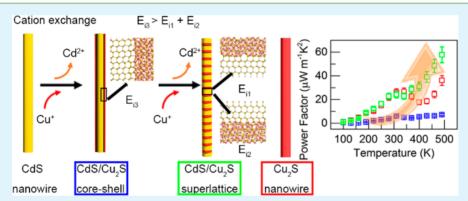


Solution-Processed CdS/Cu₂S Superlattice Nanowire with Enhanced Thermoelectric Property

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Supporting Information



ABSTRACT: Previously, the solution-based cation exchange reaction has been extensively studied for the synthesis of the complex heteroepitaxial nanocolloidals. Here, we demonstrated that the strain induced selective phase segregation technique can also be applied to large size nanowires in a well-studied CdS/Cu₂S system, leading to the formation of superlattice nanowire structure with a simple solution-based cation exchange reaction. This structural evolution is driven by the distinct interface formation energy at different CdS facets as indicated by ab initio calculation. Because of the energy filtering effect, the superlattice nanowire shows an enhanced thermopower without significant decrease of the electrical conductivity. This study provides a promising low-cost solution process to produce superlattice nanostructures for practical thermoelectric applications.

KEYWORDS: cation exchange reaction, nanowire, self-assembly, superlattice, thermoelectric applications

lacksquare t is well-known that the strain originated from the large lattice mismatch at the heteroepitaxial interface often leads to uncontrollable interface defects formation in two-dimensional thin films. In contrast, the lattice mismatch strain in nanocolloidals with the size of a few nanometers may result in controllable phase segregation that facilitated the synthesis of many complex nanostructures such as CdS/Ag₂S superlattice¹ and CdS/Cu₂S asymmetric binary nanocolloidals² via simple cation exchange reactions.³ Similarly, the cation exchange chemistry on nanowires with diameter around 100 nm has also been extensively explored.^{4,5} However, because of the large crystal size and slow ion diffusion, the cation exchange reaction does not seem to be a viable method for complex heterojunction nanowires synthesis besides coaxial nanowires.⁶ On the other hand, inspired by pioneering theoretical 7-11 and experimental studies, $\frac{12-15}{12}$ the heterojunction superlattice nanowire was suggested to be a promising thermoelectric

material due to the quantum confinement, the energy filtering effect, and the interface phonon scattering, which simultaneously offers the thermopower enhancement and the thermal conductivity reduction without significant deteriorate the electrical conductivity. In order to achieve the composition alternation for heterosuperlattice nanowires, a sequential deposition growth is usually applied. However, in this process, because each inclusion layer inside the nanowire requires a switching of the composition of the precursors, this technique is not desired for large scale synthesis and thermoelectric application where superlattices with many inclusion layers are desired. Recently, the high temperatures controllable phase segregation technique was developed in the

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gold—germanium nanowire,¹⁹ whereas other self-assembly-based techniques for thermoelectric related superlattice nanowire still need to be developed in other material systems. Furthermore, compared to the well-observed thermal conductivity suppression in superlattice nanostructures,^{17,20} the experimental demonstration of the proposed thermopower enhancement is rarely reported.

Herein, we report a simple solution-based process to synthesize CdS/Cu₂S superlattice nanowires by Cu⁺ cation exchange with physical vapor deposition (PVD) grown CdS nanowire and the enhanced thermoelectric performance of the resulting superlattice nanowires. Upon Cd²⁺ replaced by Cu⁺ in CdS nanowires, the core-shell CdS/Cu₂S nanowire with low surface defect density was first produced.⁶ With further Cu⁺ diffusion into the CdS nanowire core, the lattice mismatch induced strain is built up and prevents the further growth of the conformal Cu₂S shell. Instead, the CdS/Cu₂S nanowire is converted into a superlattice structure, similar to the CdS/Ag₂S superlattice discovered in the much smaller nanocolloidal system. Such phase evolution of Cu₂S/CdS can be explained by the distinct interface formation energies of CdS/Cu₂S attachments at different CdS facets as indicated in ab initio calculation. Moreover, this solution-processed CdS/Cu₂S superlattice nanowire exhibits an enhanced thermopower over pure Cu₂S nanowire and CdS/Cu₂S core-shell nanowire due to energy filtering effect, which provides a potential route to designing high-performance thermoelectric superlattice nanowire materials.

In our experiment, the CdS nanowires were first synthesized by PVD method described previously,²¹ where a 20 nm gold thin film was utilized as catalyst (Supporting Information). The as-synthesized CdS nanowires with diameters ranging from 80 to 200 nm and lengths up to 100 μ m are used for further cation exchange reaction. The X-ray diffraction (XRD) pattern matches very well with wurtzite phase CdS with a strong (0002) peak, indicating a preferential nanowire growth along the (0002) direction (Figures S1 and S2). Then, the CdS nanowires were dipped into 0.5 M CuCl solution at 80 °C for the different durations for cation exchange reaction (0-30 min)and examined with high-resolution transmission electron microscopy (HRTEM). As shown in Figure 1a, the phase evolution proceeds from pristine CdS nanowire to CdS/Cu₂S core-shell nanowire, and eventually to CdS/Cu₂S superlattice nanowire. Correspondingly, the X-ray diffraction results show that the CdS (0002) peak gradually diminishes with increasing reaction time, whereas the low-temperature phase of chalcocite Cu₂S (L-Cu₂S) peaks noticeably emerge after 3 min of reaction (Figure S1). Nevertheless, the CdS (1000) and ($10\overline{1}1$) peaks do not completely disappear even after 30 min reaction. Compared to the complete cation exchange conversion into Cu₂S nanowire in thin CdS nanowire, the incomplete convertion in our large diameter nanowires implies that the slow diffusion kinetics of Cd²⁺ ions could be the rate limiting step in the cation exchange reaction.

The more detailed inspection of the TEM image shows the progression of the cation exchange reaction. After 0.5 min of reaction, a CdS/Cu₂S core—shell structure can be observed with a Cu₂S shell thickness of \sim 5 nm (Figure 1c). At this stage, the Cu₂S layer is below the critical thickness, and the strain induced by lattice mismatch can be relaxed without creating interface defects. With reaction time over 3 min, the Cu₂S inclusion layers were observed in the nanowire, and the CdS/Cu₂S superlattice structure is formed (Figures 1d, 2a and Figure

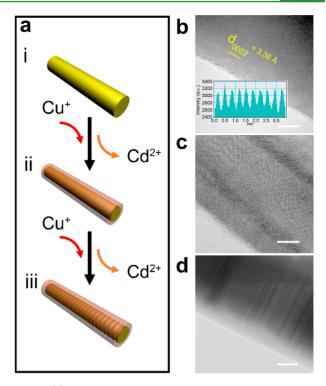


Figure 1. (a) Schematic diagram of phase evolution from pristine CdS nanowire to CdS/Cu₂S core—shell nanowire, and eventually to CdS/Cu₂S superlattice nanowire. TEM images of (b) pristine CdS nanowire, (c) CdS/Cu₂S core—shell nanowire and (d) CdS/Cu₂S superlattice nanowire. Inset: transmitted electron intensity profile along the periodic spacing denoted by yellow line, which is consistent with the lattice distance (\sim 3.36 Å) of wurtzite phase CdS (0002) plane. Scale bars: (b, c) 5 nm; (d) 30 nm.

S3). The Cu element electron energy loss spectrum (EELS) mapping image confirmed this superlattice structure (Figure 2b), which shows the copper-rich inclusion layers in CdS matrix. In order to get more in-depth information and atomic resolution image of the inclusion Cu₂S layers, the superlattice nanowires were dipped into 0.1 M HCl for 15 min to etch away the CdS segments selectively. Because the Cu₂S is insoluble in dilute HCl, the Cu₂S sections were left intact (Figure 2c), whereas most of the CdS sections are removed selectively. Figure 2d gives the corresponding EELS elemental mapping image for Cu element, indicating the long-range ordering of the superlattice structure. The high-resolution TEM image of the Cu₂S inclusion layers shows good single crystallinity (Figure 2e), which agrees well with the XRD results of crystalline L-Cu₂S phase. It is well-known that Cu₂S and CdS form type II heterojunction that is excellent for photoexcited charge separation.⁶ As shown in Figure 2f, the photoluminescence (PL) measurements of the pristine CdS nanowire shows strong typical band edge emission with the peak wavelength at 500 nm. Upon cation exchange reaction for a short time (0.5 min), the core-shell CdS/Cu₂S shows a much-suppressed band edge emission of CdS, which indicates the incomplete exciton extraction at the CdS/Cu₂S interface. With the formation of superlattice CdS/Cu₂S nanowires (3 min reaction time), the PL is dramatically quenched because of the enhanced exciton separation at the interface, leaving a broad broadband emission with the peak wavelength around 570 nm.

To rationalize the conversion from core-shell nanowire to superlattice in CdS/Cu₂S cation exchange reaction, the

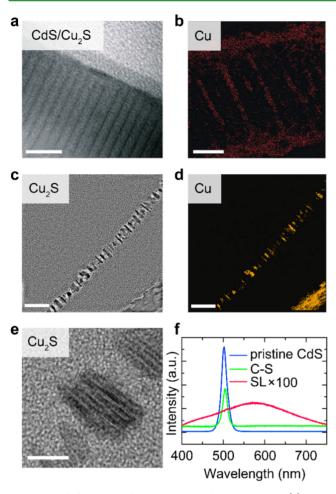


Figure 2. CdS/Cu_2S superlattice nanowire characterizations. (a) TEM and corresponding (b) Cu EELS elemental mapping images of CdS/Cu_2S superlattice nanowire. Scale bar: 20 nm. (c) TEM and (d) Cu EELS mapping images of CdS/Cu_2S superlattice nanowire after removal of CdS by 0.1 M HCl. Scale bar: 50 nm. (e) High-resolution TEM image of Cu_2S region after removal of CdS by 0.1 M HCl. Scale bar: 10 nm. (f) PL spectra of single pristine CdS nanowire, as-prepared CdS/Cu_2S core—shell nanowires (C-S) and CdS/Cu_2S superlattice nanowires (SL). For clarity, the intensity of CdS/Cu_2S superlattice nanowires is multiplied by 100.

formation energies of CdS-Cu₂S interfaces at different facets of CdS nanowire are calculated to evaluate their relative stability. Because the sulfur sublattice in Cu₂S has a small mismatch with the hexagonal close-packed sulfur sublattice in CdS, 22 the interfaces can be made by treating the Cu₂S as pseudoorthorhombic for easier modeling (Table S1, Figure S4), albeit the unit cell of L-Cu₂S is monoclinic.²³ The models of epitaxial attachments between wurtzite CdS and L-Cu₂S are shown in Figure 3. The formation energies at CdS (0001) ($E_{i1} = 0.008$ $eV/Å^2$) and $(000\overline{1})$ ($E_{i2} = 0.020 \text{ eV/Å}^2$) facets, which are the normal surface to the nanowire growth direction, are much less than that at the CdS ($10\overline{10}$) ($E_{i3} = 0.113 \text{ eV/Å}^2$) facet that is along the nanowire growth direction (Figure 3). As a result, it is thermodynamically favorable to form the Cu₂S/CdS interface perpendicular to the nanowire growth direction⁴ rather than Cu₂S shells.

We propose that the lattice mismatch strain at CdS/Cu_2S interface drives the conversion of the core—shell nanowire into a superlattice structure during the cation exchange reaction. A critical thickness ~ 23.9 nm corresponding to the formation of

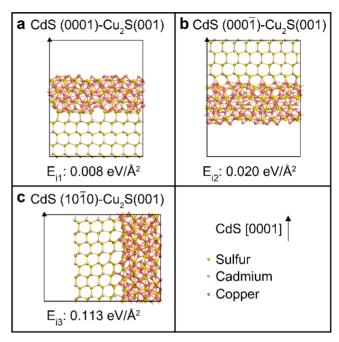


Figure 3. Models and interface formation energies (E_i) for the CdS–Cu₂S interfaces in the superlattice nanowire. (a) CdS (0001)–Cu₂S (001) and (b) CdS $(000\overline{1})$ –Cu₂S (001) interfaces, parallel to the nanowire cross section. (c) CdS $(10\overline{10})$ –Cu₂S (001) interface, parallel to the length of the nanowire. The E_i is depicted as eV per unit interfacial area.

the line dislocation in the core-shell structure can be estimated based on the theoretical analysis of strained heterojunctions, 24,25 which align with the observed Cu₂S shell thickness (<20 nm) in our samples. After the initial formation of CdS/ Cu₂S core-shell structure, the strain near the CdS-Cu₂S interface increases with growing Cu₂S shell thickness, which leads to the instability of the epitaxial interface and forms dislocation defects when approaching the critical thickness. Similar to the Stranski-Krastanov growth on the twodimensional surface,²⁶ where the semiperiodic nanoparticle islands are formed on heteroepitaxial thin film for excess stress relaxation, the semiperiodic dislocation defects can be generated by cation exchange reaction on the CdS/Cu₂S core-shell nanowire. Because of the lower formation energies at CdS (0001)- Cu_2S (001) and CdS (000 $\overline{1}$)- Cu_2S (001) interfaces, the dislocation defects serve as the initiating sites where the Cu₂S crystals grow into the CdS core at the expense of the outer Cu₂S shell until the Cu₂S span the entire diameter of CdS nanowire and form the semiperiodic inclusion layers in the nanowire. After formation of the superlattice nanowire, the further cation exchange is slowed down due to the slow diffusion of Cd²⁺ inside the nanowire, which prevents the complete conversion to pure Cu₂S nanowire as observed in nanowires with a smaller diameter.⁴ Similarly, the lattice mismatch strain also facilitates the Cu₂S formation at the ends of CdS nanowires with a smaller diameter, as have been reported in previous studies.^{2,4} The core-shell nanowire to superlattices conversion could cease when the Cu₂S shell thickness decrease below the critical thickness, and the strain is greatly relaxed. This metastable superlattice nanowire with remained Cu₂S shell can occasionally be observed in TEM (Figure S5).

With this solution-processed superlattice nanowire, we investigated the thermopower enhancement as predicted by

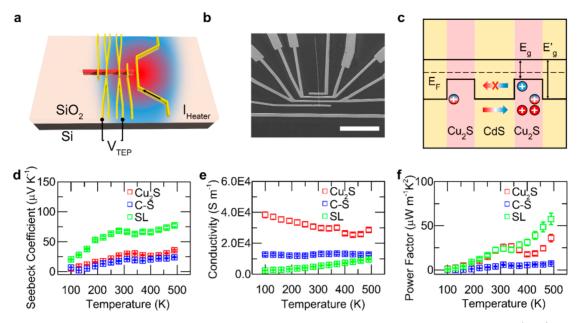


Figure 4. Temperature dependence of thermoelectric properties of Cu_2S nanowire, CdS/Cu_2S core—shell nanowires (C-S) and CdS/Cu_2S superlattice nanowires (SL). (a) The illustration for the thermoelectric properties measurement. (b) SEM image of the fabricated device for thermopower measurement. Scale bar: 30 μ m. (c) Schematic diagram of carrier energy filtering for power factor enhancement. (d) Thermopower. (e) Electrical conductivity. (f) Power factor of nanowires. With consideration of the measurement error from both σ (3.5%) and S (4%), the power factor shows 11.5% uncertainty at 95% confidence.

energy filtering effect. 7,9,10 The enhanced thermopower roots in the energy filtering affect which preferentially traps the low energy carriers. 12 To measure the thermoelectric properties of our CdS/Cu₂S superlattice nanowire, the nanowire is electrically connected to two electrodes that also serve as the temperature sensors. With a temperature gradient (ΔT) created by a DC current over a nearby heating electrode, a thermovoltage (V_{TEP}) can be generated along the nanowire and the thermopower S can be calculated as $S = -V_{\text{TEP}}/\Delta T$ (Figure 4a,b). Here, we focused on the electrical part of the thermoelectric properties of superlattice nanowire and compared it to the core-shell CdS/Cu₂S nanowire and pure Cu₂S nanowire. Because of the complete conversion from CdS to Cu₂S nanowire cannot be achieved in our large diameter nanowires even with prolonged reaction time, high quality single crystalline Cu₂S nanowires were synthesized by single precursor solution-liquid-solid (SLS) method for the comparison of the thermoelectric properties (Figure S6).

In CdS/Cu₂S superlattice nanowire, the alternating CdS and Cu_2S layers form a typical type II semiconductor junction as shown in Figure 4c.²⁷ It is known that the cation exchange reaction produces near-degenerately doped p^+ -Cu₂S with carrier concentration around $10^{20}~{\rm cm}^{-3.28}$ When contact with near intrinsic CdS produced by PVD method, the band bending almost entirely reside in CdS layer. Because the CdS layer is only a few nanometers thick, the high concentration holes in Cu₂S diffuse through the CdS layer and result in a high hole conductivity in CdS layers. As a result, the superlattice nanowire appears as a p-type semiconductor with periodic energy barrier primarily contributed from the valence band offset between two materials, which causes the energy filtering effect. Upon experiencing temperature gradient along the superlattice nanowire, the "hot carriers" with higher thermal energy can diffuse over the energy barrier to the lower temperature region while the "cold carriers" are preferentially trapped, which will effectively inhibit the back diffusion of carriers and enhance the thermopower of the superlattice nanowire. 12

As shown in Figure 4d, the positive thermopower *S* confirms that the holes indeed serve as the majority carriers in all the samples. In the core-shell nanowire produced by short time cation exchange reaction, the transport behavior is dominated by the highly conductive Cu₂S shell. Therefore, the CdS/Cu₂S core-shell nanowire and pure Cu2S nanowire display very similar thermopower across the entire temperature region. With the Cu₂S inclusion layers inside the superlattice nanowire, the thermopower will be improved due to the transport of carriers through the CdS and Cu₂S layers. It is noteworthy that the dampened S around 400 K in Cu₂S and CdS/Cu₂S core-shell nanowires is caused by the transition of Cu₂S from monoclinic low-chalcocite (LC) to hexagonal high-chalcocite (HC) phase.²⁹ In contrast, the transition of S in CdS/Cu₂S superlattice nanowire is more pronounced and significantly shifted to lower temperature (~330 K). This observation can be well explained by the size dependence of the temperatureinduced solid-solid phase transition as reported in Cu₂S nanorod.³⁰ As the critical length of the Cu₂S nanorod decreased to ~5 nm, the LC-HC transition temperature is reduced to ~330 K, which aligns with the TEM result of our superlattice nanowire where the Cu₂S inclusion thickness is also around 5 nm. Because the barrier height in our superlattices is about 1.2 eV,27 which is too large to keep the majority carrier mobility without degradation, the electrical conductivity σ of superlattice nanowire was suppressed compared to the CdS/Cu2S coreshell and pure Cu₂S nanowire (Figure 4e). Furthermore, we noticed that some defects formed in the CdS/Cu₂S superlattice nanowire after cation exchange reaction that induce many structural failures in our nanowires and could also deteriorate σ of the measured nanowires. Nevertheless, the superlattice nanowire still shows an enhanced power factor σS^2 beyond 400 K (Figure 4f), which can be further improved by lowering the energy barrier height via different materials combination such

as $CdSe/Cu_2Se$ and finely controlling the reaction condition for higher material integrity.

In conclusion, a simple aqueous solution-processed cation exchange approach has been demonstrated to convert the PVDgrown CdS nanowires into CdS/Cu₂S superlattice structure. The evolution of CdS from nanowire to core-shell CdS/Cu₂S structure and to CdS/Cu₂S superlattice nanowire can be explained by the distinct interface formation energy at different CdS facets and the self-regulated strain energy relaxation at the CdS-Cu₂S interface. The energy filtering effect favored by the junction formed at the CdS-Cu₂S interface can significantly enhance the thermopower without greatly undermining the electrical conductivity of the superlattice nanowires, which provides an enhanced power factor compared to pure Cu₂S nanowires. Considering the well demonstrated thermal conductivity suppression due to the phonons boundary scattering in superlattice nanowires, ¹⁷ an improvement of the ZT value of the CdS/Cu₂S superlattice nanowires is expected, which could serve as promising materials for refrigeration application under room temperature or for the power generation to harvest the waste heat from automobile and industrial combustion processes under higher temperature (>400 K).

■ ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsami.7b09346.

Experimental and VASP modeling details, XRD of CdS and CdS/Cu₂S nanowires, low-temperature chalcocite Cu₂S structure information, TEM of HCl etched CdS/Cu₂S superlattice nanowires, SEM and XRD of pure Cu₂S nanowires (PDF)

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Notes

The authors declare no competing financial interest.

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