRS(a,n,smu,ml,p,b) solves the n by n linear system ax = b. It assumes that a (of size $n \times n$) has been LU-factored and the pivot array p has been set by a successful call to bandGETRF(a,n,mu,ml,smu,p). The solution x is written into the b array.

8.2 The SPILS modules: SPGMR, SPBCG, and SPTFQMR



A linear solver module from the *spils* family can only be used in conjunction with an actual NVECTOR implementation library, such as the NVECTOR_SERIAL OF NVECTOR_PARALLEL provided with SUNDIALS.

8.2.1 The SPGMR module

The SPGMR package, in the files sundials_spgmr.h and sundials_spgmr.c, includes an implementation of the scaled preconditioned GMRES method. A separate code module, implemented in sundials_iterative.(h,c), contains auxiliary functions that support SPGMR, as well as the other Krylov solvers in SUNDIALS (SPBCG and SPTFQMR). For full details, including usage instructions, see the header files sundials_spgmr.h and sundials_iterative.h.

The files comprising the SPGMR generic linear solver, and their locations in the SUNDIALS *srcdir*, are as follows:

- header files (located in srcdir/include/sundials)
 sundials_spgmr.h sundials_iterative.h sundials_nvector.h
 sundials_types.h sundials_math.h sundials_config.h
- source files (located in *srcdir*/src/sundials) sundials_spgmr.c sundials_iterative.c sundials_nvector.c

Only two of the preprocessing directives in the header file sundials_config.h are required to use the SPGMR package by itself (see §A.3 for details):

• (required) definition of the precision of the SUNDIALS type realtype. One of the following lines must be present:

```
#define SUNDIALS_DOUBLE_PRECISION 1
#define SUNDIALS_SINGLE_PRECISION 1
#define SUNDIALS_EXTENDED_PRECISION 1
```

• (optional) use of generic math functions: #define SUNDIALS_USE_GENERIC_MATH 1

The sundials_types.h header file defines the SUNDIALS realtype and booleantype types and the macro RCONST, while the sundials_math.h header file is needed for the MAX and ABS macros and RAbs and RSqrt functions.

The generic NVECTOR files, sundials_nvector.(h,c) are needed for the definition of the generic N_Vector type and functions. The NVECTOR functions used by the SPGMR module are: N_VDotProd, N_VLinearSum, N_VScale, N_VProd, N_VDiv, N_VConst, N_VClone, N_VCloneVectorArray, N_VDestroy, and N_VDestroyVectorArray.

The nine files listed above can be extracted from the SUNDIALS *srcdir* and compiled by themselves into an SPGMR library or into a larger user code.

The following functions are available in the SPGMR package:

- SpgmrMalloc: allocation of memory for SpgmrSolve;
- SpgmrSolve: solution of Ax = b by the SPGMR method;
- SpgmrFree: free memory allocated by SpgmrMalloc.

The following functions are available in the support package sundials_iterative.(h,c):

- ModifiedGS: performs modified Gram-Schmidt procedure;
- ClassicalGS: performs classical Gram-Schmidt procedure;
- QRfact: performs QR factorization of Hessenberg matrix;
- QRsol: solves a least squares problem with a Hessenberg matrix factored by QRfact.

8.2.2 The SPBCG module

The SPBCG package, in the files sundials_spbcgs.h and sundials_spbcgs.c, includes an implementation of the scaled preconditioned Bi-CGStab method. For full details, including usage instructions, see the file sundials_spbcgs.h.

The files needed to use the SPBCG module by itself are the same as for the SPGMR module, but with sundials_spbcgs.(h,c) in place of sundials_spgmr.(h,c).

The following functions are available in the SPBCG package:

- SpbcgMalloc: allocation of memory for SpbcgSolve;
- SpbcgSolve: solution of Ax = b by the SPBCG method;
- SpbcgFree: free memory allocated by SpbcgMalloc.

8.2.3 The SPTFQMR module

The SPTFQMR package, in the files sundials_sptfqmr.h and sundials_sptfqmr.c, includes an implementation of the scaled preconditioned TFQMR method. For full details, including usage instructions, see the file sundials_sptfqmr.h.

The files needed to use the SPTFQMR module by itself are the same as for the SPGMR module, but with sundials_sptfqmr.(h,c) in place of sundials_spgmr.(h,c).

The following functions are available in the SPTFQMR package:

- SptfqmrMalloc: allocation of memory for SptfqmrSolve;
- SptfqmrSolve: solution of Ax = b by the SPTFQMR method;
- \bullet SptfqmrFree: free memory allocated by SptfqmrMalloc.

Appendix A

KINSOL Installation Procedure

The installation of KINSOL is accomplished by installing the SUNDIALS suite as a whole, according to the instructions that follow. The same procedure applies whether or not the downloaded file contains solvers other than ${\tt KINSOL.}^1$

The SUNDIALS suite (or individual solvers) are distributed as compressed archives (.tar.gz). The name of the distribution archive is of the form solver-x.y.z.tar.gz, where solver is one of: sundials, cvode, cvodes, ida, idas, or kinsol, and x.y.z represents the version number (of the SUNDIALS suite or of the individual solver). To begin the installation, first uncompress and expand the sources, by issuing

% tar xzf solver-x.y.z.tar.gz

This will extract source files under a directory *solver*-x.y.z.

Starting with version 2.4.0 of SUNDIALS, two installation methods are provided: in addition to the previous autotools-based method, SUNDIALS now provides a method based on CMake. Before providing detailed explanations on the installation procedure for the two approaches, we begin with a few common observations:

• In the remainder of this chapter, we make the following distinctions:

srcdir is the directory solver-x.y.z created above; i.e., the directory containing the SUNDIALS sources.

builddir is the (temporary) directory under which SUNDIALS is built.

- instdir is the directory under which the SUNDIALS exported header files and libraries will be installed. Typically, header files are exported under a directory instdir/include while libraries are installed under instdir/lib, with instdir specified at configuration time.
- For the CMake-based installation, in-source builds are prohibited; in other words, the build directory builddir can **not** be the same as srcdir and such an attempt will lead to an error. For autotools-based installation, in-source builds are allowed, although even in that case we recommend using a separate builddir. Indeed, this prevents "polluting" the source tree and allows efficient builds for different configurations and/or options.
- The installation directory *instdir* can **not** be the same as the source directory *srcdir*.
- By default, only the libraries and header files are exported to the installation directory *instdir*. If enabled by the user (with the appropriate option to configure or toggle for CMake), the



¹Files for both the serial and parallel versions of KINSOL are included in the distribution. For users in a serial computing environment, the files specific to parallel environments (which may be deleted) are as follows: all files in src/nvec_par; nvector_parallel.h (in include/nvector/); kinbbdpre.c, kinbbdpre.impl.h (in src/kinsol/); kinbbdpre.h (in include/kinsol/); fkinbbd.c, fkinbbd.h (in src/kinsol/fcmix/); all files in examples/kinsol/parallel/; all files in examples/kinsol/fcmix_parallel/. (By "serial version" of KINSOL we mean the KINSOL solver with the serial NVECTOR module attached, and similarly for "parallel version".)

examples distributed with SUNDIALS will be built together with the solver libraries but the installation step will result in exporting (by default in a subdirectory of the installation directory) the example sources and sample outputs together with automatically generated configuration files that reference the <code>installed SUNDIALS</code> headers and libraries. As such, these configuration files for the SUNDIALS examples can be used as "templates" for your own problems. The <code>configure script</code> will install makefiles. CMake installs <code>CMakeLists.txt</code> files and also (as an option available only under <code>Unix/Linux</code>) makefiles. Note that both installation approaches also allow the option of building the <code>SUNDIALS</code> examples without having to install them. (This can be used as a sanity check for the freshly built libraries.)

• Even if generation of shared libraries is enabled, only static libraries are created for the FCMIX modules. (Because of the use of fixed names for the Fortran user-provided subroutines, FCMIX shared libraries would result in "undefined symbol" errors at link time.)

A.1 Autotools-based installation

The installation procedure outlined below will work on commodity LINUX/UNIX systems without modification. However, users are still encouraged to carefully read this entire section before attempting to install the SUNDIALS suite, in case non-default choices are desired for compilers, compilation options, installation location, etc. The user may invoke the configuration script with the help flag to view a complete listing of available options, by issuing the command

```
% ./configure --help
```

from within srcdir.

The installation steps for SUNDIALS can be as simple as the following:

```
% cd (...)/srcdir
% ./configure
% make
% make install
```

in which case the SUNDIALS header files and libraries are installed under /usr/local/include and /usr/local/lib, respectively. Note that, by default, the example programs are not built and installed. To delete all temporary files created by building SUNDIALS, issue

```
% make clean
```

To prepare the SUNDIALS distribution for a new install (using, for example, different options and/or installation destinations), issue

```
% make distclean
```

The above steps are for an "in-source" build. For an "out-of-source" build (recommended), the procedure is simply:

```
% cd (...)/builddir
% (...)/srcdir/configure
% make
% make install
```

Note that, in this case, make clean and make distclean are irrelevant. Indeed, if disk space is a priority, the entire *builddir* can be purged after the installation completes. For a new install, a new *builddir* directory can be created and used.

A.1.1 Configuration options

The installation procedure given above will generally work without modification; however, if the system includes multiple MPI implementations, then certain configure script-related options may be used to indicate which MPI implementation should be used. Also, if the user wants to use non-default language compilers, then, again, the necessary shell environment variables must be appropriately redefined. The remainder of this section provides explanations of available configure script options.

General options

--prefix=PREFIX

Location for architecture-independent files.

Default: PREFIX=/usr/local

--exec-prefix=EPREFIX

Location for architecture-dependent files.

Default: EPREFIX=/usr/local

--includedir=DIR

Alternate location for installation of header files.

Default: DIR=PREFIX/include

--libdir=DIR

Alternate location for installation of libraries.

Default: DIR=EPREFIX/lib

--disable-solver

Although each existing solver module is built by default, support for a given solver can be explicitly disabled using this option. The valid values for *solver* are: cvode, cvodes, ida, idas, and kinsol.

--enable-examples

Available example programs are *not* built by default. Use this option to enable compilation of all pertinent example programs. Upon completion of the make command, the example executables will be created under solver-specific subdirectories of builddir/examples:

builddir/examples/solver/serial: serial C examples

builddir/examples/solver/parallel: parallel C examples

builddir/examples/solver/fcmix_serial : serial FORTRAN examples

builddir/examples/solver/fcmix_parallel: parallel FORTRAN examples

Note: Some of these subdirectories may not exist depending upon the solver and/or the configuration options given.

--with-examples-instdir=EXINSTDIR

Alternate location for example executables and sample output files (valid only if examples are enabled). Note that installation of example files can be completely disabled by issuing EXINSTDIR=no (in case building the examples is desired only as a test of the SUNDIALS libraries).

Default: DIR=EPREFIX/examples

--with-cppflags=ARG

Specify additional C preprocessor flags (e.g., ARG=-I<include_dir> if necessary header files are located in nonstandard locations).

--with-cflags=ARG

Specify additional C compilation flags.

--with-ldflags=ARG

Specify additional linker flags (e.g., ARG=-L<lib_dir> if required libraries are located in nonstandard locations).

--with-libs=ARG

Specify additional libraries to be used (e.g., ARG=-1<foo> to link with the library named libfoo.a or libfoo.so).

--with-precision=ARG

By default, SUNDIALS will define a real number (internally referred to as realtype) to be a double-precision floating-point numeric data type (double C-type); however, this option may be used to build SUNDIALS with realtype defined instead as a single-precision floating-point numeric data type (float C-type) if ARG=single, or as a long double C-type if ARG=extended.

Default: ARG=double

Users should not bu

Users should *not* build SUNDIALS with support for single-precision floating-point arithmetic on 32- or 64-bit systems. This will almost certainly result in unreliable numerical solutions. The configuration option --with-precision=single is intended for systems on which single-precision arithmetic involves at least 14 decimal digits.

Options for Fortran support

--disable-fcmix

Using this option will disable all FORTRAN support. The FCVODE, FKINSOL, FIDA, and FNVECTOR modules will not be built, regardless of availability.

--with-fflags=ARG

Specify additional FORTRAN compilation flags.

Options for MPI support

The following configuration options are only applicable to the parallel SUNDIALS packages:

--disable-mpi

Using this option will completely disable MPI support.

--with-mpicc=ARG

--with-mpif77=ARG

By default, the configuration utility script will use the MPI compiler scripts named mpicc and mpif77 to compile the parallelized SUNDIALS subroutines; however, for reasons of compatibility, different executable names may be specified via the above options. Also, ARG=no can be used to disable the use of MPI compiler scripts, thus causing the serial C and FORTRAN compilers to be used to compile the parallelized SUNDIALS functions and examples.

--with-mpi-root=MPIDIR

This option may be used to specify which MPI implementation should be used. The SUNDIALS configuration script will automatically check under the subdirectories MPIDIR/include and MPIDIR/lib for the necessary header files and libraries. The subdirectory MPIDIR/bin will also be searched for the C and FORTRAN MPI compiler scripts, unless the user uses --with-mpicc=no or --with-mpif77=no.

--with-mpi-incdir=INCDIR



--with-mpi-libdir=LIBDIR

--with-mpi-libs=LIBS

These options may be used if the user would prefer not to use a preexisting MPI compiler script, but instead would rather use a serial complier and provide the flags necessary to compile the MPI-aware subroutines in SUNDIALS.

Often an MPI implementation will have unique library names and so it may be necessary to specify the appropriate libraries to use (e.g., LIBS=-lmpich).

Default: INCDIR=MPIDIR/include and LIBDIR=MPIDIR/lib

--with-mpi-flags=ARG

Specify additional MPI-specific flags.

Options for library support

By default, only static libraries are built, but the following option may be used to build shared libraries on supported platforms.

--enable-shared

Using this particular option will result in both static and shared versions of the available SUNDIALS libraries being built if the system supports shared libraries. To build only shared libraries also specify --disable-static.

Note: The FCVODE, FKINSOL, and FIDA libraries can only be built as static libraries because they contain references to externally defined symbols, namely user-supplied FORTRAN subroutines. Although the FORTRAN interfaces to the serial and parallel implementations of the supplied NVECTOR module do not contain any unresolvable external symbols, the libraries are still built as static libraries for the purpose of consistency.

Options for Blas/Lapack support

The configure script will attempt to automatically determine the proper libraries to be linked for support of the new Blas/Lapack linear solver module. If these are not found, or if Blas and/or Lapack libraries are installed in a non-standard location, the following options can be used:

--with-blas

Specify the Blas library.

Default: none

--with-lapack

Specify the Lapack library.

Default: none

Environment variables

The following environment variables can be locally (re)defined for use during the configuration of SUNDIALS. See the next section for illustrations of these.

CC

F77

Since the configuration script uses the first C and FORTRAN compilers found in the current executable search path, then each relevant shell variable (CC and F77) must be locally (re)defined in order to use a different compiler. For example, to use xcc (executable name of chosen compiler) as the C language compiler, use CC=xcc in the configure step.

CFLAGS

FFLAGS

Use these environment variables to override the default C and FORTRAN compilation flags.

A.1.2 Configuration examples

The following examples are meant to help demonstrate proper usage of the configure options.

To build SUNDIALS using the default C and Fortran compilers, and default mpic and mpif77 parallel compilers, enable compilation of examples, and install libraries, headers, and example sources under appropriate subdirectories of /home/myname/sundials/, use

```
% configure --prefix=/home/myname/sundials --enable-examples
```

To disable installation of the examples, use:

The following example builds SUNDIALS using gcc as the serial C compiler, g77 as the serial FORTRAN compiler, mpicc as the parallel C compiler, mpif77 as the parallel FORTRAN compiler, and appends the -g3 compilaton flag to the list of default flags:

The next example again builds SUNDIALS using gcc as the serial C compiler, but the --with-mpicc=no option explicitly disables the use of the corresponding MPI compiler script. In addition, since the --with-mpi-root option is given, the compilation flags -I/usr/apps/mpich/1.2.4/include and -L/usr/apps/mpich/1.2.4/lib are passed to gcc when compiling the MPI-enabled functions. The --with-mpi-libs option is required so that the configure script can check if gcc can link with the appropriate MPI library. The --disable-lapack option explicitly disables support for Blas/Lapack, while the --disable-fcmix explicitly disables building the FCMIX interfaces. Note that, because of the last two options, no Fortran-related settings are checked for.

Finally, a minimal configuration and installation of SUNDIALS in /home/myname/sundials/ (serial only, no Fortran support, no examples) can be obtained with:

A.2 CMake-based installation

Support for CMake-based installation has been added to SUNDIALS primarily to provide a platform-independent build system. Like autotools, CMake can generate a Unix Makefile. Unlike autotools, CMake can also create KDevelop, Visual Studio, and (Apple) XCode project files from the same configuration file. In addition, CMake provides a GUI front end and therefore the installation process is more interactive than when using autotools.

The installation options are very similar to the options mentioned above (although their default values may differ slightly). Practically, all configurations supported by the autotools-based installation

approach are also possible with CMake, the only notable exception being cross-compilation, which is currently not implemented in the CMake approach.

The SUNDIALS build process requires CMake version 2.4.x or higher and a working compiler. On Unix-like operating systems, it also requires Make (and curses, including its development libraries, for the GUI front end to CMake, ccmake), while on Windows it requires Visual Studio. While many Linux distributions offer CMake, the version included is probably out of date. Many new CMake features have been added recently, and you should download the latest version from http://www.cmake.org/HTML/Download.html. Build instructions for Cmake (only necessary for Unix-like systems) can be found on the CMake website. Once CMake is installed, Linux/Unix user will be able to use ccmake, while Windows user will be able to use CMakeSetup.

As noted above, when using CMake to configure, build and install SUNDIALS, it is always required to use a separate build directory. While in-source builds are possible, they are explicitly prohibited by the SUNDIALS CMake scripts (one of the reasons being that, unlike autotools, CMake does not provide a make distclean procedure and it is therefore difficult to clean-up the source tree after an in-source build).

A.2.1 Configuring, building, and installing on Unix-like systems

Use ccmake from the CMake installed location. ccmake is a Curses based GUI for CMake. To run it go to the build directory and specify as an argument the build directory:

```
% mkdir (...)/builddir
% cd (...)/builddir
% ccmake (...)/srcdir
```

About ccmake:

- Iterative process
 - Select values, run configure (c key)
 - Set the settings, run configure, set the settings, run configure, etc.
- Repeat until all values are set and the generate option is available (g key)
- Some variables (advanced variables) are not visible right away
- To see advanced variables, toggle to advanced mode (t key)
- To set a variable, move the cursor to the variable and press enter
 - If it is a boolean (ON/OFF) it will flip the value
 - If it is string or file, it will allow editing of the string
 - For file and directories, the <tab> key can be used to complete
- \bullet To search for a variable press / key, and to repeat the search, press the n key

CMake will now generate makefiles including all dependencies and all rules to build SUNDIALS on this system. You should not, however, try to move the build directory to another location on this system or to another system. Once you have makefiles you should be able to just type:

```
% make
```

To install SUNDIALS in the installation directory specified at configuration time, simply run

```
% make install
```

A.2.2 Configuring, building, and installing on Windows

Use CMakeSetup from the CMake install location. Make sure to select the appropriate source and the build directory. Also, make sure to pick the appropriate generator (on Visual Studio 6, pick the Visual Studio 6 generator). Some CMake versions will ask you to select the generator the first time you press Configure instead of having a drop-down menu in the main dialog.

About CMakeSetup:

- Iterative process
 - Select values, press the Configure button
 - Set the settings, run configure, set the settings, run configure, etc.
- Repeat until all values are set and the OK button becomes available.
- Some variables (advanced variables) are not visible right away
- To see advanced variables, toggle to advanced mode ("Show Advanced Values" toggle).
- To set the value of a variable, click on that value.
 - If it is boolean (ON/OFF), a drop-down menu will appear for changing the value.
 - If it is file or directory, an ellipsis button will appear ("...") on the far right of the entry.
 Clicking this button will bring up the file or directory selection dialog.
 - If it is a string, it will become an editable string.

CMake will now create Visual Studio project files. You should now be able to open the SUNDIALS project (or workspace) file. Make sure to select the appropriate build type (Debug, Release, ...). To build SUNDIALS, simply build the ALL_BUILD target. To install SUNDIALS, simply run the INSTALL target within the build system.

A.2.3 Configuration options

A complete list of all available options for a CMake-based SUNDIALS configuration is provide below. Note that the default values shown are for a typical configuration on a Linux system and are provided as illustration only. Some of them will be different on different systems.

```
BUILD_CVODE - Build the CVODE library
```

Default: ON

BUILD_CVODES - Build the CVODES library

Default: ON

BUILD_IDA - Build the IDA library

Default: ON

BUILD_IDAS - Build the IDAS library

Default: ON

BUILD_KINSOL - Build the KINSOL library

Default: ON

BUILD_SHARED_LIBS - Build shared libraries

Default: OFF

BUILD_STATIC_LIBS - Build static libraries

Default: ON

CMAKE_BUILD_TYPE - Choose the type of build, options are: None (CMAKE_C_FLAGS used) Debug Release RelWithDebInfo MinSizeRel Default:

CMAKE_C_COMPILER - C compiler

Default: /usr/bin/gcc

 ${\tt CMAKE_C_FLAGS}$ - Flags for C compiler

Default:

 ${\tt CMAKE_C_FLAGS_DEBUG}$ - Flags used by the compiler during debug builds

Default: -g

CMAKE_C_FLAGS_MINSIZEREL - Flags used by the compiler during release minsize builds

Default: -Os -DNDEBUG

CMAKE_C_FLAGS_RELEASE - Flags used by the compiler during release builds

Default: -O3 -DNDEBUG

CMAKE_BACKWARDS_COMPATIBILITY - For backwards compatibility, what version of CMake commands and syntax should this version of CMake allow.

and syntax should this version of Civiake

Default: 2.4

CMAKE_Fortran_COMPILER - Fortran compiler

Default: /usr/bin/g77

Note: Fortran support (and all related options) are triggered only if either Fortran-C support is enabled (FCMIX_ENABLE is ON) or Blas/Lapack support is enabled (LAPACK_ENABLE is ON).

CMAKE_Fortran_FLAGS - Flags for Fortran compiler

Default:

CMAKE_Fortran_FLAGS_DEBUG - Flags used by the compiler during debug builds

Default:

 ${\tt CMAKE_Fortran_FLAGS_MINSIZEREL~Flags~used~by~the~compiler~during~release~minsize~builds}$

Default:

CMAKE_Fortran_FLAGS_RELEASE - Flags used by the compiler during release builds

Default:

CMAKE_INSTALL_PREFIX - Install path prefix, prepended onto install directories

Default: /usr/local

Note: The user must have write access to the location specified through this option. Exported SUNDIALS header files and libraries will be installed under subdirectories include and lib of CMAKE_INSTALL_PREFIX, respectively.

EXAMPLES_ENABLE - Build the SUNDIALS examples

Default: OFF

Note: setting this option to ON will trigger additional options related to how and where example programs will be installed.

EXAMPLES_GENERATE_MAKEFILES - Create Makefiles for building the examples

Default: ON

Note: This option is triggered only if enabling the building and installing of the example programs (i.e., both EXAMPLES_ENABLE and EXAMPLES_INSTALL are set to ON) and if configuration is done on a Unix-like system. If enabled, makefiles for the compilation of the example programs (using the installed SUNDIALS libraries) will be automatically generated and exported to the directory specified by EXAMPLES_INSTALL_PATH.

EXAMPLES_INSTALL - Install example files

Default: ON

Note: This option is triggered only if building example programs is enabled (EXAMPLES_ENABLE ON). If the user requires installation of example programs then the sources and sample output files for all SUNDIALS modules that are currently enabled will be exported to the directory specified by EXAMPLES_INSTALL_PATH. A CMake configuration script will also be automatically generated and exported to the same directory. Additionally, if the configuration is done under a Unix-like system, an additional option (EXAMPLES_GENERATE_MAKEFILES) will be triggered.

EXAMPLES_INSTALL_PATH - Output directory for installing example files

Default: /usr/local/examples

Note: The actual default value for this option will an examples subdirectory created under CMAKE_INSTALL_PREFIX.

EXAMPLES_USE_STATIC_LIBS - Link examples using the static libraries

Default: OFF

Note: This option is triggered only if building shared libraries is enabled (BUILD_SHARED_LIBS is ON).

FCMIX_ENABLE - Enable Fortran-C support

Default: OFF

LAPACK_ENABLE - Enable Lapack support

Default: OFF

Note: Setting this option to ON will trigger the two additional options see below.

LAPACK_LIBRARIES - Lapack (and Blas) libraries

Default: /usr/lib/liblapack.so;/usr/lib/libblas.so

LAPACK_LINKER_FLAGS - Lapack (and Blas) required linker flags

Default: -lg2c

MPI_ENABLE - Enable MPI support

Default: OFF

Note: Setting this option to ON will trigger several additional options related to MPI.

MPI_MPICC - mpicc program

Default: /home/radu/apps/mpich1/gcc/bin/mpicc

Note: This option is triggered only if using MPI compiler scripts (MPI_USE_MPISCRIPTS is ON).

${\tt MPI_MPIF77-mpif77~program}$

Default: /home/radu/apps/mpich1/gcc/bin/mpif77

Note: This option is triggered only if using MPI compiler scripts (MPI_USE_MPISCRIPTS is ON) and Fortran-C support is enabled (FCMIx_ENABLE is ON).

MPI_INCLUDE_PATH - Path to MPI header files

Default: /home/radu/apps/mpich1/gcc/include

Note: This option is triggered only if not using MPI compiler scripts (MPI_USE_MPISCRIPTS is ON).

${\tt MPI_LIBRARIES} \ - \ {\tt MPI} \ {\tt libraries}$

Default: /home/radu/apps/mpich1/gcc/lib/libmpich.a

Note: This option is triggered only if not using MPI compiler scripts (MPI_USE_MPISCRIPTS is ON).

MPI_USE_MPISCRIPTS - Use MPI compiler scripts

Default: ON

SUNDIALS_PRECISION - Precision used in SUNDIALS, options are: double, single or extended Default: double
 USE_GENERIC_MATH - Use generic (stdc) math libraries
 Default: ON

A.3 Manually building SUNDIALS

With the addition of CMake support, the installation of the SUNDIALS package on almost any platform was greatly simplified. However, if for whatever reason, neither of the two procedures described above is convenient (for example for users who prefer to own the build process or otherwise incorporate SUNDIALS or one of its solvers in a larger project with its own build system), we provide here a few directions for a completely manual installation.

The following files are required to compile a SUNDIALS solver module:

- public header files located under srcdir/include/solver
- implementation header files and source files located under srcdir/src/solver
- (optional) FORTRAN/C interface files located under srcdir/src/solver/fcmix
- shared public header files located under srcdir/include/sundials
- shared source files located under srcdir/src/sundials
- (optional) NVECTOR_SERIAL header and source files located under srcdir/include/nvector and srcdir/src/nvec_ser
- (optional) NVECTOR_PARALLEL header and source files located under *srcdir*/include/nvector and *srcdir*/src/nvec_par
- configuration header file sundials_config.h (see below)

A sample header file that, appropriately modified, can be used as sundials_config.h (otherwise created automatically by the configure or CMake scripts) is provided below.

```
/* SUNDIALS configuration header file */

#define SUNDIALS_PACKAGE_VERSION "2.4.0"

#define F77_FUNC(name,NAME) name ## _

#define F77_FUNC_(name,NAME) name ## _

#define SUNDIALS_DOUBLE_PRECISION 1

#define SUNDIALS_USE_GENERIC_MATH 1

#define SUNDIALS_MPLCOMM_F2C 1

#define SUNDIALS_MPLCOMM_F2C 1
```

The various preprocessor macros defined within sundials_config.h have the following uses:

• Precision of the SUNDIALS realtype type

Only one of the macros SUNDIALS_SINGLE_PRECISION, SUNDIALS_DOUBLE_PRECISION and SUNDIALS_EXTENDED_PRECISION should be defined to indicate if the SUNDIALS realtype type is an alias for float, double, or long double, respectively.

• Use of generic math functions

If SUNDIALS_USE_GENERIC_MATH is defined, then the functions in sundials_math.(h,c) will use the pow, sqrt, fabs, and exp functions from the standard math library (see math.h), regardless of the definition of realtype. Otherwise, if realtype is defined to be an alias for the float C-type, then SUNDIALS will use powf, sqrtf, fabsf, and expf. If realtype is instead defined to be a synonym for the long double C-type, then powl, sqrtl, fabsl, and expl will be used.

Note: Although the powf/powl, sqrtf/sqrtl, fabsf/fabsl, and expf/expl routines are not specified in the ANSI C standard, they are ISO C99 requirements. Consequently, these routines will only be used if available.

• Fortran name-mangling scheme

The macros given below are used to transform the C-language function names defined in the FORTRAN-C interface modules in a manner consistent with the preferred FORTRAN compiler, thus allowing native C functions to be called from within a FORTRAN subroutine. The name-mangling scheme is specified by appropriately defining the following parameterized macros (using the stringization operator, ##, if necessary):

```
F77_FUNC(name,NAME)F77_FUNC_(name,NAME)
```

For example, to specify that mangled C-language function names should be lowercase with one underscore appended include

```
#define F77_FUNC(name,NAME) name ## _
#define F77_FUNC_(name,NAME) name ## _
```

in the sundials_config.h header file.

• Use of an MPI communicator other than MPI_COMM_WORLD in FORTRAN

If the macro SUNDIALS_MPI_COMM_F2C is defined, then the MPI implementation used to build SUNDIALS defines the type MPI_Fint and the function MPI_Comm_f2c, and it is possible to use MPI communicators other than MPI_COMM_WORLD with the FORTRAN-C interface modules.

• Mark Sundials API functions for export/import. When building shared sundials libraries under Windows, use

```
#define SUNDIALS_EXPORT __declspec(dllexport)
```

When linking to shared SUNDIALS libraries under Windows, use

```
#define SUNDIALS_EXPORT __declspec(dllimport)
```

In all other cases (other platforms or static libraries under Windows), the SUNDIALS_EXPORT macro is empty.

A.4 Installed libraries and exported header files

Using the standard SUNDIALS build system, the command

```
% make install
```

will install the libraries under *libdir* and the public header files under *includedir*. The default values for these directories are *instdir*/lib and *instdir*/include, respectively, but can be changed using the configure script options --prefix, --exec-prefix, --includedir and --libdir (see §A.1) or the appropriate CMake options (see §A.2). For example, a global installation of SUNDIALS on a *NIX system could be accomplished using

% configure --prefix=/opt/sundials-2.1.1

Although all installed libraries reside under *libdir*, the public header files are further organized into subdirectories under *includedir*.

The installed libraries and exported header files are listed for reference in Table A.1. The file extension .lib is typically .so for shared libraries and .a for static libraries. Note that, in Table A.1, names are relative to libraries and to includedir for header files.

A typical user program need not explicitly include any of the shared SUNDIALS header files from under the *includedir*/sundials directory since they are explicitly included by the appropriate solver header files (e.g., cvode_dense.h includes sundials_dense.h). However, it is both legal and safe to do so (e.g., the functions declared in sundials_dense.h could be used in building a preconditioner).

Table A.1: SUNDIALS libraries and header files

SHARED	Libraries	n/a	
	Header files	sundials/sundials_config.h	sundials/sundials_types.h
		sundials/sundials_math.h	, , ,
		sundials/sundials_nvector.h	sundials/sundials_fnvector.h
		sundials/sundials_direct.h	sundials/sundials_lapack.h
		sundials/sundials_dense.h	sundials/sundials_band.h
		sundials/sundials_iterative.h	sundials/sundials_spgmr.h
		sundials/sundials_spbcgs.h	sundials/sundials_sptfqmr.h
NVECTOR_SERIAL	Libraries	libsundials_nvecserial.lib	libsundials_fnvecserial.a
	Header files	nvector/nvector_serial.h	
NVECTOR_PARALLEL	Libraries	libsundials_nvecparallel.lib	libsundials_fnvecparallel.a
	Header files	nvector/nvector_parallel.h	<u> </u>
CVODE	Libraries	libsundials_cvode.lib	libsundials_fcvode.a
	Header files	cvode/cvode.h	cvode/cvode_impl.h
		cvode/cvode_direct.h	cvode/cvode_lapack.h
		cvode/cvode_dense.h	cvode/cvode_band.h
		cvode/cvode_diag.h	,
		cvode/cvode_spils.h	$cvode/cvode_spgmr.h$
		cvode/cvode_sptfqmr.h	cvode/cvode_spbcgs.h
		cvode/cvode_bandpre.h	cvode/cvode_bbdpre.h
CVODES	Libraries	libsundials_cvodes.lib	1
	Header files	cvodes/cvodes.h	cvodes/cvodes_impl.h
		cvodes/cvodes_direct.h	cvodes/cvodes_lapack.h
		cvodes/cvodes_dense.h	cvodes/cvodes_band.h
		cvodes/cvodes_diag.h	, , , , , , , , , , , , , , , , , , , ,
		cvodes/cvodes_spils.h	cvodes/cvodes_spgmr.h
		cvodes/cvodes_sptfqmr.h	cvodes/cvodes_spbcgs.h
		cvodes/cvodes_bandpre.h	cvodes/cvodes_bbdpre.h
IDA	Libraries	libsundials_ida.lib	libsundials_fida.a
	Header files	ida/ida.h	ida/ida_impl.h
		ida/ida_direct.h	ida/ida_lapack.h
		ida/ida_dense.h	ida/ida_band.h
		ida/ida_spils.h	ida/ida_spgmr.h
		ida/ida_spbcgs.h	ida/ida_sptfqmr.h
		ida/ida_bbdpre.h	, I
IDAS	Libraries	libsundials_idas.lib	
	Header files	idas/idas.h	idas/idas_impl.h
		idas/idas_direct.h	idas/idas_lapack.h
		idas/idas_dense.h	idas/idas_band.h
		idas/idas_spils.h	idas/idas_spgmr.h
		idas/idas_spbcgs.h	idas/idas_sptfqmr.h
		idas/idas_bbdpre.h	, 1
KINSOL	Libraries	libsundials_kinsol.lib	libsundials_fkinsol.a
- 	Header files	kinsol/kinsol.h	kinsol/kinsol_impl.h
		kinsol/kinsol_direct.h	kinsol/kinsol_lapack.h
		kinsol/kinsol_dense.h	kinsol/kinsol_band.h
		kinsol/kinsol_spils.h	kinsol/kinsol_spgmr.h
		kinsol/kinsol_spbcgs.h	kinsol/kinsol_sptfqmr.h
		kinsol/kinsol_bbdpre.h	
		inition/ minoripodpre.ii	

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Appendix B

KINSOL Constants

Below we list all input and output constants used by the main solver and linear solver modules, together with their numerical values and a short description of their meaning.

B.1 KINSOL input constants

KINSOL main solver module			
KIN_ETACHOICE1 KIN_ETACHOICE2 KIN_ETACONSTANT KIN_NONE KIN_LINESEARCH	1 2 3 0 1	Use Eisenstat and Walker Choice 1 for η . Use Eisenstat and Walker Choice 2 for η . Use constant value for η . Use inexact Newton globalization. Use linesearch globalization.	
	Ite	rative linear solver module	
PREC_NONE PREC_RIGHT MODIFIED_GS CLASSICAL_GS	$\begin{matrix} 0 \\ 2 \\ 1 \\ 2 \end{matrix}$	No preconditioning Preconditioning on the right. Use modified Gram-Schmidt procedure. Use classical Gram-Schmidt procedure.	

B.2 KINSOL output constants

KINSOL main solver module			
KIN_SUCCESS	0	Successful function return.	
KIN_INITIAL_GUESS_OK	1	The initial user-supplied guess already satisfies the stopping criterion.	
KIN_STEP_LT_STPTOL	2	The stopping tolerance on scaled step length was satisfied.	
KIN_WARNING	99	A non-fatal warning. The solver will continue.	
KIN_MEM_NULL	-1	The kin_mem argument was NULL.	
KIN_ILL_INPUT	-2	One of the function inputs is illegal.	
KIN_NO_MALLOC	-3	The KINSOL memory was not allocated by a call to KINMalloc.	
KIN_MEM_FAIL	-4	A memory allocation failed.	
KIN_LINESEARCH_NONCONV	-5	The linesearch algorithm was unable to find an iterate suffi- ciently distinct from the current iterate.	

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KIN_MAXITER_REACHED	-6	The maximum number of nonlinear iterations has been reached.
KIN_MXNEWT_5X_EXCEEDED	-7	Five consecutive steps have been taken that satisfy a scaled step length test.
KIN_LINESEARCH_BCFAIL	-8	The linesearch algorithm was unable to satisfy the β -
KIN_LINSOLV_NO_RECOVERY	-9	condition for nbcfails iterations. The user-supplied routine preconditioner slve function failed
MIN LINIT PAIL	-10	recoverably, but the preconditioner is already current. The linear solver's initialization function failed.
KIN_LINIT_FAIL KIN_LSETUP_FAIL	-10 -11	The linear solver's setup function failed in an unrecoverable
KIN_LSEIOP_FAIL	-11	manner.
KIN_LSOLVE_FAIL	-12	The linear solver's solve function failed in an unrecoverable
		manner.
KIN_SYSFUNC_FAIL	-13	The system function failed in an unrecoverable manner.
KIN_FIRST_SYSFUNC_ERR	-14	The system function failed recoverably at the first call.
KIN_REPTD_SYSFUNC_ERR	-15	The system function had repeated recoverable errors.
		•
	KI	NDLS linear solver module
KINDLS_SUCCESS	0	Successful function return.
	-	
KINDLS_MEM_NULL	-1	The kin_mem argument was NULL. The KINDLS linear solver has not been initialized.
KINDLS_LMEM_NULL	-2 -3	
KINDLS_ILL_INPUT	-3	The KINDLS solver is not compatible with the current NVECTOR module.
KINDLS_MEM_FAIL	-4	
KINDLS_MEM_FAIL KINDLS_JACFUNC_UNRECVR	-4 -5	A memory allocation request failed. The Jacobian function failed in an unrecoverable manner.
KINDLS_JACFUNC_RECVR	-6	The Jacobian function had a recoverable error.
KINDLS_JACFUNC_RECVK	-0	The Jacobian function had a recoverable error.
	KIN	SPILS linear solver modules
VINADII A GUAGEGA	0	C
KINSPILS_SUCCESS	0	Successful function return.
KINSPILS_MEM_NULL	-1	The kin_mem argument was NULL.
KINSPILS_LMEM_NULL	-2	The KINSPILS linear solver has not been initialized.
KINSPILS_ILL_INPUT	-3	The KINSPILS solver is not compatible with the current NVEC-
WINGDII O MEM PATI	4	TOR module, or an input value was illegal.
KINSPILS_MEM_FAIL	-4	A memory allocation request failed.
KINSPILS_PMEM_NULL	-5	The preconditioner module has not been initialized.
	SPGMR	generic linear solver module
SPGMR_SUCCESS	0	Converged.
SPGMR_RES_REDUCED	1	No convergence, but the residual norm was reduced.
SPGMR_CONV_FAIL	2	Failure to converge.
SPGMR_QRFACT_FAIL	3	A singular matrix was found during the QR factorization.
SPGMR_PSOLVE_FAIL_REC	4	The preconditioner solve function failed recoverably.
SPGMR_ATIMES_FAIL_REC	5	The Jacobian-times-vector function failed recoverably.
SPGMR_MEM_NULL	-1	The SPGMR memory is NULL
SPGMR_ATIMES_FAIL_UNREC	-2	The Jacobian-times-vector function failed unrecoverably.

SPGMR_PSOLVE_FAIL_UNREC	-3	The preconditioner solve function failed unrecoverably.
SPGMR_GS_FAIL	-4	Failure in the Gram-Schmidt procedure.
SPGMR_QRSOL_FAIL	-5	The matrix R was found to be singular during the QR solve
		phase.

SPBCG generic linear solver module		
SPBCG_SUCCESS	0	Conveneed
	0	Converged.
SPBCG_RES_REDUCED	1	No convergence, but the residual norm was reduced.
SPBCG_CONV_FAIL	2	Failure to converge.
SPBCG_PSOLVE_FAIL_REC	3	The preconditioner solve function failed recoverably.
SPBCG_ATIMES_FAIL_REC	4	The Jacobian-times-vector function failed recoverably.
SPBCG_MEM_NULL	-1	The spbcg memory is NULL
SPBCG_ATIMES_FAIL_UNREC	-2	The Jacobian-times-vector function failed unrecoverably.
SPBCG_PSOLVE_FAIL_UNREC	-3	The preconditioner solve function failed unrecoverably.

SPTFQMR generic linear solver module

SPTFQMR_SUCCESS	0	Converged.
SPTFQMR_RES_REDUCED	1	No convergence, but the residual norm was reduced.
SPTFQMR_CONV_FAIL	2	Failure to converge.
SPTFQMR_PSOLVE_FAIL_REC	3	The preconditioner solve function failed recoverably.
SPTFQMR_ATIMES_FAIL_REC	4	The Jacobian-times-vector function failed recoverably.
SPTFQMR_MEM_NULL	-1	The SPTFQMR memory is NULL
SPTFQMR_ATIMES_FAIL_UNREC	-2	The Jacobian-times-vector function failed.
SPTFQMR_PSOLVE_FAIL_UNREC	-3	The preconditioner solve function failed unrecoverably.

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