

# international collegiate programming contest INDONESIA NATIONAL CONTEST INC 2019



# Problem K Odd GCD Matching

Supposed there are N integers  $A_{1...N}$ .  $A_i$  can be paired with  $A_j$  if  $GCD(A_i, A_j)$  is an odd number. GCD(a, b) is the greatest common divisor of a and b. For example, b can be paired with b because GCD(b, b) = b is an odd number; however, b cannot be paired with b because CD(b, b) = b is an even number.

An odd GCD matching of  $A_{1..N}$  is a set of pairs which satisfies the following.

- Each pair contains two integers (i, j) where  $1 \le i < j \le N$ .
- Each integer *i* only appears at most once in the set.
- If (i, j) is in the set, then  $A_i$  must be able to be paired with  $A_j$ .

Given  $A_{1..N}$ , your task is to find the size of a maximum odd GCD matching of  $A_{1..N}$ . An odd GCD matching is maximum if and only if there are no other odd GCD matching which has more pairs than it.

For example, let  $A_{1..5}=\{6,8,9,12,13\}$ . The size of a maximum odd GCD matching in this example is 2; one such example is  $\{(1,3),(2,5)\}$  which corresponds to the pairs  $(A_1=6 \text{ with } A_3=9)$  and  $(A_2=8 \text{ with } A_5=13)$ . Note that  $\{(1,3)\}$  with the size of 1 is also a valid odd GCD matching, but it is not a maximum one. On the other hand,  $\{(2,4)\}$  is not a valid odd GCD matching as  $A_2=8$  cannot be paired with  $A_4=12$  in this example.

#### Input

Input begins with a line containing an integer: N ( $1 \le N \le 20\,000$ ) representing the size of A. The next line contains N integers:  $A_i$  ( $1 \le A_i \le 10^6$ ) representing the array A.

### Output

Output in a line an integer representing the size of a maximum odd GCD matching of  $A_{1...N}$ .

### Sample Input #1

5 6 8 9 12 13

#### Sample Output #1

2

Explanation for the sample input/output #1

This is the example from the problem description.



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## Sample Input #2

3 10 10 10

## Sample Output #2

0

Explanation for the sample input/output #2

With 3 elements, the candidate pairs are only (1,2), (1,3), and (2,3). However, none of these candidates are valid as all  $GCD(A_i, A_j)$  are not an odd number, thus, the maximum odd GCD matching for this case is an empty set  $\{\}$  with a size of 0.

### Sample Input #3

7 4 3 2 4 5 6 3

## Sample Output #3

3

Explanation for the sample input/output #3

One example maximum odd GCD matching is  $\{(1,5),(2,4),(3,7)\}$  which contains 3 pairs.