

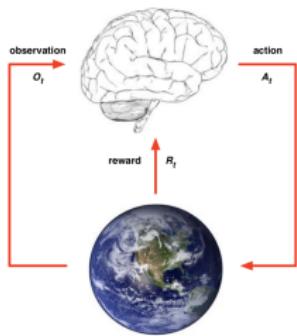
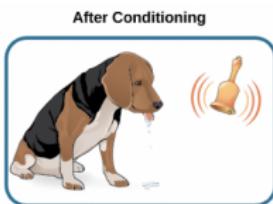
# Neuromechanics of Human Motion

## Human Behaviour

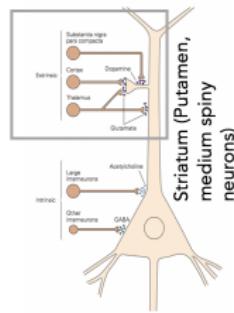
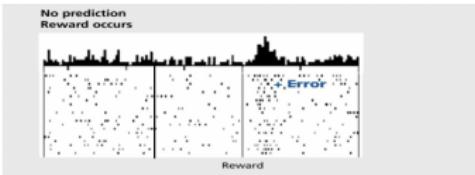
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Joshua Cashaback, PhD

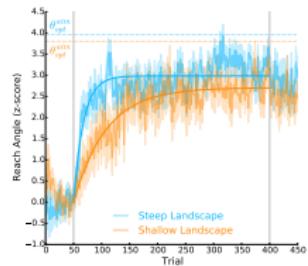
# Recap — Reinforcement Learning



# Recap — Reinforcement Learning



Shift unknown to participants



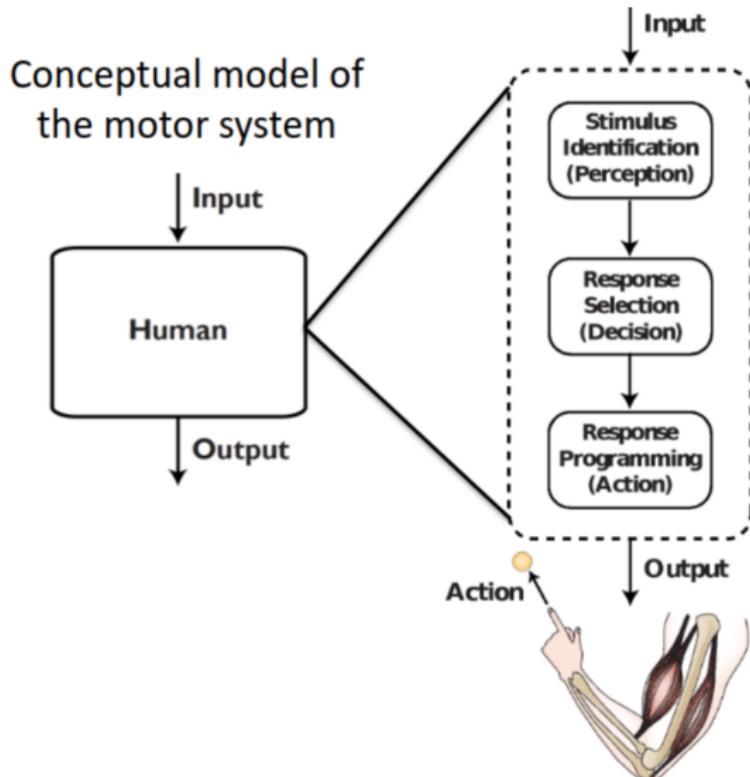
# Lecture Objectives — Human Behaviour

Brief Overview of Stereotypical Features of Human Behaviour

1. Reaction Time
  - . Hick's Law
2. Movement Time
  - . Speed-Accuracy Tradeoff
  - . Fitt's Law
3. Velocity Profiles
  - . Bell-shaped
4. Signal Dependent Noise
5. Behaviour of Redundant Systems
  - . Joint Space, Muscle Space, Load Sharing

## Reaction Time — Hick's Law

# Reaction Time — Premotor and Motor



# Reaction Time

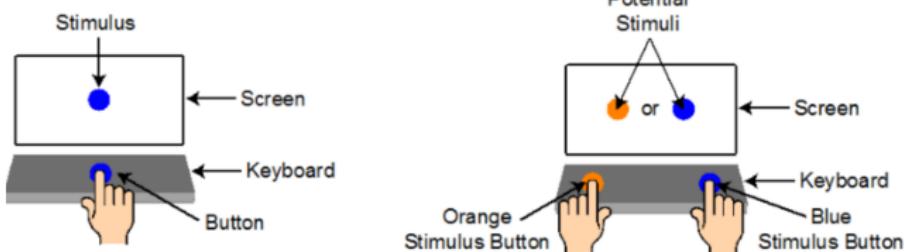
## Reaction Time

Interval between stimulus presentation and initiation of motor response

Factors that influence reaction time

1. The number of response choices (Hick's Law)
2. Stimulus modality & intensity
3. Stimulus-response compatibility
4. Anticipation

# Reaction Time — Number of Choices



# Reaction Time — Number of Choices

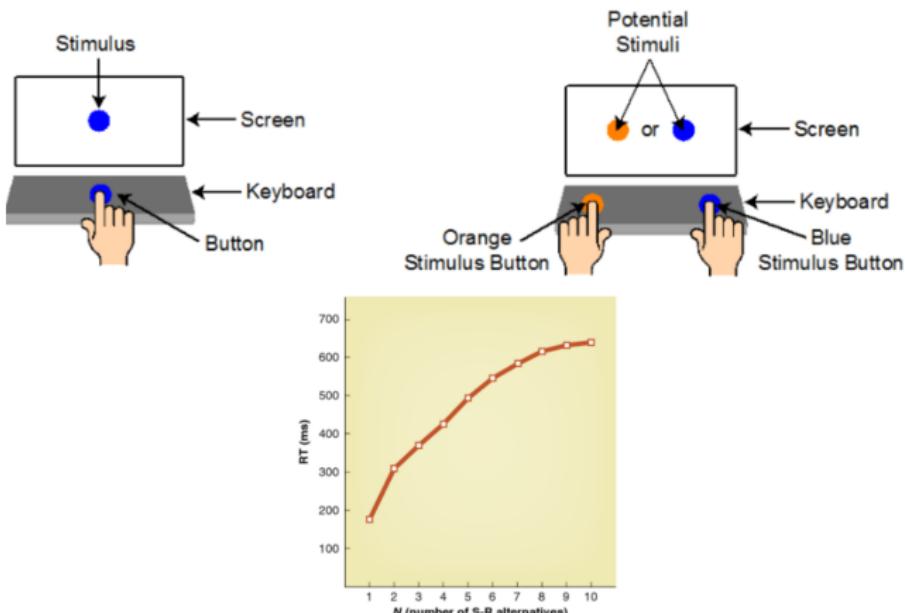
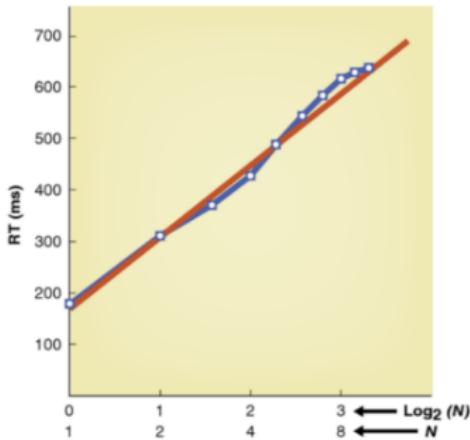


FIGURE 2.6 The relationship between the number of possible stimulus-response (S-R) alternatives and reaction time.

Reprinted by permission from Schmidt and Lee 2011; Data from Merkel 1885.

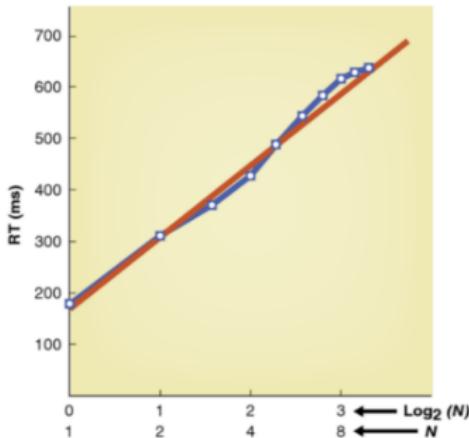
# Reaction Time — Number of Choices



**FIGURE 2.7** Hick's Law: The relation between choice RT and number of S-R alternatives ( $N$ ) is replotted using Merkel's data from figure 2.6, with choice RT as a function of  $\log_2(N)$ .

Reprinted by permission from Schmidt and Lee 2011; Data from Merkel 1885.

# Reaction Time — Number of Choices



**FIGURE 2.7** Hick's Law: The relation between choice RT and number of S-R alternatives ( $N$ ) is replotted using Merkel's data from figure 2.6, with choice RT as a function of  $\log_2(N)$ .

Reprinted by permission from Schmidt and Lee 2011; Data from Merkel 1885.

$$RT = a + b \cdot \log_2(N)$$

# Reaction Time — Hick's Law

Hick's Law (1951)

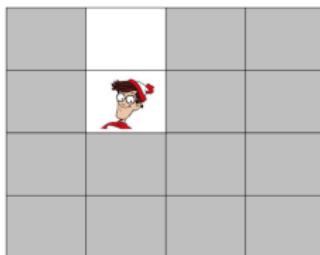
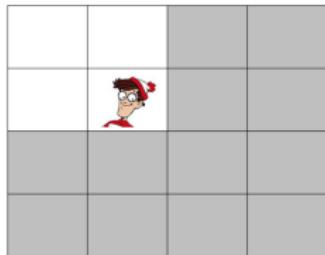
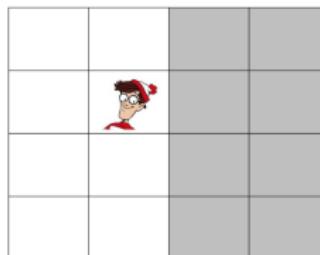
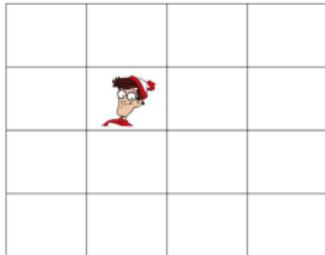
$$RT = a + b \cdot \log_2(N)$$

1.  $RT$ : Reaction Time
2.  $a$ : y-intercept (time for single choice)
3.  $b$ : slope (task, individual differences, age)
4.  $\log_2(N)$ : 'bits' of information
5.  $N$ : number of choices

# Reaction Time — Hick's Law

Why  $\log_2(N)$ ?

Binary Search (splitting the search in halves)



$$\log_2(16) = 4 \text{ OR } 2*2*2*2 = 16 \text{ (i.e., 4 binary decisions)}$$

# Reaction Time — Stimulus modality & intensity

Stimulus modality

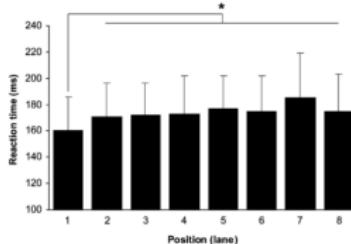
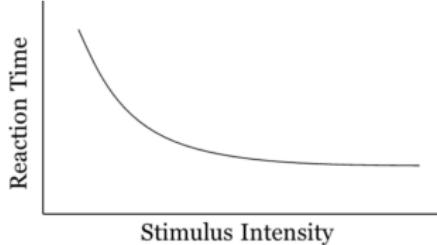
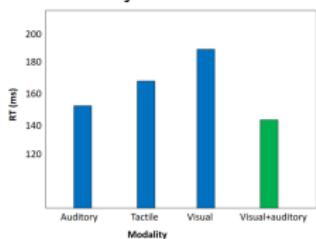


FIGURE 2—2004 Olympic Games RT. RT from the 100-m sprint and 110/100-m hurdles events grouped according to starting position. Data are expressed as mean and standard deviation (\* $P < 0.01$ , one-way ANOVA).

# Reaction Time — Stimulus-response compatibility



**Example A:** Spatially Compatible



**Example B:** Spatially Incompatible

Less compatible = greater reaction time

# Reaction Time — Anticipation

Temporal Anticipation



Spatial Anticipation



Spatial-Temporal  
Anticipation



Anticipating can decrease reaction time, but can come at a cost  
(e.g., false starts)

## Movement Time — Fitt's Law

# Speed-Accuracy Tradeoff

High Speed - Low Accuracy



Low Speed - High Accuracy



Movements can be made quickly at the cost of accuracy, or accurately at the cost of speed.

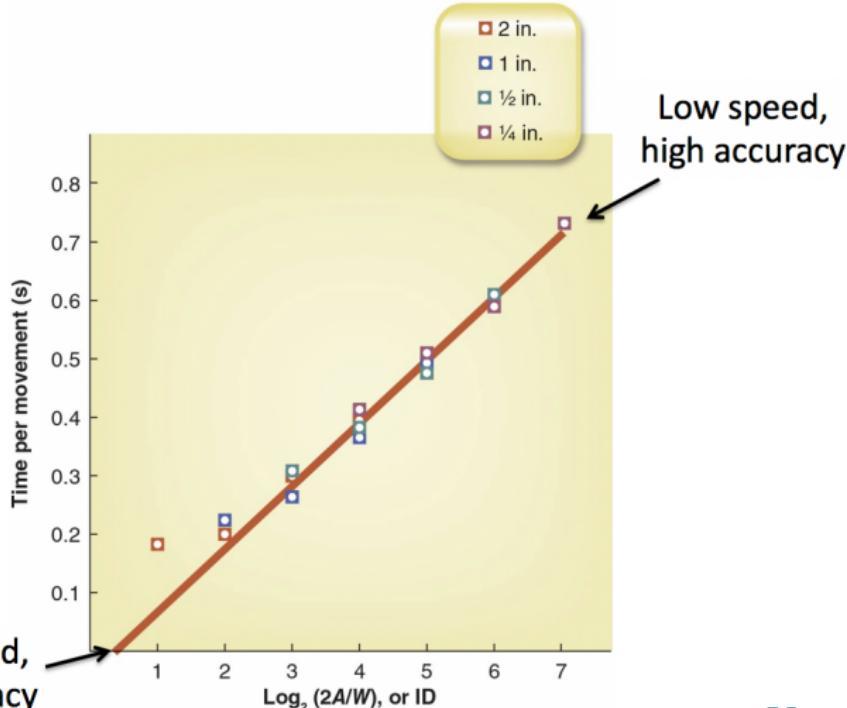
# Speed-Accuracy Tradeoff — Fitt's Law

Fitts (1954) discovered the relation between movement amplitude, accuracy, and movement time

$$MT = a + b \left[ \log_2 \left( \frac{2A}{W} \right) \right]$$

1.  $MT$ : Movement Time
2.  $a$ : y-intercept (fastest possible movement time)
3.  $b$ : slope (task, individual differences, age)
4.  $\log_2(\frac{2A}{W})$ : index of task difficulty
5.  $A$ : distance of reach
6.  $W$ : width of target

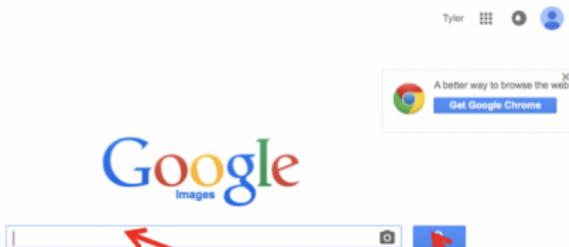
# Speed-Accuracy Tradeoff



Reprinted by permission from Schmitt and Lee 2011; Data from Fitts 1954.

# Speed-Accuracy Tradeoff

Webpage Design



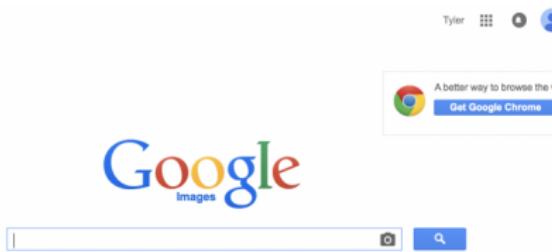
Keyboard Design



**Frequently used** areas (keys) are **larger** to reduce accuracy demand and save time

# Speed-Accuracy Tradeoff

Webpage Design



Keyboard Design



**Infrequently used areas** (keys) are smaller to increase accuracy demand at the expense of time cost. This also minimizes risk of error.

# Speed-Accuracy Tradeoff

Why is there a speed-accuracy tradeoff?

# Speed-Accuracy Tradeoff

Why is there a speed-accuracy tradeoff?

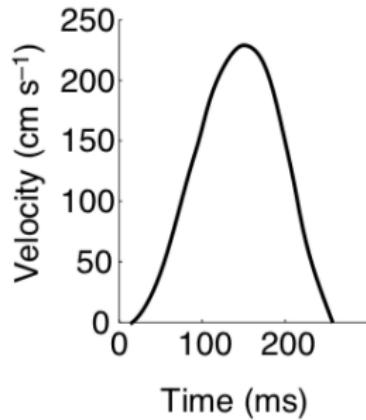
Likely candidates:

1. signal-dependent noise
2. time delays

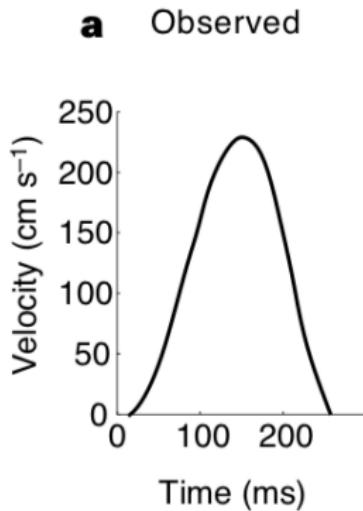
## Bell-Shaped Velocity Profiles

# Bell-Shaped Velocity Profiles

**a** Observed



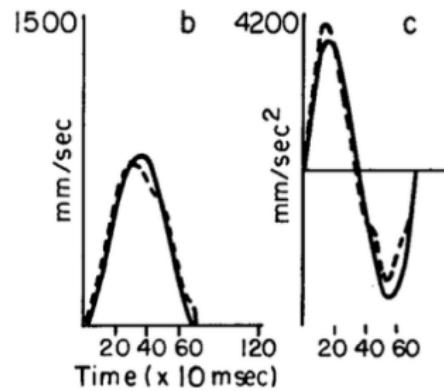
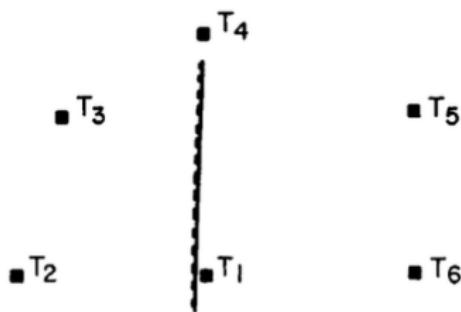
# Bell-Shaped Velocity Profiles



Why do these stereotypical velocity profile shapes arise from?

# Bell-Shaped Velocity — Min(Jerk)

Is the Brain optimizing Kinematics?



Flash and Hogan (1985) — Minimum Jerk Trajectories  
Journal of Neuroscience, 5(7), 1688-1703

# Bell-Shaped Velocity — Min(Jerk)

Flash and Hogan (1985) — Minimum Jerk Trajectories

$T$  = movement time;  $t$  = current time

$x_i, y_i$  = initial  $x,y$  position;  $x_f, y_f$  = final  $x,y$  position

$x(t), y(t)$  = current  $x,y$  position

$$x(t) = x_i + (x_f - x_i) \left[ 10(t^3/T^3) - 15(t^4/T^4) + 6(t^5/T^5) \right]$$

$$y(t) = y_i + (y_f - y_i) \left[ 10(t^3/T^3) - 15(t^4/T^4) + 6(t^5/T^5) \right]$$

$$\dot{x}(t) = (x_f - x_i) \left[ 30(t^2/T^3) - 60(t^3/T^4) + 30(t^4/T^5) \right]$$

$$\dot{y}(t) = (y_f - y_i) \left[ 30(t^2/T^3) - 60(t^3/T^4) + 30(t^4/T^5) \right]$$

$$\ddot{x}(t) = (x_f - x_i) \left[ 60(t^1/T^3) - 180(t^2/T^4) + 120(t^3/T^5) \right]$$

$$\ddot{y}(t) = (y_f - y_i) \left[ 60(t^1/T^3) - 180(t^2/T^4) + 120(t^3/T^5) \right]$$

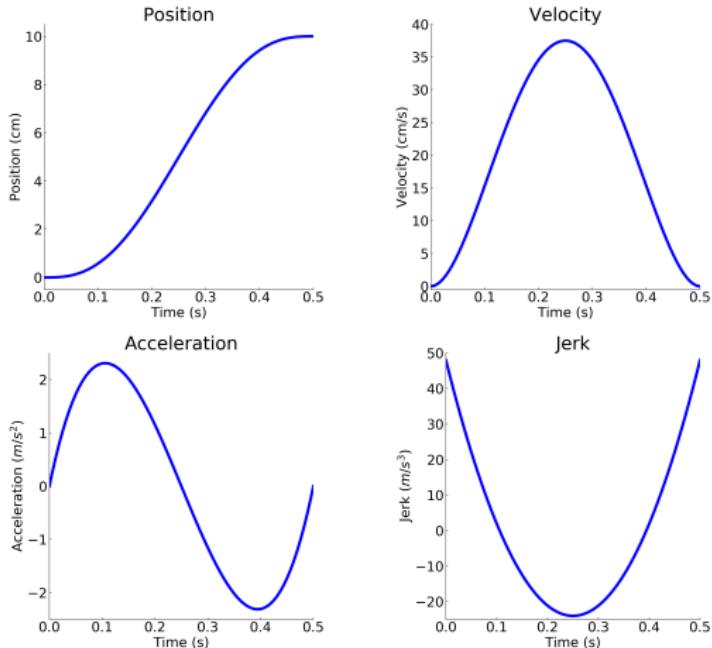
$$\dddot{x}(t) = (x_f - x_i) \left[ 60(t^0/T^3) - 360(t^1/T^4) + 360(t^2/T^5) \right]$$

$$\dddot{y}(t) = (y_f - y_i) \left[ 60(t^0/T^3) - 360(t^1/T^4) + 360(t^2/T^5) \right]$$

# Bell-Shaped Velocity — Min(Jerk)

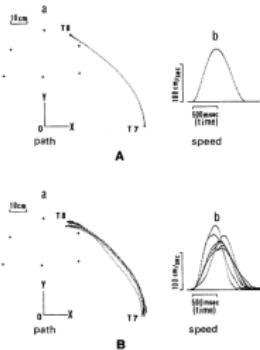
Flash and Hogan (1985) — Minimum Jerk Trajectories

$$T = 0.5; x_i, y_i = 0, 0; x_f, y_f = 0, 10$$



# Bell-Shaped Velocity — Min(Joint-Moment Rate)

Is the Brain optimizing Dynamics?



**Fig. 4A and B.** Large free movements between two targets (T7 → T8); the starting posture is stretching an arm in the side direction and the end point is approximately in front of the body. **A** Hand trajectory predicted by the minimum torque-change model; **a** shows the path and **b** shows the corresponding speed profile. **B** Observed hand trajectories for the seven subjects; **a** shows the paths and **b** shows the corresponding speed profiles.

Uno et al (1989) Biol. Cybern. 61, 1688-1703

Neuromechanics - BMEG 467/667

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# Signal Dependent Noise

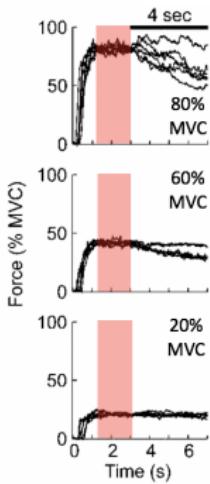
# Signal Dependent Noise

$$sdn = \sigma \cdot u$$



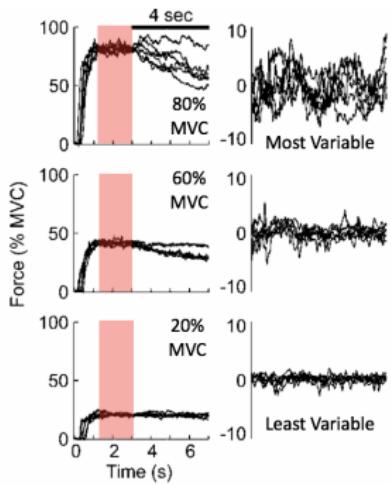
1. signal dependent noise ( $sdn$ ) scales with the control signal ( $u$ ) by some factor ( $\sigma$ )
2. increase in variance with a greater control input
3. multiplicative noise

# Signal Dependent Noise — Motor Force Variability



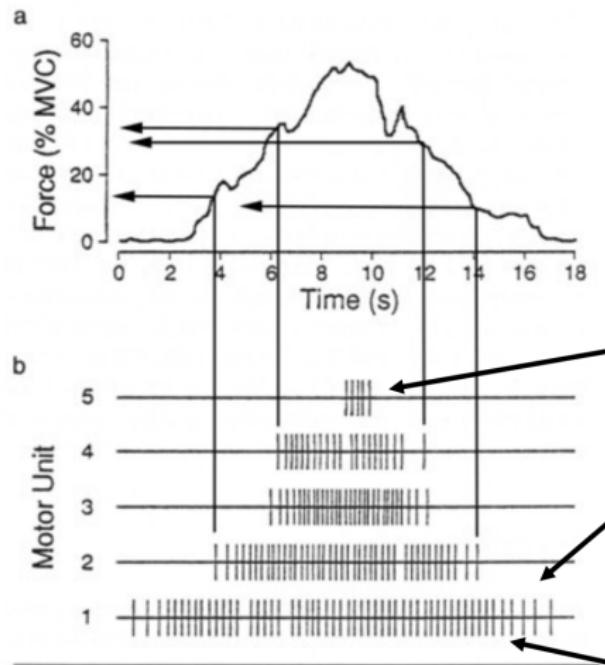
Jones, Hamilton, Wolpert (2002)

# Signal Dependent Noise — Motor Force Variability



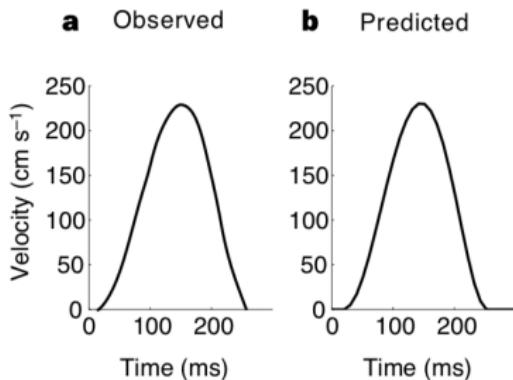
Jones, Hamilton, Wolpert (2002)

# Signal Dependent Noise — Motor Units



# Signal Dependent Noise — Min(sdn)

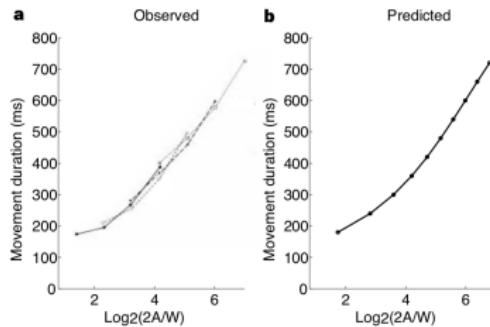
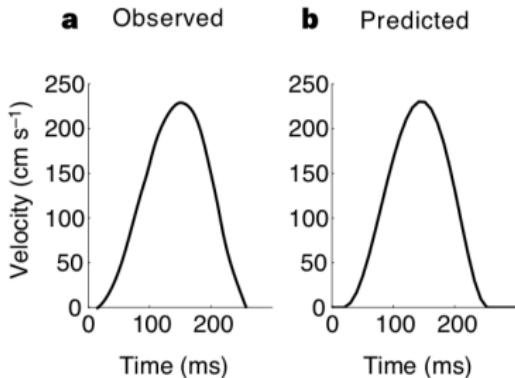
Is the Brain minimizing noise?



Harris and Wolpert (1998) — Nature, 394, 780-784

# Signal Dependent Noise — Min(sdn)

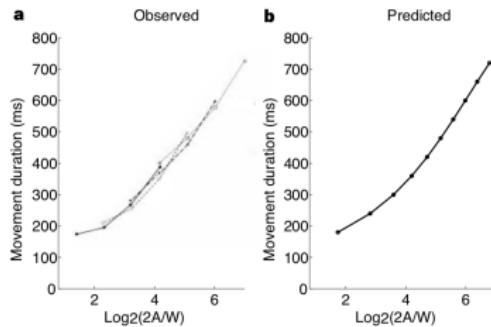
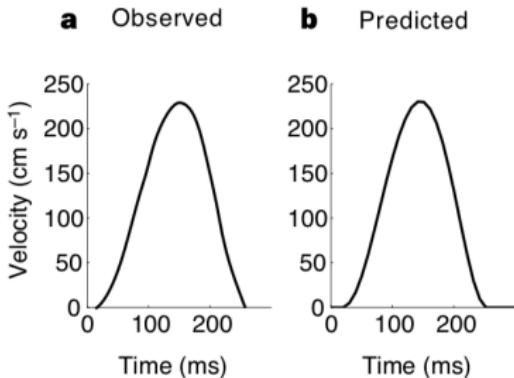
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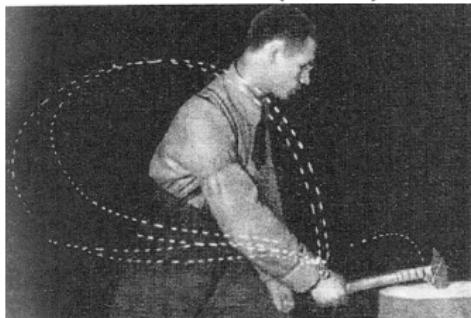
Predicts bell-shaped velocity and Fitt's Law!

But is all variability bad?

# Behaviour of Redundant Systems

# Redundant Systems — Joint Space

Bernstein (1922)



- . cyclogram: a photograph made by taking intermittent exposures (light attached to the wrist in image above)
- . Humans display lots of variability between successive movements, but can repeatedly accomplish a task goal (e.g., strike a chisel)

# Redundant Systems — Joint Space

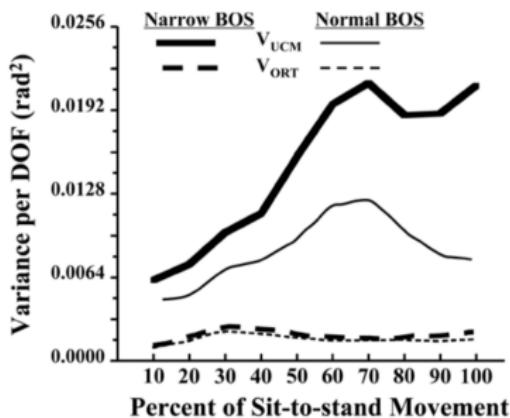
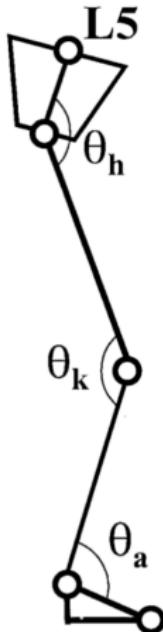
## Uncontrolled manifold hypothesis

The nervous system does not intervene (uncontrolled) with movement variability along the task-irrelevant dimension (manifold)

Pistol shooting example (Scholz, Schner, Latash, 2000):

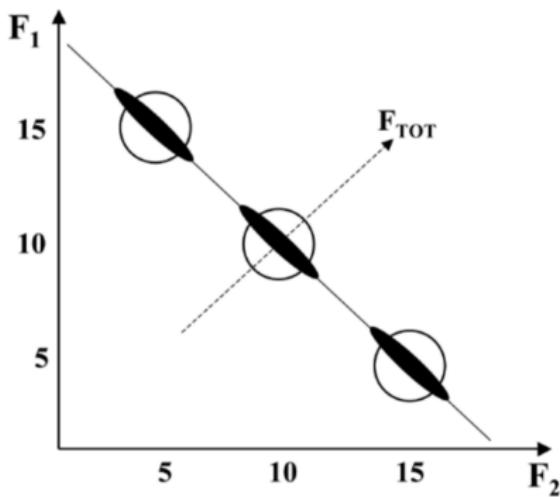
1. **Task-Irrelevant:** No bearing on task success
  - . Movement of the shoulder, elbow, and wrist *without* the location of your fingertip
2. **Task-Relevant:** Influences task success
  - . Movement of the shoulder, elbow, and wrist *changes* the location of your fingertip
3. Steps: calculate average trajectory, Jacobian null space, & partition variability along the null space (task-irrelevant) and orthogonal (task-relevant) dimensions.

# Redundant Systems — Joint Space



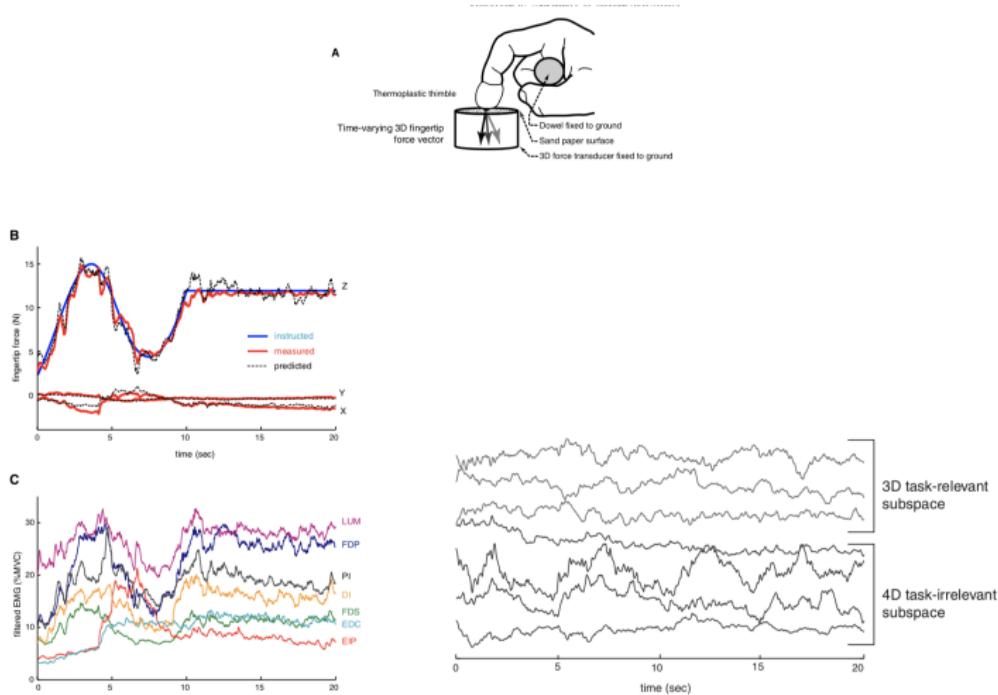
**Figure 5**—Variance of joint angles reflecting flexible patterns of joint coordination ( $V_{UCM}$ ), consistent with a stable value of the horizontal path of the body's center of mass, and variance leading to fluctuations in the horizontal CM path ( $V_{ORT}$ ) when standing up from either a narrow (thick solid line) or normal (thin solid line) base of support, computed at each percentage of normalized movement time.  $V_{ORT}$  for narrow base is represented by a thick dashed line, while that for the normal base is represented by a thin dashed line. Reproduced with permission from Scholz et al., 2001.

# Redundant Systems — Load Sharing



**Figure 1**—An illustration of the two basic features of synergies. A person tried to produce the same total force of 20 N with two fingers. Three sharing patterns are illustrated: 5:15 N, 10:10 N, and 15:5 N. This means that with changes of total force ( $F_{TOT}$ ) both finger forces change in the same direction (i.e., positive co-variation along the dashed lines). Data distri-

# Redundant Systems — Muscle Space



# Redundant Systems — Note on Dimensionality Reduction

We observe reduced dimensionality with PCA (a.k.a, 'synergies')

1. Interpretation 1: Nervous system stores and uses a particular set of motor commands (EMG) / movement pattern given a task
  - . neural and biomechanical constraints may contribute
  - . storage problems?
2. Interpretation 2: The observed motor commands / movement patterns fall out of the nervous system's control policy
  - . solves storage problem
  - . control policy can account for neural or biomechanics constraints
  - . But we do learn and store motor memories
3. Interpretation 3: Answer between these two extremes?

# Summary

How do computational models explain different Features of Human Behaviour?

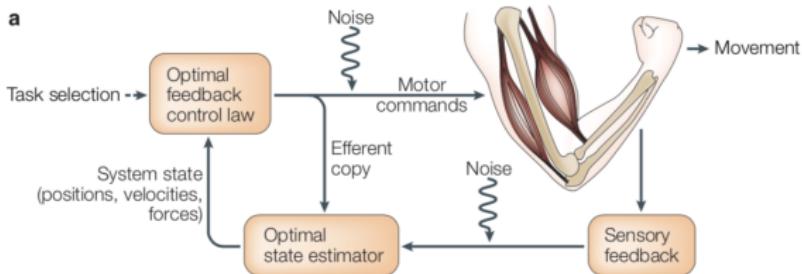
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Questions???

# Next Class

## Optimal Feedback Control and Human Behaviour

1. Fitt's Law
2. Bell-shaped Velocity Profiles
3. Task-Relevant and Task-Irrelevant Variability



# Homework

1. Play around with Hick's Law and Fitt's Law equations
2. Replicate the slide showing pos, vel, acc and jerk, using Flash and Hogan's equations
3. Use Inverse Kinematics to calculate angular position, velocity, and acceleration.
4. Use the equations of motion to calculate the required joint moments ( $Q$ ) to produce these kinematics
5. Run a forward simulation with the calculated joint moments ( $Q$ ) as an input (Euler Integration)

# Acknowledgements

Michael Carter

Tyler Cluff